

1. Show that if M is the open interval (a,b) , and p is in M , then p is a limit point of M .

Solution:

Let M be the open interval (a,b) and $p \in M$, where $a, b \in \mathbb{R}$.

Let $S = (p - \epsilon, p + \epsilon)$, where ϵ is an arbitrary positive real number and $|\epsilon|$ is such that $S \subseteq M$.

$(p + \epsilon/2)$, $p \in S$ for any $\epsilon \in \mathbb{R}^+$, and so S is an arbitrary interval that contains p and contains another point of M .

Therefore p is a limit point of M .

2. Show that if M is the closed interval $[a,b]$, and p is not in M , then p is not a limit point of M .

Solution:

Let M be the closed interval $[a,b]$, and $p \notin M$. Assume, without loss of generality, that $p > b$.

Let $\epsilon = \frac{p-b}{2}$, and let $S = (p - \epsilon, p + \epsilon)$. Hence $S \cap M = \emptyset$.

Since S is an open interval that contains p but doesn't contain any element of M , p cannot be a limit point of M .

3. Q goes here

Solution: Ans goes here