# **Logistic Regression Classifier**

```
In [ ]: import pickle
        from urllib.request import urlopen
        import numpy as np
        import matplotlib.pyplot as plt
        import seaborn as sns
        from sklearn.linear_model import LogisticRegression
        from sklearn.model_selection import train_test_split
        from sklearn.metrics import confusion_matrix, accuracy_score, precision_s
        def load_ising_data():
           url = 'https://physics.bu.edu/~pankajm/ML-Review-Datasets/isingMC/'
           file_name = "Ising2DFM_reSample_L40_T=All.pkl"
           label_file_name = "Ising2DFM_reSample_L40_T=All_labels.pkl"
           data = pickle.load(urlopen(url + file_name))
           data = np.unpackbits(data).reshape(-1, 1600).astype('int')
           data[data == 0] = -1
           labels = pickle.load(urlopen(url + label_file_name))
           return data, labels
        def train logistic regression(X train, y train):
           model = LogisticRegression()
           model.fit(X_train, y_train)
           return model
        def evaluate_model(model, X_test, y_test):
           y_pred = model.predict(X_test)
           conf_matrix = confusion_matrix(y_test, y_pred)
           accuracy = accuracy_score(y_test, y_pred)
           precision = precision_score(y_test, y_pred)
           recall = recall_score(y_test, y_pred)
           f1 = f1_score(y_test, y_pred)
           return conf_matrix, accuracy, precision, recall, f1
        def plot_confusion_matrix(conf_matrix):
           plt.figure(figsize=(8, 6))
           sns.heatmap(conf_matrix, annot=True, fmt='d', cmap='Blues', cbar=False
           plt.title('Confusion Matrix')
           plt.xlabel('Predicted Label')
           plt.ylabel('True Label')
           plt.show()
```

```
def plot_evaluation_metrics(metrics_values, metrics_names):
    plt.figure(figsize=(10, 6))
    sns.barplot(x=metrics_values, y=metrics_names, palette='viridis')
    plt.title('Model Evaluation Metrics')
    plt.xlabel('Metric Value')
    plt.show()

data, labels = load_ising_data()

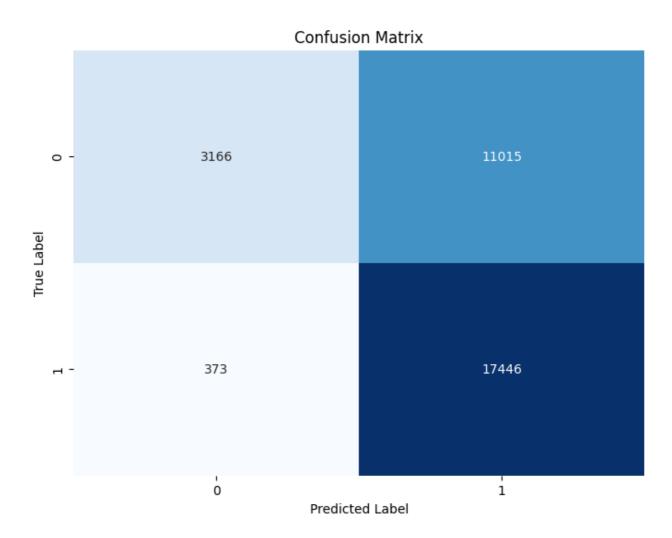
X_train, X_test, y_train, y_test = train_test_split(data, labels, test_si

model = train_logistic_regression(X_train, y_train)

conf_matrix, accuracy, precision, recall, f1 = evaluate_model(model, X_te)

plot_confusion_matrix(conf_matrix)

metrics_values = [accuracy, precision, recall, f1]
metrics_names = ['Accuracy', 'Precision', 'Recall', 'F1 Score']
plot_evaluation_metrics(metrics_values, metrics_names)
```



> /var/folders/0c/p8t8gw0s0nj8\_5tr34fz8mv40000gn/T/ipykernel\_14145/387925142 4.py:52: FutureWarning:

> Passing `palette` without assigning `hue` is deprecated and will be remove d in v0.14.0. Assign the `y` variable to `hue` and set `legend=False` for the same effect.

> sns.barplot(x=metrics\_values, y=metrics\_names, palette='viridis') /Users/bilgic/Desktop/fiz437e project/project/lib/python3.9/site-packages/ seaborn/\_base.py:949: FutureWarning: When grouping with a length-1 list-li ke, you will need to pass a length-1 tuple to get\_group in a future versio n of pandas. Pass `(name,)` instead of `name` to silence this warning. data\_subset = grouped\_data.get\_group(pd\_key)

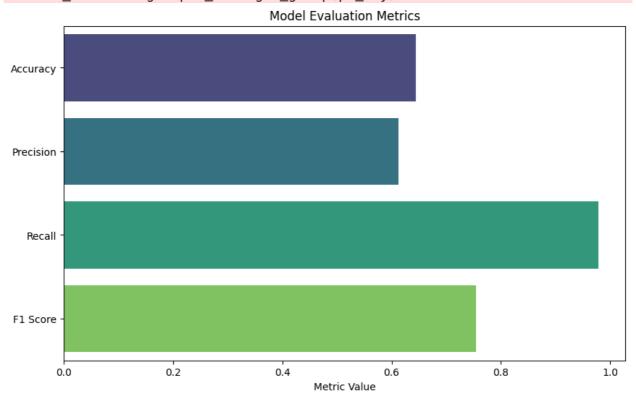
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# Random Forest Classifier (RFC)

```
In []: import pickle, os
        from urllib.request import urlopen
        import numpy as np
        from sklearn.model selection import train test split
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.metrics import accuracy_score, classification_report
        from sklearn.preprocessing import StandardScaler
        def load_ising_data():
           url = 'https://physics.bu.edu/~pankajm/ML-Review-Datasets/isingMC/'
           file_name = "Ising2DFM_reSample_L40_T=All.pkl"
           label_file_name = "Ising2DFM_reSample_L40_T=All_labels.pkl"
           data = pickle.load(urlopen(url + file name))
           data = np.unpackbits(data).reshape(-1, 1600).astype('int')
           data[data == 0] = -1
           labels = pickle.load(urlopen(url + label_file_name))
           return data, labels
        def train random forest(X train, y train):
           model = RandomForestClassifier(n_estimators=100, random_state=42)
           model.fit(X_train, y_train)
           return model
        def evaluate_model(model, X_test, y_test):
           y_pred = model.predict(X_test)
           conf_matrix = confusion_matrix(y_test, y_pred)
           accuracy = accuracy_score(y_test, y_pred)
           precision = precision_score(y_test, y_pred)
           recall = recall_score(y_test, y_pred)
           f1 = f1_score(y_test, y_pred)
           return conf_matrix, accuracy, precision, recall, f1
        def plot_confusion_matrix(conf_matrix):
           plt.figure(figsize=(8, 6))
           sns.heatmap(conf_matrix, annot=True, fmt='d', cmap='Blues', cbar=False
           plt.title('Confusion Matrix')
           plt.xlabel('Predicted Label')
           plt.ylabel('True Label')
           plt.show()
        data, labels = load ising data()
        X_train, X_test, y_train, y_test = train_test_split(data, labels, test_si
```

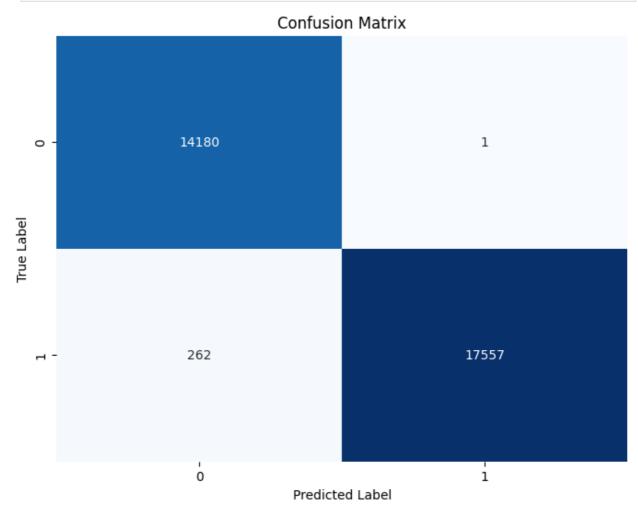
```
scaler = StandardScaler()
X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.transform(X_test)

model = train_random_forest(X_train, y_train)

conf_matrix, accuracy, precision, recall, f1 = evaluate_model(model, X_te)

plot_confusion_matrix(conf_matrix)

metrics_values = [accuracy, precision, recall, f1]
metrics_names = ['Accuracy', 'Precision', 'Recall', 'F1 Score']
plot_evaluation_metrics(metrics_values, metrics_names)
```



/var/folders/0c/p8t8gw0s0nj8\_5tr34fz8mv40000gn/T/ipykernel\_14145/387925142 4.py:52: FutureWarning:

Passing `palette` without assigning `hue` is deprecated and will be remove d in v0.14.0. Assign the `y` variable to `hue` and set `legend=False` for the same effect.

sns.barplot(x=metrics\_values, y=metrics\_names, palette='viridis')
/Users/bilgic/Desktop/fiz437e\_project/project/lib/python3.9/site-packages/
seaborn/\_base.py:949: FutureWarning: When grouping with a length-1 list-li
ke, you will need to pass a length-1 tuple to get\_group in a future versio
n of pandas. Pass `(name,)` instead of `name` to silence this warning.
 data\_subset = grouped\_data.get\_group(pd\_key)

/Users/bilgic/Desktop/fiz437e\_project/project/lib/python3.9/site-packages/seaborn/\_base.py:949: FutureWarning: When grouping with a length-1 list-like, you will need to pass a length-1 tuple to get\_group in a future version of pandas. Pass `(name,)` instead of `name` to silence this warning.

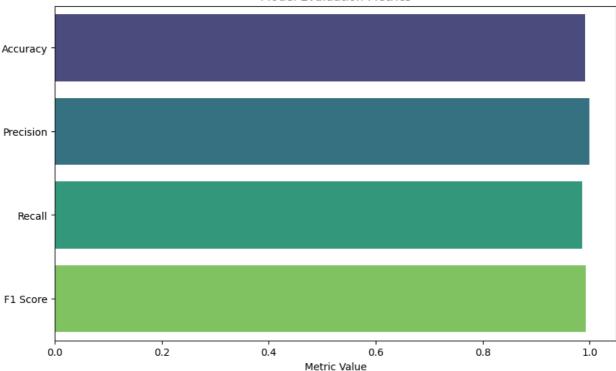
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data\_subset = grouped\_data.get\_group(pd\_key)

#### Model Evaluation Metrics



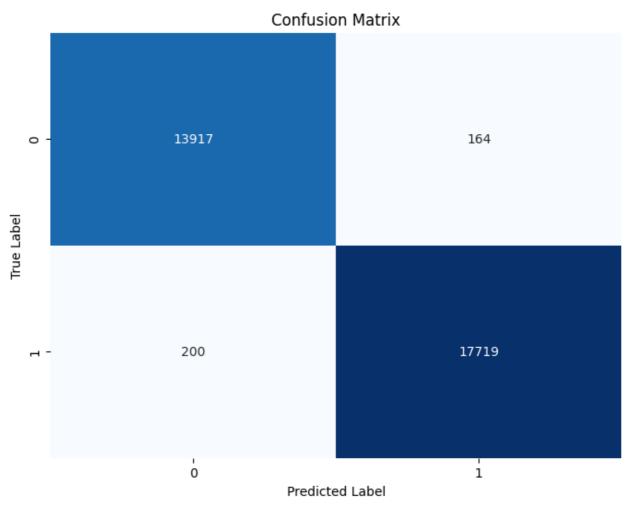
# Multi-Layer Perceptron Classifier (MLP)

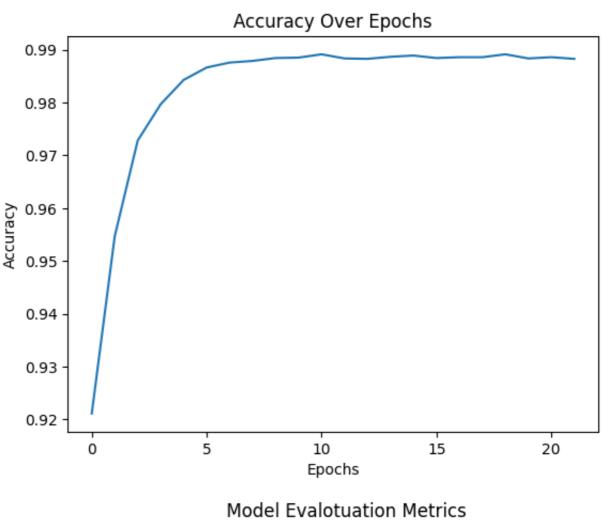
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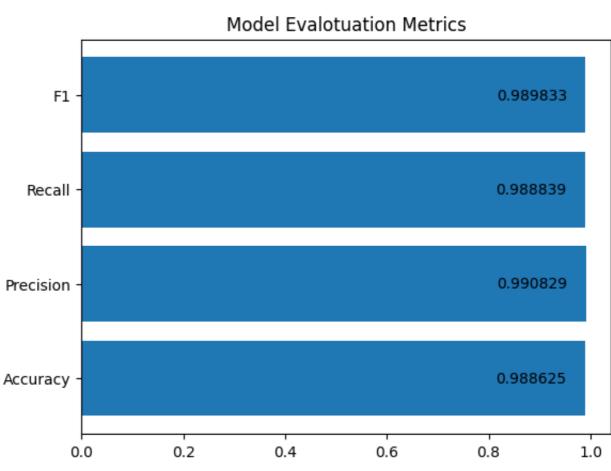
```
In [ ]: import numpy as np
        import seaborn as sns
        import pickle
        import matplotlib.pyplot as plt
        from sklearn.model_selection import train_test_split
        from sklearn.metrics import confusion_matrix, accuracy_score, precision_s
        from sklearn.neural network import MLPClassifier
        def read_t_data(t=0.25, root="../data/"):
            if t > 0.:
                data = pickle.load(open(root+'Ising2DFM_reSample_L40_T=%.2f.pkl'%)
            else:
                data = pickle.load(open(root+'Ising2DFM_reSample_L40_T=All.pkl','
            return np.unpackbits(data).astype(int).reshape(-1,1600)
        def read all data(root="../data/"):
            data = pickle.load(open(root+'Ising2DFM_reSample_L40_T=All.pkl','rb')
            label = pickle.load(open(root+'Ising2DFM_reSample_L40_T=All_labels.pk
            return np.unpackbits(data).astype(int).reshape(-1,1600), label
        data, label = read all data()
        idx = np.random.permutation(len(data))
        data, label = data[idx], label[idx]
        data[data == 0] = -1
        X_train, X_test, y_train, y_test = train_test_split(data, label, test_siz
        def train_MLPClassifier(X_train, y_train):
           model = MLPClassifier(solver='sgd', alpha=1e-3, hidden_layer_sizes=(5,
                                  early_stopping=True)
           model.fit(X_train, y_train)
           return model
        def evaluate_model(model, X_test, y_test):
           y_pred = model.predict(X_test)
           conf_matrix = confusion_matrix(y_test, y_pred)
           accuracy = accuracy_score(y_test, y_pred)
           precision = precision_score(y_test, y_pred)
           recall = recall_score(y_test, y_pred)
           f1 = f1_score(y_test, y_pred)
           return conf_matrix, accuracy, precision, recall, f1
        def plot_confusion_matrix(conf_matrix):
           plt.figure(figsize=(8, 6))
           sns.heatmap(conf_matrix, annot=True, fmt='d', cmap='Blues', cbar=False
           plt.title('Confusion Matrix')
           plt.xlabel('Predicted Label')
           plt.ylabel('True Label')
           plt.show()
```

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```
def plot_evaluation_metrics(metrics_values, metrics_names):
   plt.figure(figsize=(10, 6))
   sns.barplot(x=metrics_values, y=metrics_names, palette='viridis')
   plt.title('Model Evaluation Metrics')
   plt.xlabel('Metric Value')
   plt.show()
model = train_MLPClassifier(X_train, y_train)
conf_matrix, accuracy, precision, recall, f1 = evaluate_model(model, X_te
plot_confusion_matrix(conf_matrix)
plt.plot(model.validation_scores_)
plt.title("Accuracy Over Epochs")
plt.xlabel("Epochs")
plt.ylabel("Accuracy")
plt.show()
fig, ax = plt.subplots()
ax.set_title("Model Evalotuation Metrics")
bars = ax.barh(("Accuracy", "Precision", "Recall", "F1"), (accuracy, prec
ax.bar_label(bars,padding=-60);
plt.show()
```







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# **Convolutional Neural Network (CNN)**

```
In []: # %%
        import numpy as np
        import pickle
        import pandas as pd
        from urllib.request import Request, urlopen
        import matplotlib.pyplot as plt
        from keras.models import Sequential
        from keras.layers import Dense, Conv2D, Flatten, Dropout, MaxPooling2D
        from keras import regularizers, optimizers
        from keras.callbacks import ModelCheckpoint
        from sklearn.model_selection import train_test_split
        from keras.utils import to_categorical
        # %%
        url main = 'https://physics.bu.edu/~pankajm/ML-Review-Datasets/isingMC/'
        # The data consists of 16*10000 samples taken in T=np.arange(0.25,4.0001,
        data_file_name = "Ising2DFM_reSample_L40_T=All.pkl"
        # The labels are obtained from the following file:
        label file name = "Ising2DFM reSample L40 T=All labels.pkl"
        #DATA
        # pickle reads the file and returns the Python object (1D array, compress
        # Decompress array and reshape for convenience
        # map 0 state to -1 (Ising variable can take values +/-1)
        def load_data_from_url(url):
            request = Request(url, headers={'User-Agent': 'Mozilla/5.0'})
            with urlopen(request) as f:
                return pickle.load(f)
        # Load data and labels
        data = load_data_from_url(url_main + data_file_name)
        data = np.unpackbits(data).reshape(-1, 1600)
        data = data.astype('int')
        \#data[np.where(data == 0)] = -1 \# map 0 state to -1
        #LABELS (convention is 1 for ordered states and 0 for disordered states)
        # pickle reads the file and returns the Python object (here just a 1D arr
        labels = load_data_from_url(url_main + label_file_name)
        #labels[labels == 0] = -1 # Map 0 state to -1
        # %%
        # Print the entire data array and its shape
        print("Data Array:\n", data)
        print("Shape of Data Array:", data.shape)
        # Print the entire labels array and its shape
        print("\nLabels Array:\n", labels)
        print("Shape of Labels Array:", labels.shape)
        # Print the first sample from the data array
```

```
print("\nFirst Sample in Data Array:\n", data[0])
# Print the last sample from the data array
print("\nLast Sample in Data Array:\n", data[-1])
# %%
# Calculate magnetization for each sample in the data by taking the mean
mag = np.mean(data, axis=1)
print(f"Shape of Magnetization Array: {mag.shape}")
# Create an array to represent sample sizes
sample_size = np.arange(len(data))
print(f"Shape of Sample Size Array: {sample_size.shape}")
# Create an array to represent temperature
temp_range = np.arange(0.25, 4.25, 0.25)
# Repeat the temperature values to match the length of the data (assuming
tc = np.repeat(temp_range, 10000)
print(f"Temperature Array: {tc}")
print(f"Length of Temperature Array: {len(tc)}, Shape of Temperature Arra
# Plot the 'labels' data with a blue line
plt.plot(labels, c='blue', label='Magnetization')
# Set labels for the x and y axes
plt.xlabel('Samples')
plt.ylabel('Magnetization')
# Set the title of the plot
plt.title('Magnetization vs. Sample Size Labels Plot')
# Add a legend to the plot
plt.legend()
# Add a grid to the plot
plt.grid(True)
# Display the plot
plt.show()
# %%
# Create a DataFrame
df = pd.DataFrame({
    'Data': list(data),
    'Labels': labels.
    'Temperature': tc
})
# %%
# Define a function for slicing the data
def slice_data(df, num_slices):
```

```
# Calculate the size of each slice
    slice_size = len(df) // num_slices
    sliced_data = []  # List to store sliced data
sliced_labels = []  # List to store sliced labels
    sliced_temperatures = [] # List to store sliced temperatures
   # Loop through the specified number of slices
    for i in range(num_slices):
        start_idx = i * slice_size
        end_idx = (i + 1) * slice_size if (i < num_slices - 1) else len(d)
        # Slice the data, labels, and get the unique temperature value fo
        sliced_data.append(df['Data'][start_idx:end_idx].tolist())
        sliced labels.append(df['Labels'][start idx:end idx].tolist())
        sliced_temperatures.append(df['Temperature'][start_idx:end_idx].u
   # Return the sliced data, labels, and temperatures
    return sliced_data, sliced_labels, sliced_temperatures
# Define the number of slices
num_slices = 16
# Apply the slicing function to the DataFrame 'df'
sliced_data, sliced_labels, sliced_temperatures = slice_data(df, num_slic
# Display information about each slice
for i, data_slice in enumerate(sliced_data):
    print(f"Slice {i + 1}:")
    print(f"Data Shape: {np.array(data_slice).shape}")
    print(f"Labels Shape: {np.array(sliced labels[i]).shape}")
    print(f"Temperature Value: {sliced_temperatures[i]}\n")
# %%
# Loop through the slices of data
for i in range(num slices):
    slice_data = np.array(sliced_data[i])
    slice_labels = np.array(sliced_labels[i])
    slice temperature = sliced temperatures[i]
   # Create a DataFrame for the current slice
   df_slice = pd.DataFrame(slice_data)
   df slice['Label'] = slice labels # Add a 'Label' column
   df_slice['Temperature'] = slice_temperature # Add a 'Temperature' co
   # Display information about the DataFrame
    print(f"DataFrame for Slice {i+1}")
   # Print the first few rows of the DataFrame
   print(df slice.head())
   # Print the shape (number of rows and columns) of the DataFrame
    print(f"Shape of Slice {i+1}: {df_slice.shape}\n")
```

```
# %%
import numpy as np
import matplotlib.pyplot as plt
# Define the size of the figure
plt.figure(figsize=(10, 6))
# Loop over the slices of data
for i in range(num slices):
    slice_data = np.array(sliced_data[i])
    slice_labels = np.array(sliced_labels[i])
    slice_temperature = sliced_temperatures[i]
   # Calculate Magnetization
   mag = np.mean(slice_data, axis=1)
   # Plot the Magnetization vs Temperature
    plt.plot([slice_temperature] * len(mag), mag, 'o', label=f'T={slice_t
# Add a vertical line at the critical temperature (2.26K) for reference
plt.axvline(x=2.26, color='red', linestyle='--', label='Critical Temperat
# Set labels for the x and y axes
plt.xlabel('Temperature')
plt.ylabel('Magnetization')
# Set the title of the plot
plt.title('Magnetization vs Temperature for Different Slices')
# Add a legend to the plot
plt.legend()
# Display the plot
plt.show()
# %%
# Create a figure with a specific size
plt.figure(figsize=(10, 6))
# Loop through the slices of data
for i in range(num_slices):
    slice_labels = np.array(sliced_labels[i])
    slice_temperature = sliced_temperatures[i]
   # Create a scatter plot of state (Ordered/Disordered) vs Temperature
    plt.scatter([slice_temperature] * len(slice_labels), slice_labels, al
# Add a vertical dashed red line at the critical temperature (2.26K)
plt.axvline(x=2.26, color='red', linestyle='--', label='Critical Temperat
```

```
# Set labels for the x and y axes
plt.xlabel('Temperature')
plt.ylabel('State (Ordered/Disordered)')
# Set the title of the plot
plt.title('Ordered and Disordered States at Different Temperatures')
# Add a legend to the plot
plt.legend()
# Display the plot
plt.show()
# %%
# Define the critical temperature
critical_temp = 2.26
# Define temperature ranges for the ordered and unordered regions
lower bound ordered = 0.25
upper_bound_ordered = 2.25
lower_bound_unordered = 2.5001
upper_bound_unordered = 4.001
# Separate the data into ordered and unordered regions
ordered data = df[(df['Temperature'] >= lower bound ordered) & (df['Tempe
unordered_data = df[(df['Temperature'] >= lower_bound_unordered) & (df['T
# Define the critical temperature region
critical_data = df[(df['Temperature'] > upper_bound_ordered) & (df['Tempe
# Print the temperature range and the number of data points in the critic
critical_temp_range = (upper_bound_ordered, lower_bound_unordered)
critical_data_count = len(critical_data)
print(f"Critical Temperature Region: {critical_temp_range}")
print(f"Number of Data Points in Critical Temperature Region: {critical_d
# %%
# Print the temperature range and the number of data points for the order
ordered_temp_range = (lower_bound_ordered, upper_bound_ordered)
ordered_data_count = len(ordered_data)
print(f"Ordered Data Temperature Range: {ordered temp range}")
print(f"Number of Ordered Data Points: {ordered_data_count}")
# Print the temperature range and the number of data points for the unord
unordered_temp_range = (lower_bound_unordered, upper_bound_unordered)
unordered_data_count = len(unordered_data)
print(f"Unordered Data Temperature Range: {unordered_temp_range}")
print(f"Number of Unordered Data Points: {unordered_data_count}")
# %%
```

```
# After splitting the ordered data, check the dimensions
x_ordered_train, x_ordered_test, y_ordered_train, y_ordered_test = train_
    ordered_data['Data'].values, ordered_data['Labels'].values, random_st
# Print the dimensions to ensure the data is split correctly
print("Ordered Data Set:")
print(f"x ordered train.shape: {x ordered train.shape}")
print(f"x_ordered_test.shape: {x_ordered_test.shape}")
print(f"y_ordered_train.shape: {y_ordered_train.shape}")
print(f"y_ordered_test.shape: {y_ordered_test.shape}")
# After splitting the unordered data, check the dimensions
x_unordered_train, x_unordered_test, y_unordered_train, y_unordered_test
    unordered_data['Data'].values, unordered_data['Labels'].values, rando
# Print the dimensions to ensure the data is split correctly
print("\nUnordered Data Set:")
print(f"x_unordered_train.shape: {x_unordered_train.shape}")
print(f"x_unordered_test.shape: {x_unordered_test.shape}")
print(f"y_unordered_train.shape: {y_unordered_train.shape}")
print(f"y_unordered_test.shape: {y_unordered_test.shape}")
# %%
# Define the critical temperature
critical temp = 2.26
# Define temperature ranges for the ordered and unordered regions
lower_bound_ordered = 0.25
upper bound ordered = 2.25
lower_bound_unordered = 2.5001
upper_bound_unordered = 4.001
# Separate the data into ordered and unordered regions
ordered_data = df[(df['Temperature'] >= lower_bound_ordered) & (df['Tempe
unordered_data = df[(df['Temperature'] >= lower_bound_unordered) & (df['T
# Define the critical temperature region
critical_data = df[(df['Temperature'] > upper_bound_ordered) & (df['Tempe
# Set a flag to determine whether to split the data
split = True
# Split the data based on the 'split' flag
if split:
   x_critical_train, x_critical_test, y_critical_train, y_critical_test
        critical_data['Data'].values, critical_data['Labels'].values, ran
else:
   x_critical_train, x_critical_test = critical_data['Data'].values, Non
   y_critical_train, y_critical_test = critical_data['Labels'].values, N
# Split the ordered and unordered data into training and testing sets
x_ordered_train, x_ordered_test, y_ordered_train, y_ordered_test = train_
```

```
ordered data['Data'].values, ordered data['Labels'].values, random st
x_unordered_train, x_unordered_test, y_unordered_train, y_unordered_test
    unordered_data['Data'].values, unordered_data['Labels'].values, rando
# Print the results
print("Critical Region Data:")
print(f"x_critical_train.shape: {x_critical_train.shape}")
print(f"x_critical_test.shape: {x_critical_test.shape if split else 'Not
print(f"y_critical_train.shape: {y_critical_train.shape}")
print(f"y_critical_test.shape: {y_critical_test.shape if split else 'Not
print("\nOrdered Data:")
print(f"x ordered train.shape: {x ordered train.shape}")
print(f"x_ordered_test.shape: {x_ordered_test.shape}")
print(f"y_ordered_train.shape: {y_ordered_train.shape}")
print(f"y_ordered_test.shape: {y_ordered_test.shape}")
print("\nUnordered Data:")
print(f"x_unordered_train.shape: {x_unordered_train.shape}")
print(f"x_unordered_test.shape: {x_unordered_test.shape}")
print(f"y_unordered_train.shape: {y_unordered_train.shape}")
print(f"y_unordered_test.shape: {y_unordered_test.shape}")
# %%
# Concatenate the training sets from the ordered and unordered regions
x_train = np.concatenate((x_ordered_train, x_unordered_train))
y_train = np.concatenate((y_ordered_train, y_unordered_train))
# Concatenate the test sets from the ordered and unordered regions
x_test = np.concatenate((x_ordered_test, x_unordered_test))
y_test = np.concatenate((y_ordered_test, y_unordered_test))
# Print the shapes of the combined sets
print("Combined Training Set:")
print(f"x_train shape: {x_train.shape}")
print(f"y train shape: {y train.shape}")
print("\nCombined Test Set:")
print(f"x_test shape: {x_test.shape}")
print(f"y_test shape: {y_test.shape}")
# Specify the value of L
L = 40
# Initialize lists to store the reshaped images
x train images = []
x_{\text{test_images}} = []
# Reshape the combined training set
```

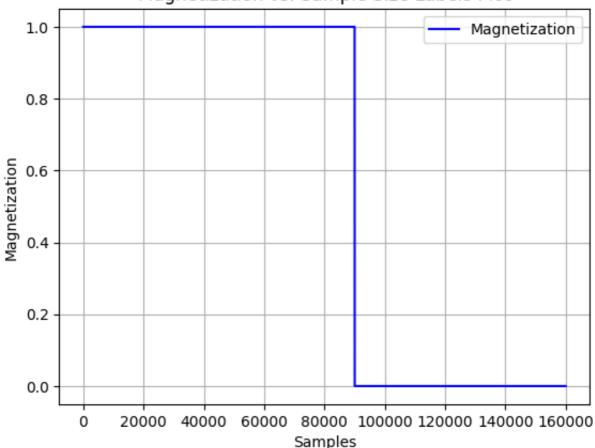
```
for i in range(x train.shape[0]):
    image = x_train[i].reshape(L, L, 1)
    x_train_images.append(image)
# Reshape the combined test set
for i in range(x test.shape[0]):
    image = x_test[i].reshape(L, L, 1)
    x_test_images.append(image)
# Convert the lists to numpy arrays
x_train_images = np.array(x_train_images)
x_test_images = np.array(x_test_images)
# Check the dimensions of the reshaped data
print("Combined Non-Critical Training Set:")
print(f"x_train_images.shape: {x_train_images.shape}")
print("Combined Non-Critical Test Set:")
print(f"x_test_images.shape: {x_test_images.shape}")
# %%
from tensorflow.keras import layers, models
# Define the CNN model
model = models.Sequential()
# Convolutional Layer 1
model.add(layers.Conv2D(3, (3, 3), activation='tanh', input_shape=(L, L,
# You can uncomment the following lines to add max-pooling and additional
# model.add(layers.MaxPooling2D((2, 2)))
# Convolutional Layer 2 (You can uncomment this section if needed)
# model.add(layers.Conv2D(64, (3, 3), activation='relu'))
# model.add(layers.MaxPooling2D((2, 2)))
# Convolutional Layer 3 (You can uncomment this section if needed)
# model.add(layers.Conv2D(64, (3, 3), activation='relu'))
# Flatten the output
model.add(layers.Flatten())
model.add(layers.Dropout(0.5)) # Dropout layer to reduce overfitting
# Fully Connected Layers (You can uncomment this section if needed)
# model.add(layers.Dense(64, activation='relu'))
# Output layer for binary classification
model.add(layers.Dense(1, activation='sigmoid'))
# Compile the model with optimizer, loss function, and metrics
model.compile(optimizer='adam',
              loss='binary_crossentropy',
              metrics=['accuracy'])
```

```
# Print model summary
model.summary()
# %%
# Train the model using training data and labels and obtain the history o
history = model.fit(x_train_images, y_train,
                    epochs=3, # Number of training epochs
                    validation_split=0.1) # 10% validation split
# %%
# Test the model on test data and labels
score = model.evaluate(x_test_images, y_test, verbose=0)
# Print the test loss and test accuracy
print(f"Test Loss: {score[0]:.4f}")
print(f"Test Accuracy: {score[1]:.4f}")
# %%
# Create a figure with two subplots side by side
fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(12, 5))
# Plot training & validation loss values
ax1.plot(history.history['loss'], label='Train')
ax1.plot(history.history['val_loss'], label='Validation')
ax1.set_title('Model Loss')
ax1.set xlabel('Epoch')
ax1.set_ylabel('Loss')
ax1.legend(loc='upper right')
# Plot training & validation accuracy values
ax2.plot(history.history['accuracy'], label='Train')
ax2.plot(history.history['val_accuracy'], label='Validation')
ax2.set_title('Model Accuracy')
ax2.set xlabel('Epoch')
ax2.set ylabel('Accuracy')
ax2.legend(loc='lower right')
# Adjust spacing between subplots
plt.tight_layout()
# Show the plot
plt.show()
```

/Users/bilgic/Desktop/fiz437e\_project/project/lib/python3.9/site-packages/urllib3/\_\_init\_\_.py:34: NotOpenSSLWarning: urllib3 v2 only supports OpenSS L 1.1.1+, currently the 'ssl' module is compiled with 'LibreSSL 2.8.3'. Se e: https://github.com/urllib3/urllib3/issues/3020 warnings.warn(

```
Data Array:
 [[0 0 0 ... 0 0 0]
 [1 1 1 ... 1 1 1]
 [1 1 1 ... 1 1 1]
 [1 \ 1 \ 1 \ \dots \ 1 \ 1 \ 0]
 [1 \ 1 \ 1 \ \dots \ 1 \ 0 \ 0]
 [1 1 1 ... 1 0 0]]
Shape of Data Array: (160000, 1600)
Labels Array:
 [1 \ 1 \ 1 \ \dots \ 0 \ 0 \ 0]
Shape of Labels Array: (160000,)
First Sample in Data Array:
 [0 0 0 ... 0 0 0]
Last Sample in Data Array:
 [1 1 1 ... 1 0 0]
Shape of Magnetization Array: (160000,)
Shape of Sample Size Array: (160000,)
Temperature Array: [0.25 0.25 0.25 ... 4.
                                                4.
                                                      4. ]
Length of Temperature Array: 160000, Shape of Temperature Array: (160000,)
```

# Magnetization vs. Sample Size Labels Plot



Slice 1:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 0.25

#### Slice 2:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 0.5

#### Slice 3:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 0.75

### Slice 4:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 1.0

#### Slice 5:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 1.25

### Slice 6:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 1.5

### Slice 7:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 1.75

#### Slice 8:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 2.0

#### Slice 9:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 2.25

# Slice 10:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 2.5

# Slice 11:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 2.75

#### Slice 12:

Data Shape: (10000, 1600)

Labels Shape: (10000,) Temperature Value: 3.0

Slice 13:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 3.25

Slice 14:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 3.5

Slice 15:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 3.75

Slice 16:

Data Shape: (10000, 1600) Labels Shape: (10000,) Temperature Value: 4.0

DataFrame for Slice 1

	0	1	2	3	4	5	6	7	8	9	 1592	1593	1594	1595	1596	1597
\																
0	0	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0
1	1	1	1	1	1	1	1	1	1	1	 1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1	1	 1	1	1	1	1	1
3	1	1	1	1	1	1	1	1	1	1	 1	1	1	1	1	1
4	1	1	1	1	1	1	1	1	1	1	 1	1	1	1	1	1

	1598	1599	Label	lemperature
0	0	0	1	0.25
1	1	1	1	0.25
2	1	1	1	0.25
3	1	1	1	0.25
4	1	1	1	0.25

[5 rows x 1602 columns]

Shape of Slice 1: (10000, 1602)

DataF	ram	e f	or	Sli	ce	2	
_	-	_	_	4	_		,

0	1	2	3	4	5	6	7	8	9		1592	1593	1594	1595	1596	1597
1	1	1	1	1	1	1	1	1	1		1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1		1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1		1	1	1	1	1	1
0	0	0	0	0	0	0	0	0	0		0	0	0	0	0	0
1	1	1	1	1	1	1	1	1	1		1	1	1	1	1	1
	1 1 1 0	1 1 1 1 1 1 0 0	1 1 1 1 1 1 1 1 1 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 0 0	1 0 0 0 0	1     1     1     1     1     1     1     1     1       1     1     1     1     1     1     1     1       1     1     1     1     1     1     1     1     1       1     1     1     1     1     1     1     1     1       0     0     0     0     0     0     0     0	1     1     1     1     1     1     1     1     1     1       1     1     1     1     1     1     1     1     1       1     1     1     1     1     1     1     1     1     1       1     1     1     1     1     1     1     1     1     1       0     0     0     0     0     0     0     0     0     0	1     1 <td>1     1<td>1     1<td>1     1<td>1       1</td><td>1       1</td><td>0       1       2       3       4       5       6       7       8       9        1592       1593       1594       1595       1596         1</td></td></td></td>	1     1 <td>1     1<td>1     1<td>1       1</td><td>1       1</td><td>0       1       2       3       4       5       6       7       8       9        1592       1593       1594       1595       1596         1</td></td></td>	1     1 <td>1     1<td>1       1</td><td>1       1</td><td>0       1       2       3       4       5       6       7       8       9        1592       1593       1594       1595       1596         1</td></td>	1     1 <td>1       1</td> <td>1       1</td> <td>0       1       2       3       4       5       6       7       8       9        1592       1593       1594       1595       1596         1</td>	1       1	1       1	0       1       2       3       4       5       6       7       8       9        1592       1593       1594       1595       1596         1

1598 1599 Label Temperature 0 1 1 1 0.5

```
1
        1
                1
                         1
                                        0.5
2
        1
                1
                         1
                                        0.5
3
        0
                0
                         1
                                        0.5
4
        1
                1
                         1
                                        0.5
```

[5 rows x 1602 columns] Shape of Slice 2: (10000, 1602)

```
DataFrame for Slice 3
        1
            2
                3
                    4
                             6
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                                                             1593
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                                                                                       1596
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```

Label Temperature 0.75 0.75 0.75 0.75 0.75

[5 rows x 1602 columns] Shape of Slice 3: (10000, 1602)

DataFrame for Slice 4 . . . . . . 

Label Temperature 1.0 1.0 1.0 1.0 1.0

[5 rows x 1602 columns] Shape of Slice 4: (10000, 1602)

DataFrame for Slice 5 . . . 

```
0
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   1598
           1599
                           Temperature
                  Label
0
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                       1
                                    1.25
       1
                                    1.25
1
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2
       0
                       1
                                    1.25
               0
3
       0
               0
                       1
                                    1.25
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                                    1.25
4
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[5 rows x 1602 columns]
Shape of Slice 5: (10000, 1602)
DataFrame for Slice 6
       1
              3
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           1599
                  Label
                           Temperature
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[5 rows x 1602 columns]
Shape of Slice 6: (10000, 1602)
DataFrame for Slice 7
                  4
       1
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                             7
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3
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                       1
                                    1.75
4
       0
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                                    1.75
[5 rows x 1602 columns]
Shape of Slice 7: (10000, 1602)
DataFrame for Slice 8
           2
              3 4
                      5
                         6
                            7
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```

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           1599
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3
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[5 rows x 1602 columns]
Shape of Slice 8: (10000, 1602)
DataFrame for Slice 9
                   4
        1
           2
               3
                       5
                           6
                               7
                                   8
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                   Label
                            Temperature
0
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                                      2.25
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2
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3
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                                      2.25
        1
               1
                         1
                                      2.25
[5 rows x 1602 columns]
Shape of Slice 9: (10000, 1602)
DataFrame for Slice 10
        1
           2
               3
                   4
                       5
                           6
                               7
                                   8
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4
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    1598
           1599
                   Label
                            Temperature
```

2.5

2.5

2.5

2.5

2.5

[5 rows x 1602 columns]

Shape of Slice 10: (10000, 1602)

```
DataFrame for Slice 11
                3
                    4
                                7
                                    8
                                        9
                                                  1592
                                                           1593
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                                                                                           1597
            2
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2
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4
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    1598
            1599
                    Label
                             Temperature
0
        1
                1
                         0
                                      2.75
        1
                                      2.75
1
                1
                         0
2
        0
                0
                         0
                                      2.75
3
        0
                0
                         0
                                      2.75
        1
                1
                         0
                                      2.75
[5 rows x 1602 columns]
Shape of Slice 11: (10000, 1602)
DataFrame for Slice 12
        1
            2
                3
                    4
                        5
                            6
                                7
                                    8
                                        9
                                                  1592
                                                           1593
                                                                   1594
                                                                           1595
                                                                                   1596
                                                                                           1597
0
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3
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            1
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                            1
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4
        1
            1
                    0
                            1
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    1
                0
                        0
                                    1
                                        1
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                                                       1
    1598
            1599
                    Label
                             Temperature
0
        0
                0
                                        3.0
                         0
1
        1
                1
                         0
                                        3.0
2
        1
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                         0
                                        3.0
3
        0
                1
                         0
                                        3.0
        1
                1
                         0
                                        3.0
[5 rows x 1602 columns]
Shape of Slice 12: (10000, 1602)
DataFrame for Slice 13
            2
                    4
                                7
        1
                3
                        5
                            6
                                    8
                                        9
                                                  1592
                                                           1593
                                                                   1594
                                                                           1595
                                                                                   1596
                                                                                           1597
0
    1
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2
    1
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                    1
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3
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                        0
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4
        1
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                    0
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                                                                                       0
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    1
                0
                                                       1
    1598
                             Temperature
            1599
                    Label
0
        1
                1
                         0
                                      3.25
        0
1
                0
                         0
                                      3.25
2
        1
                1
                         0
                                      3.25
3
        1
                1
                         0
                                       3.25
```

1598 1599 Label Temperature

1 0

0 0

1 1

0 0 0 1 0

2 0 0

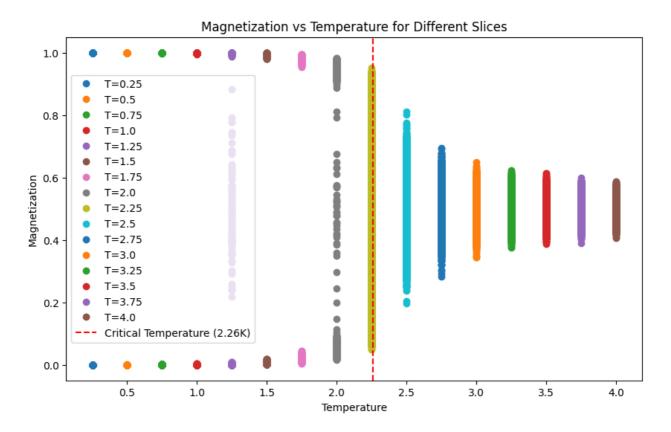
3 1 0 1 1 1 0 1 1 1 0

0 1

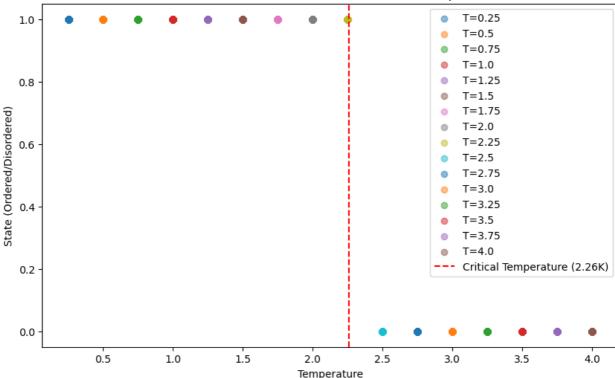
0	0	0	0	4.0
1	1	1	0	4.0
2	0	0	0	4.0
3	1	1	0	4.0
4	1	0	0	4.0

[5 rows x 1602 columns]

Shape of Slice 16: (10000, 1602)



### Ordered and Disordered States at Different Temperatures



Critical Temperature Region: (2.25, 2.5001)

Number of Data Points in Critical Temperature Region: 10000

Ordered Data Temperature Range: (0.25, 2.25)

Number of Ordered Data Points: 90000

Unordered Data Temperature Range: (2.5001, 4.001)

Number of Unordered Data Points: 60000

Ordered Data Set:

x\_ordered\_train.shape: (67500,)

x\_ordered\_test.shape: (22500,)

y\_ordered\_train.shape: (67500,)

y\_ordered\_test.shape: (22500,)

#### Unordered Data Set:

x\_unordered\_train.shape: (45000,)

x\_unordered\_test.shape: (15000,)

y\_unordered\_train.shape: (45000,)

y\_unordered\_test.shape: (15000,)

Critical Region Data:

x\_critical\_train.shape: (7500,)

x\_critical\_test.shape: (2500,)

y\_critical\_train.shape: (7500,)

y\_critical\_test.shape: (2500,)

# Ordered Data:

x\_ordered\_train.shape: (67500,)

x\_ordered\_test.shape: (22500,)

y\_ordered\_train.shape: (67500,)

y\_ordered\_test.shape: (22500,)

#### Unordered Data:

x\_unordered\_train.shape: (45000,)

x\_unordered\_test.shape: (15000,)
y\_unordered\_train.shape: (45000,)
y\_unordered\_test.shape: (15000,)

Combined Training Set:
x\_train shape: (112500,)
y\_train shape: (112500,)

Combined Test Set: x\_test shape: (37500,) y\_test shape: (37500,)

Combined Non-Critical Training Set:
x\_train\_images.shape: (112500, 40, 40, 1)

Combined Non-Critical Test Set:

x\_test\_images.shape: (37500, 40, 40, 1)

Model: "sequential"

Layer (type)	Output Shape	Param #
conv2d (Conv2D)	(None, 38, 38, 3)	30
flatten (Flatten)	(None, 4332)	0
dropout (Dropout)	(None, 4332)	0
dense (Dense)	(None, 1)	4333

\_\_\_\_\_

Total params: 4363 (17.04 KB)
Trainable params: 4363 (17.04 KB)
Non-trainable params: 0 (0.00 Byte)

2024-01-23 22:25:53.593117: I metal\_plugin/src/device/metal\_device.cc:115

4] Metal device set to: Apple M2

2024-01-23 22:25:53.593185: I metal\_plugin/src/device/metal\_device.cc:296]

systemMemory: 8.00 GB

2024-01-23 22:25:53.593200: I metal\_plugin/src/device/metal\_device.cc:313]

maxCacheSize: 2.67 GB

2024-01-23 22:25:53.593538: I tensorflow/core/common\_runtime/pluggable\_device/pluggable\_device\_factory.cc:306] Could not identify NUMA node of platf orm GPU ID 0, defaulting to 0. Your kernel may not have been built with NU MA support.

2024-01-23 22:25:53.593917: I tensorflow/core/common\_runtime/pluggable\_device/pluggable\_device\_factory.cc:272] Created TensorFlow device (/job:local host/replica:0/task:0/device:GPU:0 with 0 MB memory) -> physical Pluggable Device (device: 0, name: METAL, pci bus id: <undefined>)

Epoch 1/3

2024-01-23 22:25:55.543639: I tensorflow/core/grappler/optimizers/custom\_g raph\_optimizer\_registry.cc:117] Plugin optimizer for device\_type GPU is enabled.

