

## 1. How do you represent "Neko is a cat" in predicate logic?

- **Answer:** You'd use a simple predicate, like `Cat(neko)`.
  - Here, `Cat()` is the **predicate** (representing the property of being a cat), and `neko` is a **constant** (representing the specific entity, Neko).

What's the logical form for "Something is sleeping"?

- **Answer:**  $\exists x \text{ Sleeping}(x)$ 
  - The **existential quantifier**  $\exists x$  means "there exists at least one x," and  $\text{Sleeping}(x)$  means "x is sleeping." So, this reads as "There exists some x such that x is sleeping."

How would you write "All birds can fly"?

- **Answer:**  $\forall x (Bird(x) \rightarrow CanFly(x))$ 
  - The **universal quantifier**  $\forall x$  means "for all x." The formula reads, "For any entity x, **if** x is a bird, **then** x can fly." We use an **implication** ( $\rightarrow$ ) with the universal quantifier for conditional statements like this.

What's the logical representation of "John did not laugh"?

- **Answer:**  $\neg \text{Laugh}(\text{john})$ 
  - This is a straightforward negation.  $\text{Laugh}(\text{john})$  means "John laughed," and the **negation** symbol  $\neg$  in front of it means "it is not the case that John laughed."

How do you translate "Some students are smart"?

- **Answer:**  $\exists x (\text{Student}(x) \wedge \text{Smart}(x))$ 
  - This means "There exists some x such that x is a student **and** x is smart." When using the existential quantifier  $\exists$  to specify a property of a subset, you almost always use a **conjunction** ( $\wedge$ ).

What is the logical form for "Every student read a book"?

- **Answer:**  $\forall x (\text{Student}(x) \rightarrow \exists y (\text{Book}(y) \wedge \text{Read}(x,y)))$ 
  - This breaks down as: "For every x, if x is a student, then there exists some y such that y is a book, and x read y." This captures the relationship between students and the books they read.

How do you represent "No one likes taxes"?

- **Answer:**  $\neg \exists x (\text{Person}(x) \wedge \text{Likes}(x, \text{taxes}))$  or its equivalent  $\forall x (\text{Person}(x) \rightarrow \neg \text{Likes}(x, \text{taxes}))$ 
  - The first reads, "It is not the case that there exists a person  $x$  who likes taxes." The second reads, "For every person  $x$ , it is the case that  $x$  does not like taxes." Both are logically equivalent and correct!

What is the logical form for "Everyone loves someone"?

- **Answer:**  $\forall x (Person(x) \rightarrow \exists y (Person(y) \wedge Loves(x,y)))$ 
  - This classic sentence shows the interaction of two quantifiers. It states that for every person  $x$ , you can find at least one person  $y$  whom  $x$  loves. The person  $y$  can be different for each  $x$ .



How do you differentiate "Everyone loves someone" from "Someone is loved by everyone"?

- **Answer:** By swapping the quantifier order.
  - **Everyone loves someone:**  $\forall x \exists y \text{ Loves}(x, y)$
  - **Someone is loved by everyone:**  $\exists y \forall x \text{ Loves}(x, y)$
  - In the second sentence, the existential quantifier  $\exists y$  comes first. This means there is **one specific person**  $y$  who exists, and for all people  $x$ ,  $x$  loves that single person  $y$ . The order of quantifiers is critical for meaning!







