

UMass Boston CS 310 Homework 1

Due in class on Thursday, February 2, 2017

It is recommended that you typeset your answers by L^AT_EX(<https://www.latex-project.org/get/>) or Word. Handwritten answers will be accepted only if clearly legible.

1. Solve this sum of a geometric series: $\sum_{i=1}^{\infty} (2/5)^i$.
2. (a) How many binary digits are there in 2^{50} and 10^{50} ? How are the two numbers related?
Hint: This is a question about logarithm.
(b) Show that $\log_a(x) = c * \log_b(x)$ for some constant c expressed only in terms of constants a and b .
3. (a) Problem 5.19 of the textbook. Except in the obvious cases, give reasons for your ranking.
(b) Rank the following functions: $\log n$, $\log(n^2)$, $\log \log n$, and $\log^2 n$. Explain reasons for your ranking.

You may find it useful to remember that one way to compare the relative growth rates of $f(n)$ and $g(n)$ is to look at the ratio $f(n)/g(n)$ as $n \rightarrow \infty$. If that ratio approaches 0, then g grows faster than f : $f(n) = O(g(n))$. If it approaches infinity then f grows faster than g : $f(n) = \Omega(g(n))$. If the ratio approaches a constant different from both 0 and ∞ , then f and g grow at the same rate.

4. Problem 5.26 of the textbook.
5. Use the telescoping technique to derive this equation:

$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$