

Homework 1 Part 2 CSE 246 Analysis of Algorithms, Spring 2018

1.(a) An array $A[0..n-2]$ contains $n-1$ integers from 1 to n in increasing order. (Thus one integer in the range is missing.) Design the most efficient algorithm you can to find the missing integer and indicate its time efficiency.

Answer : Since array A is sorted , binary search implementation can be used to find missing number.

```

find_missing(A[0...n-2])
    int middle = floor (length/2) //length :length of array A
    int left_side = middle - 0 //number of integers that is less than minimum middle index (left part)
    int right_side = length - middle - 1 // number of integers that is greater than middle index (right part)
    int right_middle = 0 // middle index of the left part
    int left_middle = 0 //middle index of the right part

    //If the left side is greater than right side , the missing number is in the right part
    if (left_side > right_side)
    {
        while ( middle < length )
        {
            right_middle = (length - middle) / 2
            middle =middle + right_middle
        }

    }

    //If the right side is greater than left side , the missing number is in the left part
    else if (left_side < right_side)
    {
        while (middle >= left_middle)
        {
            left_middle = (middle -length) / 2
            middle = middle - left_middle
        }

    }

    else return -1
return middle // gives the missing number .

```

Time efficiency of this algorithm is $\Theta(\log n)$.

1.(b) Repeat (a) for an unsorted array (instead of an array in increasing order).

Answer : To find missing number ,first array A is sorted with MergeSort and same algorithm in section (a) is used for finding missing number in this array . Time efficiency will be $\Theta(n \log n)$.

2. For each of the following problems design a divide-and-conquer algorithm. Code your algorithm in a programming language of your choice. For each of the problem give the following:

i. Step-by-step description of your algorithm.

ii. Code (No need to give in a separate file, just a printed copy inside the HW report)

iii. At least three sample input/output.

(a) Problem 1: Consider an integer list $A[0..n-1]$ that includes negative and positive integers. Among all subsequences in this list, find the sum of the subsequence that has largest sum.

Answer : For this problem, first a binary tree is built, a middle element of the array A is set as root of this tree, then rest of the elements will be placed in binary tree. After that, right nodes of this tree is sum. If the right tree has only left child, then this node will be picked too. To see the code of this algorithm with detail, see the Codes – Inputs and Outputs, 2.a part.

(b) Problem 2: Consider an integer list $A[0..n-1]$ that includes negative and positive integers. Find the longest all-negative subsequence

Answer : For this problem, array A is divided into two parts which are left and right. In each part, longest path are checked, after that middle element is checked. If the middle element of array A is negative number and next and previous elements are negatives, this means, the longest path begins from left side and ends in the right part. To count max element To see the code of this algorithm with detail, see the Codes – Inputs and Outputs, 2.b part.

(c) Problem 3: Consider a binary list $B[0..n-1]$ that includes 0's and 1's. Find the length of the longest alternating subsequence 010101.....

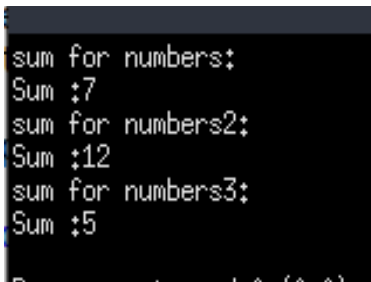
Answer : Solution of this problem is similar as problem two. The array B is divided into two parts which are left and right. In each part, longest alternating path are checked, after that middle element is checked. If the middle element of array A is different from the next and previous element, the longest path may begin from left side and ends in the right part. To see the code of this algorithm with detail, see the Codes – Inputs and Outputs, 2.c part.

3. Let $A = \{ a_1, \dots, a_n \}$ and $B = \{ b_1, \dots, b_m \}$ be two sets of numbers and $m=n^2$. Consider the problem of finding their intersection, i.e., the set C of all the numbers that are in both A and B . Design an efficient algorithm for solving this problem and determine its efficiency class in terms of n .

Answer : For this problem, first, Array A is sorted with MergeSort algorithm, then each element of array B is searched in array A by using binary search algorithm. Time efficiency of this algorithm to solve this problem is $\Theta(n^2 \log n)$.

Codes – Inputs and Outputs**2.a****Inputs :**

numbers [8] = {-2,-5,6,-2,-3,1,5,-6};
numbers2 [9] = {-2,-5,6,-2,-3,1,5,5,-8};
numbers3 [6] = {-2,-2,-3,1,5,4};

Outputs :

```
sum for numbers:
Sum :7
sum for numbers2:
Sum :12
sum for numbers3:
Sum :5
```

Code :

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>

struct treeNode {
    struct treeNode *leftPtr; /* pointer to left subtree */
    int data; /* node value */
    struct treeNode *rightPtr; /* pointer to right subtree */
}; /* end structure treeNode */
typedef struct treeNode TreeNode; /* synonym for struct treeNode */
typedef TreeNode *TreeNodePtr; /* synonym for TreeNode* */
/* prototypes */
void insertNode( TreeNodePtr *treePtr, int value );
void inOrder( TreeNodePtr treePtr );
void preOrder( TreeNodePtr treePtr );
void postOrder( TreeNodePtr treePtr );

int main( void ){
    int i; /* counter to loop for construct binary tree */
    TreeNodePtr rootPtr = NULL; /* tree initially empty */
    TreeNodePtr root2Ptr = NULL; /* tree initially empty */
    TreeNodePtr root3Ptr = NULL; /* tree initially empty */

    //Middle element of the arrays
    int numbers [8] = {-2,-5,6,-2,-3,1,5,-6};
    int length = sizeof(numbers)/sizeof(int);
    int pivot = ceil(length/2);
```

```
int numbers2 [9] = {-2,-5,6,-2,-3,1,5,5,-8};
int length2 = sizeof(numbers2)/sizeof(int);
int pivot2 = ceil(length2/2);
```

```
int numbers3 [6] = {-2,-2,-3,1,5,4};
int length3 = sizeof(numbers3)/sizeof(int);
int pivot3 = ceil(length3/2);
```

```
//middle element is put to the root of the binary search tree
```

```
insertNode(&rootPtr,numbers[pivot]);
insertNode(&root2Ptr,numbers2[pivot2]);
insertNode(&root3Ptr,numbers3[pivot3]);
```

```
//Adding elements of the arrays in a binary Search Tree
```

```
for ( i = 0; i < length; i++ ){
    if (i != pivot)
        insertNode( &rootPtr, numbers[i] );
}
```

```
for ( i = 0; i < length2; i++ ){
    if (i != pivot2)
        insertNode( &root2Ptr, numbers2[i] );
}
```

```
for ( i = 0; i < length3; i++ ){
    if (i != pivot2)
        insertNode( &root3Ptr, numbers3[i] );
}
```

```
printf("sum for numbers:\n");
find_max_sum(rootPtr);
```

```
printf("sum for numbers2:\n");
find_max_sum(root2Ptr);
```

```
printf("sum for numbers3:\n");
find_max_sum(root3Ptr);
return 0;
}
```

```
//This method finds the sum of the subsequence that has largest sum .
```

```
void find_max_sum (TreeNodePtr treeptr)
{
    if (treeptr != NULL) //The tree is not empty
    {
        int sum = 0;
        while (treeptr != NULL)
```

```

{
sum += treeptr->data;
//If the right child of the node is empty but still has a left child , this element will be
//added to sum.
if(treeptr->rightPtr == NULL && treeptr->leftPtr != NULL)
{
//Elements of
treeptr = treeptr->leftPtr;
sum += treeptr->data; }
treeptr = treeptr->rightPtr; }
printf("Sum :%d \n",sum); }
else //If the tree is empty
{
printf("Tree is empty \n");
return -1; }
}

void insertNode( TreeNodePtr *treePtr, int value ) {
/* if tree is empty */
if ( *treePtr == NULL ) {
*treePtr = malloc( sizeof( TreeNode ) );
/* if memory was allocated then assign data */
if ( *treePtr != NULL ) {
( *treePtr )->data = value;
( *treePtr )->leftPtr = NULL;
( *treePtr )->rightPtr = NULL;
} /* end if */
else {
printf( "%d not inserted. No memory available.\n", value );
} /* end else */
} /* end if */
else { /* tree is not empty */
/* data to insert is less than data in current node */
if ( value <= ( *treePtr )->data ) {
insertNode( &( ( *treePtr )->leftPtr ), value );
} /* end if */
/* data to insert is greater than data in current node */
else {
insertNode( &( ( *treePtr )->rightPtr ), value );
} /* end else if */
} /* end else */
} /* end function insertNode */

```

2.b

Inputs:

numbers [10] = {2,5,0,3,5,0,10,2,1,2};

numbers1 [10] = {2,5,0,-3,-5,0,-1,-2,-1,2};

numbers2 [10] = {2,5,0,-3,-5,-3,-1,-2,-1,2};

Outputs:

```
Length of longest negative path for numbers is :0
Length of longest negative path for numbers1 is :3
Length of longest negative path for numbers2 is :6
```

Code:

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>

int main( void )
{
//Inputs and outputs
int numbers [10] = {2,5,0,3,5,0,10,2,1,2};
int length = sizeof(numbers)/sizeof(int);
printf("Length of longest negative path for numbers is :%d \n",longest_negative_path(numbers,length));

int numbers1 [10] = {2,5,0,-3,-5,0,-1,-2,-1,2};
int length1 = sizeof(numbers1)/sizeof(int);
printf("Length of longest negative path for numbers1 is :%d
\n",longest_negative_path(numbers1,length1));

int numbers2 [10] = {2,5,0,-3,-5,-3,-1,-2,-1,2};
int length2 = sizeof(numbers2)/sizeof(int);
printf("Length of longest negative path for numbers2 is :%d
\n",longest_negative_path(numbers2,length1));

return 0;
}

/*middle = middle element of index of the array
max_l = longest negative path of left path
max_r = longest negative path of right path
c_left = counter for negative path in the left side of the array
c_right = counter for negative path in the right side of the array
max_total = longest negative path in this array*/

int longest_negative_path (int number [] , int length)
{
int i;
int middle = ceil(length/2);
int max_l = 0, max_r = 0,c_left=0,c_right=0 , max_total;

//Finds longest negative path in left part , number [0 to middle]

for (i= 0;i<middle;i++)
{
```

```
if (number[i] < 0 && number [i+1] <0)
{
    c_left ++;
    if (c_left > max_l) //If there is a corrupted negative path , max_l will keep previous longest negative path
        max_l = c_left;
}
else
{
    c_left = 0; //If a positive number comes next element , counter will be set to 0.
}
}

//Finds longest negative path in right part , number [middle to length]

for (i= middle+1;i<length;i++)
{
    if (number[i] < 0 && number [i+1] <0)
    {
        c_right ++;
        if (c_right > max_r)
            max_r = c_right; //If there is a corrupted negative path , max_l will keep previous longest negative path
    }

    else
    {
        c_right = 0; //If a positive number comes next element , counter will be set to 0.
    }
}

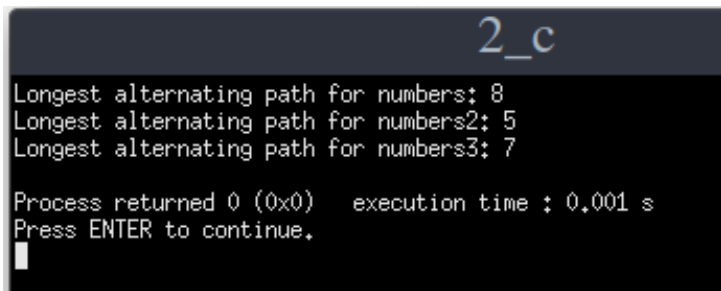
/*Middle element of the array is checked , if it is a negative number
next and previous of the elements will be checked to see whether
they are negative or not .If the condition is provided , then negative path
begins from left part and ends in right path*/

/*If the longest path is in the left part , then max_l will be longest path*/
/*If the longest path is in the right part , then max_r will be longest path*/
if (number[middle] < 0 && number[middle-1] < 0 && number[middle+1] <0)
    max_total = max_l + max_r + 2;
else
{
    if (max_l > max_r)
        max_total = max_l + 1;
    else if (max_l == 0 && max_r == 0)
        max_total = 0;
    else
        max_total = max_r + 1 ;
}

return max_total;
}
```

2.c**Inputs:**

```
int numbers[15] = {0, 1, 0, 1, 0, 0, 0, 1, 0,1,0,1,0,1,1};  
int numbers2 [8] = {1, 1, 1, 0,1 ,0 , 1, 1};  
int numbers3 [15] = {0, 1, 0, 1, 0, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1};
```

Outputs:

```
2_c  
Longest alternating path for numbers: 8  
Longest alternating path for numbers2: 5  
Longest alternating path for numbers3: 7  
  
Process returned 0 (0x0)   execution time : 0.001 s  
Press ENTER to continue.  
█
```

Code :

```
#include <stdio.h>  
#include <stdlib.h>  
#include <math.h>  
  
//2. question part c  
  
int main( void )  
{  
  
    //Inputs and outputs  
    int numbers[15] = {0, 1, 0, 1, 0, 0, 0, 1, 0,1,0,1,0,1,1};  
    int length = sizeof(numbers)/sizeof(int);  
    printf("Longest alternating path for numbers: %d\n",longest_alternating_path(numbers,length));  
  
    int numbers2 [8] = {1, 1, 1, 0,1 ,0 , 1, 1};  
    int length2 = sizeof(numbers2)/sizeof(int);  
    printf("Longest alternating path for numbers2: %d\n",longest_alternating_path(numbers2,length2));  
  
    int numbers3 [15] = {0, 1, 0, 1, 0, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1};  
    int length3 = sizeof(numbers3)/sizeof(int);  
    printf("Longest alternating path for numbers3: %d\n",longest_alternating_path(numbers3,length3));  
    return 0;  
}  
  
//Returns longest alternating path  
int longest_alternating_path (int number [] , int length)  
{  
    int i; //For loop
```



```
/*middle = middle element of index of the array
max_l = longest alternating path of left path
max_r = longest alternating path of right path
c_left = counter for alternating path in the left side of the array
c_right = counter for alternating path in the right side of the array
max_total = longest alternating path in this array*/
```

```
int middle = ceil(length/2);
int max_l = 0, max_r = 0, c_left=0, c_right=0 , max_total;
```

```
//Finds longest alternating path in left part , number [0 to middle]
```

```
for (i= 0;i<middle;i++)
{
    if (number[i] != number [i+1] )
    {
        c_left ++;
        if (c_left > max_l)
            max_l = c_left; /*If there is a corrupted alternating path , max_l will keep previous longest
                                alternating path*/
    }
    else
    {
        c_left = 0; //If the current element is equal to the next element , counter will be set to 0.
    }
}
```

```
//Finds longest alternating path in right part , number [middle to length]
```

```
for (i= middle+1;i<length-2;i++)
{
    if (number[i] != number [i+1] )
    {
        c_right ++;
        if (c_right > max_r)
            max_r = c_right; //If there is a corrupted alternating path , max_r will keep previous longest alternating
path
    }

    else
    {
        c_right = 0; //If the current element is equal to the next element , counter will be set to 0.
    }
}
```

```
/*Middle element of the array is checked , if this element is not equal to the previous and next element ,
the longest alternating path may begin from left and end with right part . To see this , if counter is not
zero ,
```

we can say that this path begins from left and end with right part . */

/*If the longest path is in the left part , then max_l will be longest path*/

/*If the longest path is in the right part , then max_r will be longest path*/

```
if ( number[middle] != number[middle+1] && number[middle] != number [middle-1] )  
    max_total = c_left + max_r + 2;
```

```
else  
{  
    if (max_l > max_r)  
        max_total = max_l + 1;  
    else if (max_l == 0 && max_r == 0)  
        max_total = 0;  
    else  
        max_total = max_r + 1 ;  
}  
return max_total;  
}
```