

# GIT Department of Computer Engineering

## CSE 222/505 - Spring 2020

### Homework 6

#### Q1:

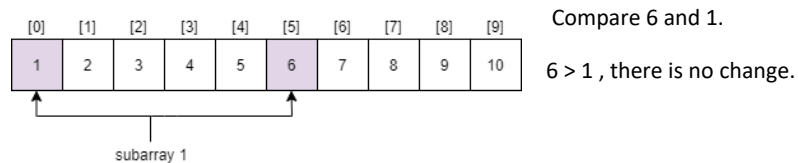
- a)  $A = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$
- b)  $B = \{10, 9, 8, 7, 6, 5, 4, 3, 2, 1\}$
- c)  $C = \{5, 2, 13, 9, 1, 7, 6, 8, 1, 15, 4, 11\}$
- d)  $D = \{'S', 'B', 'I', 'M', 'H', 'Q', 'C', 'L', 'R', 'E', 'P', 'K'\}$

a)

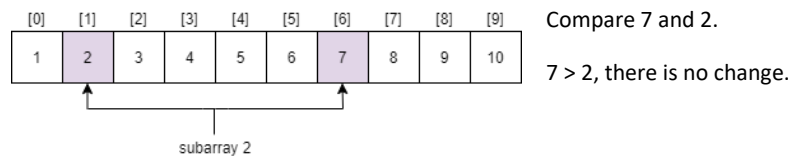
Shell Sort:

gap value =  $A.length / 2 = 5$

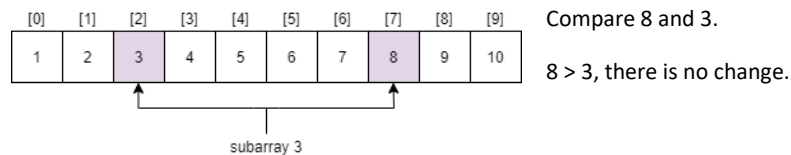
Sort subarray 1:



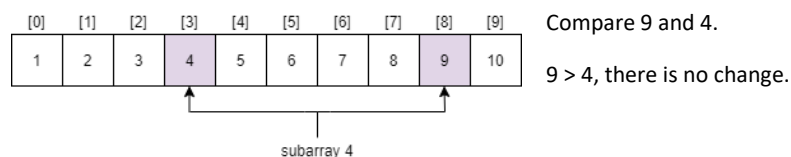
Sort subarray 2:



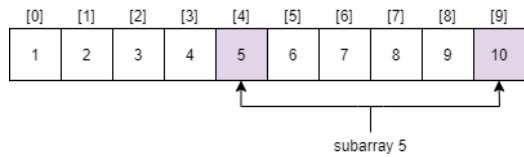
Sort subarray 3:



Sort subarray 4:



Sort subarray 5:

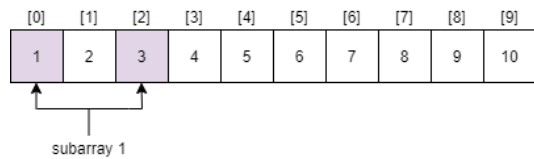


Compare 10 and 5.

10 > 5, there is no change.

gap value =  $5 / 2.2 = 2$

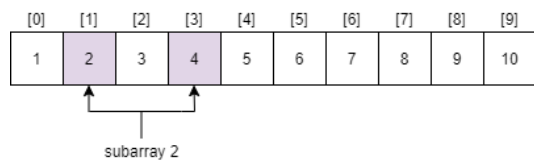
Sort subarray 1:



Compare 3 and 1.

3 > 1, there is no change.

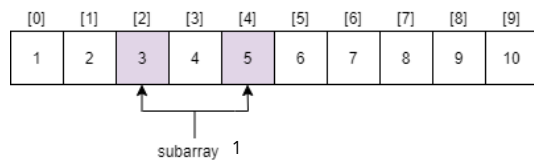
Sort subarray 2:



Compare 4 and 2.

4 > 2, there is no change.

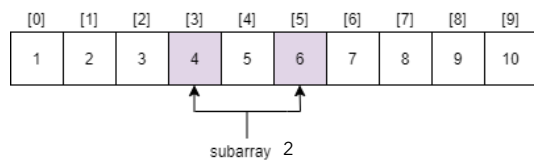
Sort subarray 1:



Compare 5 and 3.

5 > 3, there is no change.

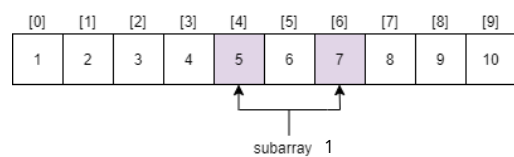
Sort subarray 2:



Compare 6 and 4.

6 > 4, there is no change.

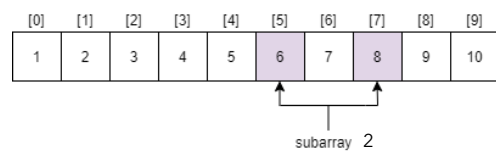
Sort subarray 1:



Compare 7 and 5.

7 > 5, there is no change.

Sort subarray 2:



Compare 8 and 6.

8 > 6, there is no change.

Sort subarray 1:

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

subarray 1

Compare 9 and 7.

$9 > 7$ , there is no change.

Sort subarray 2:

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

subarray 2

Compare 10 and 8.

$10 > 8$ , there is no change.

gap value = 1 ( a regular insertion sort )

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

↑

Compare 2 and 1.

$2 > 1$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

↑

Compare 3 and 2.

$3 > 2$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

↑

Compare 4 and 3.

$4 > 3$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

↑

Compare 5 and 4.

$5 > 4$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

↑

Compare 6 and 5.

$6 > 5$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

↑

Compare 7 and 6.

$7 > 6$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

↑

Compare 8 and 7.

$8 > 7$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

↑

Compare 9 and 8.

$9 > 8$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10

Compare 10 and 9.

10 > 9, there is no change.



Merge Sort:

1. Step:

Split table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

2. Step:

Recursive call for left table.

Split left table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

1	2
---	---

Right

3	4	5
---	---	---

3. Step.

Recursive call for left table.

Split left table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

1	2
---	---

Right

3	4	5
---	---	---

Left

1
---

Right

2
---

4. Step:

Return left and right table directly because their size is 1. If a table has one element, it is sorted.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

1	2
---	---

Right

3	4	5
---	---	---

5. Step:

Recursive call for right table.

Split right table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

1	2
---	---

Right

3	4	5
---	---	---

Left

3
---

Right

4	5
---	---

6. Step:

Return left table, the table has one element, it is sorted.

Split right table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

1	2
---	---

Right

3	4	5
---	---	---

Left

3
---

Right

4	5
---	---

Left

4
---

Right

5
---

7. Step:

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left				
1	2	3	4	5

Right				
6	7	8	9	10

Left		Right		
1	2	3	4	5

Left	Right	
3	4	5

8. Step:

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element ( 3, 4 , 5).

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left				
1	2	3	4	5

Right				
6	7	8	9	10

Left		Right		
1	2	3	4	5

9. Step:

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element (1, 2, 3, 4 , 5).

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left				
1	2	3	4	5

Right				
6	7	8	9	10

10. Step:

The left table is returned.

So, Recursive call for right table.

Split right table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

6	7
---	---

Right

8	9	10
---	---	----

11. Step:

Recursive call for left table.

Split left table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

6	7
---	---

Right

8	9	10
---	---	----

Left

6
---

Right

7
---

12. Step:

Return left and right table.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 6 , 7 )

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

6	7
---	---

Right

8	9	10
---	---	----

13. Step:

Return the left table.

Recursive call for the right table.

Split right table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

6	7
---	---

Right

8	9	10
---	---	----

Left

8
---

Right

9	10
---	----

14. Step:

The left table is returned.

Recursive call for the right table.

Split right table into halves.

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

6	7
---	---

Right

8	9	10
---	---	----

Left

8
---

Right

9	10
---	----

Left

9
---

Right

10
----

15. Step:

Return left and right table, and merge these halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 9, 10 )



1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

6	7
---	---

Right

8	9	10
---	---	----

Left

8
---

Right

9	10
---	----

16. Step:

Merge halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 8, 9, 10 )

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

Left

6	7
---	---

Right

8	9	10
---	---	----

17. Step:

The left and right tables are returned.

Merge halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 6, 7, 8, 9, 10 )

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Left

1	2	3	4	5
---	---	---	---	---

Right

6	7	8	9	10
---	---	---	---	----

18. Step:

The left and right tables are returned.

Merge halves.


Find the smaller and insert it into the table. Perform this process for each element. ( 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 )


1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----





















## Heap Sort:



















### 1. Step : Build Heap

Symbols:

 : is index of parent

 : is index of child

Array	Action	Result
1 2 3 4 5 6 7 8 9 10  	Compare parent and child ( 0 and 1) parent < child swap (parent, child)	2 1 3 4 5 6 7 8 9 10
2 1 3 4 5 6 7 8 9 10  	Compare parent and child (0 and 2) parent < child swap(parent, child)	3 1 2 4 5 6 7 8 9 10
3 1 2 4 5 6 7 8 9 10  	Compare parent and child (1 and 3) parent < child swap(parent, child), child = 1, parent = 0  Compare parent and child parent < child swap(parent, child)	3 4 2 1 5 6 7 8 9 10    4 3 2 1 5 6 7 8 9 10
4 3 2 1 5 6 7 8 9 10  	Compare parent and child (1 and 4) parent < child swap(parent, child), child = 1, parent = 0  Compare parent and child parent < child swap(parent, child)	4 5 2 1 3 6 7 8 9 10    5 4 2 1 3 6 7 8 9 10
5 4 2 1 3 6 7 8 9 10  	Compare parent and child (2 and 5) parent < child swap(parent, child), child = 2, parent = 0  Compare parent and child parent < child swap(parent, child)	5 4 6 1 3 2 7 8 9 10    6 4 5 1 3 2 7 8 9 10
6 4 5 1 3 2 7 8 9 10  	Compare parent and child (2 and 6) parent < child swap(parent, child), child = 2, parent = 0  Compare parent and child parent < child swap(parent, child)	6 4 7 1 3 2 5 8 9 10    7 4 6 1 3 2 5 8 9 10

7 4 6 1 3 2 5 8 9 10  	Compare parent and child (3 and 7) parent < child swap(parent, child), child = 3, parent = 1  Compare parent and child parent < child swap(parent, child), child = 1, parent = 0  Compare parent and child parent < child swap(parent, child)	7 4 6 8 3 2 5 1 9 10    7 8 6 4 3 2 5 1 9 10    8 7 6 4 3 2 5 1 9 10
8 7 6 4 3 2 5 1 9 10  	Compare parent and child (3 and 8) parent < child swap(parent, child), child = 3, parent = 1  Compare parent and child parent < child swap(parent, child), child = 1, parent = 0  Compare parent and child parent < child swap(parent, child)	8 7 6 9 3 2 5 1 4 10    8 9 6 7 3 2 5 1 4 10    9 8 6 7 3 2 5 1 4 10
9 8 6 7 3 2 5 1 4 10  	Compare parent and child (4 and 9) parent < child swap(parent, child), child = 4, parent = 1  Compare parent and child parent < child swap(parent, child), child = 1, parent = 0  Compare parent and child parent < child swap(parent, child)	9 8 6 7 10 2 5 1 4 3    9 10 6 7 8 2 5 1 4 3    10 9 6 7 8 2 5 1 4 3

Heap : 10 9 6 7 8 2 5 1 4 3

## 2. Step: Shrink Heap

Symbols:




































: is index of parent








: is index of max child

n : end of the heap

Array	Action	Result
10 9 6 7 8 2 5 1 4 3	n = 9, swap(0, n)	3 9 6 7 8 2 5 1 4 10
3 9 6 7 8 2 5 1 4 10  	Compare parent and max child (0 and 1) parent < max child swap(parent, max child), parent = 1	9 3 6 7 8 2 5 1 4 10 


9 3 6 7 8 2 5 1 4 10  	Compare parent and max child (1 and 4) parent < max child swap(parent, max child), parent = 4	9 8 6 7 3 2 5 1 4 10 
9 8 6 7 3 2 5 1 4 10	n = 8, swap(0, n)	4 8 6 7 3 2 5 1 9 10
4 8 6 7 3 2 5 1 9 10  	Compare parent and max child (0 and 1) parent < max child swap(parent, max child), parent = 1	8 4 6 7 3 2 5 1 9 10 
8 4 6 7 3 2 5 1 9 10  	Compare parent and max child (1 and 3) parent < max child swap(parent, max child), parent = 3	8 7 6 4 3 2 5 1 9 10 
8 7 6 4 3 2 5 1 9 10  	Compare parent and max child (3 and 7) parent > max child	8 7 6 4 3 2 5 1 9 10
8 7 6 4 3 2 5 1 9 10	n = 7, swap(0, n)	1 7 6 4 3 2 5 8 9 10
1 7 6 4 3 2 5 8 9 10  	Compare parent and max child (0 and 1) parent < max child swap(parent, max child), parent = 1	7 1 6 4 3 2 5 8 9 10 
7 1 6 4 3 2 5 8 9 10  	Compare parent and max child (1 and 3) parent < max child swap(parent, max child), parent = 3	7 4 6 1 3 2 5 8 9 10 
7 4 6 1 3 2 5 8 9 10	n = 6, swap(0, n)	5 4 6 1 3 2 7 8 9 10
5 4 6 1 3 2 7 8 9 10  	Compare parent and max child (0 and 2) parent < max child swap(parent, max child), parent = 2	6 4 5 1 3 2 7 8 9 10 
6 4 5 1 3 2 7 8 9 10  	Compare parent and max child (2 and 5) parent > max child	6 4 5 1 3 2 7 8 9 10
6 4 5 1 3 2 7 8 9 10	n = 5, swap(0, n)	2 4 5 1 3 6 7 8 9 10
2 4 5 1 3 6 7 8 9 10  	Compare parent and max child (0 and 2) parent < max child swap(parent, max child), parent = 2	5 4 2 1 3 6 7 8 9 10 
5 4 2 1 3 6 7 8 9 10	n = 4, swap(0, n)	3 4 2 1 5 6 7 8 9 10
3 4 2 1 5 6 7 8 9 10  	Compare parent and max child (0 and 1) parent < max child swap(parent, max child), parent = 1	4 3 2 1 5 6 7 8 9 10 
4 3 2 1 5 6 7 8 9 10  	Compare parent and max child (1 and 3) parent > max child	4 3 2 1 5 6 7 8 9 10
4 3 2 1 5 6 7 8 9 10	n = 3, swap(0, n)	1 3 2 4 5 6 7 8 9 10









































  1 3 2 4 5 6 7 8 9 10	Compare parent and max child (0 and 1) parent < max child swap(parent, max child), parent = 1	 3 1 2 4 5 6 7 8 9 10
3 1 2 4 5 6 7 8 9 10	n = 2, swap(0, n)	2 1 3 4 5 6 7 8 9 10
  2 1 3 4 5 6 7 8 9 10	Compare parent and max child (0 and 1) parent < max child swap(parent, max child), parent = 1	1 2 3 4 5 6 7 8 9 10



























Quicksort:







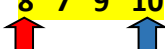
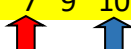










Symbols:







 : is up

 : is down

Array	Action	Result
1 2 3 4 5 6 7 8 9 10	Put the median of table[first], table[middle], table[last] into table[first], and use this value as the pivot.	6 2 3 4 5 1 7 8 9 10
 6 2 3 4 5 1 7 8 9  10	Compare pivot and up, pivot >= up, up++	6  2 3 4 5 1 7 8 9  10
6  2 3 4 5 1 7 8 9  10	Compare pivot and up, pivot >= up, up++	6 2  3 4 5 1 7 8 9  10
6 2  3 4 5 1 7 8 9  10	Compare pivot and up, pivot >= up, up++	6 2 3  4 5 1 7 8 9  10
6 2 3  4 5 1 7 8 9  10	Compare pivot and up, pivot >= up, up++	6 2 3 4  5 1 7 8 9  10
6 2 3 4  5 1 7 8 9  10	Compare pivot and up, pivot >= up, up++	6 2 3 4 5  1 7 8 9  10
6 2 3 4 5  1 7 8 9  10	Compare pivot and up, pivot >= up, up++	6 2 3 4 5 1  7 8 9  10
6 2 3 4 5 1  7 8 9  10	Compare pivot and up, pivot < up. Compare pivot and down, pivot < down, down--	6 2 3 4 5 1  7  8 9 10
6 2 3 4 5 1  7  8 9 10	Compare pivot and down, pivot < down, down--	6 2 3 4 5 1   7 8 9 10
6 2 3 4 5 1   7 8 9 10	Compare pivot and down, pivot < down, down--	6 2 3 4 5 1   7 8 9 10
6 2 3 4 5 1   7 8 9 10	Compare pivot and down, pivot > down, down--	6 2 3 4 5  1  7 8 9 10

6 2 3 4 5 1 7 8 9 10 	Compare pivot and down, pivot > down.	6 2 3 4 5 1 7 8 9 10 
6 2 3 4 5 1 7 8 9 10 	Swap(first, down)  Return down	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10	Recursive call for left table	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10	Put the median of table[first], table[middle], table[last] into table[first], and use this value as the pivot.	3 2 1 4 5 6 7 8 9 10
3 2 1 4 5 6 7 8 9 10 	Compare pivot and up, pivot >= up, up++	3 2 1 4 5 6 7 8 9 10 
3 2 1 4 5 6 7 8 9 10 	Compare pivot and up, pivot >= up, up++	3 2 1 4 5 6 7 8 9 10 
3 2 1 4 5 6 7 8 9 10 	Compare pivot and up, pivot >= up, up++	3 2 1 4 5 6 7 8 9 10 
3 2 1 4 5 6 7 8 9 10 	Compare pivot and up, pivot < up.  Compare pivot and down, pivot < down, down--	3 2 1 4 5 6 7 8 9 10 
3 2 1 4 5 6 7 8 9 10 	Compare pivot and down, pivot < down, down--	3 2 1 4 5 6 7 8 9 10 
3 2 1 4 5 6 7 8 9 10 	Compare pivot and down, pivot > down	3 2 1 4 5 6 7 8 9 10 
3 2 1 4 5 6 7 8 9 10 	Swap(first, down)  Return down	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10	Recursive call for left table (1 2)	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10 	Put the median of table[first], table[middle], table[last] into table[first], and use this value as the pivot.	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot >= up, up++	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot < up.  Compare pivot and down, pivot < down, down--	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and down, pivot = down.  Swap(first, down)  Return down	1 2 3 4 5 6 7 8 9 10 

1 2 3 4 5 6 7 8 9 10	Return this part. ( 1 2 ) Recursive call for the right table ( 3 4 )	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10	Put the median of table[first], table[middle], table[last] into table[first], and use this value as the pivot.	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot >= up, up++	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot < up.  Compare pivot and down, pivot < down, down--	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and down, pivot = down.  Swap(first, down)  Return down	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10	Return this part. ( 4 5 )	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10	Return left table ( 1 2 3 4 5 )  Recursive call right table ( 7 8 9 10 )	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10	Put the median of table[first], table[middle], table[last] into table[first], and use this value as the pivot.	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot >= up, up++	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot >= up, up++	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot < up.  Compare pivot and down, pivot < down	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and down, pivot < down	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and down, pivot > down	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Swap(first, down)  Return down	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10	Recursive call for the left part ( 7 ) Return left part.  Recursive call for the right part.( 9 10 )	1 2 3 4 5 6 7 8 9 10

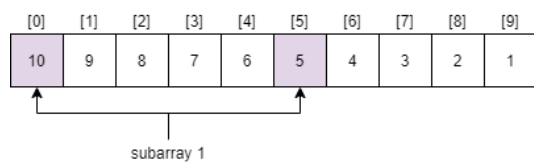
1 2 3 4 5 6 7 8 9 10	Put the median of table[first], table[middle], table[last] into table[first], and use this value as the pivot.	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot >= up, up++	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and up, pivot < up. Compare pivot and down, pivot < down, down --	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10 	Compare pivot and down, pivot = down. Swap(first, down) Return down	1 2 3 4 5 6 7 8 9 10 
1 2 3 4 5 6 7 8 9 10	Return this part. ( 4 5 )	1 2 3 4 5 6 7 8 9 10
1 2 3 4 5 6 7 8 9 10	Return right table ( 7 8 9 10 )	1 2 3 4 5 6 7 8 9 10

b)

Shell Sort:

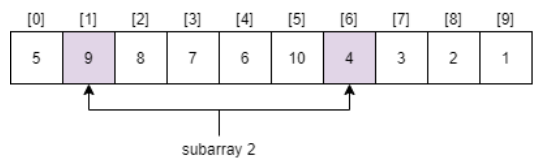
gap value =  $A.length / 2 = 5$

Sort subarray 1:



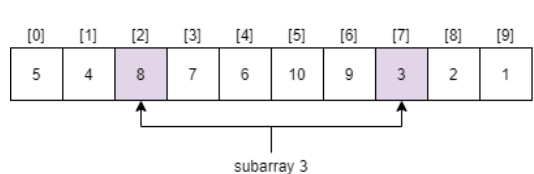
Compare 5 and 10.  
5 < 10, table[5] = 10,  
table[0] = 5

Sort subarray 2:



Compare 4 and 9.  
4 < 9, table[6] = 9,  
table[1] = 4

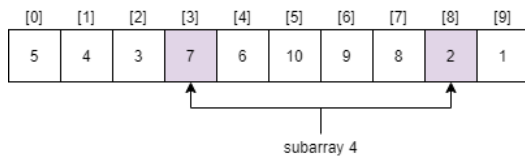
Sort subarray 3:



Compare 3 and 8.  
3 < 8, table[7] = 8,  
table[2] = 3



Sort subarray 4:

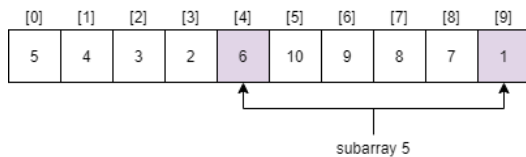


Compare 2 and 7.

$2 < 7$ ,  $\text{table}[8] = 7$ ,

$\text{table}[3] = 2$

Sort subarray 5:



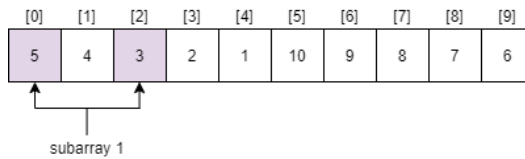
Compare 1 and 6.

$1 < 6$ ,  $\text{table}[9] = 6$ ,

$\text{table}[4] = 1$

gap value =  $5 / 2.2 = 2$

Sort subarray 1:

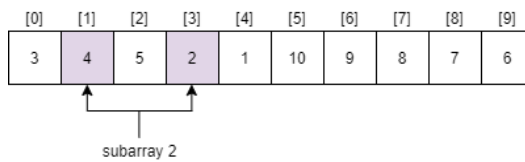


Compare 3 and 5.

$3 < 5$ ,  $\text{table}[2] = 5$ ,

$\text{table}[0] = 3$

Sort subarray 2:

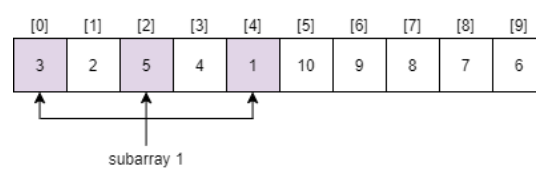


Compare 2 and 4.

$2 < 4$ ,  $\text{table}[3] = 4$ ,

$\text{table}[1] = 2$

Sort subarray 1:

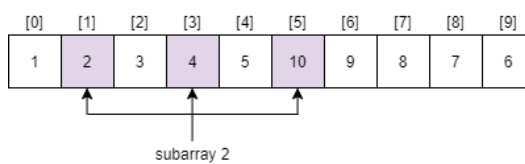


Compare 1 and 5,  $1 < 5$ ,  $\text{table}[4] = 5$ ,

Compare 1 and 3,  $1 < 3$ ,  $\text{table}[2] = 3$ ,

$\text{table}[0] = 1$

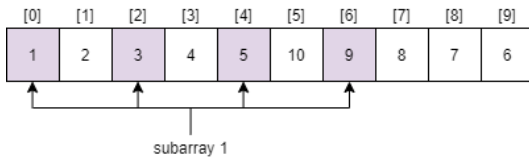
Sort subarray 2:



Compare 10 and 4,  $10 > 4$ ,

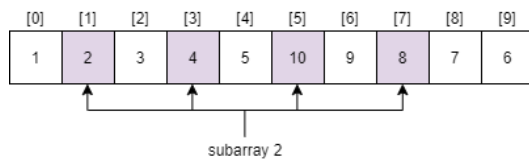
There is no change.

Sort subarray 1:



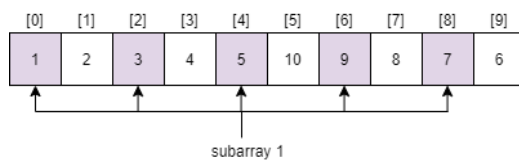
Compare 9 and 5,  $9 > 5$ ,  
There is no change.

Sort subarray 2:



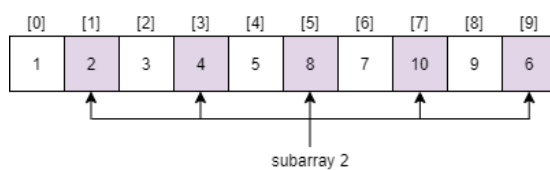
Compare 8 and 10,  $8 < 10$ ,  $\text{table}[7] = 10$ ,  
Compare 8 and 4,  $8 > 4$ ,  
 $\text{table}[5] = 8$

Sort subarray 1:



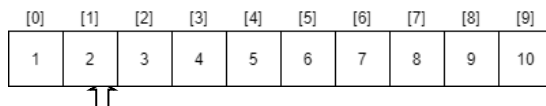
Compare 7 and 9,  $7 < 9$ ,  $\text{table}[8] = 9$ ,  
Compare 7 and 5,  $7 > 5$ ,  
 $\text{table}[6] = 7$ .

Sort subarray 2:

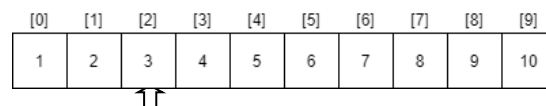


Compare 6 and 10,  $6 < 10$ ,  $\text{table}[9] = 10$ ,  
Compare 6 and 8,  $6 < 8$ ,  $\text{table}[7] = 8$ ,  
Compare 6 and 4,  $6 > 4$ ,  
 $\text{table}[5] = 6$

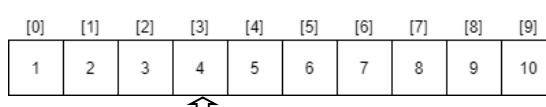
gap value = 1 ( a regular insertion sort )



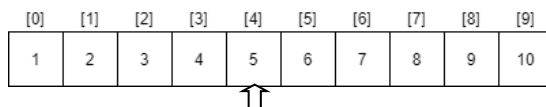
Compare 2 and 1.  
 $2 > 1$ , there is no change.



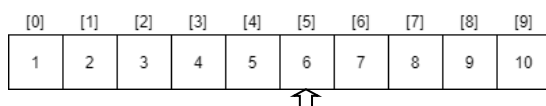
Compare 3 and 2.  
 $3 > 2$ , there is no change.



Compare 4 and 3.  
 $4 > 3$ , there is no change.




Compare 5 and 4.  
 $5 > 4$ , there is no change.



Compare 6 and 5.  
 $6 > 5$ , there is no change.


[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10



Compare 7 and 6.

$7 > 6$ , there is no change.


[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10



Compare 8 and 7.

$8 > 7$ , there is no change.


[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10



Compare 9 and 8.

$9 > 8$ , there is no change.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	2	3	4	5	6	7	8	9	10



Compare 10 and 9.

$10 > 9$ , there is no change.

Merge Sort:

1. Step:

Split table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left

10	9	8	7	6
----	---	---	---	---

Right

5	4	3	2	1
---	---	---	---	---

2. Step:

Recursive call for left table.

Split left table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left

10	9	8	7	6
----	---	---	---	---

Right

5	4	3	2	1
---	---	---	---	---

Left

10	9
----	---

Right

8	7	6
---	---	---

3. Step:

Recursive call for left table.

Split left table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
10	9	8	7	6

Right				
5	4	3	2	1

Left		Right		
10	9	8	7	6

Left	Right
10	9

4. Step:

Return left and right table directly because their size is 1. If a table has one element, it is sorted.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 10 , 9 )

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
10	9	8	7	6

Right				
5	4	3	2	1

Left		Right		
9	10	8	7	6

5. Step:

Return Left table.

Recursive call for the right table.

Split right table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
10	9	8	7	6

Right				
5	4	3	2	1

Left		Right		
9	10	8	7	6

Left	Right
8	7 6

6. Step:

Return left table, the table has one element, it is sorted.

Recursive call for right table.

Split right table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
10	9	8	7	6

Right				
5	4	3	2	1

Left	
9	10

Right		
8	7	6

Left
8

Right	
7	6

Left
7

Right
6

7. Step:

Return left and right table.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 7 , 6 )

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
10	9	8	7	6

Right				
5	4	3	2	1

Left	
9	10

Right		
8	7	6

Left
8

Right	
6	7

8. Step:

Return right table.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 8 , 6 , 7 )

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
10	9	8	7	6

Right				
5	4	3	2	1

Left	
9	10

Right		
6	7	8

9. Step:

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 9, 10, 6, 7, 8 )

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left

6	7	8	9	10
---	---	---	---	----

Right

5	4	3	2	1
---	---	---	---	---

10. Step:

Return left tables.

Recursive call for right table.

Split right table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left

6	7	8	9	10
---	---	---	---	----

Right

5	4	3	2	1
---	---	---	---	---

Left

5	4
---	---

Right

3	2	1
---	---	---

11. Step:

Recursive call for left table.

Split left table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left

6	7	8	9	10
---	---	---	---	----

Right

5	4	3	2	1
---	---	---	---	---

Left

5	4
---	---

Right

3	2	1
---	---	---

Left

5
---

Right

4
---

12. Step:

Return left and right table.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 5 , 4 )

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
6	7	8	9	10

Right				
5	4	3	2	1

Left	
4	5

Right		
3	2	1

13. Step:

Return left table.

Recursive call for right table.

Split right table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
6	7	8	9	10

Right				
5	4	3	2	1

Left	
4	5

Right		
3	2	1

Right	
3	
2	1

14. Step:

Return left table.

Recursive call for right table.

Split right table into halves.

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
6	7	8	9	10

Right				
5	4	3	2	1

Left	
4	5

Right		
3	2	1

Left	
3	
2	1

Left	
2	
Right	
1	

15. Step:

Recursive call left and right table.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 2, 1 )

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
6	7	8	9	10

Right				
5	4	3	2	1

Left	
4	5

Right		
3	2	1

Left
3

Right	
1	2

16. Step:

Return right table.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 3, 1, 2 )

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
6	7	8	9	10

Right				
5	4	3	2	1

Left	
4	5

Right		
1	2	3

17. Step:

Return right table.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 4, 5, 1, 2, 3 )

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

Left				
6	7	8	9	10

Right				
1	2	3	4	5

18. Step:

Return right table.

Merge the halves.

Find the smaller and insert it into the table. Perform this process for each element. ( 6, 7, 8, 9, 10, 1, 2, 3, 4, 5 )

1	2	3	4	6	5	7	8	9	10
---	---	---	---	---	---	---	---	---	----