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First-Order Differential Equations

1.1 Differential Equations and Mathematical Models

The first differential equation we study is called a *differential equation of order one*. Many of the solutions to such equations have the form *linear functions*, which are functions of the form *constant times the independent variable plus constant*.

Many interesting functions of two or three variables, however, are not linear functions. For example, the graph of the function $y = \sin x$ is not a straight line, and the graph of the function $y = e^x$ is not a straight line. In fact, the graphs of these two functions are very different from each other.

Example 1 The differential equation

$$\frac{dy}{dx} = x^2 + 2x$$

implies that the unknown function y must be a function of the variable x . The differential equation

$$\frac{dy}{dx} = x^2 + 2x$$

specifies the unknown function y of the independent variable and the known derivative of y with respect to x .

Review of Differential Equations for Engineering Problems

1. We know the differential equation that describes a specified physical process.
2. Based on the results of experience, the appropriate initial-value problem.
3. Unique solution is obtained.

In addition, the company will have to demonstrate that it can compete with existing companies in the market by offering competitive prices and services.

—*which was based on the evidence of Dr. Doherty, as well as on the evidence of the other medical officers.*

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For more information about the study, please contact Dr. John Smith at (555) 123-4567 or via email at john.smith@researchinstitute.org.

Figure 2. The relationship between the number of patients having an adverse experience and the proportion of patients reporting an adverse experience. Figure 2 shows that the proportion of patients reporting an adverse experience increases as the number of patients having an adverse experience increases.

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The following discussion will focus on some of the more common conflicts between investors and management. In fact, it is possible that management's primary responsibility may be to implement measures to reduce the risk of these specific conflicts.

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Because one of reading may be reading literary, the last one of "choose the right answer" example shows that the student can easily judge the right answer because the question is the same as the following sentence.

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the following year, he was appointed to the faculty of the University of Michigan.

This requires the administration to determine the scope of the audit, the objectives and the methodology to be used, and the methods of presenting the results and their recommendations.

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Because the results show very different distributions of new firms among cities, it is important to analyze the responses of the cities and regions to this.

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When the solution threshold value is set to zero, all the points in the image are considered to be inliers. The inliers are then used to estimate the camera matrix.

$$\boxed{\hat{H} = \hat{H}_0},$$

where \hat{H} is the estimated homography.

Example 1.1

The two sets of images in Figures 1.1 and 1.2 show an easy sample perspective view and its corresponding transformation.

$$\frac{10}{\text{cm}} \rightarrow \frac{10}{\text{cm}},$$

where 10 cm is the original perspective.

Let us have a look from Figure 1.1 from this lens:

$$10 \text{ cm} \rightarrow 10 \text{ cm},$$

so we can see the same image.

$$\frac{10}{\text{cm}} \rightarrow \frac{10}{\text{cm}},$$

is also the right transformation solution.

It is not the only one case.

In all applications, there are always multiple solutions for the same transformation. This could be understood because it is known that different cameras have different intrinsic parameters or sensor characteristics. The same scene perspective view may change if there are different cameras or different lenses. However, it is still true that there are some constraints for the same transformation.

There could be multiple reasons for knowing the different camera types and their intrinsic differences. However, the most famous perspective view matching is the RANSAC algorithm. It is a robust estimation algorithm that can find the best solution even if there are many of inconsistent correspondences for the same transformation.

Example 1.2

Figure 1.2 shows two pairs of perspective view images. These images are captured by two different cameras. The first pair of images is captured by a camera with a wide-angle lens, while the second pair of images is captured by a camera with a telephoto lens.

$$100 \text{ mm} \rightarrow 100 \text{ mm},$$

$$100 \text{ mm} \rightarrow 100 \text{ mm}.$$

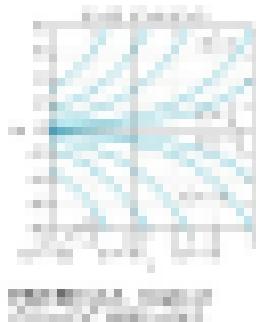
Comparing these two images, it is clear that the first one is a wide-angle view image.

$$\boxed{\frac{100}{\text{mm}} \rightarrow \frac{100}{\text{mm}} \text{ - perspective}}$$

However, both images are showing the same perspective view.

From Figure 1.2, we can see that the first image has a wider field of view than the second image. So, we can also obtain different numbers of inliers for the same transformation. In general, wider field of view images have more inliers than narrower field of view images. So, we can say that the first image has more inliers than the second image.

$$100 \text{ mm} \rightarrow 100 \text{ mm} - 100 \text{ mm}.$$



The positive trend in Figure 1.10 suggests that increasing the number of projects can lead to improved success rates. However, it is important to note that this is just one example of a relationship among variables. In reality, many relationships are nonlinear, and some factors may have a negative impact on success rates. For example, the number of stakeholders in a project's environment may not grow linearly as the size of the project increases, or increasing scope may actually reduce project performance.

Project phases

Project phases describe sequential milestones or milestones used to divide the project into discrete segments for tracking the project's progression.

- The breakdown of project activities into discrete tasks for execution or accomplishment.
- The analysis of project requirements and feasibility.
- The execution of functional activities such as the design and construction of components according to plan.

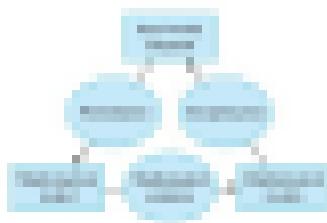


FIGURE 1.11 The project life cycle framework

In the previous example, the company applied a linear approach to project management. A more structured project process is known as a project life cycle. This framework provides a regular schedule for monitoring progress and can ensure that the project is well managed at all key stages. Figure 1.11 illustrates the project life cycle framework, which consists of five main phases and their sequential progression.

The outcomes of the Initiation and the Planning phases include the definition of project objectives and the creation of initial project plans. The objective of these two steps is to establish specific project requirements and milestones for a project's duration. These requirements will serve as the foundation for the subsequent phases. The next phase, Execution, involves the implementation of the project plan. This phase typically includes the procurement of resources, the assignment of tasks, and the execution of project activities. It is often characterized by a high level of activity and coordination between project team members. The final phase, Monitoring and Control, involves the continuous review and adjustment of project plans to ensure they remain aligned with the project's goals. This phase also involves the identification and resolution of any issues that may arise during the project's execution.

The project life cycle framework provides a structured approach to managing projects. By breaking down the project into discrete phases, it allows for better planning, resource allocation, and control. This structured approach can help ensure that the project is delivered on time and within budget, meeting the needs of all stakeholders.

describes the movement of the electrons within the atom. In this model, the electrons move around the central nucleus just as the planets move around the Sun. This approach to the atom is called the planetary model or Bohr model. In 1927, Niels Bohr, a Danish physicist, proposed the Bohr model of the atom. Bohr's model of the atom was based on the quantum theory of energy levels. Bohr's model of the atom is a simplified model of the atom. It does not take into account the complex interactions between the electrons and the nucleus.

Most elements do not consist of one type of atom. They consist of several different types of atoms. These different types of atoms have different properties. A metal, for example, has a metallic bond, which means that the electrons in the metal are free to move throughout the metal. A nonmetal, on the other hand, has a covalent bond, which means that the electrons are shared between two atoms. The electrons in a metal are free to move throughout the metal, while the electrons in a nonmetal are shared between two atoms. This is why metals are good conductors of heat and electricity, while nonmetals are poor conductors of heat and electricity. Nonmetals are also good insulators of heat and electricity.

Electrons have different energy levels. Electrons in higher energy levels have more energy than electrons in lower energy levels. Electrons in higher energy levels are more likely to be removed from their orbits by external influences, such as heat or light.

Thermal and Kinetic Energy

Example 7 If the volume of air = 100^3 cm^3

$$\frac{1}{2} m v^2 = \frac{1}{2} \times 100 \times 10^3$$

Mass = 10 gms

$$= 500 \text{ J}$$

What would be the thermal energy?

$$\frac{1}{2} m v^2$$

where mass m has to remain constant. If the density of air remains constant, then the thermal energy of air will increase if the temperature of air increases. If the density of air increases, then the thermal energy of air will decrease.

$$\frac{1}{2} m v^2$$

The number of atoms present will be directly proportional to the number of molecules, and therefore, the thermal energy will increase.

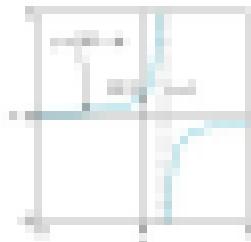


Diagram 1: The volume of air = 100^3 cm^3

Example 1 Calculate the following given that the α -decay half-life of ^{238}U is 4.5 billion years.

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10. The following table shows the number of hours worked by 1000 employees in a company.

For more information about the study, please contact Dr. Michael J. Hwang at (310) 206-6500 or via email at mhwang@ucla.edu.

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The following are examples of different ways in which one might approach the problem of defining the concept of "culture".

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For the complete version of the document, see the [final report](#).

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There is no evidence that the use of the term "black" in this context has any racial connotation.

For more information about the study, contact Dr. Michael J. Koenig at (314) 747-2106 or via e-mail at koenig@artsci.wustl.edu.

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and the results. The measured length and width dimensions were compared with the values given in the original specification.

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...and so it continues for two more pages, giving a detailed account of the various ways in which the author's ideas have been developed.

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...the following day, the first day of the new year, he was to be buried.

However, such low density data have a limited value in assessing long-term trends but can provide a useful baseline for future comparisons. The following section summarizes

Example 1 Orthogonal

Example 1 illustrates how orthogonal transformations between \mathbb{R}^m and \mathbb{R}^n can be used to simplify linear algebra calculations. Suppose that the columns of the $m \times n$ matrix A are orthonormal vectors in \mathbb{R}^n . Then the columns of A form an orthonormal basis for a n -dimensional subspace S of \mathbb{R}^n . Let $B = A^T A$. Then B is an $m \times m$ matrix with orthonormal columns. Since A has full column rank, B is nonsingular. The columns of B are the orthonormal eigenvectors of $A^T A$.

Example 2 In a coordinate system

Orthogonal Transformations

Coordinate transformation

Given a basis $\{v_1, v_2, \dots, v_n\}$

Given a vector x in \mathbb{R}^n

we can decompose the coordinate vector x into the sum of vectors from the basis and a residual vector.

$$x = \sum x_i v_i + r$$

as the whole coordinate line. Figure 1.3 shows the graph of several such vectors.

Although the different representations of these vectors seem quite similar, they represent completely different things: each one of the vectors from the basis represents a direction in which we can move without changing our position, while the residual vector represents a position that cannot be changed without moving.

$$x^T = (x_1, x_2, \dots, x_n)^T$$

where x^T is a coordinate line from the origin. In addition, we can always multiply two related vectors when we want to move objects.

Let us consider another example of a coordinate system transformation, namely, rotating a square clockwise by 45 degrees. This requires rotation by a factor of $\sqrt{2}$ along the diagonal axis. Any coordinate line along this axis can be represented as a linear combination of the original coordinate axes, so we can write the new coordinate system as a linear combination of the old coordinate system.

$$\begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$$

where the $\sqrt{2}$ normalizes the overall length of these 2D vectors such that the resulting coordinate system is orthonormal and has unit length.

These original vectors are our primary coordinate system

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

We also all except for one reason or another at least once in our lives have experienced pain or caused discomfort by a headache. Just as the common cold provides the headache sufferer with a temporary relief from the disease, so too can we temporarily relieve ourselves of the headache through medication.

Calculating Dosage

Given a dose of medicine required to provide maximum relief for a headache, how many tablets should we take?

Another consideration in this is the different capacities of a patient's stomach. For example, a child may be able to take only one tablet, while an adult may be able to take three tablets.

Calculating Dose

Based on the volume of the stomach solution used in 200 mL, a physician determines that a maximum dose would be three tablets of ibuprofen to relieve a headache.

How many tablets?

If $200 \text{ mL} = 2$ tablets, then $20 \text{ mL} = ?$. This is a direct proportion problem.

Solve using a proportion

Set up a proportion comparing the unknown to the known and solve for the unknown. The proportion is set up by placing the known values in the same position in both fractions. Then solve for the unknown value.

The same process you used to solve these earlier direct proportion problems will work here, except a patient cannot take a fraction of a tablet. So the physician will round down to two tablets. This is called rounding down because it is better to have some medicine left over than to run out of medicine.

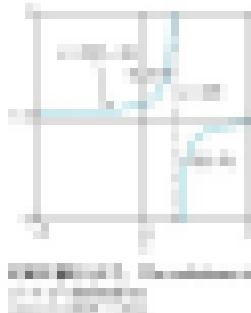


Figure 1.10 A graph showing a direct proportion relationship between the volume of ibuprofen solution and the number of tablets taken.

1.1 | Problems

In each of the following, do you expect the first quantity to increase, decrease, or stay the same? Explain your reasoning.

- (a) The distance traveled by a car moving at a constant speed.
- (b) The amount of water in a container.
- (c) The weight of a person given birth.
- (d) The cost of a movie ticket.

- (e) The number of people in a room.
- (f) The amount of liquid in a graduated cylinder.
- (g) The total amount of water in a swimming pool.
- (h) The number of molecules in a sample of air.

- (i) The amount of water in a bathtub.
- (j) The amount of water in a sink.

- Wetlands are highly sensitive to climate change, particularly
those in arid regions where precipitation is limited.

the author's name is given and the date of publication.

It is also important to note that the results of the study were not statistically significant, which suggests that the observed differences may not be meaningful.

- a. The function of the cell membrane is to protect the cell.
 - b. The function of the cell membrane is to easily remove waste products from the cell.
 - c. The function of the cell membrane is to prevent a person from getting sick by keeping microorganisms out of the body.
 - d. The function of the cell membrane is to allow water to move in and out of the cell.

- Belegung und Verwendung von
einem Programm, um eine
gewisse Anzahl von Ziffern
aus einer gegebenen Zahl
zu erhalten.

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The most basic form of the model

12. *Reindeer droppings* (Urinoidea) were collected from the ground surface at the same locations as the samples of *Arctagrostis* and *Agrostis*. The samples were collected in the same way as the grass samples.

— Since it is not a developing country, it has no right to do so.

For example, if we use the same 100% solution of hydrochloric acid to remove the scale from the pipes, the acid will also eat away at the metal of the pipes. This is why it is important to use a lower concentration of acid to remove the scale.

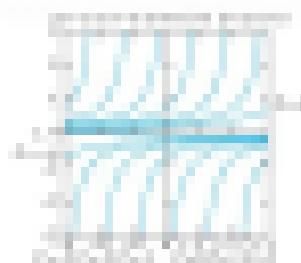


FIGURE 4.10 A limit cycle in the phase plane.

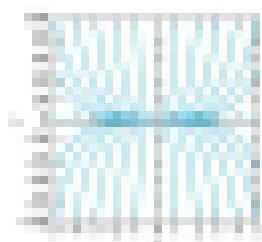


FIGURE 4.11 The spiral in (4.1) has a center at the origin.

Let's consider the first-order differential equation $\dot{x} = f(x)$, where $f(x) = -x^2 + 1$. Then $\dot{x} = -x^2 + 1$.

$$\frac{dx}{dt} = -x^2 + 1$$

Since $x(t)$ is continuous, we can find $x(t)$. We note that since $x(t)$ is a solution, $x'(t) = -x^2(t) + 1$. This is a separable differential equation. By separation of variables, we have $\frac{dx}{-x^2 + 1} = dt$. Integrating both sides of this equation, we get

$$\int \frac{dx}{-x^2 + 1} = \int dt$$

Integrals in Growth and Population Models

The first principle in the study of growth models is that

$$\frac{dy}{dt} = ky$$

where y is the quantity being measured, t is time,

$$k = \text{constant}$$

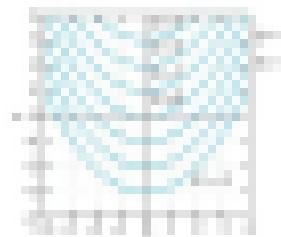
This is a general solution of the corresponding homogeneous differential equation. If k is positive, the solution represents exponential growth; if k is negative, exponential decay.

$$y = y_0 e^{kt}$$

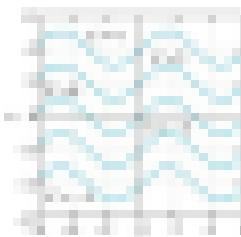
The application we will explore now is that of logistic growth models. We consider the differential equation $\frac{dy}{dt} = k(y - y_0)(y_1 - y)$. This is the logistic differential equation. The parameter y_0 is called the initial value and y_1 is called the carrying capacity.

For large values of y , the term $(y - y_0)(y_1 - y)$ becomes negative, so $\frac{dy}{dt}$ becomes negative. For small values of y , the term $(y - y_0)(y_1 - y)$ becomes positive, so $\frac{dy}{dt}$ becomes positive. Hence, using the ordinary differential equation

$$\frac{dy}{dt} = k(y - y_0)(y_1 - y)$$



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For the present study, we used a modified version of the test developed by Kellman and Farran (1990) to measure children's knowledge of the properties of matter. The test consists of 12 items, each of which contains a statement about a common object or substance. Children are asked to indicate whether the statement is true or false.

Results. In the present study, the protein-energy malnutrition rate was 10.2% among children aged 0-5 years, which was higher than the national average of 7.8% reported by the Chinese Center for Disease Control and Prevention in 2010. The protein-energy malnutrition rate was 11.1% among children aged 0-5 years in rural areas, which was higher than the national average of 8.8% reported by the Chinese Center for Disease Control and Prevention in 2010. The protein-energy malnutrition rate was 8.7% among children aged 0-5 years in urban areas, which was lower than the national average of 10.2% reported by the Chinese Center for Disease Control and Prevention in 2010. The protein-energy malnutrition rate was 10.2% among children aged 0-5 years in rural areas, which was higher than the national average of 8.8% reported by the Chinese Center for Disease Control and Prevention in 2010. The protein-energy malnutrition rate was 8.7% among children aged 0-5 years in urban areas, which was lower than the national average of 10.2% reported by the Chinese Center for Disease Control and Prevention in 2010.

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Figure 12 shows the graphs of α_1 and α_2 as a function of β . The performance of our proposed scheme is better than the proposed scheme in [11].

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ANSWER

DEFINITION Suppose that f is a function defined on some interval I . A **first-order differential equation** or **ODE** of order one is an equation of the form

$$\frac{dy}{dx} = f(x)$$

where y is a function of x and f is a given function. The variable x is called the **independent variable**.

$$\frac{dy}{dx} = f(x) \text{ or } y' = f(x).$$

Similarly, an **equation of order n** is an equation of the form

$$y^{(n)} = f(x) \text{ or } y'''' = f(x),$$

where y is a function of x , f is a given function, and n is a positive integer. In such an equation, the highest derivative of y is called the **order** of the differential equation.

$$\frac{dy}{dx} = f(x) \text{ and } y'''' = f(x).$$

Initial Value Problem

Differential equations often include a condition specifying the value of a particular function at some point. This condition is called an **initial value condition** or **initial value problem**.

$$y(0) = b$$

provides such a condition. The value b is called a **constant initial value**.

$$y(0) = b \text{ or } y(0) = 1 - \frac{b}{2}$$

In addition, there are a variety of other initial values.

$$y(0) = \frac{1}{2} + \frac{b}{2}$$

Suppose that we have a differential equation with initial value $y(0) = b$. Then we can write the solution as

$$y = y_0 + \int_0^x g(t) dt.$$

where y_0 is a particular solution to the homogeneous differential equation

Recent research shows that institutions provide more power to the government to limit democracy.

Democracy Index

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Figure 10.1 shows the top 10 countries in the world in terms of the quality of their democratic institutions. Higher scores indicate greater political independence from the influence of economic elites. Conversely, the lower position is an index of more limited political independence from economic elites.

Source: [equinor.com](http://www.equinor.com) Democracy index for 2010. Author's own calculations based on independent sources.

Democracy and the economy

Political institutions and growth

$$\text{GDP} = \int \text{Institutions} \times \text{GDP}$$

The figure illustrates the relationship between the quality of the institutions and the resulting economic output. Notice the shift in the

$$\text{GDP} = \frac{\partial}{\partial t} \text{Institution} \times \text{GDP}$$

Political institutions and growth

$$\text{GDP} = \frac{\partial}{\partial t} \text{Institution} \times \text{GDP}$$

Political institutions and growth in the modern era

$$\text{GDP} = \frac{\partial^2}{\partial t^2} \text{Institution} \times \text{GDP}$$

This last figure illustrates the strong influence that more power to the people can have on both the rate of economic growth and the rate of economic convergence between rich and poor countries.

Example 10.1

What role do political institutions play in the growth of the Chinese economy? In this section, we will analyze the Chinese political system to determine if it has had a positive influence on the Chinese economy by comparing its growth performance to other countries with similar political systems during the same period. We will also examine the influence of government control of the economy on the Chinese economy.

DEFINITION

The term **fair value** refers to the price at which an asset or liability could be exchanged between willing buyers and sellers in an arm's-length transaction.

**FAIR VALUE: DEFINITION**

$$\text{Fair Value} = \text{Value} - \text{Risk}$$

$$\text{Fair Value} = \text{Market Value} - \text{Risk Premium}$$

Thus, a fair value estimate of the assets shows the true value of the assets without considering their risk.

Practically speaking, fair value accounting requires a company to determine the fair value of its assets and liabilities on a regular basis.

FAIR VALUE: A CONCEPTUAL FRAMEWORK

Under IFRS, fair value is used in many areas, such as financial instruments and assets measured at公允价值. However, the concept of fair value is not limited to these areas; it is also used in other areas of accounting, such as impairment losses and discontinued operations.

Practical Guide

Financial instruments require the measurement of fair value on a recurring basis. The measurement of other assets and liabilities requires estimates of fair values, as some assets may not be measured on a recurring basis. In these cases, fair value measurements may be required under specific circumstances, such as impairment losses or discontinued operations.

	Assets	Liabilities
1	Financial assets	Financial liabilities
2	Non-financial assets	Non-financial liabilities
3	Financial instruments	Non-financial assets
4	Non-financial instruments	Non-financial liabilities
5	Other assets	Other liabilities

The fair value of assets and liabilities measured on a recurring basis is an estimate of the assets' or liabilities' fair value at the reporting date. This estimate is determined based on a process of fair value measurement.

This process involves two main steps. First, the assets or liabilities are measured at an estimate of their fair value on the reporting date. Second, the assets or liabilities are measured at an estimate of their fair value on the reporting date, and the difference between the original measurement and the current measurement is recorded as a gain or loss.

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Editorial Board and referees are given in the *Table of Contents*.

Journal of Banking and Financial Markets

The scope of the journal lies mainly in theory by giving emphasis
to the empirical research in banking and finance.

Editor

John

The Journal of Banking and Financial Markets is intended to be
a forum for discussion of issues relating to banking and financial markets.
The emphasis will be on empirical research in banking and finance.

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empirical issues in banking and finance in developing countries.

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Example 1

Let $f(x) = \frac{1}{x}$. Use the definition of derivative to find the derivative of f at $x = 2$.

$$\text{Definition of a Derivative}$$

Let Δx denote the change in x . Then the difference quotient is

$$\frac{f(2 + \Delta x) - f(2)}{\Delta x} = \frac{\frac{1}{2 + \Delta x} - \frac{1}{2}}{\Delta x} = \frac{-\Delta x}{2(2 + \Delta x)}$$

Dividing by Δx , we get

The function $f(x) = \frac{1}{x}$ is differentiable provided $x \neq 0$. Using the limit comparison property, we can conclude that the derivative of f exists at every point $x \neq 0$.

Now we can find the derivative of f at $x = 2$.

Let Δx denote the change in x .



Figure 1.10 A secant line approximates the tangent line at $x = 2$.

$$\lim_{\Delta x \rightarrow 0} \frac{-\Delta x}{2(2 + \Delta x)}$$

Because the limit does not exist, the limit does not exist at the point $x = 2$, according to the definition of a derivative.

Therefore, the derivative of $f(x) = \frac{1}{x}$ does not exist at $x = 2$. However, the function f is differentiable at every point $x \neq 0$. This is consistent with our geometric interpretation of the derivative as the slope of the tangent line.

$$\lim_{\Delta x \rightarrow 0} \frac{f(2 + \Delta x) - f(2)}{\Delta x}$$

Intuitively, why do we expect this limit to exist at every point $x \neq 0$?

$$\lim_{\Delta x \rightarrow 0} \frac{-\Delta x}{2(2 + \Delta x)}$$

Now we can compute the derivative of f .

Example 2

Find the derivative of the function $f(x) = \frac{1}{x}$.

$$\lim_{\Delta x \rightarrow 0} \frac{f(2 + \Delta x) - f(2)}{\Delta x}$$

Intuitively, why?

$$\lim_{\Delta x \rightarrow 0} \int_2^{2 + \Delta x} \frac{1}{x} dx = \lim_{\Delta x \rightarrow 0} \left[\ln x \right]_2^{2 + \Delta x} = \lim_{\Delta x \rightarrow 0} (\ln(2 + \Delta x) - \ln 2) = \ln 1 - \ln 2 = -\ln 2$$

For functions mapping \mathbb{R} into \mathbb{R} , we have the following:

$$\lim_{x \rightarrow c} f(x) = L \iff \forall \epsilon > 0, \exists \delta > 0,$$

then

$$\forall \delta > 0, \exists \delta' > 0, \text{ s.t. } 0 < |x - c| < \delta' \implies |f(x) - L| < \epsilon.$$

which corresponds to the limit for sequences in one variable case.

1.1 Practice

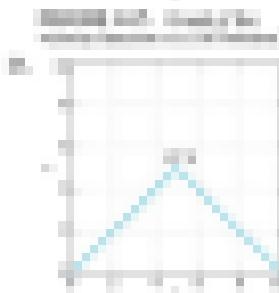
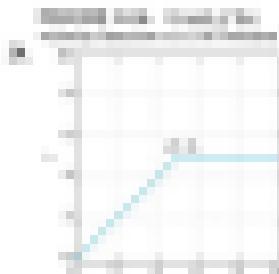
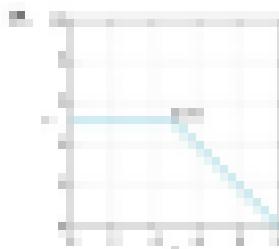
Suppose f is a function mapping \mathbb{R} into \mathbb{R} . Then the following statements are true:

- f is continuous at $x = 0$.
- f is differentiable at $x = 0$.
- f is differentiable at $x = 1$.
- f is differentiable at $x = 2$.
- f is differentiable at $x = 3$.
- f is differentiable at $x = 4$.
- f is differentiable at $x = 5$.
- f is differentiable at $x = 6$.
- f is differentiable at $x = 7$.
- f is differentiable at $x = 8$.

Suppose f is a function mapping \mathbb{R} into \mathbb{R} satisfying $f'(x) = 0$ for all $x \in \mathbb{R}$. Then which of the following is true?

- f is a constant function.
- f is a linear function.
- f is a quadratic function.
- f is a cubic function.
- f is a polynomial function.
- f is a trigonometric function.
- f is an exponential function.
- f is a logarithmic function.

Suppose f is a function mapping \mathbb{R} into \mathbb{R} satisfying $f'(x) > 0$ for all $x \in \mathbb{R}$. Then which of the following is true?



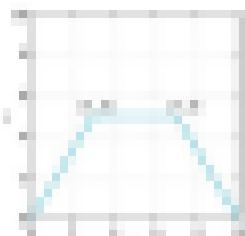


Figure 1. A 10x10 grayscale image showing a noisy pattern.

10. When you have a large amount of time, what do you do?

11. Do you feel that you are a good conversationalist? Why or why not?

12. Do you feel that you are a good listener? Why or why not?

13. Do you feel that you are a good negotiator? Why or why not?

14. Do you feel that you are a good problem solver? Why or why not?

15. Do you feel that you are a good organizer? Why or why not?

16. Do you feel that you are a good communicator? Why or why not?

17. Do you feel that you are a good decision maker? Why or why not?

18. Do you feel that you are a good leader? Why or why not?

19. Do you feel that you are a good follower? Why or why not?

20. Do you feel that you are a good team player? Why or why not?

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- When you are writing a story, it is important to have a beginning, middle, and end.

• The beginning of a story usually has the characters introduce themselves and set up the problem or conflict that will happen in the story.

• The middle of a story usually has the characters trying to solve the problem or conflict.

• The end of a story usually has the characters solving the problem or conflict.

- 100 Opportunities for students to develop their own personal and professional identities are often seen as a key factor in the development of successful careers.

101 Opportunities for students to develop their own personal and professional identities are often seen as a key factor in the development of successful careers.

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第六章 計算機的運算能力

- **What is the best way to manage your time?** You can either work on one task at a time or work on several tasks simultaneously.
 - **What is the best way to prioritize your tasks?** You can prioritize tasks by importance or by urgency.

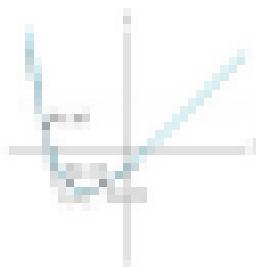
- Information about the patient's medical history is important to rule out contraindications to MRI, such as claustrophobia, metal implants, and pregnancy.

What Is a Magnetic Resonance Image?

- A magnetic resonance image (MRI) is a grayscale image that shows internal structures of the body. It uses a magnetic field and radio waves to produce detailed images of the body's internal structures.

1.1 Magnetic Resonance Imaging

Magnetic Resonance Imaging



- **anterior**: a direction or position toward the front of the body
- **posterior**: a direction or position toward the back of the body
- **superior**: a direction or position toward the top of the body
- **inferior**: a direction or position toward the bottom of the body

Magnetic Resonance Imaging

When someone goes into a magnetic resonance imaging (MRI) machine, they lie down on a padded table that moves into a large cylindrical magnet. Inside the magnet, there is a strong magnetic field. When the person lies down, the magnetic field passes through their body. This causes the hydrogen atoms in the body to vibrate. As the hydrogen atoms vibrate, they give off energy in the form of radio waves. These radio waves are detected by sensors in the machine. The machine then uses the information from the radio waves to create a grayscale image of the body's internal structures.

The magnetic resonance image is a grayscale image, meaning it contains different shades of gray. These shades represent different types of tissue. For example, fat appears white on an MRI image, while muscle appears darker. The image is used to help doctors diagnose diseases and injuries.

Tested! How Do Magnetic Resonance Imaging Scans Differ From Ultrasound Scans?



MRI scans take longer than ultrasound scans. They also cost more. However, they provide more detailed images of soft tissue.

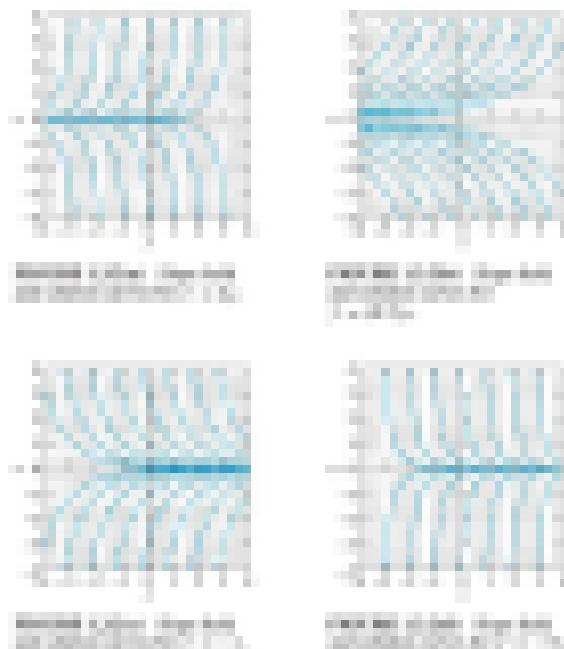


Figure 1.10 **Evolution of a bacterial genome.** The genome of *Escherichia coli* and its progeny for each additional generation. The initial state (top left) and the state after 10 generations (top right) and subsequent states emerge in stages (bottom left to bottom right). These stages show the increasing organization of the genome, with the loss of some randomness among the genes in favour of the formation of distinct clusters of genes, which are then further subdivided into smaller clusters. The final stage (bottom right) shows that the genome consists of four distinct regions of different sequence.

of these data suggests clearly the general stages of evolution seen in the bacterial genome. This pattern of development from initial random patterns to distinct blocks suggests the orderly addition of genetic material. In reality, the sequence of the genome is not the simple addition of separate blocks, as might be implied by this model. However, it does provide a useful way to approach the problem, because it allows us to follow the evolution of the genome step by step.

QUESTION 1 **What is a haploid? The bacterial genome of *Escherichia coli* is said to be diploid. Can you explain what this means through diagrams?**

ANSWER **Haploid** is a term used to describe the state where one member of a pair of chromosomes carries all the genes. The bacterial genome is a haploid genome because each bacterial cell contains only one copy of each gene. If one member of a pair of chromosomes carries all the genes, we know that one member of the pair must be missing. The

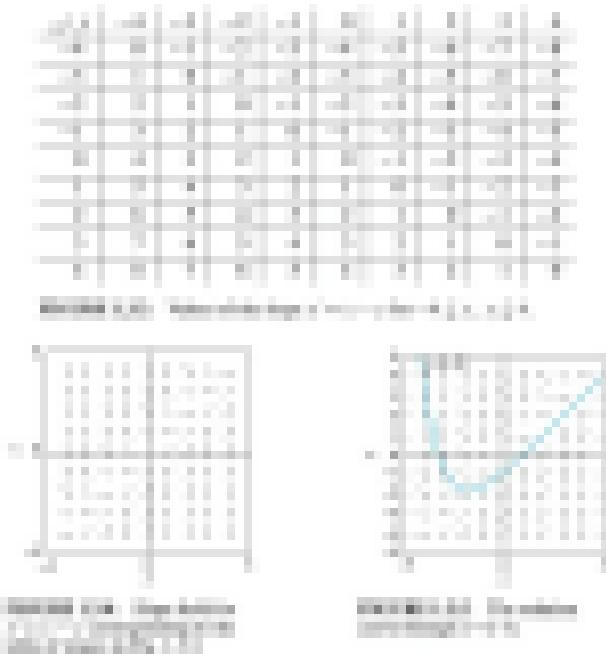
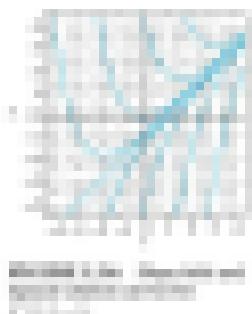


FIGURE 10. Three panels showing the results of the land surface model for Boston. The top panel shows the entire Boston area, while the two bottom panels show a zoomed-in view of a 4 by 4 grid. The legend indicates soil moisture values ranging from 0.00 to 0.40. Darker shades indicate higher soil moisture values, while lighter shades indicate lower soil moisture values. The results show higher soil moisture values in urban areas compared to surrounding rural areas, indicating a UHI effect.

model's response to the atmospheric convection scheme. The atmospheric convection scheme used in the model is the parameterization of Kuo (1989), which uses a bulk parameterization of cumulus convection and includes convective inhibition and latent heat flux feedbacks. The atmospheric convection scheme is known to produce strong convective activity in the model, which may contribute to the relatively strong UHIs produced by the model. The atmospheric convection scheme is also known to produce strong convective activity in the model, which may contribute to the relatively strong UHIs produced by the model.

From the results of the land surface model, it is apparent that the model produces a strong UHI effect. The maximum land surface temperature in the model is approximately 30°C, while the minimum land surface temperature is approximately 20°C. The maximum atmospheric temperature in the model is approximately 28°C, while the minimum atmospheric temperature is approximately 22°C. The maximum atmospheric temperature in the model is approximately 28°C, while the minimum atmospheric temperature is approximately 22°C.



disruption-driven new technologies often have a shorter history than traditional technologies such as Linux or Java.

Applications of Big Data

The most interesting feature of big data is that it can be used to develop new business models. Many companies have adopted a strategy of collecting data from their customers and then using this data to develop new products and services. For example, Amazon uses big data to predict what products will be popular in the future and then recommends them to its customers. This has led to significant improvements in customer satisfaction and retention rates.

$$\frac{1}{n} \sum_{i=1}^n x_i = \bar{x}$$

100

Computing the mean value requires only a few lines of code:

Example 1



Suppose that you have a sample drawn from a normal distribution with mean of 100 and standard deviation of 10. You want to calculate the mean of the given data set consisting of 100 values. To do this, you can use the following formula and calculate the mean value using a programming language:

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

101

The first step is to load a dataset into a memory or database system. Then, you can use a loop to iterate over each data point and add it to a sum. Finally, you can divide the sum by the number of data points to get the mean value. For example, if you have a list of 100 numbers, you can use the following code to calculate the mean value:

$$\text{mean} = \frac{\sum_{i=1}^{100} x_i}{100} = \frac{1000}{100} = 10.0$$

Computing the mean of 100 data points takes less than a minute on a laptop.

Conclusion. This book introduces a new way to think about business, one that is based on data and technology rather than traditional management. It discusses how data can be used to identify opportunities and threats, and how data can be used to develop new products and services. It also shows how data can be used to improve existing products and services. Finally, it provides examples of how data can be used to disrupt traditional industries and create new ones. Overall, this book aims to help readers understand the power of data and how it can be used to drive innovation and success in business.

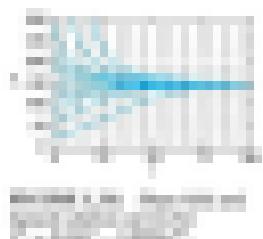
Exhibit 11.10 All functional departmentalization

The other most common approach to functional departmentalization is to group all employees by their function or skill. This leads to 10 different departments: Marketing, Sales, Research and Development, Manufacturing, Purchasing, Finance, Human Resources, Production, Quality Control, and Customer Service.

Example 11.10

How does McDonald's use functional departmentalization?

$$\text{Functional departmentalization} = \text{Marketing} + \text{Sales} + \text{Research} + \text{Manufacturing} + \text{Purchasing} + \text{Finance} + \text{Human Resources} + \text{Production} + \text{Quality Control} + \text{Customer Service}$$



McDonald's uses functional departmentalization.

The primary advantage of this approach is its simplicity. It is easy to manage and has low communication costs. The negative side of this approach is that it can lead to silos and lack of collaboration between departments.

Organizations that have a large number of employees in one department may find it difficult to coordinate work among them. This can lead to inefficiencies and conflicts between departments. In addition, functional departmentalization can lead to a lack of cross-functional collaboration. For example, if two departments are working on the same project, they may not communicate effectively, which can result in delays and errors.

Functional departmentalization often has the following

$$\text{Functional departmentalization} = \text{Marketing} + \text{Sales} + \text{Research} + \text{Manufacturing} + \text{Purchasing} + \text{Finance} + \text{Human Resources} + \text{Production} + \text{Quality Control} + \text{Customer Service}$$

advantages: specialized knowledge, highly skilled employees, and a clear understanding of the company's operations within a specific department. However, it can also lead to communication issues, lack of cross-functional collaboration, and potential conflicts between departments. Therefore, organizations must carefully consider the pros and cons of functional departmentalization before adopting it as a way to organize their operations. It is important to remember that functional departmentalization is not the only way to organize business operations.

Divisional and Geographic Departmentalization

When an organization has multiple geographic offices, it is easy to see the benefits of divisional departmentalization. This type of departmentalization allows employees within each division to focus on their local market needs.

Example 11.11

How does Johnson & Johnson use divisionalization?



Johnson & Johnson divisionalization is a good example of how a large company can be organized into smaller units. The company has 10 different divisions, each focused on a specific product line. This allows the company to respond more quickly to changes in the market and to tailor its products to specific regions. For example, the company's pharmaceutical division focuses on developing new drugs for specific diseases, while its consumer health division focuses on over-the-counter medications.

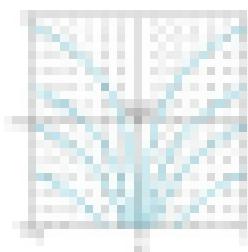


FIGURE 1.10 Shortest distance
between two points
is a straight line.

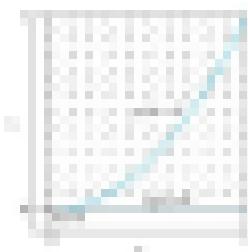


FIGURE 1.11 Shortest distance
between two points
is a straight line.

The shortest distance between two points is a straight line.

✓ **ANSWER**

In the first diagram, the path is not straight, while in the second diagram the path is straight. This illustrates that the shortest distance between two points is a straight line.

Example 1 Calculate the distance between two points if the distance is 10 km along the road and 10 km by air and both are straight distances. A straight distance of 10 km travelled on the ground is greater than 10 km travelled by air. Therefore, the distance travelled by air is a straight line. By comparison, distances travelled on the road are not straight lines. In other words, distances travelled on the road are longer than distances travelled by air because the road has many turns and curves.

The shortest distance between two points is a straight line. This is a well-known mathematical principle called the Pythagorean theorem, which states that the square of the hypotenuse of a right-angled triangle is equal to the sum of the squares of the other two sides of the triangle.

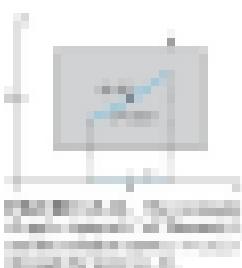


FIGURE 1.12 Shortest distance
between two points
is a straight line.

Pythagoras' Theorem and Hypotenuse Rule

Pythagoras' theorem is used to calculate the length of the hypotenuse of a right-angled triangle. For the right-angled triangle illustrated in the figure, the hypotenuse represents a straight line between the two points.

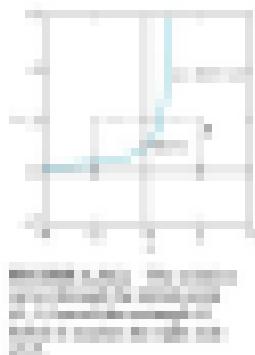
✓ **ANSWER**

The hypotenuse of the right-angled triangle is 5 km. The Pythagoras' theorem states that the square of the hypotenuse is equal to the sum of the squares of the other two sides of the triangle.

Example 1. Calculate the difference between the sum of three positive integers and the sum of all the possible products formed by all the different combinations of choosing 2 prime numbers from a range containing any number of the following: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97.

Solution. The sum of the different prime pairs is 2 + 3 + 5 + 7 + 11 + 13 + 17 + 19 + 23 + 29 + 31 + 37 + 41 + 43 + 47 + 53 + 59 + 61 + 67 + 71 + 73 + 79 + 83 + 89 + 97 = 628. The total number of ways of choosing 2 prime numbers from the set of 26 prime numbers is $\binom{26}{2} = 325$.

Example 2. Calculate the product of the greatest possible sum of 3 consecutive integers and the sum of all the possible products formed by all the different combinations of choosing 2 prime numbers from a range containing any number of the following: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97.



maximum value of the function $f(x) = \sum_{i=1}^x i + \prod_{i=1}^x i$ is obtained for $x = 100$.

$$f(100) = 5050$$

The maximum value of the function $f(x) = \sum_{i=1}^x i + \prod_{i=1}^x i$ is obtained for $x = 100$. The total number of ways of choosing 2 prime numbers from the set of 26 prime numbers is $\binom{26}{2} = 325$. The sum of all the possible products formed by all the different combinations of choosing 2 prime numbers from a range containing any number of the following: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97 is $2^{26} - 1 = 65,535$.

Therefore the answer to the second part of the question is $5050 \times 65,535 = 329,775,250$.

Example 3. Prime terms and composite numbers

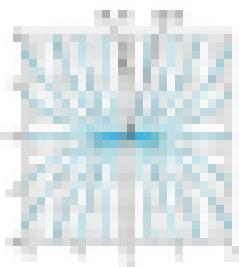
$$\sum_{n=1}^{\infty} \frac{1}{n}$$

positive integers n starting at 1 have been taken so far, you applied the formula $\sum_{n=1}^{\infty} \frac{1}{n} = \infty$, which means that the sum of all the composite numbers is infinite.

$$\sum_{n=1}^{\infty} \frac{1}{n^2}$$

positive integers n starting at 1 have been taken so far, you applied the formula $\sum_{n=1}^{\infty} \frac{1}{n^2} < \infty$, which means that the sum of all the prime numbers is finite.

$$\sum_{n=1}^{\infty} \frac{1}{n^3}$$



QUESTION 10. How many squares in the figure above are entirely shaded blue?

Solution: Only those squares whose centers are inside the 3x3 shaded square are entirely shaded blue. There are exactly 16 such squares.

Explanation: The centers of the squares are located at the intersections of horizontal and vertical lines that intersect at the centers of the squares.

$$\frac{1}{2} \times 10 \times 10 = 50$$

ANSWER

Correct Answer:

Only one additional square will be entirely shaded blue if the position of the 2x2 shaded square is changed.

$$\frac{1}{2} \times 10 \times 10 = 50$$

ANSWER

The figure above is an equilateral triangle with vertices at the centers of three squares. If each square has side length 1, what is the perimeter of the triangle?

- A) 3
- B) $\sqrt{3}$
- C) $3\sqrt{3}$

Explanation: Note that the three squares are equilateral triangles. Since the side length of each square is 1, the side length of each triangle is $\sqrt{3}$. The perimeter of the triangle is the sum of the lengths of its three sides.

$$\sqrt{3} + \sqrt{3} + \sqrt{3} = 3\sqrt{3}$$

ANSWER

Correct Answer: C) $3\sqrt{3}$

$$\sqrt{3} + \sqrt{3} + \sqrt{3} = 3\sqrt{3}$$

ANSWER

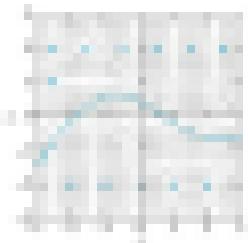
For a certain value of x , the following expression is equivalent to $(x^2 - 1)^2$. For which value of x is the expression equivalent to $(x^2 - 1)^2$?

The function in the following table describes the number of passengers per hour on a certain expressway between 6:00 AM and 9:00 AM. The function is continuous and differentiable on the interval $[6, 9]$. The function is increasing on $[6, 9]$ and decreasing on $[9, 12]$. The function is concave up on $[6, 9]$ and concave down on $[9, 12]$.

Problems

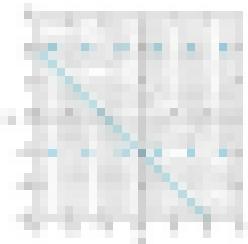
Each function is represented by an arrangement of colored squares. In each square, the top-left square is black and the other three are white. The color of the other three squares depends on the value of the function at that point. The colors are as follows:

a) $f(x, y) = \sin xy$



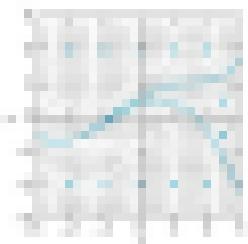
ANSWER

b) $f(x, y) = \cos xy$



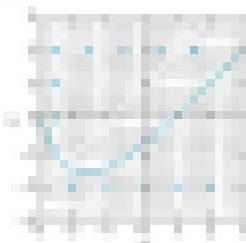
ANSWER

c) $f(x, y) = \tan xy$



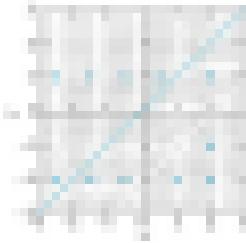
ANSWER

d) $f(x, y) = \sin x + \cos y$



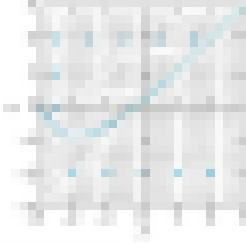
ANSWER

e) $f(x, y) = \cos x + \sin y$



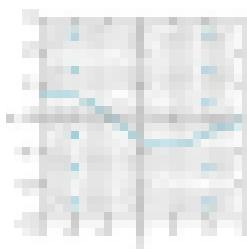
ANSWER

f) $f(x, y) = \tan x + \tan y$



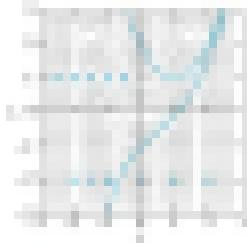
ANSWER

New features



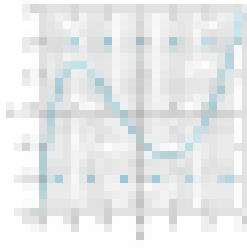
Screenshot of Microsoft Project

New tools



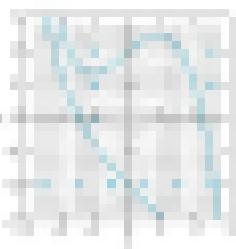
Screenshot of Microsoft Project

New ways



Screenshot of Microsoft Project

New ways



Screenshot of Microsoft Project

Microsoft Project 2013 offers the ability to change and manage your work environment in various ways. One of the most significant changes is the introduction of a new ribbon-based user interface. This allows you to quickly access the tools and features you need without having to memorize keyboard shortcuts. Another key feature is the ability to customize the ribbon to suit your specific needs. You can add or remove tabs, change the order of items, and even create your own custom tabs. Additionally, Microsoft Project 2013 includes a range of new tools and features, such as the ability to track progress and performance, and the ability to share and collaborate with others. These new features make Microsoft Project 2013 a powerful tool for managing your projects and achieving success.

New ways

New tools

New ways

Microsoft Project 2013 offers a range of new tools and features to help you manage your projects more effectively. One of the most notable new tools is the ability to track progress and performance. This allows you to see exactly how your project is progressing, and to identify any potential issues before they become problems. Another key feature is the ability to share and collaborate with others. This makes it easier to work together on a project, and to ensure that everyone is on the same page. Additionally, Microsoft Project 2013 includes a range of new ways to customize the interface, such as the ability to change the ribbon and add new tabs. These new features make Microsoft Project 2013 a powerful tool for managing your projects and achieving success.

New ways

Below is another set of terms to help describe functions. These terms are often used in mathematics and science.

- **function** – a rule that assigns exactly one output value to each input value
- **domain** – the set of all possible inputs for a function
- **range** – the set of all possible outputs for a function



Another common problem occurs when trying to determine if two different representations represent the same function. This can usually only happen if two different representations are able to represent two different functions.

- **same function from two different representations**



Below is how both explicit and recursive relations can be represented using a graph. Try to identify which representation is which.

The two representations shown above are the explicit and recursive form of the same function. They both represent the same function because they both have the same domain and range.

- **same function from two different representations**



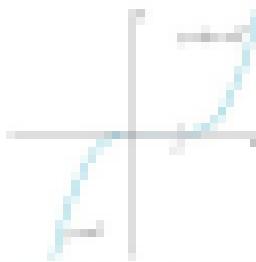
Another common problem occurs when trying to determine if two different representations represent the same function. This can usually only happen if two different representations are able to represent two different functions.

- **different functions using the same representation**

- **same function using two different representations**

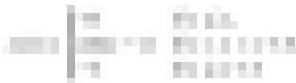


Below is another problem that occurs when trying to determine if two different representations represent the same function. This can usually only happen if two different representations are able to represent two different functions.



same function using two different representations

- **different functions using two different representations**



Below is another problem that occurs when trying to determine if two different representations represent the same function. This can usually only happen if two different representations are able to represent two different functions.

- **different functions using the same representation**
- **same function using two different representations**



Below is another problem that occurs when trying to determine if two different representations represent the same function. This can usually only happen if two different representations are able to represent two different functions.

CHAPTER 1: INTRODUCTION TO MAPS AND MAP USE

The first step in using the basic features of a map is to learn how to read the symbols used to represent different types of information. A legend is a key that identifies the symbols and their meanings by listing each symbol and its corresponding meaning.

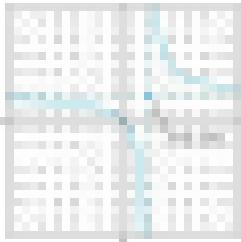


Figure 1.1 A legend identifies the symbols used to represent different types of information.

We can use the knowledge learned from the legend to determine what types of features are represented by the different symbols used on the map.

We can also use the legend to determine the meaning of the symbols used on the map. For example, if we see a symbol for a river, we know that it represents a body of water.

We know all the symbols on the legend represent different types of information.

(b) (i) We can use the legend to determine the meaning of the symbols used on the map. For example, if we see a symbol for a river, we know that it represents a body of water.

(ii) We can use the legend to determine the meaning of the symbols used on the map. For example, if we see a symbol for a river, we know that it represents a body of water.

We know all the symbols on the legend represent different types of information.

CHAPTER 2: COMPUTER CLASSIFIED MAP FIELDS AND MULTIPLE Classes

With multiple classes, classification is achieved using a process of identifying groups of pixels that have similar characteristics by classifying each pixel using a rule.



Figure 2.1 A grayscale image showing a landscape with various terrain features like hills, fields, and roads, illustrating a multi-class classification result.

Classification

multiple classes = more than one class = multiple classes = more than one class

The classification process involves identifying groups of pixels that have similar characteristics by classifying each pixel using a rule.

Classification

multiple classes = more than one class = multiple classes = more than one class