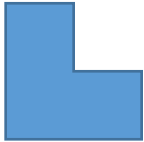


Geometric Puzzle

Definition of the puzzle

An interior designer is commissioned to cover a wall of a computer scientist's home with tiles. The shape of the wall is a square of size 2^n by 2^n . Computer scientist suggests to use L shaped tiles of size 2 by 2. Since 2^{n+1} cannot be evenly divided by 3 (i.e., the area of the L shaped tile) computer scientist also allows designer to use one 1x1 tile. He also would like to initiate tiling by placing the 1x1 tile randomly.



An L-shaped tile

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| 3 | 3 | 4 | 4 | 9 | 9 | 10 | 10 |
| 3 | 2 | 2 | 4 | 9 | 8 | 8 | 10 |
| 5 | 2 | 1 | 1 | 7 | 7 | 8 | 11 |
| 5 | 5 | | 1 | 6 | 7 | 11 | 11 |
| 19 | 19 | 17 | 6 | 6 | 12 | 14 | 14 |
| 19 | 18 | 17 | 17 | 12 | 12 | 13 | 14 |
| 21 | 18 | 18 | 20 | 16 | 13 | 13 | 15 |
| 21 | 21 | 20 | 20 | 16 | 16 | 15 | 15 |

8x8 wall with randomly selected initial 1x1 tile.

The numbers are indicating both L-shaped tiles and their placing order depending on a algorithm that the interior designer come up with. (This algorithm may not be the only one!)

- a) Find an algorithm to cover the wall.
- b) Write a program in C to find solution for such an operation. Input is coordinate of 1x1 tile and the output is a matrix representing the wall covered by tiles.
 - I. Design and implement the program for 8x8 wall
 - II. Generalize them for wall size $2^n \times 2^n$.