

PSYC 650 APPLIED DATA ANALYSIS MISSING DATA

November 5, 2018

MISSING DATA MECHANISMS

Note. function of analysis (not the dataset)

Missing completely at random (MCAR)

- probability of missing data is completely unsystematic (where random = random effect, probabilistic)
- Ex. Research assistant drops random set of surveys in mud puddle

Missing at random (MAR)

- systematic missingness, where missing data is related to other measured variables in the analysis
- Ex. Dropout related to severity, which is a covariate

Missing not at random (MNAR) aka non-ignorable missingness (NIM)

- probability of missing data is related to missing values
- Ex. Dropout related to outcomes, not included in the model

WHAT CAN A RESEARCHER DO WITH MISSING DATA?

Mechanisms of missing data are rarely known

- What can you do?
 - Worst case...
 - Ignore missingness and risk biasing results
 - Best case...
 - Use theory to make educated guesses as to why data are missing
 - Include variables that predict missingness in the analyses
 - Use robust tools for handling missing data

APPROACHES TO HANDLING MISSING DATA

Deletion methods

Single imputation methods

- Mean substitution, regression substitution
- Stochastic regression imputation
- Longitudinal data
 - Last (or baseline) observation carried forward (LOCF, BOCF)
- Missing = failure

Model based methods

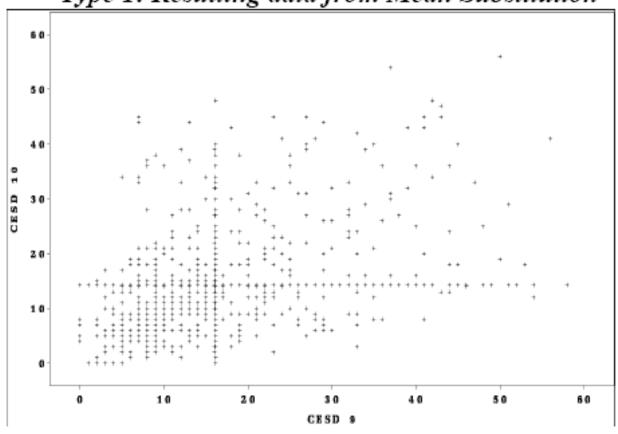
- Multiple imputation
- Maximum likelihood
- Pattern mixture models
- Selection models

DELETION: COMPLETE CASE ANALYSIS

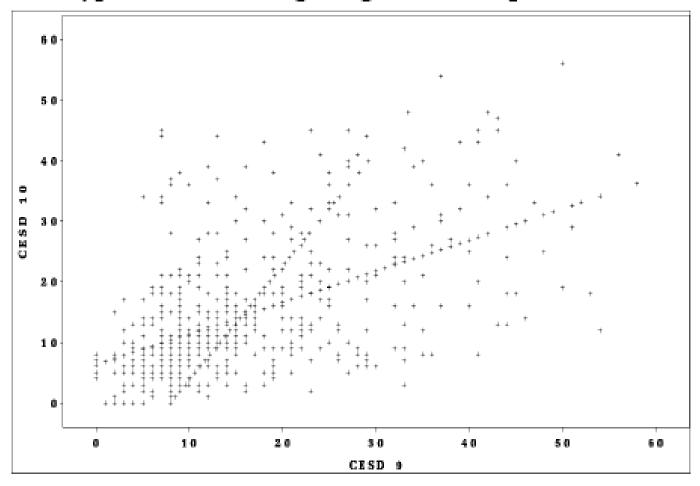
Participants with incomplete data not included

| Subj ID | Treatment Condition | Baseline PHD | Within-treatment PHD | Post-treatment PHD |
|---------|------------------------|--------------|-------------------------|--------------------|
| 1 | 0 | 88 | 0 | 56 |
| 2 | 0 | 72 | 0 | |
| 3 | 0 | 100 | 24 | 100 |
| 4 | 1 | 100 | 0 | 0 |
| 5 | 1 | 100 | | |
| 6 | 1 | 75 | 0 | 75 |

Type 1: Resulting data from Mean Substitution



Type 2: Data using Regression Imputation



SINGLE IMPUTATION: LAST OBSERVATION CARRIED FORWARD

- Missing values replaced with the last observed value of the same variable
- Must be done manually or through programming

| Subj ID | Treatment Condition | Baseline PHD | Within-treatment PHD | Post-treatment PHD |
|---------|------------------------|--------------|-------------------------|--------------------|
| 1 | 0 | 88 | 0 | 56 |
| 2 | 0 | 72 | 0_ | 0 |
| 3 | 0 | 100 | 24 | 100 |
| 4 | 1 | 100 | 0 | 0 |
| 5 | 1 | 100_ | | 100 |
| 6 | 1 | 75 | 0 | 75 |

SINGLE IMPUTATION: MISSING = FAILURE

- Missing values replaced with 100% heavy drinking days
- "Conservative" to assume dropout indicates relapse

| Subj ID | Treatment Condition | Baseline PHD | Within-treatment PHD | Post-treatment PHD |
|---------|------------------------|--------------|-------------------------|--------------------|
| 1 | 0 | 88 | 0 | 56 |
| 2 | 0 | 72 | 0 | 100 |
| 3 | 0 | 100 | 24 | 100 |
| 4 | 1 | 100 | 0 | 0 |
| 5 | 1 | 100 | 100 | 100 |
| 6 | 1 | <i>75</i> | 0 | 75 |

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PROBLEMS WITH SINGLE IMPUTATION METHODS

Mean substitution

- Unbigsed means when data are MCAR
- Attenuated correlation, biased means when MAR, reduced variability

Regression imputation

- Unbiased means when data are MCAR or MAR
- Overestimate correlated, reduced variability

Stochastic regression imputation

- Unbiased when MCAR or MAR
- Underestimated standard errors inflate Type I error

MULTIPLE IMPUTATION

Imputation step

- Multiple copies of a dataset with unique estimates of the missing values drawn at random
- Data augmentation with iterative algorithm
 - Imputation step identical to stochastic regression
 - Posterior step add random error to estimates

Analysis step

• Yields several estimates of each parameter and standard error (e.g., 20 datasets = 20 estimates for each parameter and each standard error)

Pooling step

Pool parameter estimates adjusting for within imputation variance and between imputation variance

MULTIPLE IMPUTATION - PART 1

Generate plausible values for missing values Residual error added to imputed values

| | | | lmp. 1 | lmp. 2 | | Imp. 3 | | lmp. <i>m</i> |
|----------------|----------------------|----------------------------------|-----------------------------|--------------------------------|---|--------------------------------|-----|-------------------------|
| Treat- ment | Base- line PHD | Within- treat- ment PHD | Post- treat- ment PHD | Post- treat- ment PHD | | Post- treat- ment PHD | ••• | Post-treat- ment PHD |
| 0 | 88 | 0 | 56 | 56 | | 56 | ' | 56 |
| 0 | 72 | 0 | 25 | 17 | | 0 | | 40 |
| 0 | 100 | 24 | 100 | 100 | | 100 | | 100 |
| 1 | 100 | 0 | 0 | 0 | | 0 | | 0 |
| 1 | 100 | | 68 | 90 | | 75 | | 100 |
| 1 | 75 | 0 | 75 | 75 | • | 75 | | 75 |

MULTIPLE IMPUTATION - PART 2

Generate plausible values for missing values, "m" times and then pool results to estimate effects

| Imputation number | Treatment effect (β) | Standard Error (SE) |
|-------------------|----------------------|---------------------|
| 1 | -4.31 | 3.11 |
| 2 | -6.85 | 3.87 |
| 3 | -2.88 | 2.99 |
| ••• | ••• | ••• |
| m | -3.92 | 3.50 |
| Pooled estimate | -4.49 | 3.57 |

MAXIMUM LIKELIHOOD

Uses all available data to identify parameter values that have the highest probability of producing the sample data

- Same concept as OLS regression
- Identify parameter estimates that maximize the sum of the log-likelihood values; repeated until estimates that minimize the distance to the observed data

FULL INFORMATION MAXIMUM LIKELIHOOD

Use all available data:

| ID | Treatment | Baseline PHD | Within-TX PHD | Post-TX PHD | |
|----|-----------|--------------|---------------|-------------|--|
| 1 | 0 | 88 | 0 | 56 | |
| 2 | 0 | 72 | 0 | | |
| 3 | 0 | 100 | 24 | 100 | |
| 4 | 1 | 100 | 0 | 0 | |
| 5 | 1 | 100 | | | |
| 6 | 1 | 75 | 0 | 75 | |

To create variance-covariance matrix:

| | Treatment | Baseline PHD | Within TX PHD | Post Tx PHD |
|---------------|-----------|--------------|---------------|-------------|
| Treatment | 0.250 | 0.003 | 0.014 | 0.001 |
| Baseline PHD | 0.003 | 0.082 | 0.014 | 0.015 |
| Within Tx PHD | 0.014 | 0.014 | 0.082 | 0.067 |
| Post Tx PHD | 0.001 | 0.015 | 0.067 | 0.099 |

Identify parameter values that have highest probability (i.e., maximize the likelihood) of producing the sample data

AUXILIARY VARIABLES

Improve estimation (reduces SE) without directly influencing parameter estimates

Best to use auxiliary variables that are highly correlated with incomplete analysis model variables

MISSING DATA MODELS IN MPLUS

FIML is default

Listwise deletion by adding to DATA: command

DATA:

FILE is filename.csv; LISTWISE IS ON;

MI is two step process

- Create imputation datasets
- Pool estimates across imputed datasets

MULTIPLE IMPUTATION: IMPUTATION STEP

VARIABLE: USEVARIABLES ARE opioids asitot0-asitot12; DATA IMPUTATION: IMPUTE opioids (c) asitot0-asitot12; NDATASETS 50; SAVE = asimi*.dat; ANALYSIS: TYPE = BASIC; OUTPUT: TECH8;

AFTER IMPUTATION FILE

asimi1.dat asimi2.dat asimi3.dat asimi4.dat asimi5.dat asimi6.dat asimi7.dat asimi8.dat asimi9.dat asimi 10.dat asimi11.dat asimi 12.dat asimi 13.dat asimi 14.dat asimi 15.dat asimi 16.dat asimi 17.dat asimi 18.dat asimi 19.dat asimi20.dat

asimilist.dat

MULTIPLE IMPUTATION: ANALYSIS STEP

```
DATA:

FILE is asimilist.dat;

TYPE = IMPUTATION;

VARIABLE:

NAMES ARE opioids asitot0-asitot12;

MISSING ARE *;

USEVARIABLES ARE opioids asitot12;

MODEL:

asitot12 on opioids;
```

MULTIPLE IMPUTATION RESULTS

MODEL RESULTS

| | Estimate | S.E. E | st./S.E. | P-Value |
|------------------|----------|--------|----------|---------|
| ASITOT12 ON | | | | |
| OPIOIDS | 8.209 | 4.099 | 2.003 | 0.045 |
| Intercepts | | | | |
| ASITOT12 | 11.006 | 2.027 | 5.430 | 0.000 |
| Residual Varianc | es | | | |
| ASITOT12 | 682.786 | 74.273 | 9.193 | 0.000 |

MAXIMUM LIKELIHOOD

VARIABLE:

MISSING ARE ALL (999)
USEVARIABLES ARE opioids asitot12;
AUXILIARY ARE (m) asitot0-asitot11;

MODEL:

asitot12 on opioids;

OUTPUT:

SAMPSTAT CINTERVAL STANDARDIZED;

EXAMPLE OF MAXIMUM LIKELIHOOD WITH AUXILIARY VARIABLES

MODEL RESULTS

| | Estimate | S.E. Est., | /S.E. P-V | ′alue |
|------------------|----------|------------|-----------|-------|
| ASITOT12 ON | | | | |
| OPIOIDS | 8.975 | 4.286 | 2.094 | 0.036 |
| Intercepts | | | | |
| ASITOT12 | 11.295 | 2.146 | 5.262 | 0.000 |
| Residual Variand | ces | | | |
| ASITOT12 | 690.321 | 80.537 | 8.571 | 0.000 |

EXAMPLE OF MAXIMUM LIKELIHOOD WITHOUT AUXILIARY VARIABLES

MODEL RESULTS

| | Estimate | S.E. Est. | /S.E. P-\ | /alue | | |
|--------------------|----------|-----------|-----------|-------|--|--|
| ASITOT12 ON | | | | | | |
| OPIOIDS | 9.138 | 4.332 | 2.109 | 0.035 | | |
| Intercepts | | | | | | |
| ASITOT12 | 10.903 | 2.166 | 5.033 | 0.000 | | |
| Residual Variances | | | | | | |
| ASITOT12 | 689.524 | 80.429 | 8.573 | 0.000 | | |

COMPARISON OF ESTIMATES

| | n | Estimate | SE | Est/SE | p-value |
|---------------------|-----|----------|-------|--------|---------|
| Listwise deletion | 146 | 9.139 | 4.362 | 2.095 | 0.038 |
| Mean imputation | 197 | 6.793 | 3.247 | 2.092 | 0.038 |
| BOCF | 193 | 8.605 | 6.811 | 1.263 | 0.208 |
| Multiple imputation | 200 | 8.209 | 4.099 | 2.003 | 0.045 |
| Maximum likelihood | 197 | 8.975 | 4.286 | 2.094 | 0.036 |

WHAT ABOUT MNAR DATA?

Pattern mixture models

- assume that the substantive data are conditional on the missing data mechanism
- Include missing data patterns as main effects with random effect means mixed across the different missing data patterns to yield single estimates of parameters

Selection models

- assume that the missing data mechanism is conditional on the substantive data
- Incorporate indicators of the probability of missing data, regressed on outcomes

PATTERN MIXTURE MODELS

assume that the substantive data are conditional on the missing data mechanism

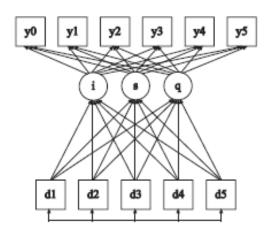


Figure 2. Pattern-mixture modeling (ds are dropout dummy variables).

SELECTION MODELS

assume that the missing data mechanism is conditional on the substantive data

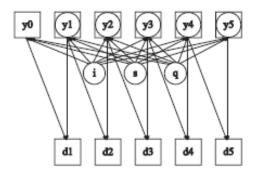


Figure 4. Diggle-Kenward selection modeling (ds are survival indicators).

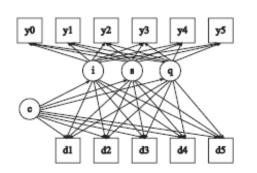


Figure 8. Beunckens mixture model (mixture Wu-Carroll model).

RESULTS SUGGEST THAT LGC RESULTS ARE ROBUST TO MISSING DATA MAR ASSUMPTION

| Model | BIC | Intercept | Linear Slope | Quad Slope |
|----------------|---------|--------------|--------------|-------------|
| LGC | 39602.4 | 27.88 (0.62) | -5.60 (0.29) | 0.33 (0.04) |
| Dropout PMM | 39634.6 | 27.68 (0.80) | -5.91 (0.37) | 0.36 (0.05) |
| Diggle Kenward | 45452.2 | 28.23 (0.64) | -5.90 (0.32) | 0.36 (0.04) |
| Wu Carroll | 45639.3 | 28.23 (0.65) | -5.67 (0.34) | 0.33 (0.05) |