SEQUENTIAL CIRCUITS

- In the first part of the course, combinational circuits were covered.
 The outputs of the combinational circuits depend only on the current inputs.
 Combinational circuit: Output = G (Input)
- In sequential circuits, the outputs depend both on the inputs and the "state" of the circuit.

Sequential circuit: Output = G (Input , Current State)

Next State = H (Input , Current State)

Memory units are required to store (remember) the state of the circuit.

For example, vending machines keep track of (remember) the coins that were inserted into the machine.

With each coin, the state of the machine (total amount of inserted coins) is updated.

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6.1

Digital Circuits

Types of sequential circuits:

There are two types of sequential circuits:

A) Synchronous sequential circuits:

Their state can change at a discrete instance of time.

All memory elements are synchronized by a common clock signal.

Therefore these circuits are also called "clocked synchronous sequential" circuit.

B) Asynchronous sequential circuit:

Their state can change at any instant of time depending upon the input signals.

In this course we will deal only with clocked synchronous sequential circuits, because nearly all sequential logic today is clocked synchronous.

For example microprocessors are clocked synchronous sequential circuits.

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Finite State Machine (FSM) Model

Sequential circuits are designed using "finite state machine - FSM" model.

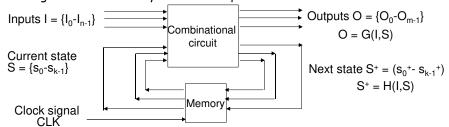
This model is also used in the design of many other systems.

- When the machine is started, it is in a certain state (initial state: s_0).
- An output is produced depending on the inputs and the current state. O = f(I,S)
- Transition into a new state happens depending on the input and the current state.

A FSM has two parts:

- a) Combinational circuit for logical operations
- b) Memory unit to remember the current state

Block diagram of a clocked synchronous sequential circuit:



We will see details of the FSM and clocked synchronous sequential circuits (in chapters 7 and 8) after we cover memory units.

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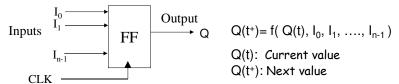
6.3

Digital Circuits

Memory Units

'Flip-flop': One-bit memory unit.

They are designed as logical circuits with multiple inputs and a single output.



Q output shows the current value of the flip-flop (0,1). This value is the state of the flip-flop.

The next value of the output Q (denoted by Q(t+1), $Q(t^+)$ or Q^+) is a function of the current state (denoted by Q(t) or Q) and the current inputs.

Clock signal (denoted as CLK) determines the time when the next state function is evaluated and the output of the flip-flop changes its value.

The output of the flip-flop can only change when the clock signal is active (the definition of being active will be described in the next slides).

If the clock signal is not active, flip-flop output will not change even if the input values change.

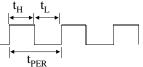
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Clock Signal:

Clock signal is a periodic square wave that synchronizes the gates in the circuit.



Logic units with clock signal input (such as flip-flops) are enabled only when the clock signal is active. If clock signal is not active, they preserve their state.

There are two types of units in terms of clock signal activation:

a) Level-triggered units

b) Edge-triggered units

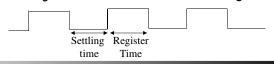
Level-triggered units use a level of the clock signal (1 in positive logic) as active. These units activate and change their outputs when the clock signal is at **high** level. They preserve their state when the clock signal is at **low** level.

When the clock signal is at high level ("1"), the inputs should not change as they are processed.

Otherwise the output of the sequential circuit is undetermined (random).

This time is called register time.

The inputs can change when the clock signal is 0. This time is called settling time.



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6.5

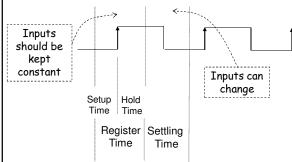
Digital Circuits

Edge-triggered units:

These units use an edge (rising edge in positive logic) of the clock signal as active. Positive edge-triggered units use $0\rightarrow1$ transition of the clock signal (rising edge) to change their state and output. At other times, they preserve their state.

As the inputs are used (processed) during $0\rightarrow 1$ transition, inputs should be kept constant for certain time before and after the transition.

Otherwise, the output of the sequential unit is undetermined (random).



The **register time** is the sum of the setup and hold times.

Setup time is the minimum amount of time the data signal should be held steady before the clock transition.

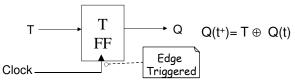
Hold time is the minimum amount of time the data signal should be held steady after the clock transition.

The inputs should be kept constant during the register time so that the sequential circuit works correctly.

In negative logic, all transactions happen at 1-0 transition (falling edge).



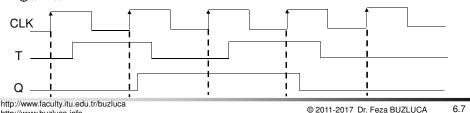
Before detailed explanation of flip-flops, a T flip-flop is used as an example.



The next output (state) of the T flip-flop Q(t+) is equal to its current output (state) XOR its input (T).

According to this, the output of the flip-flop does not change when T=0 because

The output of the flip-flop is inverted (complemented) when T=1 because $1 \oplus x = \bar{x}$.



Digital Circuits

Digital Circuits

Feedback Connections

In order to construct a circuit that has memory, we must introduce feedback into the circuit.

By **feedback**, we mean that the output of one of the gates is connected back into the input of another gate in the circuit so as to form a closed loop.

If, at some instant of time, the inverter input A is "0", this "0" will propagate through the inverter and cause the output Z to become "1".

This 1 is fed back into the input, so after the propagation delay, the inverter output Z will become "0".

When this "0" feeds back into the input A, the output Z will again switch to "1", and so forth.

The inverter output Z will continue to oscillate back and forth between "0" and "1" as shown in the figure below, and it will never reach a stable condition (unstable).

This unstable circuit cannot be used as a memory.

The rate at which the circuit oscillates is determined by the propagation delay in the inverter.



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Feedback Loop with Two Inverters (Bistable Circuit)

Next, consider a feedback loop which has two inverters in it, shown below.

In this case, the network has two stable conditions (bistable), often referred to as stable states.

Stable state 1:

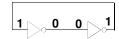
If the input to the first inverter is 0, its output will be 1.

Then, the input to the second inverter will be 1, and its output will be 0.

This 0 will feed back into the first inverter, but since this input is already 0, no changes will occur.

The circuit is then in a stable state.

Stable state 2:



A second stable state of the circuit occurs when the input to the first inverter is 1 and the input to the second inverter is 0.

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6.0

Digital Circuits

Bistable (Two stable states) Circuit (cont'd)

The bistable circuit in slide 6.9 can be also drawn as shown at right.

Remember, this circuit will always be in one of the **two** possible **stable** states.

State 1:
$$V_{in1} = 1$$
, $V_{out1} = V_{in2} = 0$, $V_{out2} = 1$

State 2:
$$V_{in1} = 0$$
, $V_{out1} = V_{in2} = 1$, $V_{out2} = 0$

This circuit has two stable states: Q = 0 and Q = 1,

Q_L is complement of Q $Q_L = \overline{Q}$.

These are necessary properties for memory units.

But this circuit has no external inputs.

It is <u>impossible</u> to control (change) the state of the circuit as it has no inputs.

When this circuit is turned on, it takes a random state.

Therefore, it cannot be used as a memory unit.

A memory unit must have

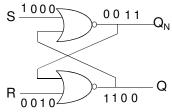
- 1. two stable states,
- 2. control input(s), which can be used to change or preserve the state of the unit.

S-R (Set-Reset) Latch

S-R Latch is a one-bit memory built by introducing feedback into two NAND or two NOR gates.

All other latches and flip-flops can be built from this fundamental memory unit with certain extensions.

S-R latch with NOR gates:



S: Set
R: Reset
Q: Output (State)
Q_N: Complemented output (Q')

Recall: When one input of a NOR

Recall: When one input of a NOR gate is "1", the output will be "0" regardless of the other input.

- S R Q Q_N

 1 0 1 0
 0 0 1 0 After S=1, R=0
 0 1 0 1
 0 0 0 1 After S=0, R=1
 1 1 0 0 Forbidden input
- The input S is used to write (store) a "1" to the latch, (an input S = 1 "sets" the output to Q = 1).
- The input R is used to write a "0" (an input R = 1 "resets" the output to Q = 0).
- \bullet If both inputs are "0", the SR latch preserves its state.
- Both inputs should not be "1" at the same time.

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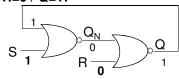
6 11

Digital Circuits

State Changes of the S-R (Set-Reset) Latch

To show how states of an S-R latch change we can draw the circuits as seen below.

S=1, R=0 / Q=1:



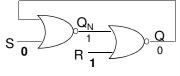
 $S \xrightarrow{1 \\ 0} Q_N \\ Q \\ R \xrightarrow{0} Q_1$

S=0, R=0 / Q=1:

If S=1, R=0, Q_N will be 0. Since both inputs of the second gate are 0, Q will become 1.

If S changed to 0, the latch will remain in the present state (1) because Q=1 is fed back into the first gate will cause $Q_{\rm N}$ to remain 0, as shown above.

S=0, R=1 / Q=0:

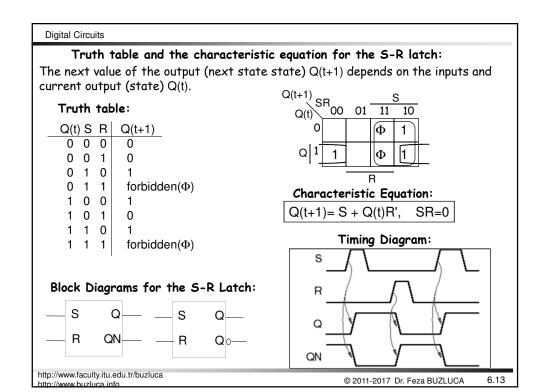


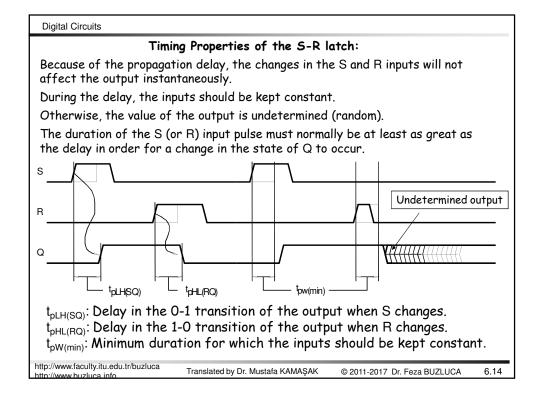
If we now change R to 1, Q will become 0 and Q_N will then change back to 1.

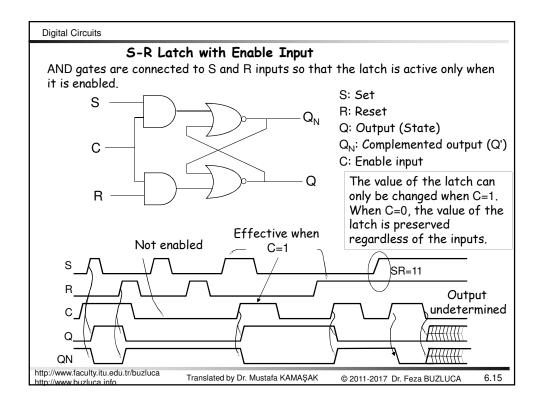
If we then change R back to 0, the latch remains in the present state (0).

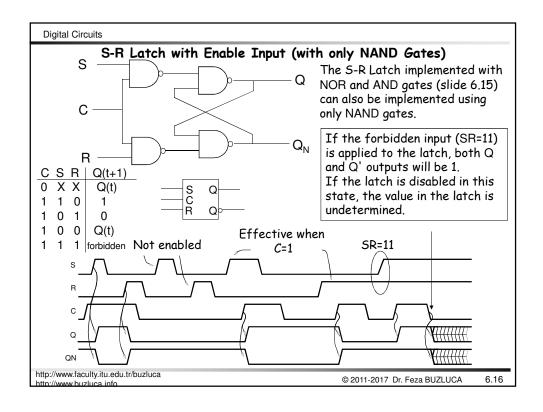
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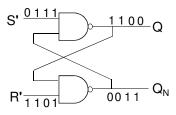
Difference between a Latch and a Flip-Flop:

A latches is not triggered by a clock signal. The value of the latch can be changed whenever the latch is enabled.

A flip-flop is a memory units that is triggered by a clock signal.

S-R Latch with NAND Gates (S'-R' Latch)

An S-R latch can be implemented using NAND gates instead of NOR. These results in an S'-R' latch.



S': Complement of Set

R': Complement of Reset Q: Output (State)

S' R'

 Q_N : Complemented output (Q')

 $Q Q_N$

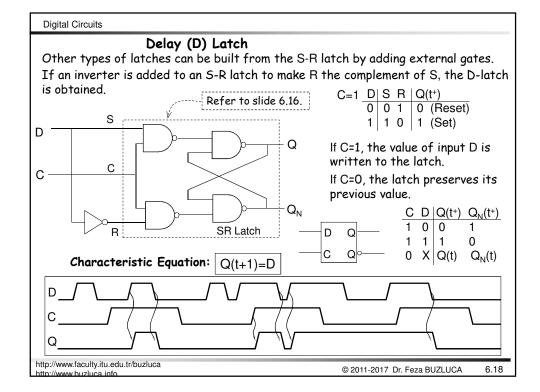
This latch is different from the latches in slides 6.15 and 6.16.

Recall: If one of the inputs of a NAND gate is "O", the output will be "1" regardless of the other input.

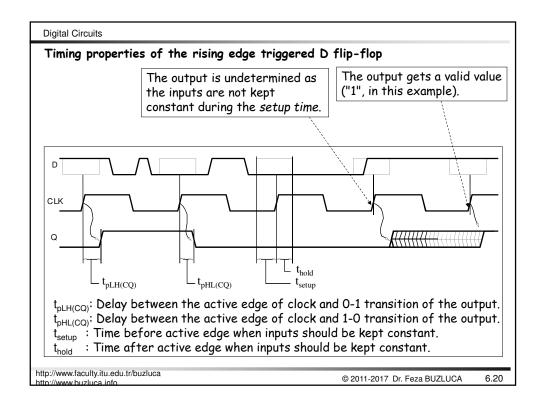
0 After S'=0, R'=1 1 1 1 1 0 0 1 After S'=1, R'=0 1 1 1 0 Forbidden inputs 0 0

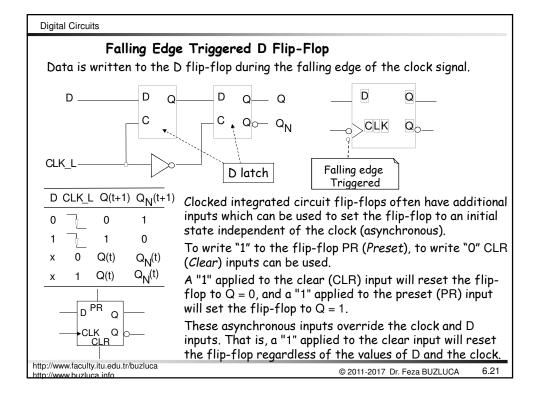
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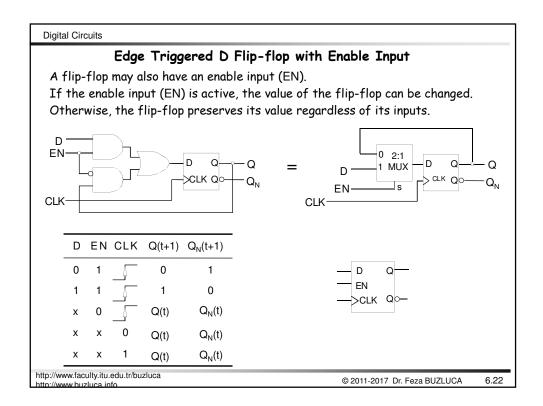
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Digital Circuits Rising Edge Triggered D Flip-Flop A latch changes its value (depending on its input) when it is enabled. A flip-flop, on the other hand, changes its value when the clock signal is active. CLK Q(t+1) $Q_N(t+1)$ D 0 1 0 0 Q(t) $Q_N(t)$ $Q_N(t)$ D Latch QM ΩN http://www.faculty.itu.edu.tr/buzluca © 2011-2017 Dr. Feza BUZLUCA 6.19







Digital Circuits Edge Triggered D Flip-flop with Enable Input (cont'd) Can we design a simpler circuit by connecting an AND gate to the CLK input of the D flip-flop? This is not a proper solution. Q-This circuit has some problems. CLK Qo-1. It is not a good idea to increase the ΕN delay at the CLK input. Clock It can cause synchronization problems. 2. If Clock=1 and EN=0 then CLK=0 and the flip-flop is disabled (it's OK). But if EN becomes 1 while clock=1, flip-flop will get a rising edge on the CLK input and it will process its input D. However the real clock signal is 1; There is not a 0-1 transition on the clock input. Problem: Clock There is not a real edge but the FF gets an rising edge. Flip-flop is disabled. It is OK ΕN http://www.faculty.itu.edu.tr/buzluca 6.23 © 2011-2017 Dr. Feza BUZLUCA

Digital Circuits

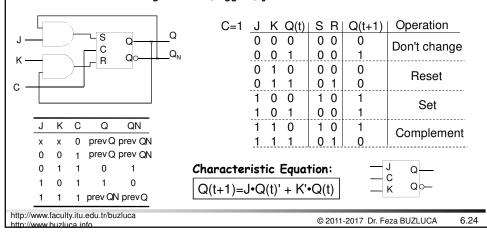
J-K Latch

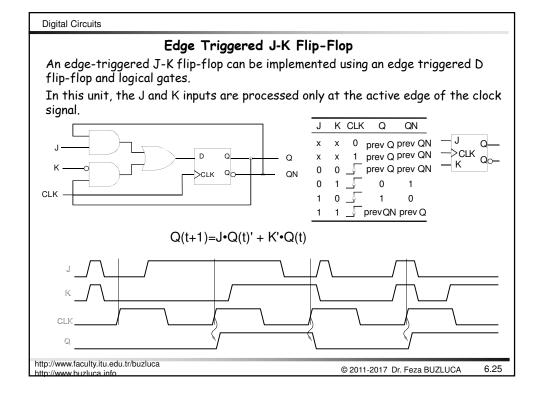
The J-K latch combines the features of the S-R and T latches.

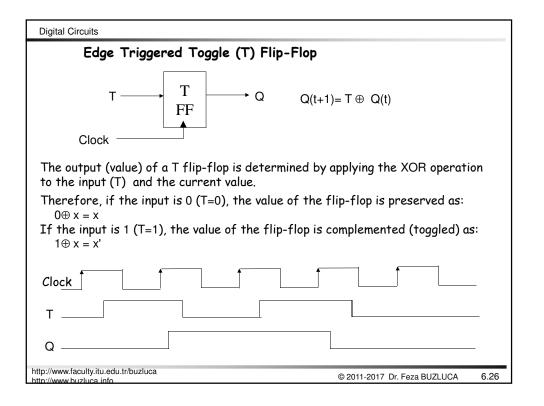
A "1" input applied to J or K alone acts exactly like an S or R input, respectively.

That is, if J=1, the latch output is set to Q=1; and if K=1, the latch output is reset to Q=0.

Unlike the S-R latch, it is permissible to apply a "1" input simultaneously to J and K, in which case the latch changes state (toggles) just like a T latch.







Characteristic Equations of latches and flip-flops:

The functional behavior of a latch or flip-flop can be described by a **characteristic equation** that specifies the next state of the flip-flop (or latch) as a function of its inputs and current state.

Characteristic equations for the flip-flops:

S-R FF:Q(t+1) = S + R' \cdot Q(t), SR=0

J-K FF: $Q(t+1) = J \cdot Q(t)' + K' \cdot Q(t)$

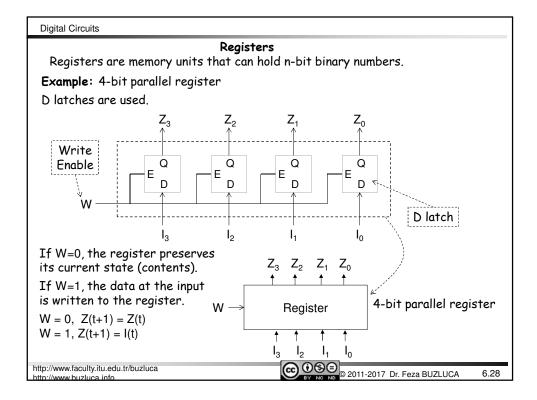
D FF: Q(t+1) = D

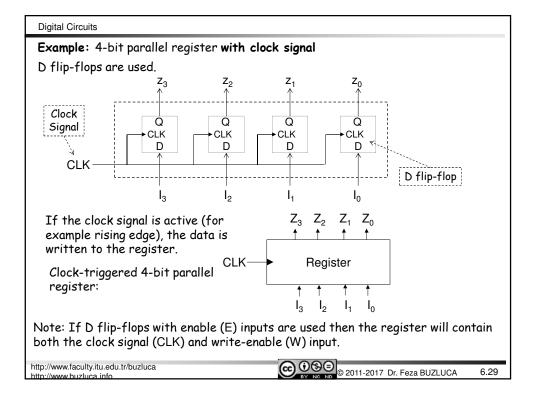
T FF: $Q(t+1) = T \oplus Q(t)$

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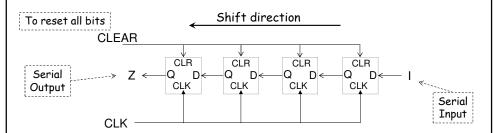




Serial Shift Registers

Serial shift registers can hold and shift binary numbers to left or right one bit at each active transition of the clock signal.

Example: 4-bit serial left shift register



The data is shift left one bit at each active transition of the clock signal.

By changing the order of the flip-flops a right-shift register can be implemented.

In this design it is not possible to load an initial value to the register (except zero) in parallel.

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