

Analyzing Foodborne Disease Outbreaks Over Time

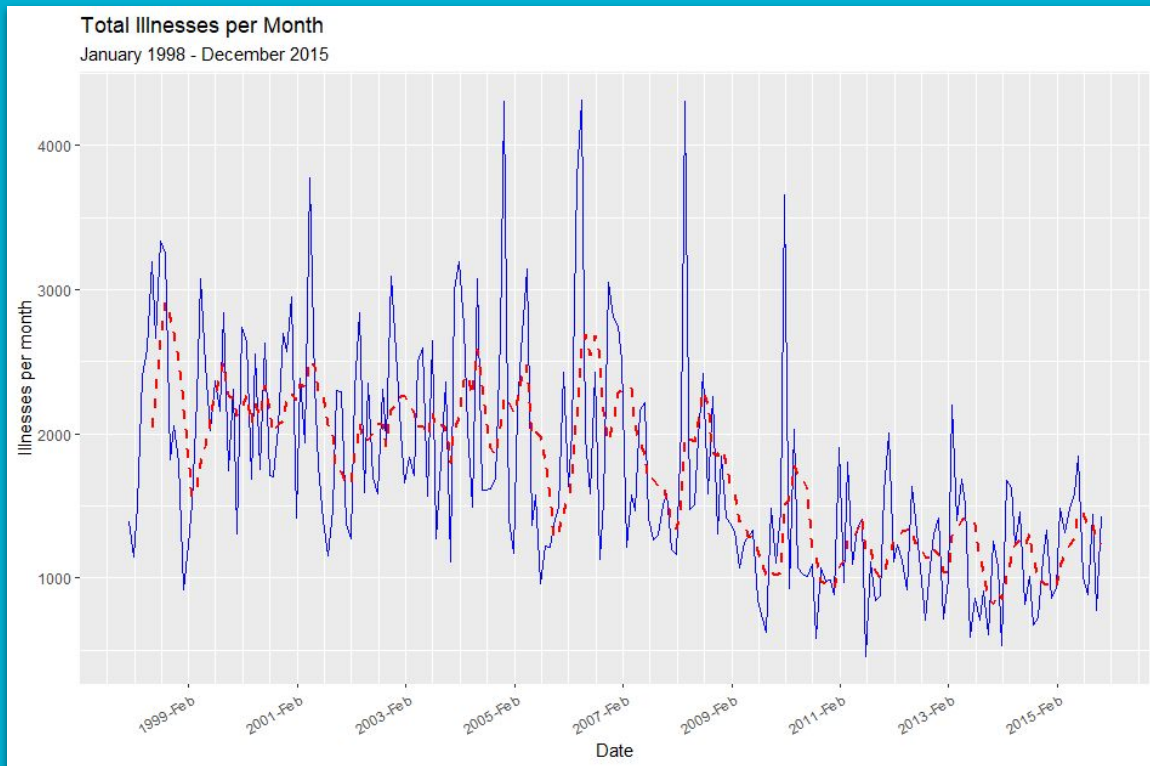
A look into illnesses and more

Group 12

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- Steven Macapagal
- Journey Martinez
- Yuan Yao
- Heather Nagy
- Kenneth Porter

Summary of prior findings

A reminder of what our data look like



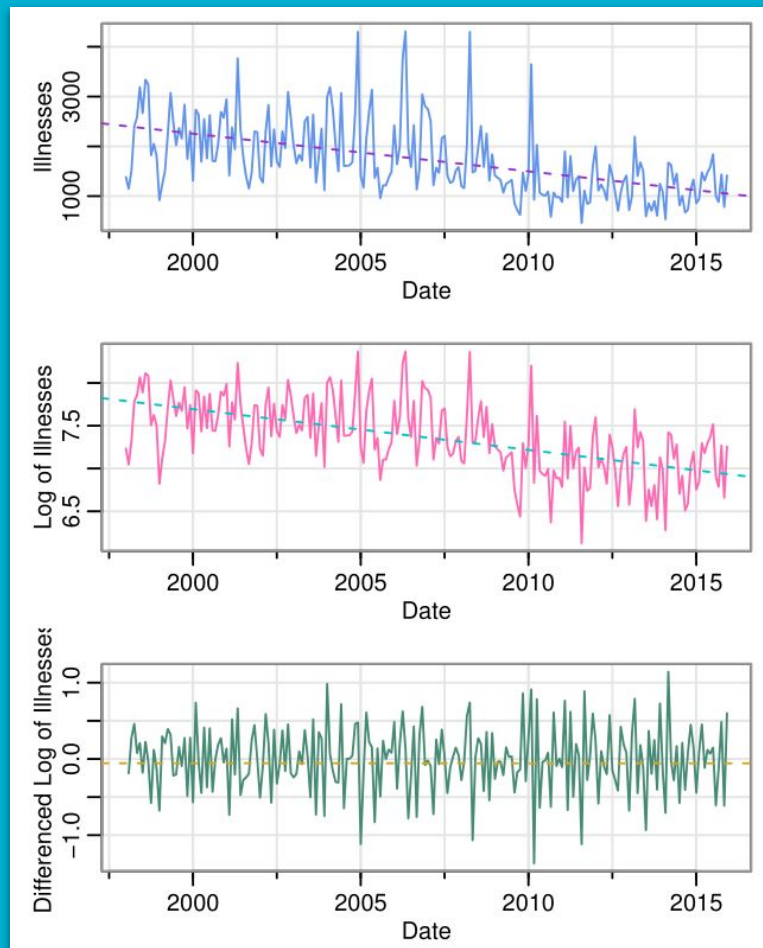
Solid blue line
represents the
original time series

Dotted red line
represents a
filtered time series
over a 6-month
period

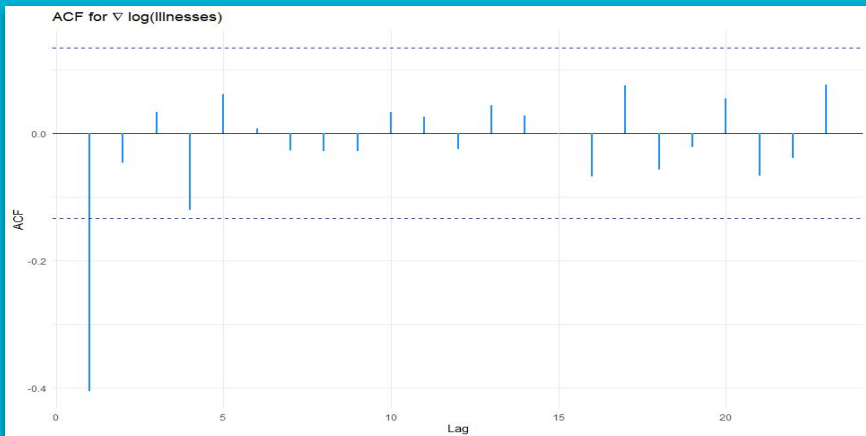
Stationarity

Variability is much greater from 1998 to 2010 and decreases from 2011 to 2015. Illnesses also seem to be trending downward and might be seasonal.

Log transforming and differencing achieved a more constant variance and got rid of the trend, giving us stationary data to work with.

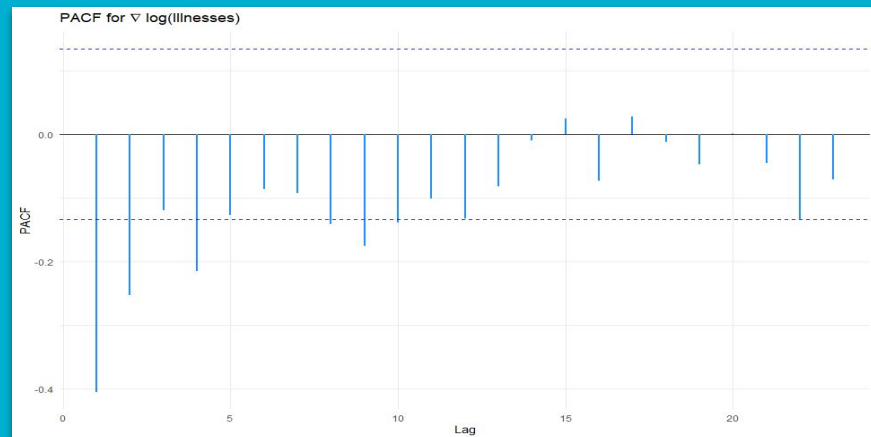


ACF and PACF



The partial autocorrelogram appears to tail off over time. The first few lags are significant, and the magnitude of PACF decreases over time.

Only the first lag appears to be significant, while the ACF is not significantly different from zero afterwards.



Parameter Estimation of MA(1)

- MLE estimation (unconditional least squares) with the sarima function in the astsa library
- Using $p = 0$, $d = 1$ (using log data) and $q = 1$ yielded best results
 - Values converged = > reasonable model
 - Conditional SS = -1.010483
 - Unconditional SS = -1.017639
 - MA(1) term significant
 - $\hat{\theta} = -.9103, \hat{\sigma}_w^2 = 0.1296$

$x_t = \text{difference in log(Illnesses) for time } t$

$$x_t = \omega_t - .9103_{(0.02)} \omega_{t-1}$$

```
Coefficients:
      ma1
      -0.9103
s.e.      0.0290

sigma^2 estimated as 0.1296:  log likelihood = -86.28,  aic = 176.56

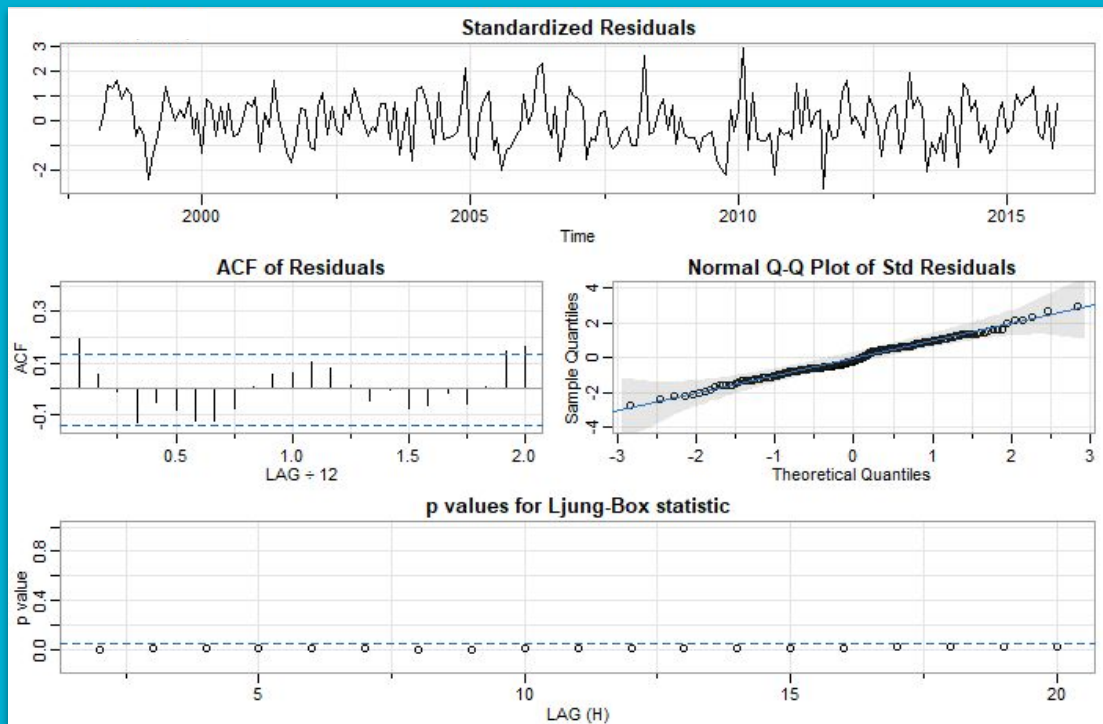
$degrees_of_freedom
[1] 214

$ttable
      Estimate      SE  t.value p.value
ma1  -0.9103  0.029  -31.3782      0

$AIC
[1] 0.8212041
```

Estimation Output of MA(1)

- Scattered, Normally distributed residuals
- ACF shows no departure from model assumptions
- p-values for Q tests are all less than 0.05
 - Residuals are correlated!



Parameter estimation of ARIMA(1,1,1)

- MLE estimation (unconditional least squares) with the sarima function in the astsa library
- Using $p = 1$, $d = 1$ (using log data) and $q = 1$ yielded best results
 - Values converged = > reasonable model
 - Conditional SS = -1.014162
 - Unconditional SS = -1.039521
 - AR(1) and MA(1) terms significant
 - Smaller AIC and BIC than AR(1) and MA(1) models
 - $\hat{\phi} = 0.2193, \hat{\theta} = -0.9351, \hat{\sigma}_w^2 = 0.1241$

$x_t = \text{difference in log(illnesses) for time } t$

$$x_t = 0.2193_{(0.07)}x_{t-1} - .9351_{(0.02)}\omega_{t-1} + \omega_t$$

```
Coefficients:
      ar1      ma1
      0.2193 -0.9351
s.e.    0.0710  0.0210

sigma^2 estimated as 0.1241:  log likelihood = -81.57,  aic = 169.15

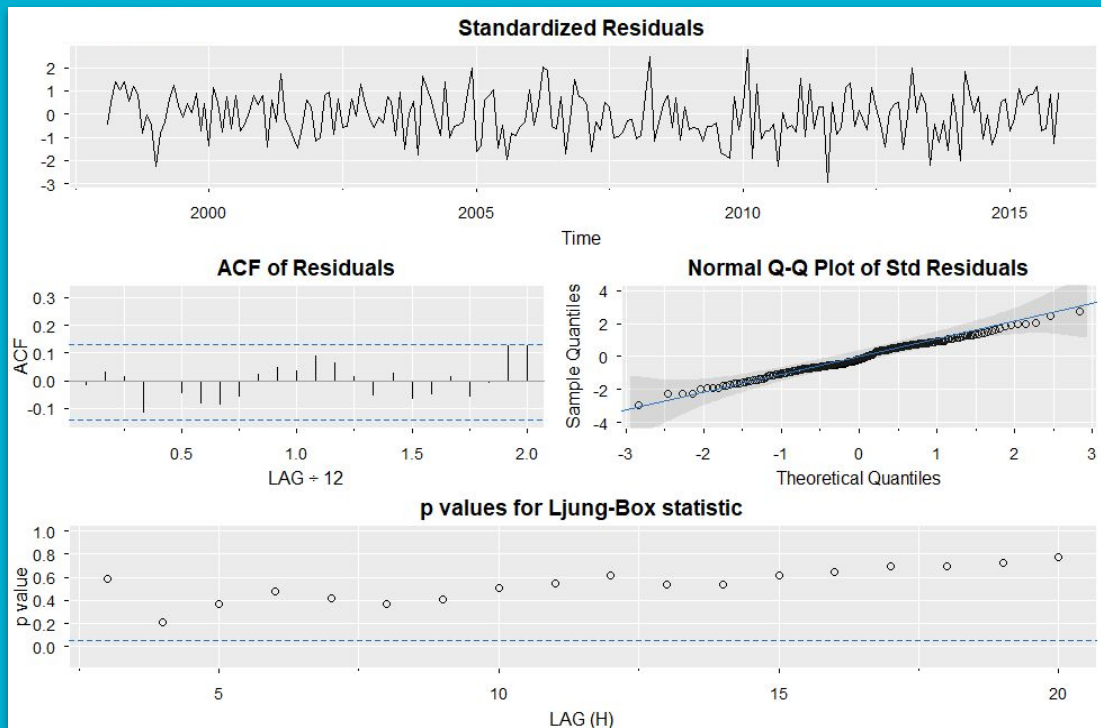
$degrees_of_freedom
[1] 213

$tttable
      Estimate    SE  t.value p.value
ar1    0.2193  0.071    3.0912  0.0023
ma1   -0.9351  0.021   -44.6319  0.0000

$AIC
[1] 0.7867413
```

Estimation Output of ARIMA(1,1,1)

- Scattered, Normally distributed residuals
- ACF shows no departure from model assumptions
- p-values for Q tests all greater than 0.05
 - Residuals are uncorrelated

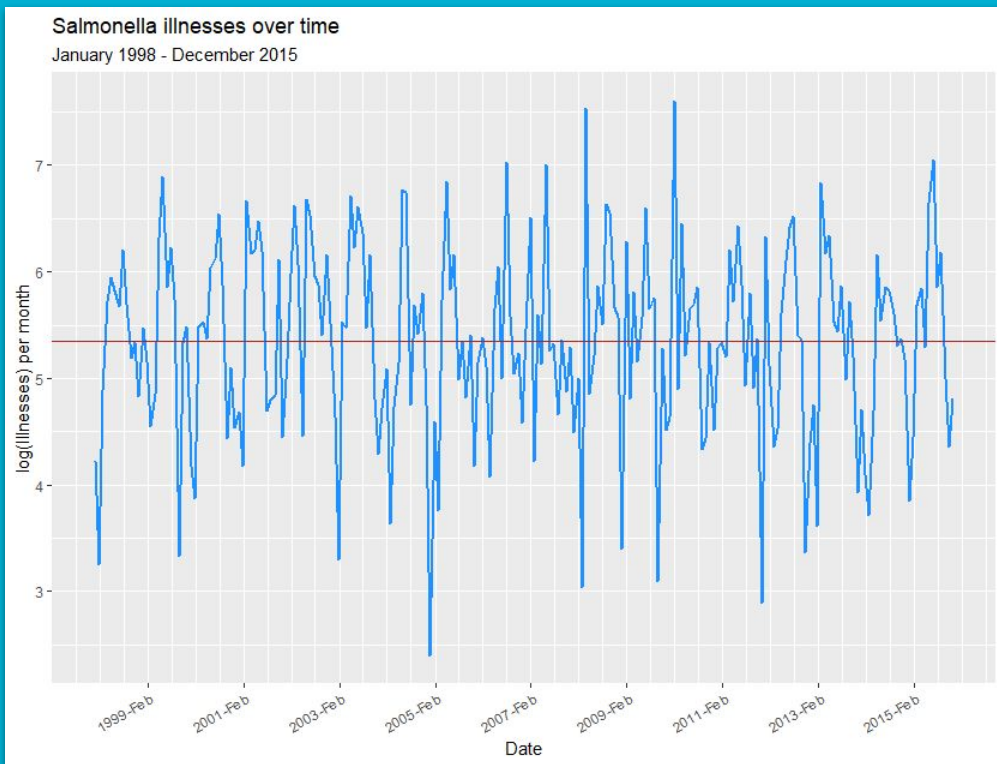


Our plan

1. Compare subsets of the data to see if there is an underlying pattern to foodborne disease outbreaks.
2. Compare models of foodborne illness to models of hospitalizations related to foodborne illness.
3. Compare different models to our previously established ARIMA(1, 1, 1) model on fit characteristics and prediction.

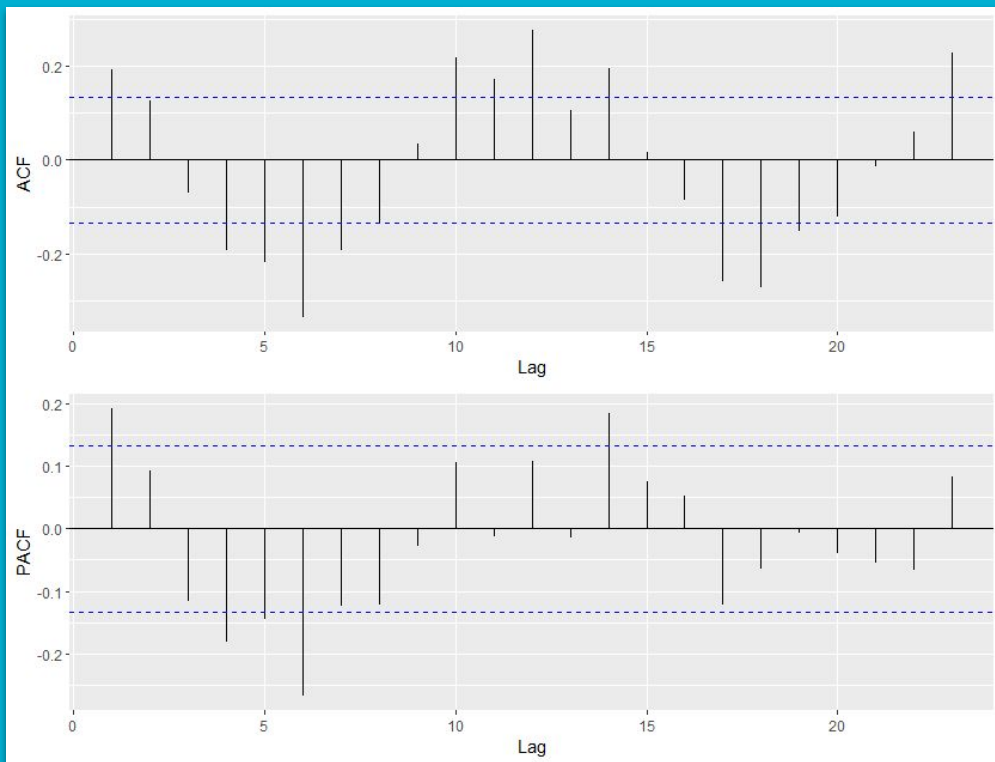
Analyzing source of outbreaks

Analysis of salmonella cases



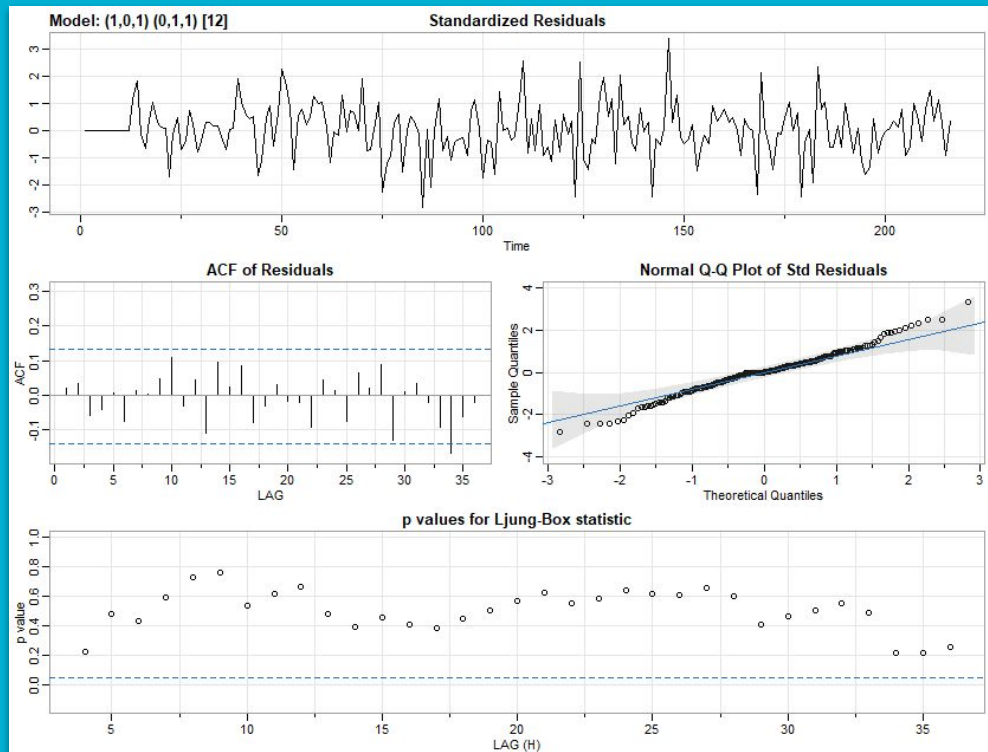
- Plot of $\log(\text{illnesses})$ for salmonella cases appears to be stationary
- Seems to have a seasonal component

Analysis of salmonella cases



- Seasonal differencing needed: ACF is large and significant for every 12th lag, seems to tail off slowly
- ACF and PACF have significant 1st lags

Analysis of salmonella cases



SARIMA(1, 0, 1) x (0, 1, 1)₁₂

- Residuals appear to be normally distributed white noise
- P-values for Ljung-Box statistic appear to be nonsignificant

Analysis of salmonella cases

SARIMA(1, 0, 1) x (0, 1, 1)₁₂

Estimated coefficients:

$$\phi_1 = 0.76$$

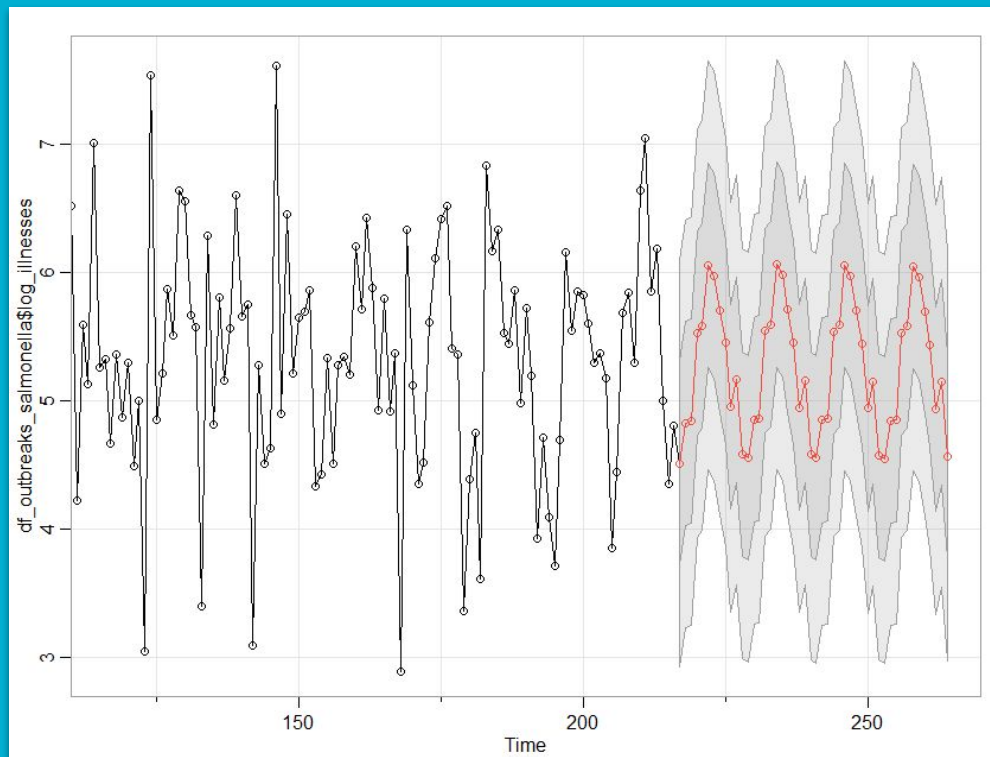
$$\theta_1 = -0.84$$

$$\Theta_1 = -1$$

$$\sigma^2 = 0.59, df = 200$$

```
sigma^2 estimated as 0.5933:  log likelihood = -253.66,  aic = 517.33
$degrees_of_freedom
[1] 200
$tttable
      Estimate      SE t.value p.value
ar1      0.7605 0.1754  4.3361 0.0000
ma1     -0.8399 0.1487 -5.6491 0.0000
sma1     -0.9999 0.1044 -9.5770 0.0000
constant -0.0006 0.0006 -1.0191 0.3094
```

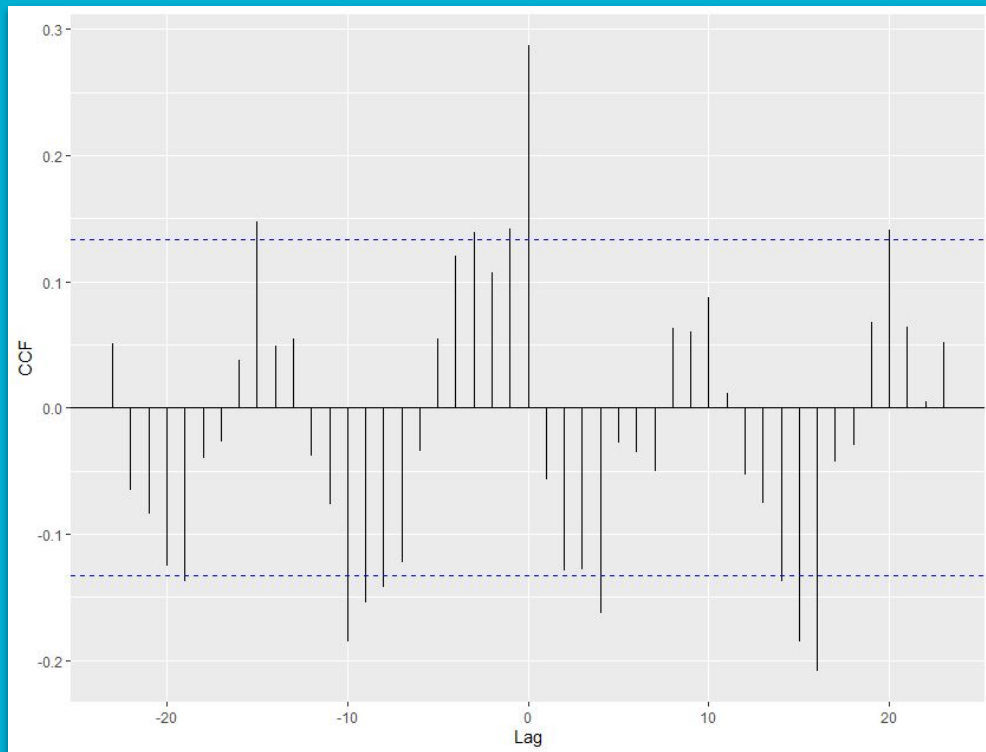

Analysis of salmonella cases



Seasonal forecasts of
 $\log(\text{salmonella})$

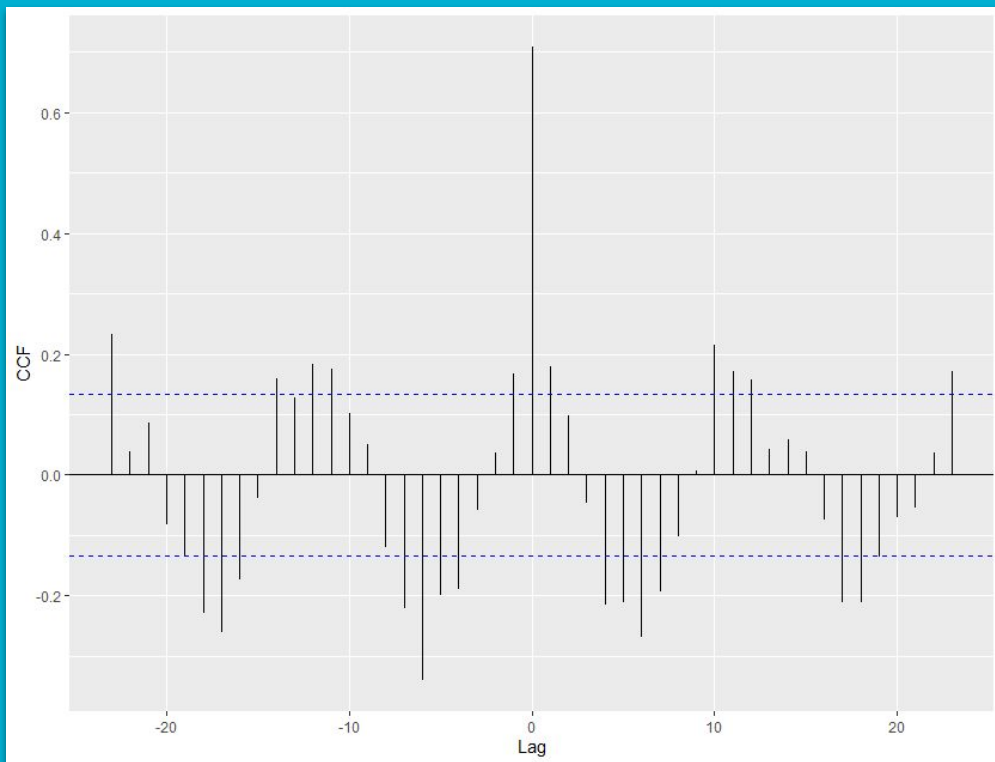
Relationships between illnesses and hospitalizations

CCF of overall illnesses and hospitalizations



- Strongest cross-correlation between illnesses and hospitalizations in the same period
- Appears to have some seasonality

Analysis of salmonella cases



CCF of $\log(\text{illnesses})$ and $\log(\text{hospitalizations})$

- Seasonal patterns of illness still apparent
- Strongest cross-correlations in same period (hospitalizations follow a diagnosed illness closely)

Comparisons to baseline ARIMA(1, 1, 1) model

Steps

Modeling process:

1. Model formulation
2. Model estimation
3. Model diagnostics
4. Model selection

We will also compare their forecasts to the actual data released for 2016 through 2019.

Models:

1. ARIMA(1, 1, 1) [baseline]
2. ARIMA(1, 1, 0) [Li et al. (2021)]
3. ARIMA(1, 1, 1) + GARCH(1, 0)
4. ARIMA(1, 1, 1) \times (1, 0, 1)₁₂
5. ARIMA(1, 1, 1) \times (0, 1, 1)₁₂
6. Prophet (*examined later*)

Comparing models suggested in prior literature

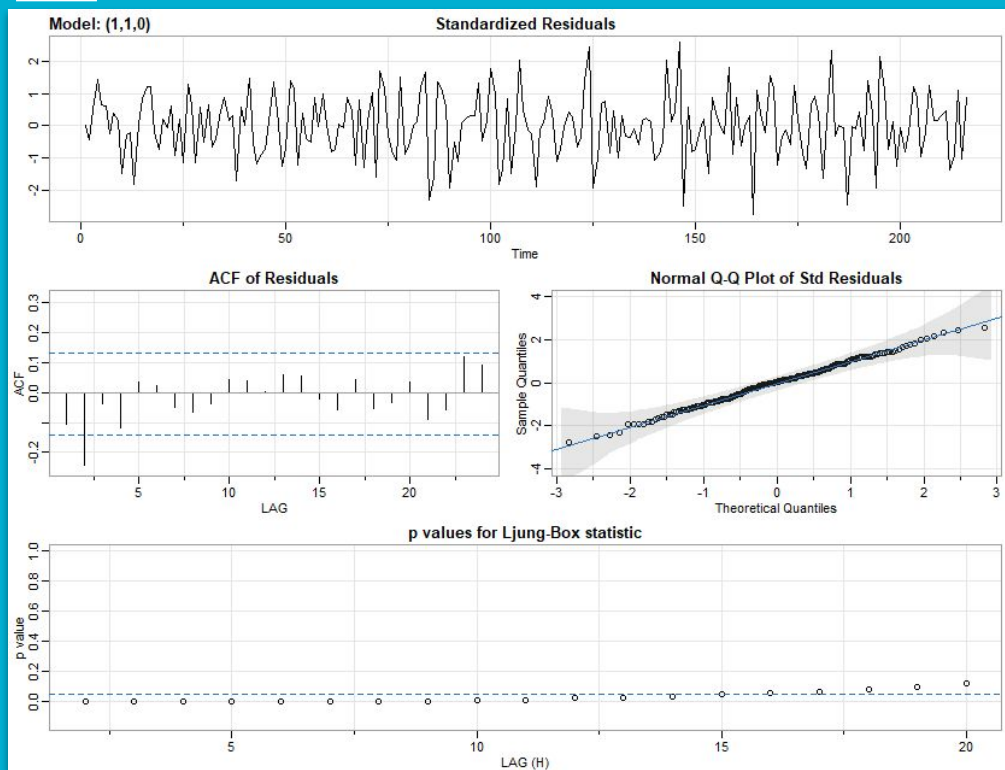
Li, et al. (2021) suggested an ARIMA(1, 1, 0) model to describe the incidence of foodborne illnesses over time.

- Performance and prediction compared to ARIMA(1, 1, 1) model we had previously found to fit our data

Li, S., Peng, Z., Zhou, Y., & Zhang, J. (2021). Time series analysis of foodborne diseases during 2012–2018 in Shenzhen, China. *Journal of Consumer Protection and Food Safety*, 17(2), 83–91.



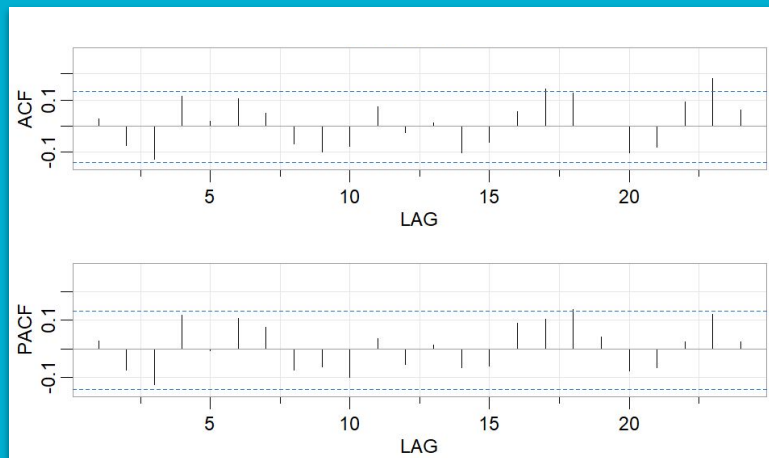
ARIMA(1, 1, 0) [Li et al., 2021]



- Diagnostics show residuals are not white noise, still have some autocorrelation
- Estimated coefficients:
 $\phi_1 = -0.41 (0.06)$
 $\sigma^2 = 0.16, df = 214$
- AIC = 1.02
BIC = 1.05

ARIMA(1,1,1) + GARCH(1,0)

- Some small dependence left in ARIMA(1,1,1) squared residuals
 - Average of residuals = 0.012
- ARIMA(1,1,1) + GARCH(1,0) on transformed data does not have significant alpha term
- GARCH(1,0) not needed

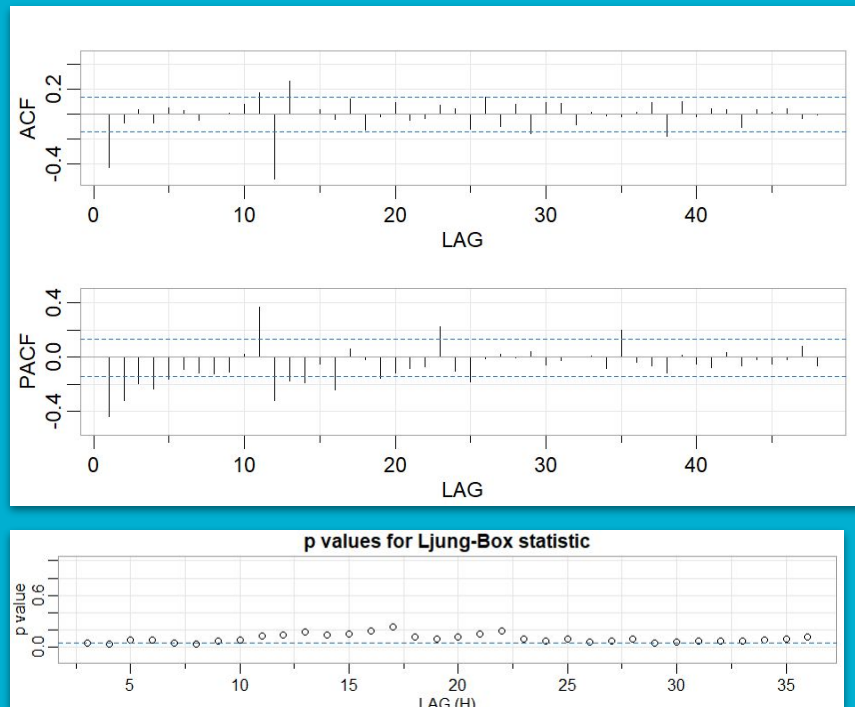


```
Error Analysis:
      Estimate Std. Error t value Pr(>|t|)
mu      3.65873   0.46265   7.908 2.66e-15 ***
ar1      0.50357   0.06260   8.044 8.88e-16 ***
omega    0.14864   0.02054   7.237 4.57e-13 ***
alpha1    0.01944   0.08138    0.239  0.8112
shape   10.00000   3.93673    2.540  0.0111 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Log Likelihood:
-97.76341      normalized: -0.4526084
```

Seasonality

- There appears to be a seasonal component
 - ACF cuts off at lag 12, PACF tails off
 - Try adding SMA1 term
- $\text{ARIMA}(1,1,1) \times (0,1,1)_{12}$ is possible
 - However, AR1 is not significant
- $\text{ARIMA}(0,1,1) \times (0,1,1)$ did not have white noise residuals
- $\text{ARIMA}(1,1,1) \times (1,1,1)_{12}$
 - AR1 and SAR1 terms not significant



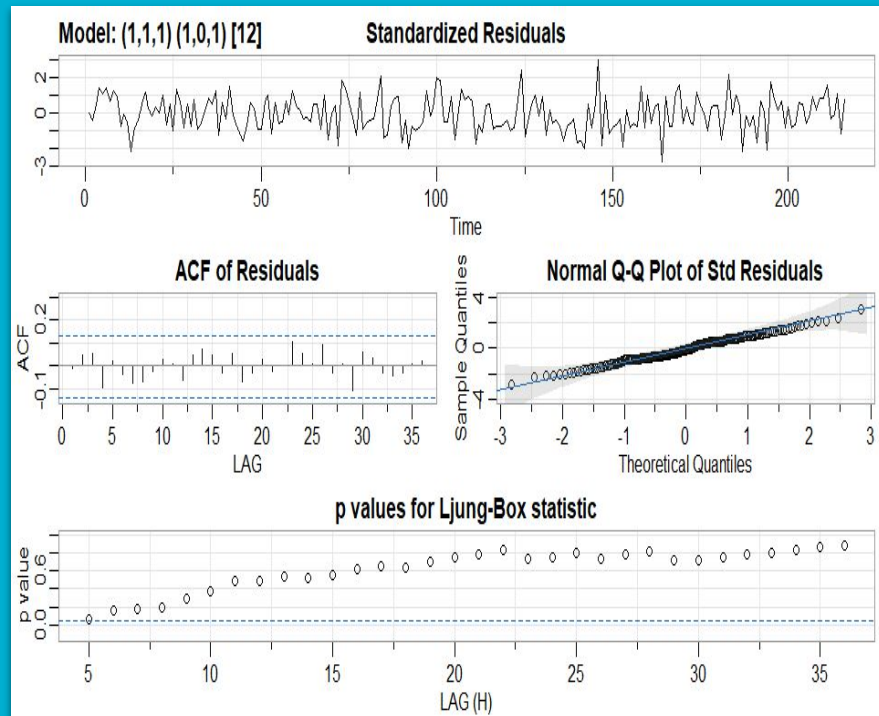
```
$ttable
      Estimate      SE  t.value p.value
ar1    0.1371 0.0752   1.8244 0.0696
ma1   -0.9393 0.0290 -32.3892 0.0000
sma1  -0.9093 0.0857 -10.6136 0.0000
```

```
$ttable
      Estimate      SE  t.value p.value
ar1    0.1275 0.0764   1.6691 0.0967
ma1   -0.9342 0.0303 -30.7925 0.0000
sar1  -0.0858 0.0917  -0.9352 0.3508
sma1  -0.8572 0.0925  -9.2709 0.0000
```

Selecting seasonal component

- ARIMA(1,1,1)x(1,0,1)₁₂ has significant estimates
- Slightly smaller AIC compared to ARIMA(1,1,1)
- Residuals appear to be white noise
- AIC = 0.769, BIC = 0.847
 - AIC = 0.787, BIC = 0.834 for baseline ARIMA

	Estimate	SE	t.value	p.value
ar1	0.1692	0.0729	2.3201	0.0213
ma1	-0.9403	0.0226	-41.5258	0.0000
sar1	0.9509	0.0912	10.4234	0.0000
sma1	-0.8796	0.1443	-6.0948	0.0000



ARIMA(1,1,1) x (1,0,1)₁₂

- Less dependence in squared residuals compared to ARIMA(1,1,1)
- Mean(residuals) = 0.006
 - Closer to zero than mean of ARIMA(1,1,1) residuals
- Less biased forecast



	Estimate	SE	t.value	p.value
ar1	0.1692	0.0729	2.3201	0.0213
ma1	-0.9403	0.0226	-41.5258	0.0000
sar1	0.9509	0.0912	10.4234	0.0000
sma1	-0.8796	0.1443	-6.0948	0.0000

$$x_t = (1 + \phi)x_{t-1} - \phi x_{t-2} + \Phi x_{t-12} - \Phi(\phi + 1)x_{t-13} + \Phi\phi x_{t-14} + w_t + \theta w_{t-1} + \Theta w_{t-12} + \Theta\theta w_{t-13}$$

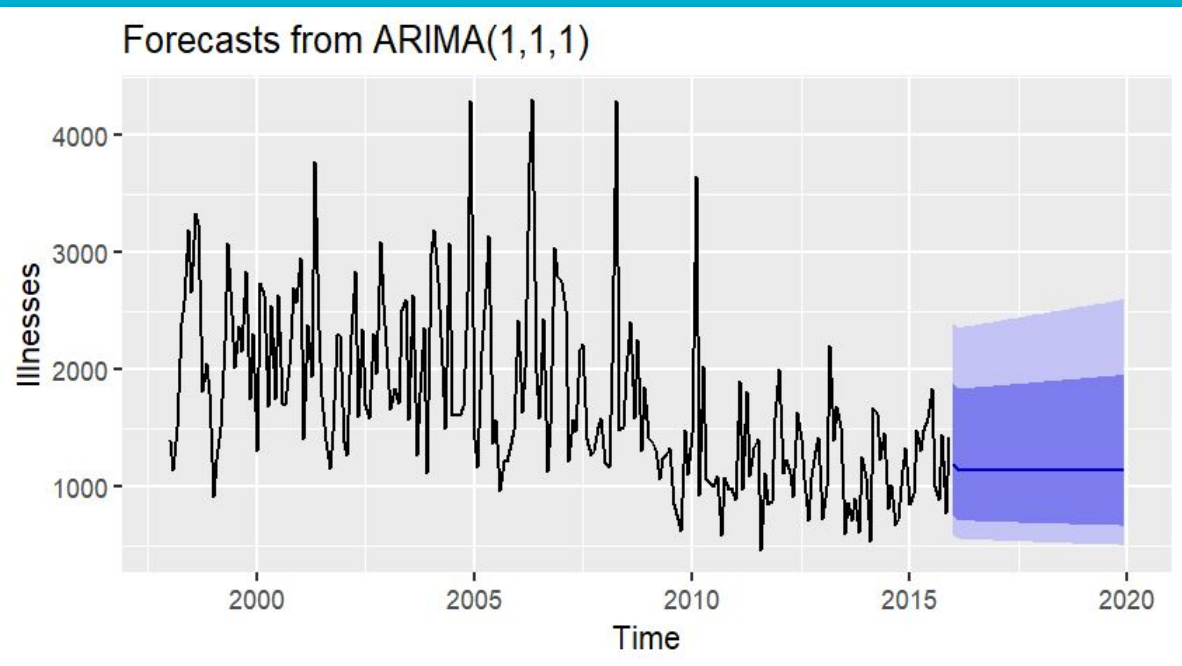
$$x_t = 1.1692x_{t-1} - 0.1692x_{t-2} + 0.9509x_{t-12} - 1.1118x_{t-13} + 0.1608x_{t-14} + w_t - 0.9403w_{t-1} - 0.8796w_{t-12} + 0.8271w_{t-13}$$

Models/Forecasts comparison

Model Comparisons

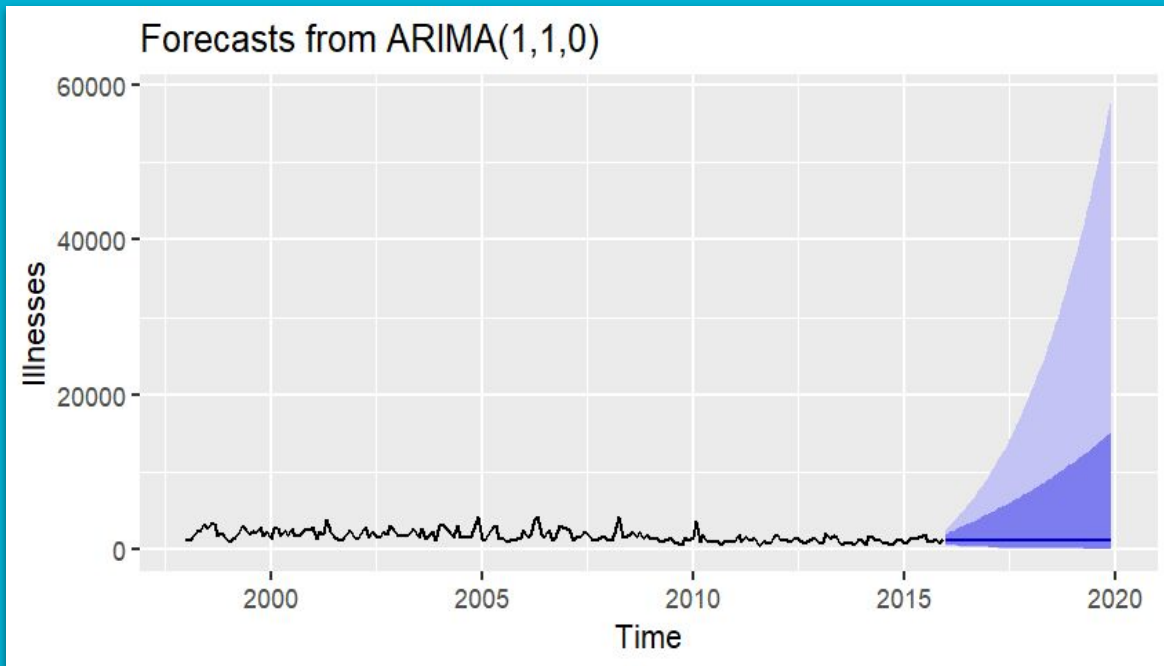
Model	AIC	BIC
ARIMA(1, 1, 1)	0.787	0.834
ARIMA(1, 1, 0)	1.020	1.051
ARIMA(1,1,1)x(1,0,1) ₁₂	0.769	0.847
ARIMA(1,1,1)x(0,1,1) ₁₂	0.881	0.946
ARIMA(1,1,1)-GARCH(1,0)	0.926	0.989

Forecast for ARIMA(1, 1, 1)



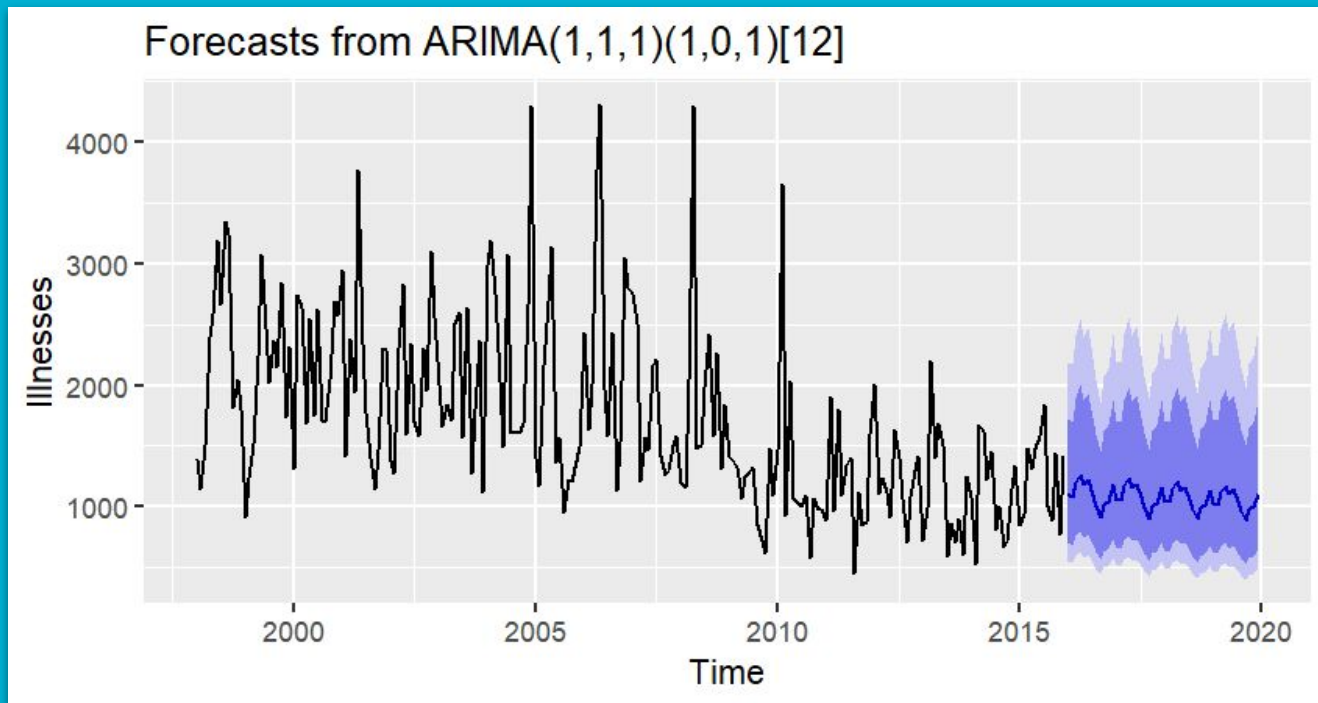
- The model mean's forecast appears to match mean of data
- But it doesn't appear to capture seasonal volatility well

Forecast for ARIMA(1, 1, 0)



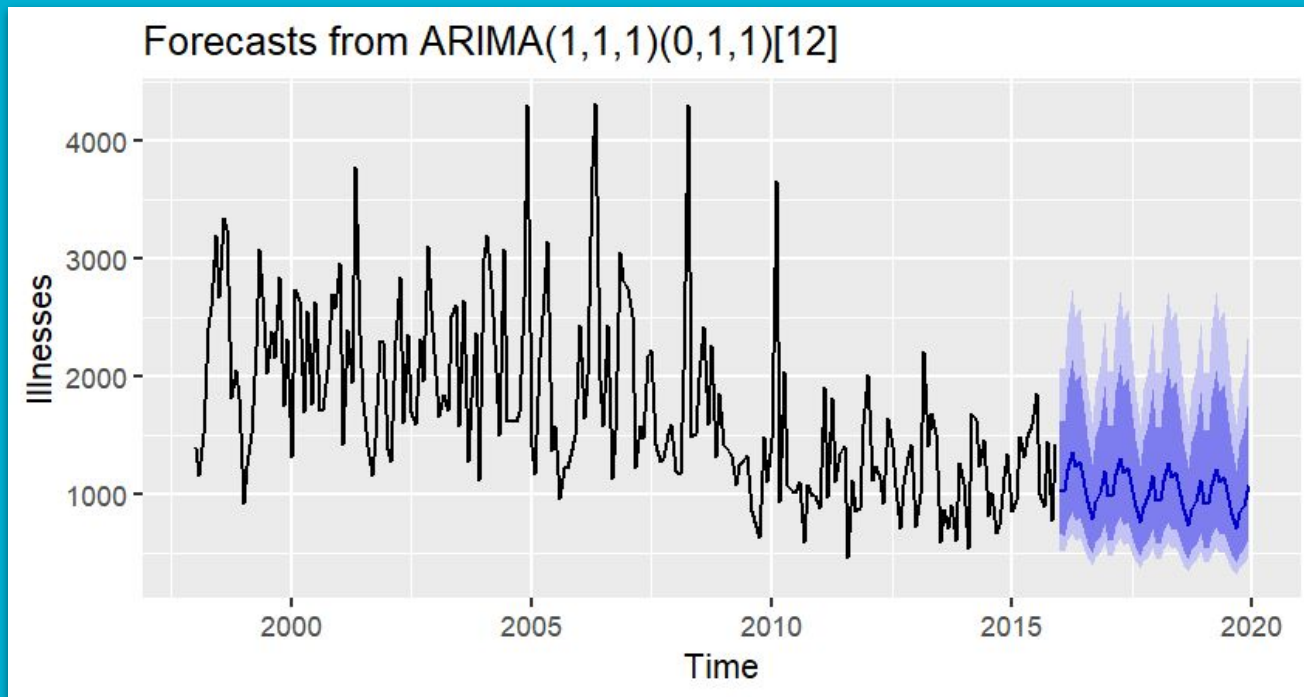
- Clearly not an ideal forecast due to the high upper CI bound
- However, the mean forecast appears to be accurate

Forecast for $\text{ARIMA}(1,1,1) \times (1,0,1)_{12}$



- Good performance for forecasting compared to actuals

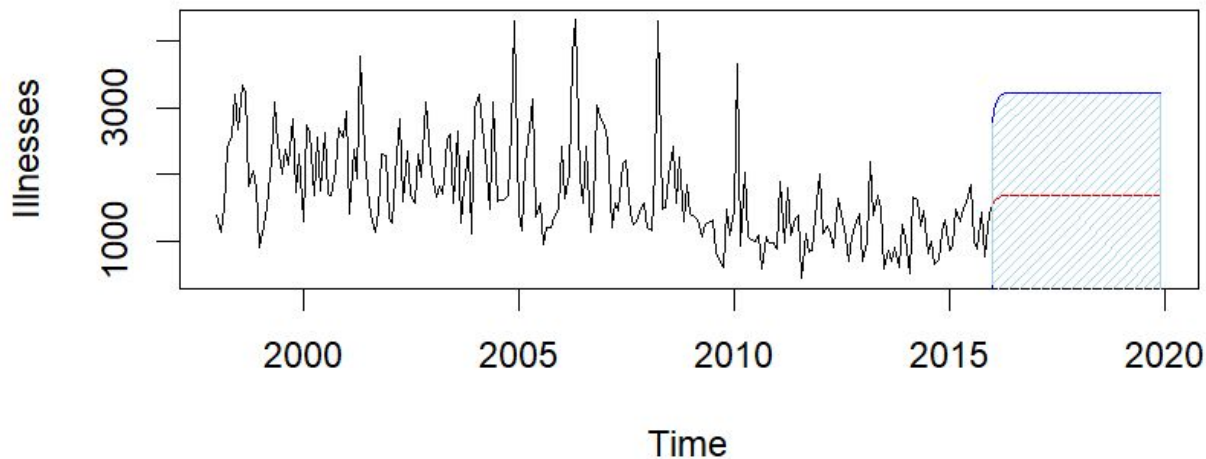
Forecast for ARIMA(1,1,1)x(0,1,1)₁₂



- This model appears to capture more of volatility
- This model did not have a significant AR1 term

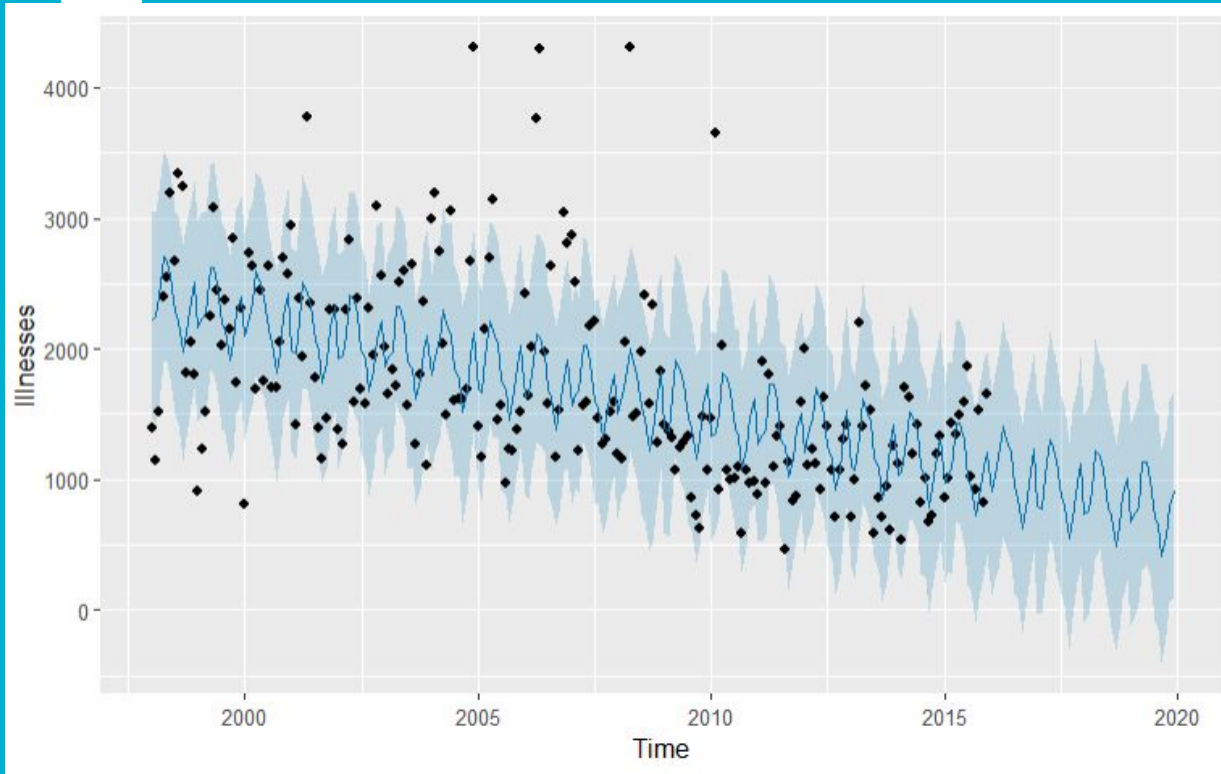
Forecast for ARIMA(1,1,1) + GARCH(1,0)

Forecast from ARIMA(1,1,1)+GARCH(1,0) model



- Like the non seasonal ARIMA models but the lower CI limit is 0
- Similar pattern for forecasting using log data vs untransformed data

Forecast for Prophet



- The model forecast appears to do a good job of capturing the seasonality of the historical data
- The forecast also appears to have a slight negative trend

Forecasting Comparisons

Model	RMSE
ARIMA(1, 1, 1)	489.42
ARIMA(1, 1, 0)	474.94
ARIMA(1,1,1)x(1,0,1) ₁₂	488.63
ARIMA(1,1,1)x(0,1,1) ₁₂	487.91
ARIMA(1,1,1)-GARCH(1,0)	552.43
Prophet	638

Data from 2016 and beyond

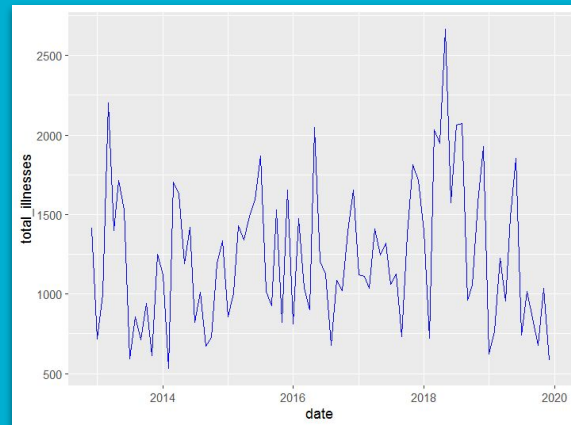
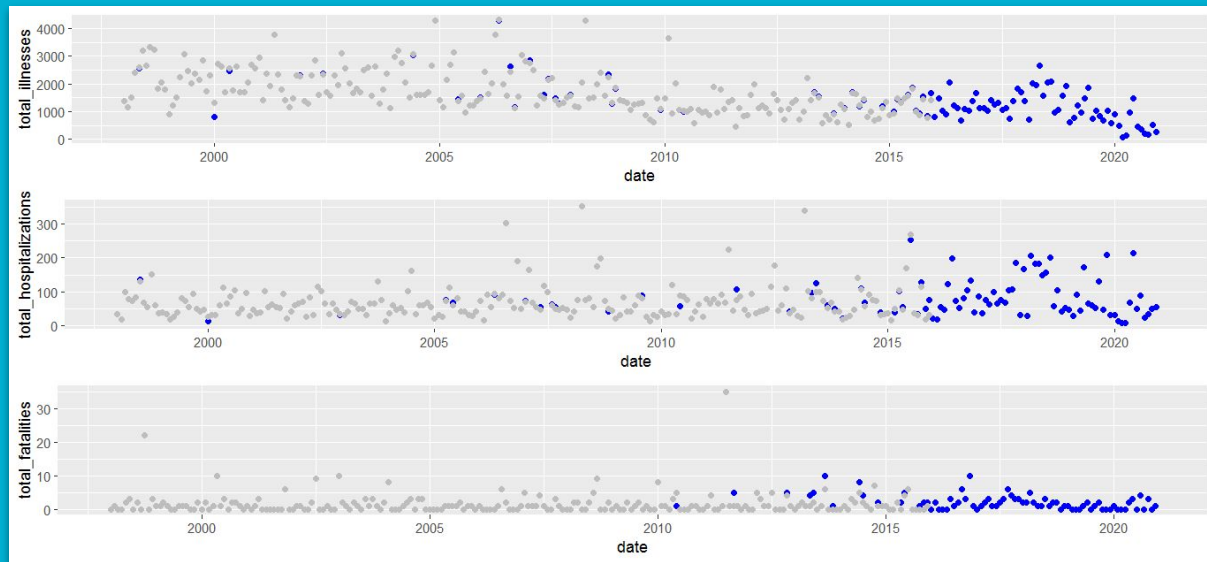
Data1: Foodborne illness data set (1998 - 2015):

<https://www.kaggle.com/datasets/cdc/foodborne-diseases>

Data2: National Outbreak Reporting System(1998 - 2020)

<https://wwwn.cdc.gov/norsdashboard>

Validate 2016 and beyond data



2013 - 2020 illness from data 2
Choose 2016 - 2019(48 month)
For forecast comparing

Real data and forecasting of ARIMA(1,1,1)

Model output from data before 2016

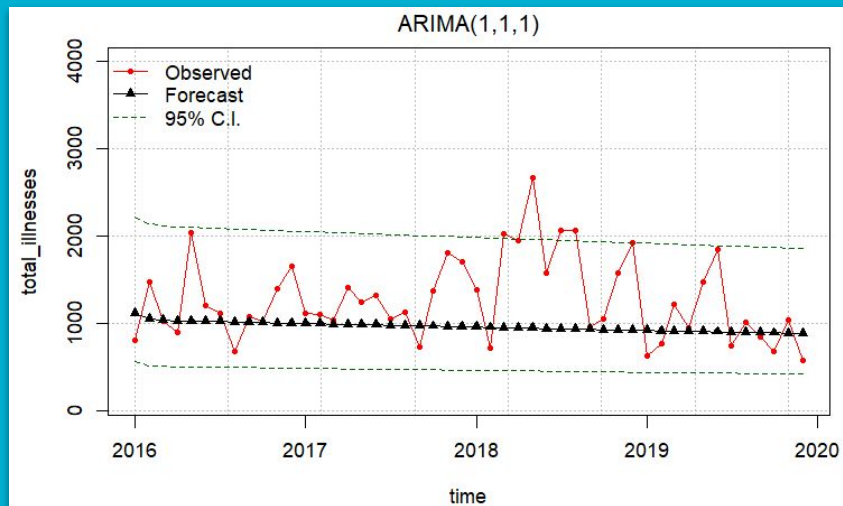
Data 1

```
$ttable
      Estimate      SE  t.value p.value
ar1    0.2193  0.071   3.0912  0.0023
ma1   -0.9351  0.021  -44.6319  0.0000
```

Data 2

```
$ttable
      Estimate      SE  t.value p.value
ar1    0.1998  0.0714   2.7971  0.0056
ma1   -0.9337  0.0216  -43.2306  0.0000
```

Forecast for data between 2016 - 2019



Real data and forecasting of ARIMA(1,1,0)

Model output from data before 2016

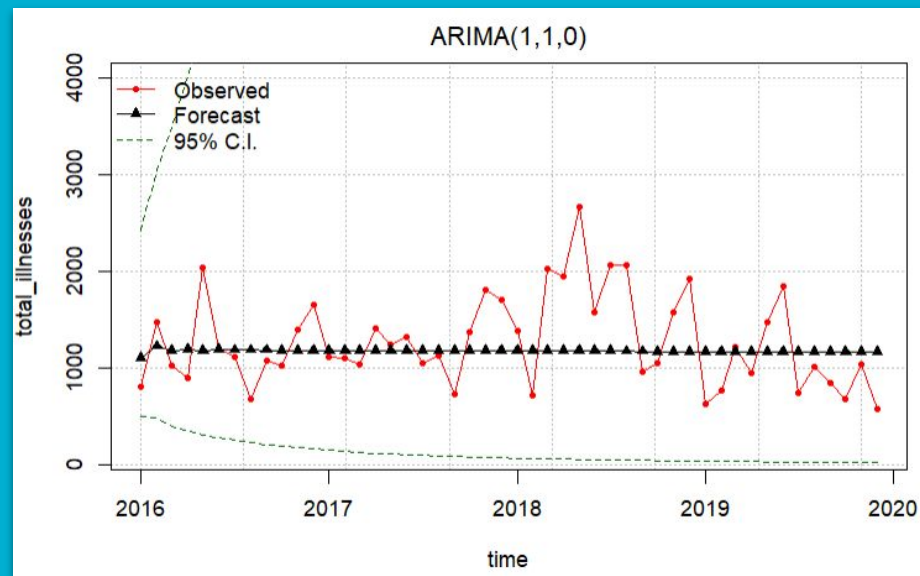
Data 1

```
$ttable
      Estimate      SE t.value p.value
ar1  -0.4078 0.0624  -6.535    0
```

Data 2

```
$ttable
      Estimate      SE t.value p.value
ar1  -0.4171 0.0622  -6.7047    0
```

Forecast for data between 2016 - 2019



Real data and forecasting of SARIMA(1,1,1)x(1,0,1)₁₂

Model output from data before 2016

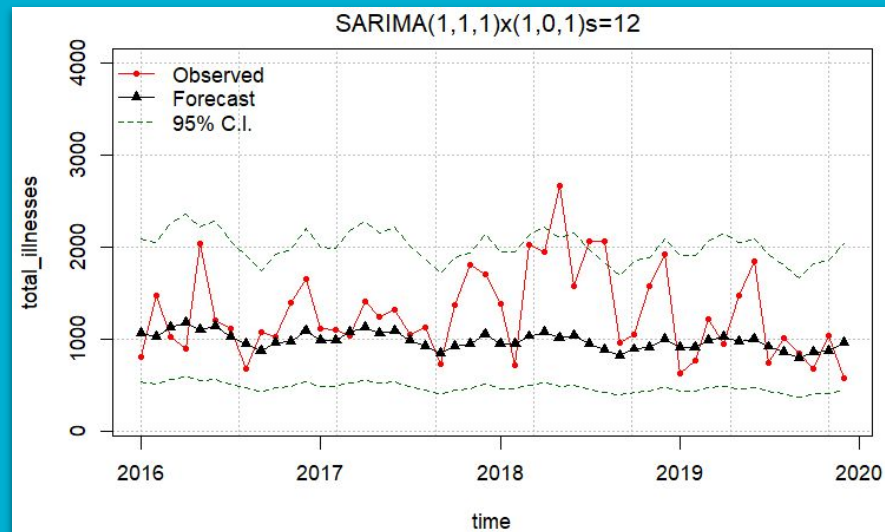
Data 1

\$ttable				
	Estimate	SE	t.value	p.value
ar1	0.1692	0.0729	2.3201	0.0213
ma1	-0.9403	0.0226	-41.5258	0.0000
sar1	0.9509	0.0912	10.4234	0.0000
sma1	-0.8796	0.1443	-6.0948	0.0000

Data 2

\$ttable				
	Estimate	SE	t.value	p.value
ar1	0.1501	0.0736	2.0395	0.0426
ma1	-0.9375	0.0237	-39.5128	0.0000
sar1	0.9474	0.0951	9.9615	0.0000
sma1	-0.8755	0.1472	-5.9484	0.0000

Forecast for data between 2016 - 2019



Real data and forecasting of SARIMA(1,1,1)x(0,1,1)₁₂

Model output from data before 2016

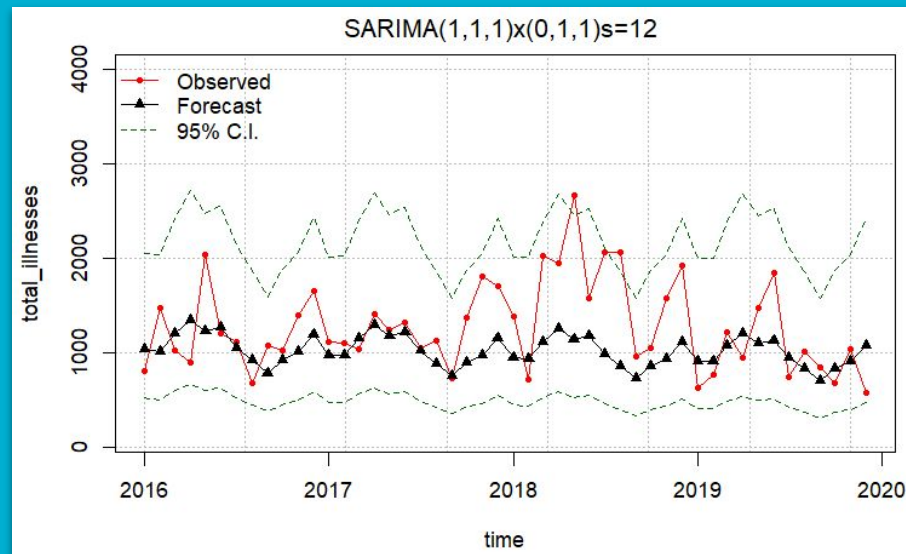
Data 1

```
$ttable
      Estimate      SE  t.value p.value
ar1    0.1371 0.0752   1.8244 0.0696
ma1   -0.9393 0.0290 -32.3892 0.0000
sma1  -0.9093 0.0857 -10.6136 0.0000
```

Data 2

```
$ttable
      Estimate      SE  t.value p.value
ar1    0.1164 0.0759   1.5346 0.1265
ma1   -0.9336 0.0300 -31.1513 0.0000
sma1  -0.9034 0.0820 -11.0127 0.0000
```

Forecast for data between 2016 - 2019



Real data and forecasting of ARIMA(1,1,1)-GARCH(1,0)

Model output from data before 2016

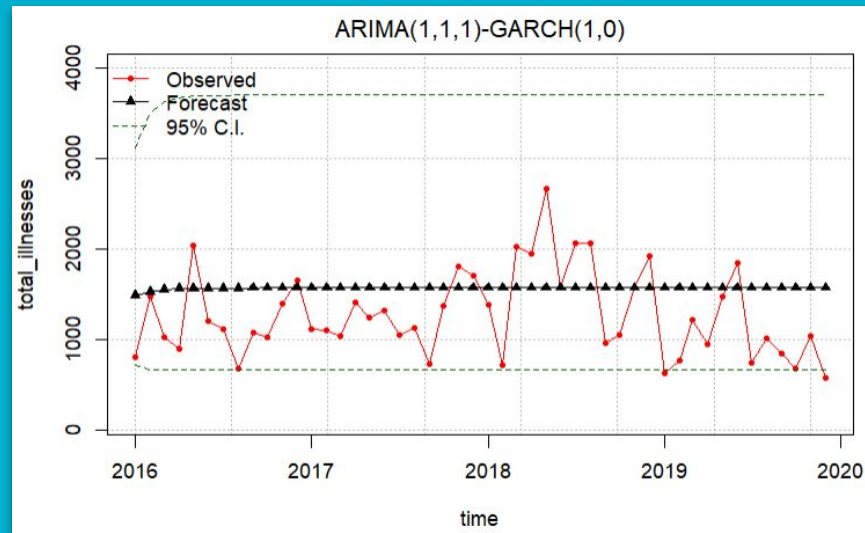
Data 1

Error Analysis:					
	Estimate	Std. Error	t value	Pr(> t)	
mu	3.65004	0.47009	7.765	8.22e-15	***
arl	0.50416	0.06355	7.934	2.22e-15	***
omega	0.14052	0.01639	8.575	< 2e-16	***
alpha1	0.01375	0.06644	0.207	0.836	

Data 2

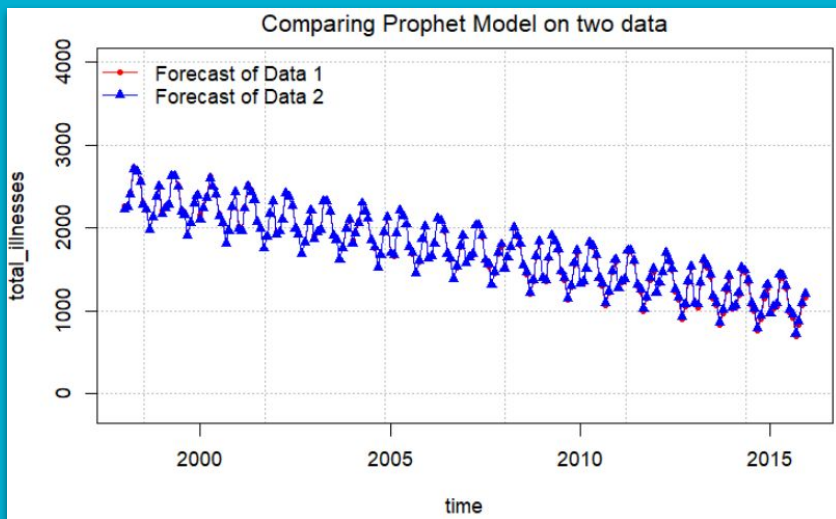
Error Analysis:					
	Estimate	Std. Error	t value	Pr(> t)	
mu	3.74032	0.48335	7.738	9.99e-15	***
arl	0.49186	0.06530	7.532	5.00e-14	***
omega	0.14107	0.01671	8.444	< 2e-16	***
alpha1	0.03958	0.07106	0.557	0.578	

Forecast for data between 2016 - 2019

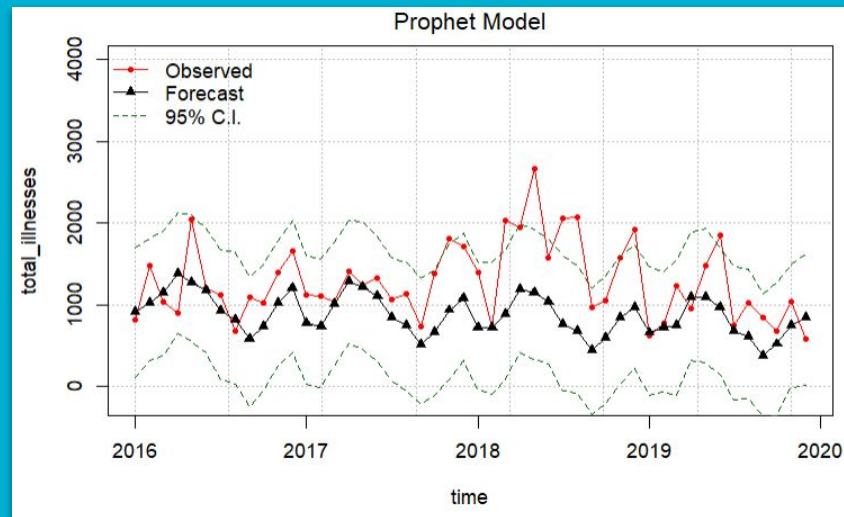


Real data and forecasting of Prophet Model

Fitting output from data before 2016



Forecast for data between 2016 - 2019



Conclusions

Key takeaways

1. *Model formulation and estimation.* We constructed six models (two ARIMA, two SARIMA, ARIMA-GARCH, Prophet) and compared their fit and forecasts.
2. *Model selection.* We chose the $\text{ARIMA}(1, 1, 1) \times (1, 0, 1)_{12}$ model, based on these criteria:
 - The seasonal ARIMA model has lower AIC and BIC values.
 - The forecast captures the seasonality of foodborne disease outbreaks better than non-seasonal models.
3. *Validation.* The RMSE of the forecast is the lowest of all models that include seasonality.

Learnings

Key Concepts:

- Importance of the data
- Time changes everything
- Impact of the Data

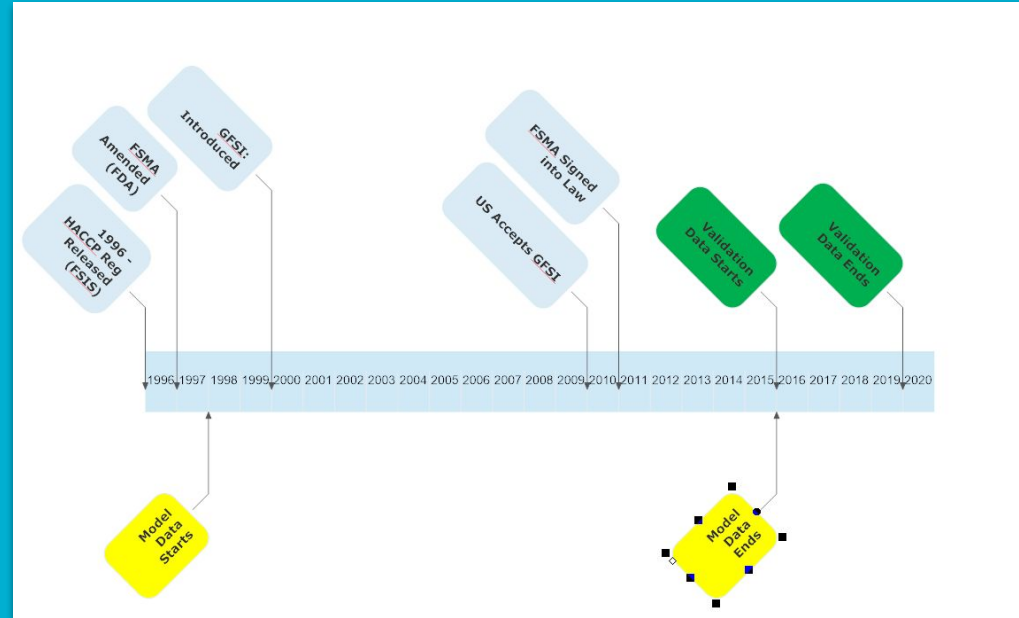
Importance of Data

- Data Cleaning
 - Source of the information
 - Understanding the basics of the project
 - Consumer habits
 - 2022 - Sal - 572 (92 / 2)
Backyard Poultry



Time Changes Everything

- Regulatory Changes
 - Time Delays in Implementation
- Improvements in Data Collection
- Improvements in Testing



“Salmonella contamination on broiler chickens (carcasses) decreased by 56 percent from 1995, before the HACCP final rule was announced, to 2000. The number of foodborne illness cases attributed to Salmonella on broilers was 190,000 lower in 2000 than in 1995.” — Williams and Ebel study, 2012

Outbreaks

- 1999 - Hot Dogs - LM - 100
- 2006 - Spinach - EC 205
- 2006 - Taco Bell - EC 71
- 2009 - Peanut Butter - SAL - 714
- 2011 - Canteloupes - LM 147
- 2011 - Ground Turkey - SAL - 136
- 2013 - Chicken - Sal - 634
- 2015 - Chipotle - EC - 55
- 2015 - Mexi Cucumbers - SAL - 907
- 2016 - Flour - EC 63
- 2017 - Leafy Greens - EC 25
- 2018 - Romaine - EC 272
- 2019 - Ground Beef - EC 209
- 2019 - Flour - EC 167



Impacts of the Data

- Determines success of the industry
- Basis for Regulatory Goals and Changes
 - Healthy People Goals - CDC
 - USDA / FDA Strategy
- Regulatory Changes -
 - Sal Adulterant - Kiev / Cordon Blue
 - Flour Mills
 - Exclusion of Supply



Questions, comments, suggestions?

**Thank you for your
engagement and feedback!**

Surprisingly good of Prophet Model

