### Computer Organization and Architecture

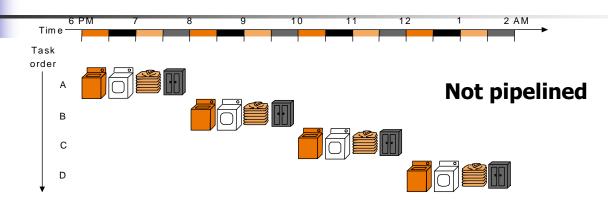
Slide Sources: Patterson &
Hennessy COD book site
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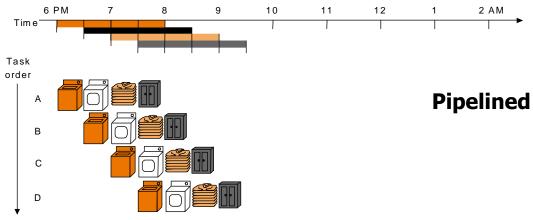
### COD Ch. 6 Enhancing Performance with Pipelining

#### **Pipelining**

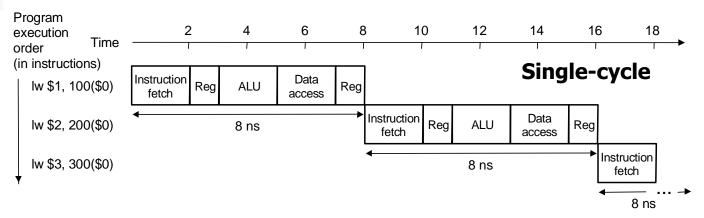
Start work ASAP!! Do not waste time!



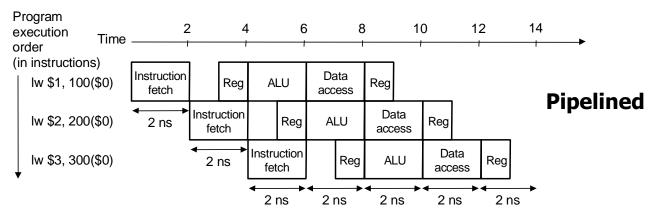
Assume 30 min. each task — wash, dry, fold, store — and that separate tasks use separate hardware and so can be overlapped



### Pipelined vs. Single-Cycle Instruction Execution: the Plan



Assume 2 ns for memory access, ALU operation; 1 ns for register access: therefore, single cycle clock 8 ns; pipelined clock cycle 2 ns.



#### Pipelining: Keep in Mind

- Pipelining does not reduce latency of a single task, it increases throughput of entire workload
- Pipeline rate *limited by longest stage*
  - potential speedup = number pipe stages
  - unbalanced lengths of pipe stages reduces speedup
- Time to fill pipeline and time to drain it when there is slack in the pipeline reduces speedup



#### **Example Problem**

- *Problem: for the laundry fill in the following table when* 
  - the stage lengths are 30, 30, 30 30 min., resp.
  - 2. the stage lengths are 20, 20, 60, 20 min., resp.

Person	Unpipelined finish time	-	Ratio unpipelined to pipeline 1	-	Ratio unpiplelined to pipeline 2
1			1 1		1 1
2					
3					
4					
n					

Come up with a formula for pipeline speed-up!

#### Pipelining MIPS

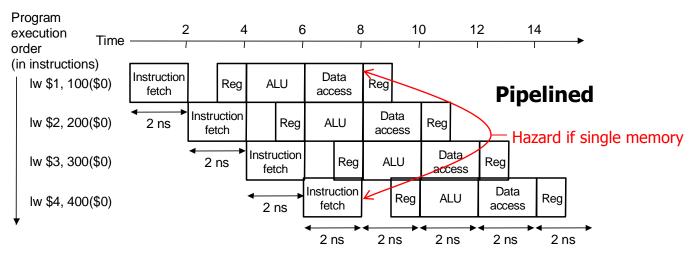
- What makes it easy with MIPS?
  - all instructions are same length
    - so fetch and decode stages are similar for all instructions
  - just a few instruction formats
    - simplifies instruction decode and makes it possible in one stage
  - memory operands appear only in load/stores
    - so memory access can be deferred to exactly one later stage
  - operands are aligned in memory
    - one data transfer instruction requires one memory access stage

#### Pipelining MIPS

- What makes it hard?
  - structural hazards: different instructions, at different stages, in the pipeline want to use the same hardware resource
  - control hazards: succeeding instruction, to put into pipeline, depends on the outcome of a previous branch instruction, already in pipeline
  - data hazards: an instruction in the pipeline requires data to be computed by a previous instruction still in the pipeline
- Before actually building the pipelined datapath and control we first briefly examine these potential hazards individually...

#### Structural Hazards

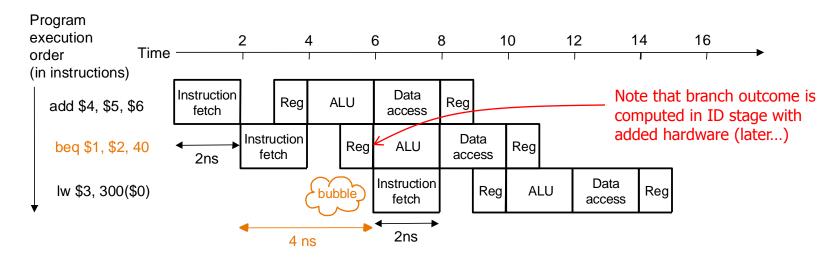
- Structural hazard: inadequate hardware to simultaneously support all instructions in the pipeline in the same clock cycle
- E.g., suppose single not separate instruction and data memory in pipeline below with one read port
  - then a structural hazard between first and fourth lw instructions



MIPS was designed to be pipelined: structural hazards are easy to avoid!

#### **Control Hazards**

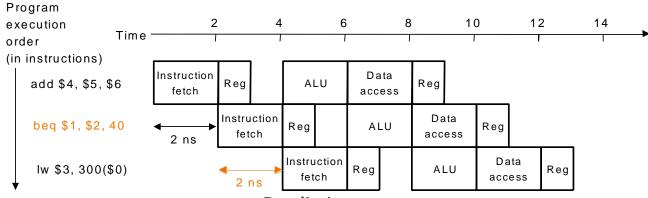
- Control hazard: need to make a decision based on the result of a previous instruction still executing in pipeline
- Solution 1 Stall the pipeline



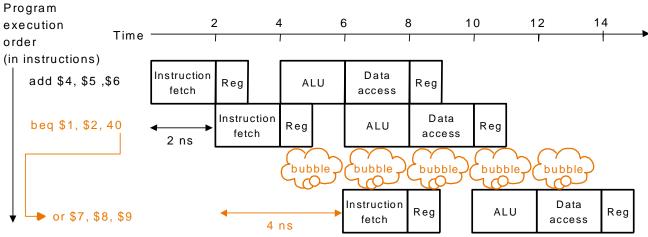
Pipeline stall

#### **Control Hazards**

- Solution 2 Predict branch outcome
  - e.g., predict branch-not-taken :



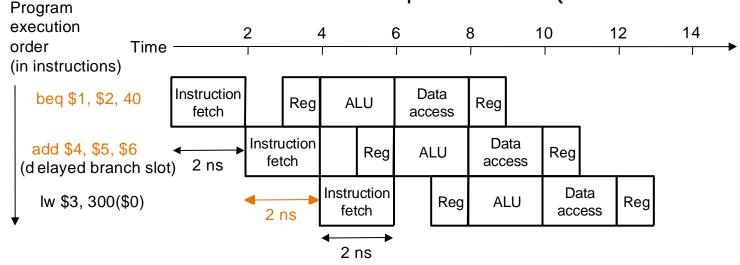
#### Prediction success



Prediction failure: undo (=flush) lw

#### **Control Hazards**

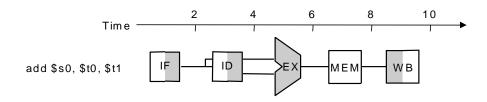
- Solution 3 Delayed branch: always execute the sequentially next statement with the branch executing after one instruction delay compiler's job to find a statement that can be put in the slot that is independent of branch outcome
  - MIPS does this but it is an option in SPIM (Simulator -> Settings)



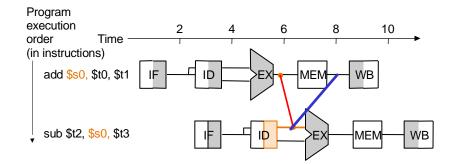
Delayed branch beq is followed by add that is independent of branch outcome

#### **Data Hazards**

- Data hazard: instruction needs data from the result of a previous instruction still executing in pipeline
- Solution Forward data if possible...



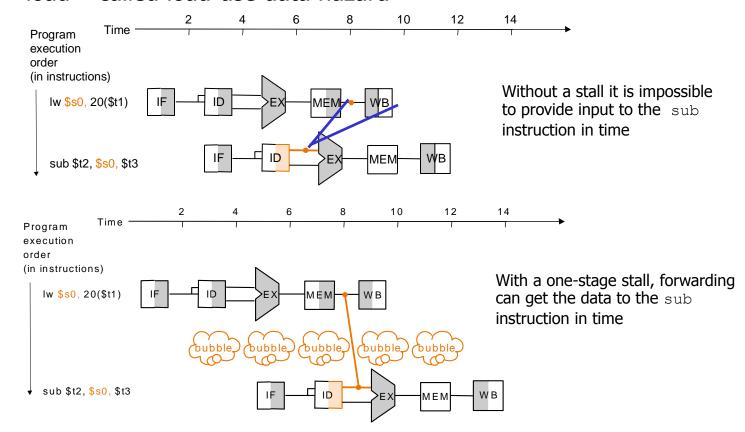
Instruction pipeline diagram: shade indicates use – left=write, right=read



Without forwarding – blue line – data has to go back in time; with forwarding – red line – data is available in time

#### **Data Hazards**

- Forwarding may not be enough
  - e.g., if an R-type instruction following a load uses the result of the load – called *load-use data hazard*



#### Reordering Code to Avoid Pipeline Stall (Software Solution)

#### Example:

```
lw $t0, 0($t1)
lw $t2, 4($t1)
sw $t2, 0($t1)
Data hazard
sw $t0, 4($t1)
```

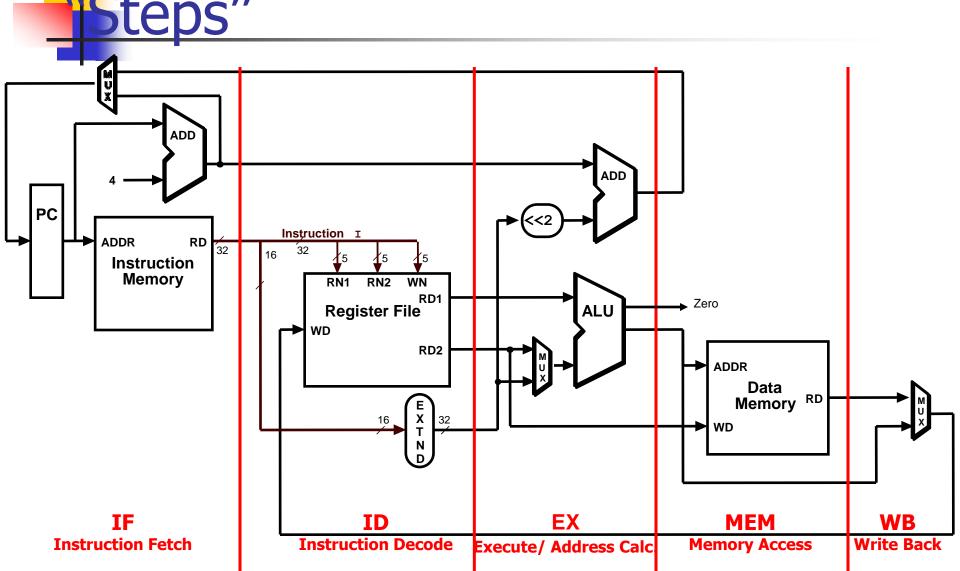
#### Reordered code:

```
lw $t0, 0($t1)
lw $t2, 4($t1)
sw $t0, 4($t1)
sw $t2, 0($t1)
Interchanged
```

#### Pipelined Datapath

- We now move to actually building a pipelined datapath
- First recall the 5 steps in instruction execution
  - Instruction Fetch & PC Increment (IF)
  - Instruction Decode and Register Read (ID)
  - 3. Execution or calculate address (EX)
  - 4. Memory access (MEM)
  - 5. Write result into register (WB)
- Review: single-cycle processor
  - all 5 steps done in a single clock cycle
  - dedicated hardware required for each step
- What happens if we break the execution into multiple cycles, but keep the extra hardware?

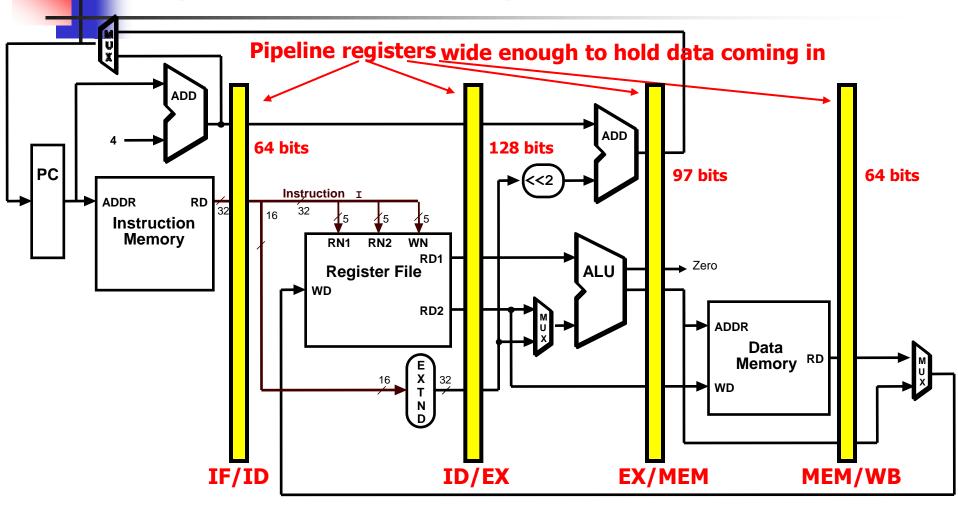
### Review - Single-Cycle Datapath



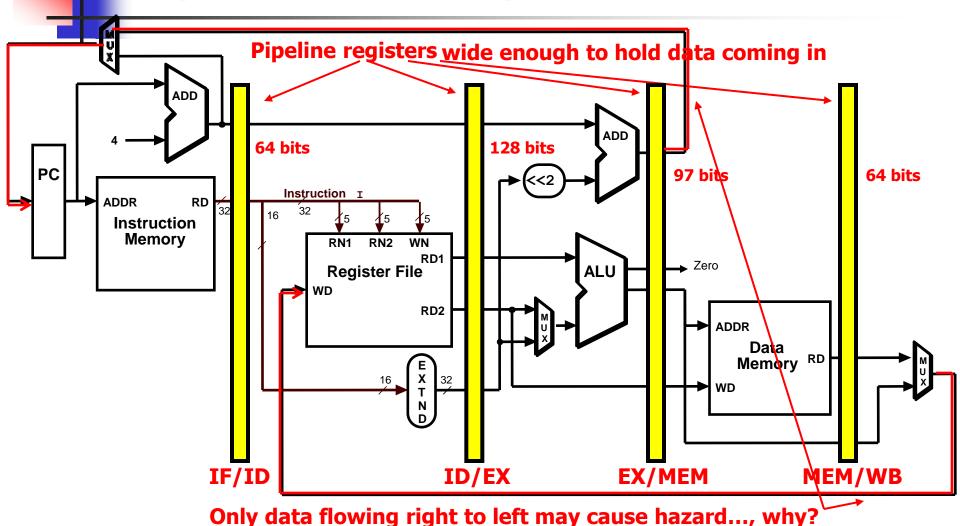
#### Pipelined Datapath – Key Idea

- What happens if we break the execution into multiple cycles, but keep the extra hardware?
  - Answer: We may be able to start executing a new instruction at each clock cycle pipelining
- ...but we shall need extra registers to hold data between cycles
  - pipeline registers

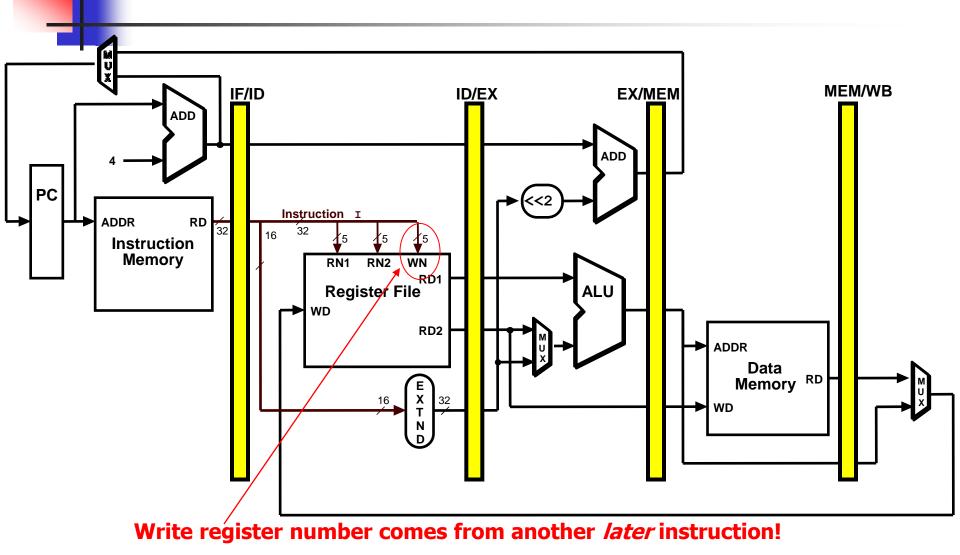
#### Pipelined Datapath



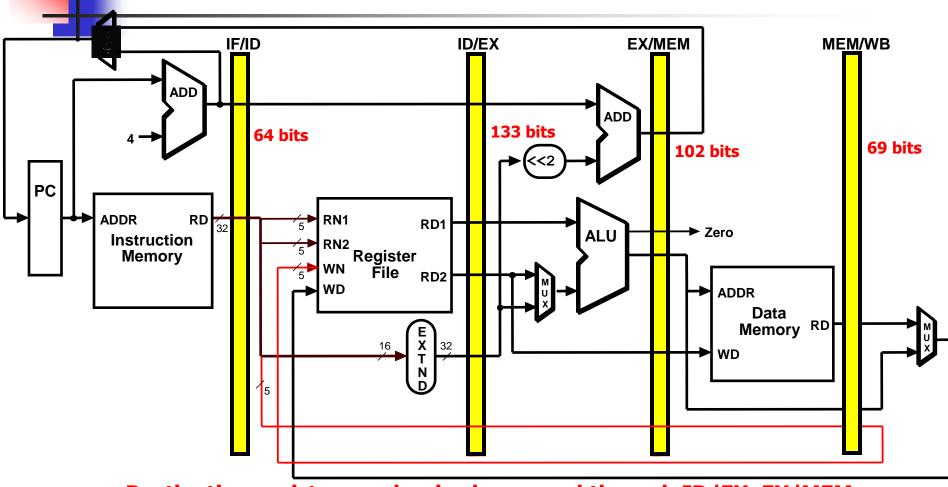
#### Pipelined Datapath



#### Bug in the Datapath



#### **Corrected Datapath**



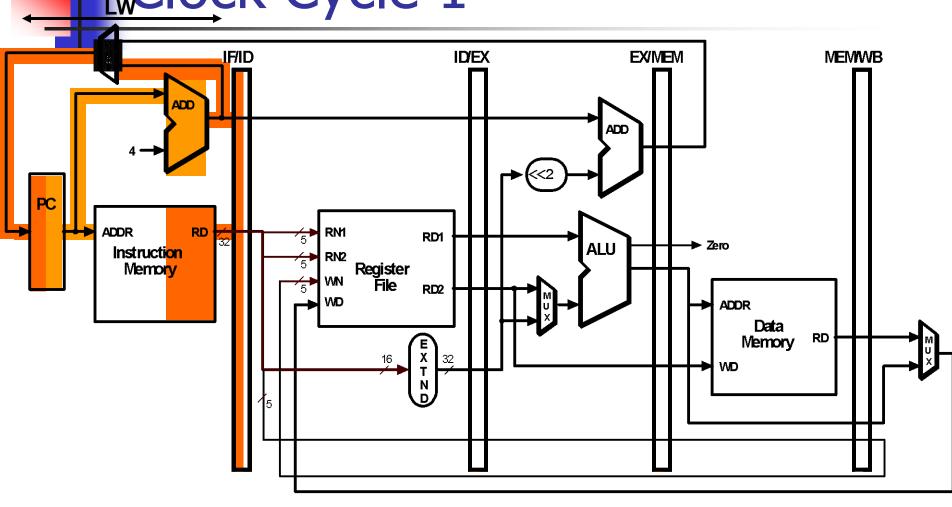
Destination register number is also passed through ID/EX, EX/MEM and MEM/WB registers, which are now wider by 5 bits

#### Pipelined Example

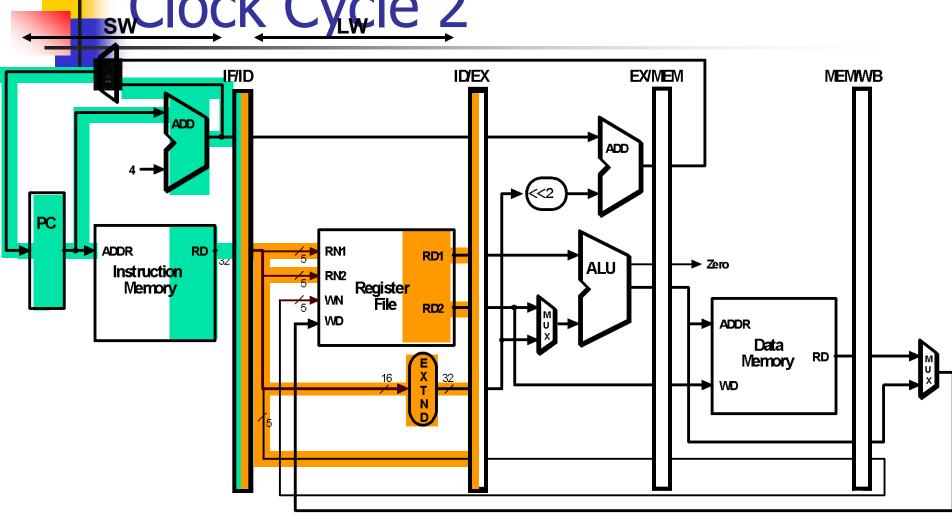
Consider the following instruction sequence:

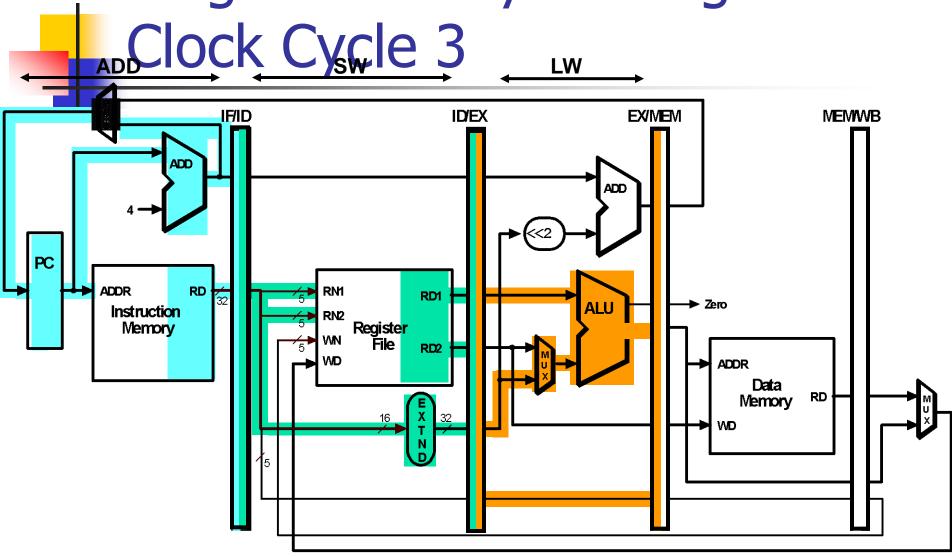
```
lw $t0, 10($t1)
sw $t3, 20($t4)
add $t5, $t6, $t7
sub $t8, $t9, $t10
```

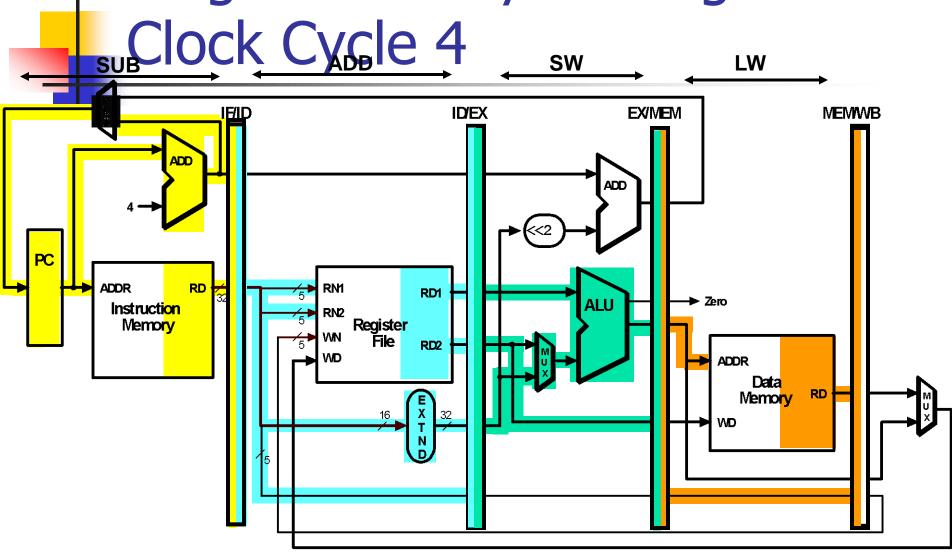
# Single-Clock-Cycle Diagram: Clock Cycle 1

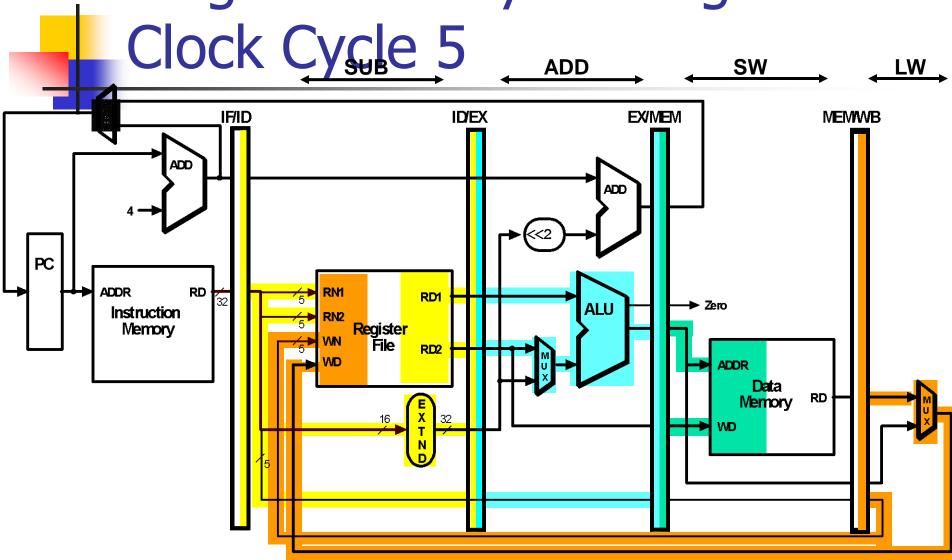


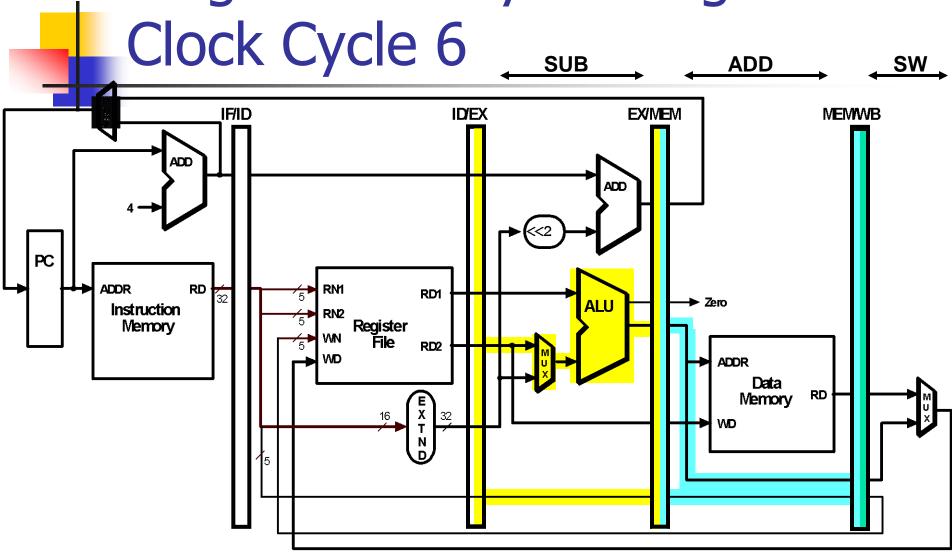
# Single-Clock-Cycle Diagram: Clock Cycle 2



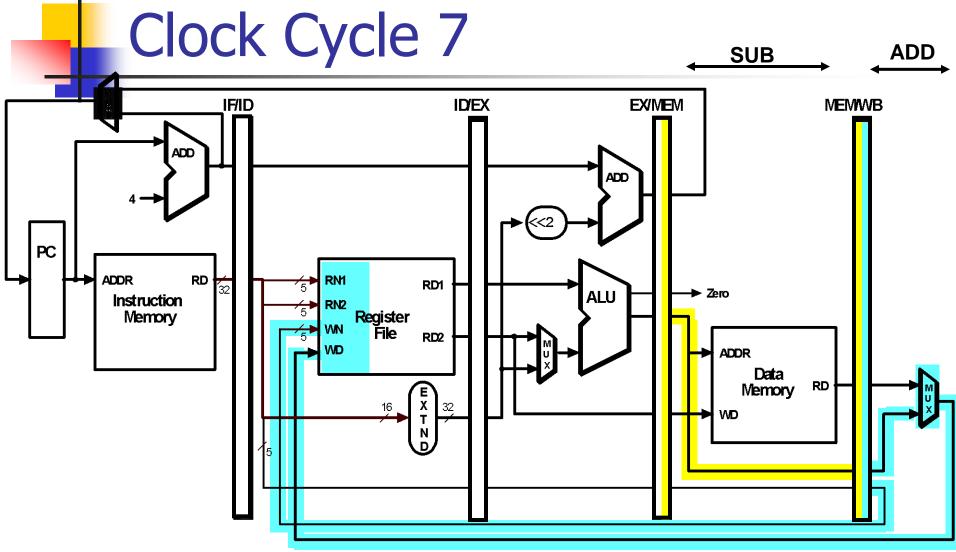




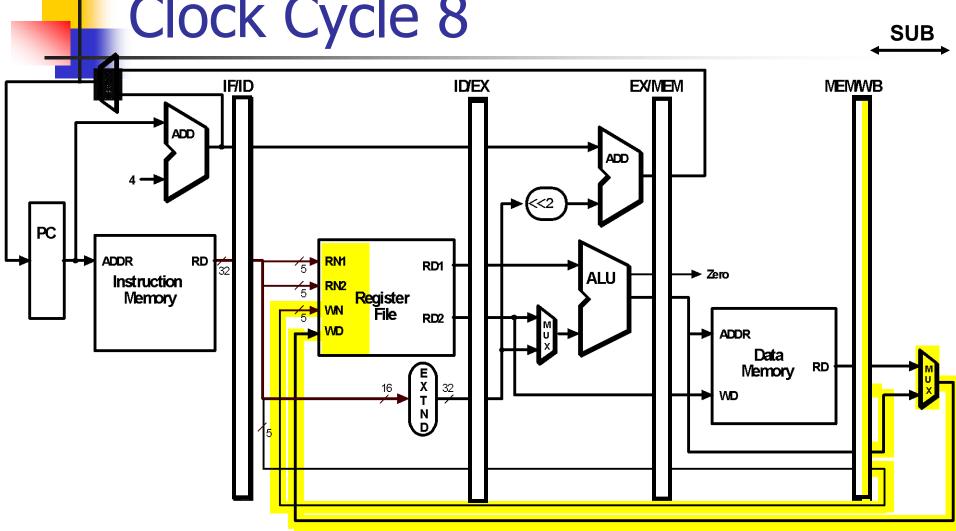




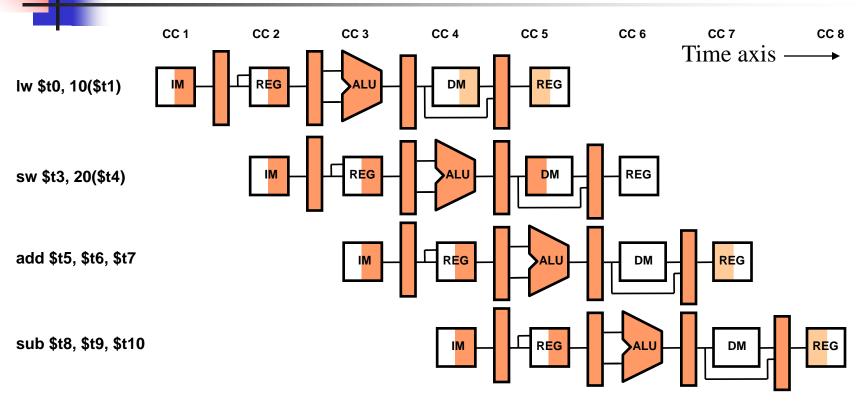
## Single-Clock-Cycle Diagram: Clock Cycle 7



# Single-Clock-Cycle Diagram: Clock Cycle 8



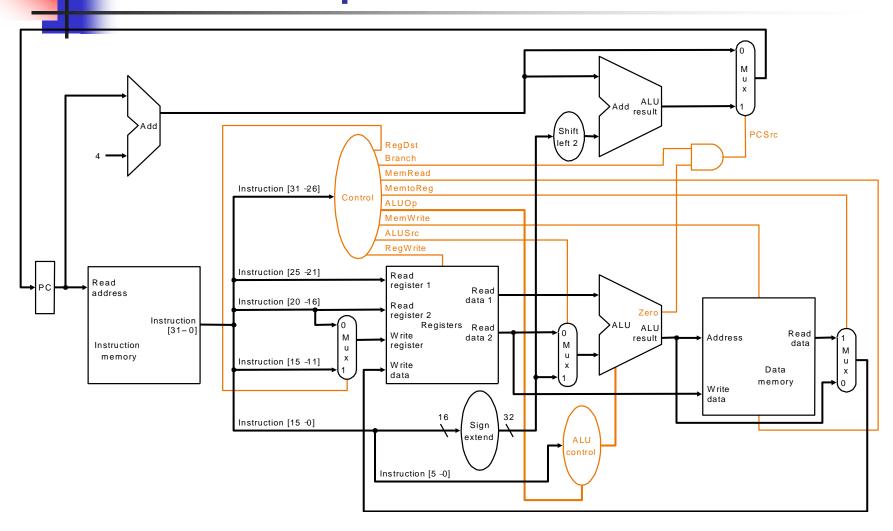
#### Alternative View – Multiple-Clock-Cycle Diagram



#### **Notes**

- One significant difference in the execution of an R-type instruction between multicycle and pipelined implementations:
  - register write-back for the R-type instruction is the 5<sup>th</sup> (the last write-back) pipeline stage vs. the 4<sup>th</sup> stage for the multicycle implementation. Why?
  - think of structural hazards when writing to the register file...
- Worth repeating: the essential difference between the pipeline and multicycle implementations is the insertion of pipeline registers to decouple the 5 stages
- The CPI of an ideal pipeline (no stalls) is 1. Why?
- The RaVi Architecture Visualization Project of Dortmund U. has pipeline simulations – see link in our Additional Resources page
- As we develop control for the pipeline keep in mind that the text does not consider jump – should not be too hard to implement!

## Recall Single-Cycle Control – the Datapath



#### Recall Single-Cycle – ALU Control

Instruction	AluOp	Instruction	Funct Field	Desired	ALU control
opcode		operation		<b>ALU</b> action	input
LW	00	load word	XXXXXX	add	010
SW	00	store word	XXXXXX	add	010
Branch eq	01	branch eq	XXXXXX	subtract	110
R-type	10	add	100000	add	010
R-type	10	subtract	100010	subtract	110
R-type	10	AND	100100	and	000
R-type	10	OR	100101	or	001
R-type	10	set on less	101010	set on less	111

ALUOp			Funct field					Operation
ALUOp1 ALUOp0		F5	F4	F3	F2	F1	F0	-
0	0	Χ	Χ	Χ	Χ	Χ	Χ	010
0	1	Χ	Χ	Χ	Χ	Χ	Χ	110
1	Χ	Χ	Χ	0	0	0	0	010
1	Χ	Χ	Χ	0	0	1	0	110
1	Χ	Χ	Χ	0	1	0	0	000
1	Χ	Χ	Χ	0	1	0	1	001
1	Χ	Χ	Χ	1	0	1	0	111

**Truth table for ALU control bits** 

#### Recall Single-Cycle – Control Signals

Signal Name	Effect when deasserted	Effect when asserted				
RegDst	The register destination number for the	The register destination number for the				
	Write register comes from the rt field (bits 20-16)	Write register comes from the rd field (bits 15-11)				
RegWrite	None	The register on the Write register input is written				
-		with the value on the Write data input				
AlLUSrc	The second ALU operand comes from the	The second ALU operand is the sign-extended,				
	second register file output (Read data 2)	lower 16 bits of the instruction				
PCSrc	The PC is replaced by the output of the adder	The PC is replaced by the output of the adder				
	that computes the value of PC + 4	that computes the branch target				
MemRead	None	Data memory contents designated by the address				
		input are put on the first Read data output				
MemWrite	None	Data memory contents designated by the address				
1 ICIII WIICC	Hone	input are replaced by the value of the Write data input				
MemtoReg	The value fed to the register Write data input	The value fed to the register Write data input				
Hemioney	-	•				
I	comes from the ALU	comes from the data memory				

Determining control bits

	Instruction	RegDst	ALUSrc	Memto- Reg				Branch	ALUOp1	ALUp0
	R-format	1	0	0	1	0	0	0	1	0
	lw	0	1	1	1	1	0	0	0	0
	SW	Х	1	Х	0	0	1	0	0	0
	beq	Х	0	Х	0	0	0	1	0	1

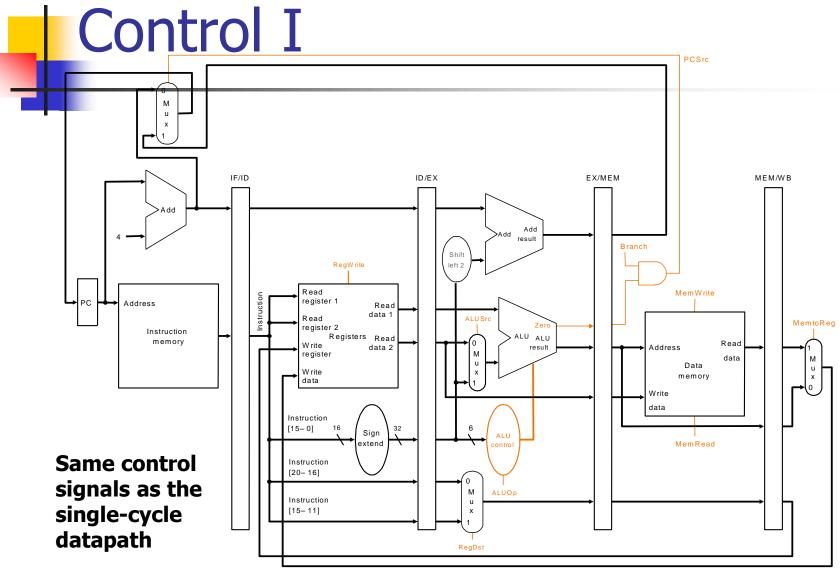
### Pipeline Control

- Initial design motivated by single-cycle datapath control use the same control signals
- Observe:
  - No separate write signal for the PC as it is written every cycle
  - No separate write signals for the pipeline registers as they are written every cycle

Will be modified by hazard detection unit!!

- No separate read signal for instruction memory as it is read every clock cycle
- No separate read signal for register file as it is read every clock cycle
- Need to set control signals during each pipeline stage
- Since control signals are associated with components active during a single pipeline stage, can group control lines into five groups according to pipeline stage

## Pipelined Datapath with



### Pipeline Control Signals

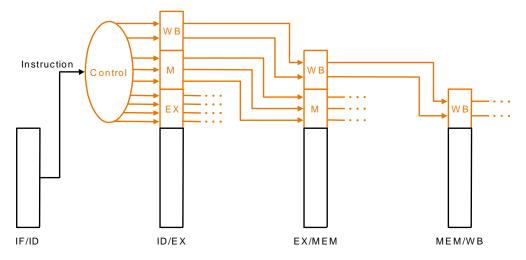
- There are five stages in the pipeline
  - instruction fetch | PC increment
  - instruction decode | register fetch
  - execution | address calculation
  - memory access
  - write back

Nothing to control as instruction memory read and PC write are always enabled

	Execution/Address Calculation stage control lines				Memory access stage control lines			stage control	
Instruction	Reg Dst	ALU Op1	ALU Op0	ALU Src	Branch	Mem Read	Mem Write	Reg write	Mem to Reg
R-format	1	1	0	0	0	0	0	1	0
lw	0	0	0	1	0	1	0	1	1
SW	Х	0	0	1	0	0	1	0	Х
beq	Х	0	1	0	1	0	0	0	X

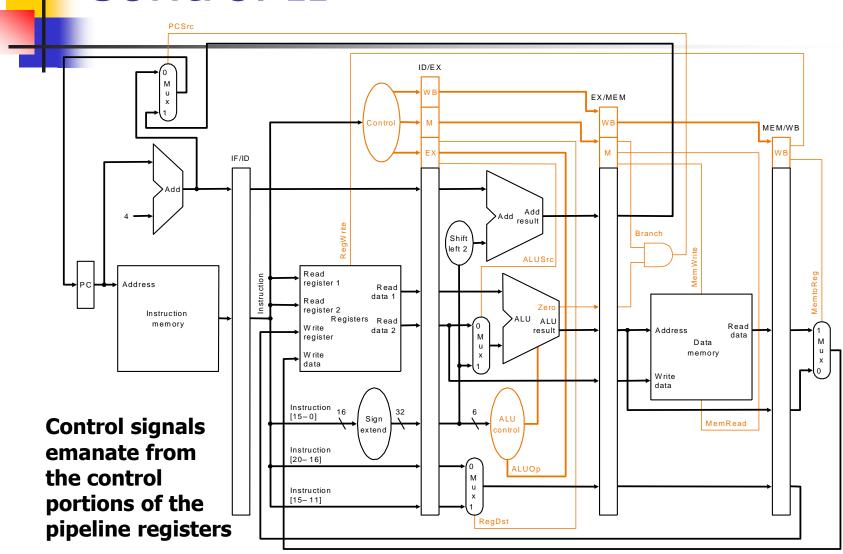
## Pipeline Control Implementation

 Pass control signals along just like the data – extend each pipeline register to hold needed control bits for succeeding stages



Note: The 6-bit funct field of the instruction required in the EX stage to generate ALU control can be retrieved as the 6 least significant bits of the immediate field which is sign-extended and passed from the IF/ID register to the ID/EX register

## Pipelined Datapath with Control II



Pipelined Execution

IF: lw \$10, 20(\$1)

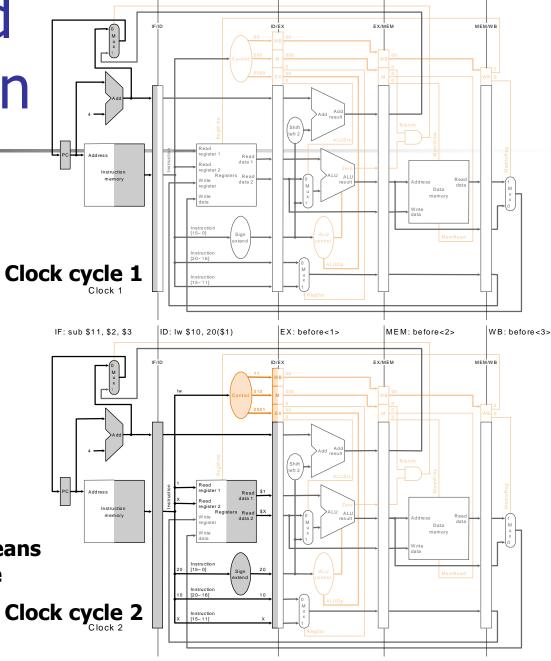
ID: before<1>

**Control** 

Instruction sequence:

lw \$10, 20(\$1)
sub \$11, \$2, \$3
and \$12, \$4, \$7
or \$13, \$6, \$7
add \$14, \$8, \$9

Label "before<i>" means i th instruction before 1w



EX: before<2>

MEM: before<3>

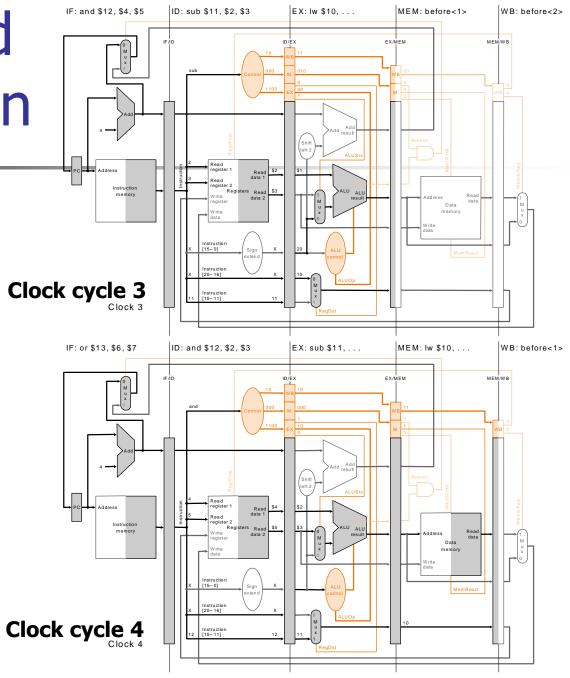
WB: before<4>

# Pipelined Execution

### **Control**

Instruction sequence:

lw \$10, 20(\$1)
sub \$11, \$2, \$3
and \$12, \$4, \$7
or \$13, \$6, \$7
add \$14, \$8, \$9



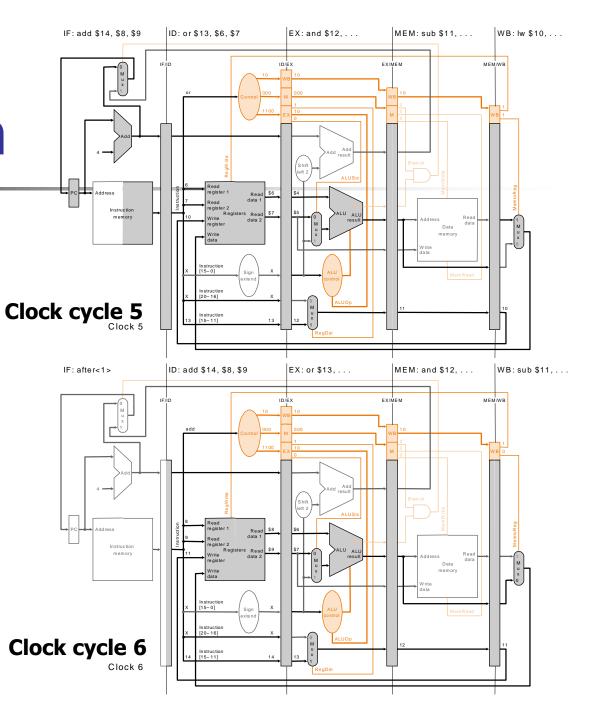
## Pipelined Execution

Control

Instruction sequence:

lw \$10, 20(\$1)
sub \$11, \$2, \$3
and \$12, \$4, \$7
or \$13, \$6, \$7
add \$14, \$8, \$9

Label "after<i>" means i th instruction after add



Pipelined
Execution
and
Control

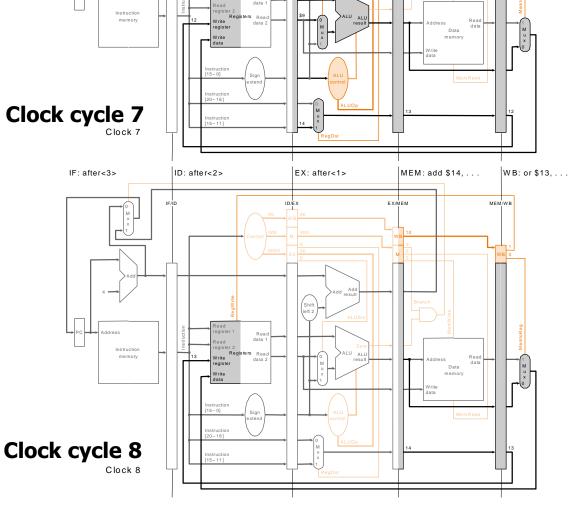
IF: after<2>

ID: after<1>

Instruction

sequence:

lw \$10, 20(\$1)
sub \$11, \$2, \$3
and \$12, \$4, \$7
or \$13, \$6, \$7
add \$14, \$8, \$9



EX: add \$14, . . .

MEM: or \$13, . . .

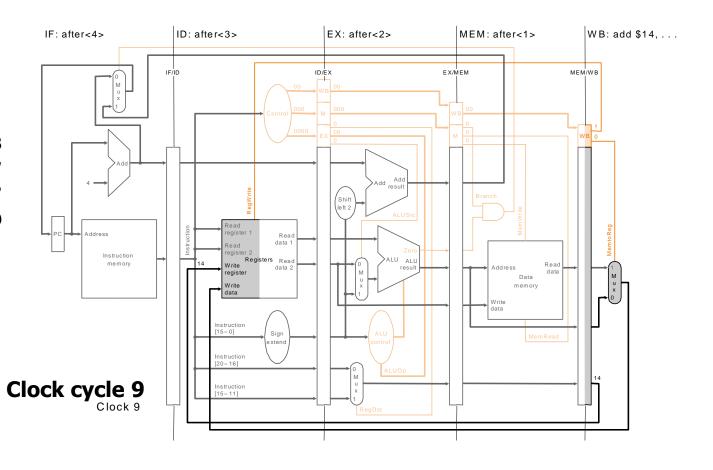
WB: and \$12....

MEM/WB

## Pipelined Execution and Control

Instruction sequence:

```
lw $10, 20($1)
sub $11, $2, $3
and $12, $4, $7
or $13, $6, $7
add $14, $8, $9
```

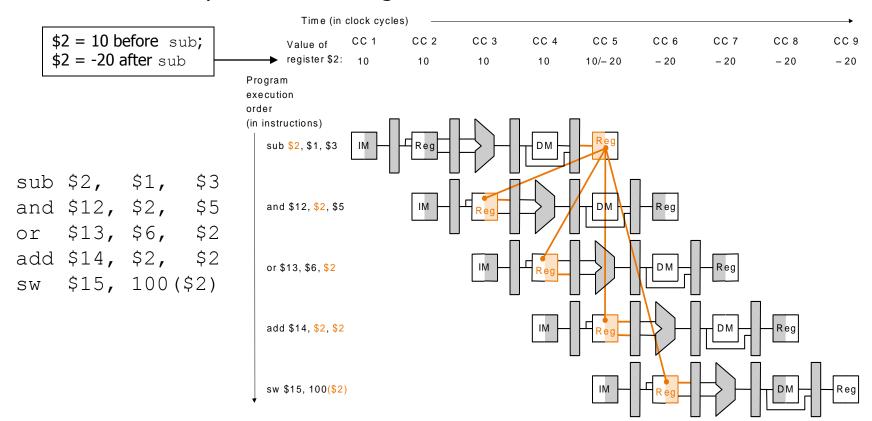




- So far our datapath and control have ignored hazards
- We shall revisit data hazards and control hazards and enhance our datapath and control to handle them in hardware...

### Data Hazards and Forwarding

- Problem with starting an instruction before previous are finished:
  - data dependencies that <u>go backward in time</u> called *data hazards*



### **Software Solution**

- Have compiler guarantee never any data hazards!
  - by rearranging instructions to insert independent instructions between instructions that would otherwise have a data hazard between them,
  - or, if such rearrangement is not possible, insert nops

```
      sub
      $2, $1, $3
      sub
      $2, $1, $3

      lw
      $10, 40($3)
      nop

      slt
      $5, $6, $7
      nop

      and
      $12, $2, $5
      or
      and
      $12, $2, $5

      or
      $13, $6, $2
      or
      $13, $6, $2

      add
      $14, $2, $2
      add
      $14, $2, $2

      sw
      $15, 100($2)
      sw
      $15, 100($2)
```

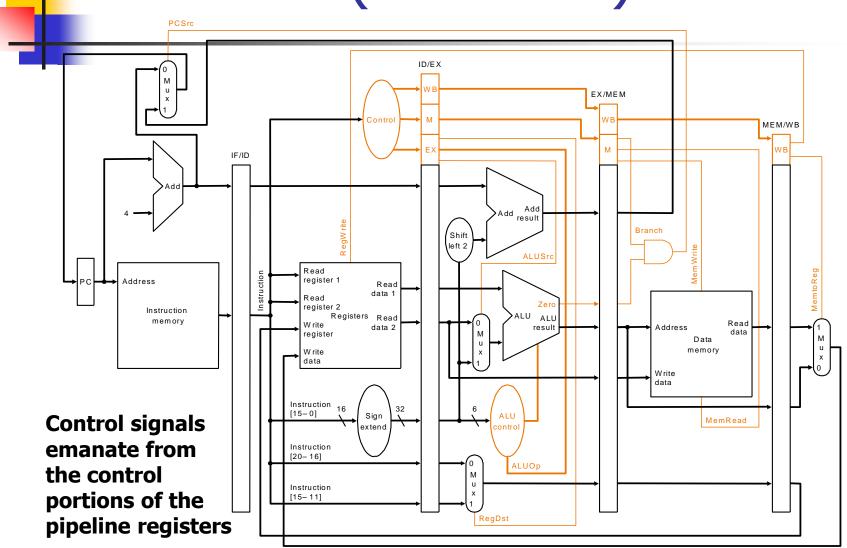
 Such compiler solutions may not always be possible, and nops slow the machine down

```
MIPS: nop = "no operation" = 00...0 (32bits) = s11 $0, $0, 0
```

# Hardware Solution: Forwarding

- Idea: use intermediate data, do not wait for result to be finally written to the destination register. Two steps:
  - Detect data hazard
  - 2. Forward intermediate data to resolve hazard

# Pipelined Datapath with Control II (as before)



### **Hazard Detection**

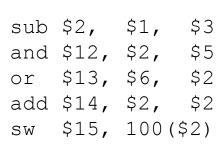
#### Hazard conditions:

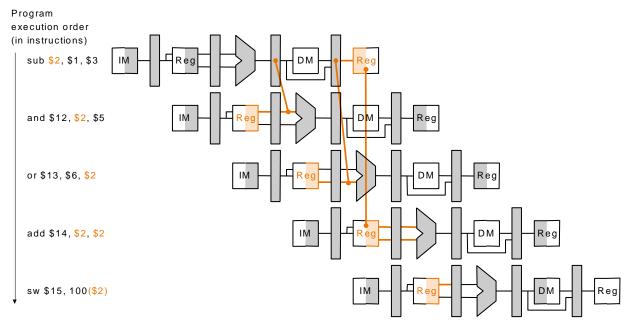
- 1a. EX/MEM.RegisterRd = ID/EX.RegisterRs
- 1b. EX/MEM.RegisterRd = ID/EX.RegisterRt
- 2a. MEM/WB.RegisterRd = ID/EX.RegisterRs
- 2b. MEM/WB.RegisterRd = ID/EX.RegisterRt
  - Eg., in the earlier example, first hazard between sub \$2, \$1, \$3 and and \$12, \$2, \$5 is detected when the and is in EX stage and the sub is in MEM stage because
    - EX/MEM.RegisterRd = ID/EX.RegisterRs = \$2 (1a)
- Whether to forward also depends on:
  - if the later instruction is going to write a register if not, no need to forward, even if there is register number match as in conditions above
  - if the destination register of the later instruction is \$0 in which case there is no need to forward value (\$0 is always 0 and never overwritten)

## Data Forwarding

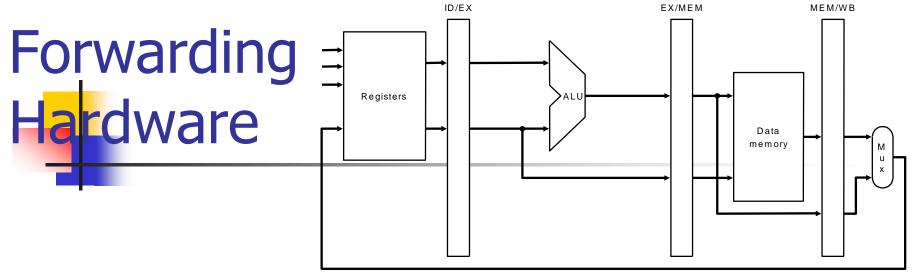
- - allow inputs to the ALU not just from ID/EX, but also later *pipeline registers*, and
  - use multiplexors and control signals to choose appropriate *inputs* to ALU

lime (in clock	cycles) —							$\longrightarrow$
CC 1	CC 2	CC 3	CC 4	CC 5	CC 6	CC 7	CC 8	CC 9
Value of register \$2: 10	10	10	10	10/- 20	- 20	- 20	- 20	- 20
Value of EX/MEM: X	X	X	- 20	X	Χ	X	X	X
Value of MEM/WB: X	Χ	Χ	Χ	- 20	Χ	Χ	Χ	Χ

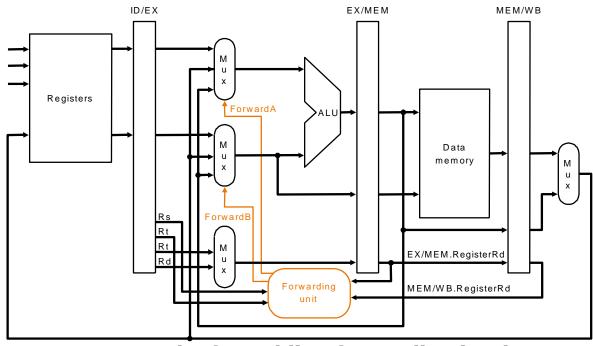




Dependencies between pipelines move forward in time



#### a. No forwar Datapath before adding forwarding hardware



b. With forwarding Datapath after adding forwarding hardware

## Forwarding Hardware: Multiplexor Control

Mux control	Source	Explanation
ForwardA = $00$	ID/EX	The first ALU operand comes from the register file
ForwardA = $10$	EX/MEM	The first ALU operand is forwarded from prior ALU result
ForwardA = $01$	MEM/WB	The first ALU operand is forwarded from data memory
		or an earlier ALU result —
ForwardB $= 00$	ID/EX	The second ALU operand comes from the register file
ForwardB = 10	EX/MEM	The second ALU operand is forwarded from prior ALU result
ForwardB $= 01$	MEM/WB	The second ALU operand is forwarded from data memory
		or an earlier ALU result

Depending on the selection in the rightmost multiplexor (see datapath with control diagram)

## Data Hazard: Detection and Forwarding

Forwarding unit determines multiplexor control according to the following rules:

#### EX hazard

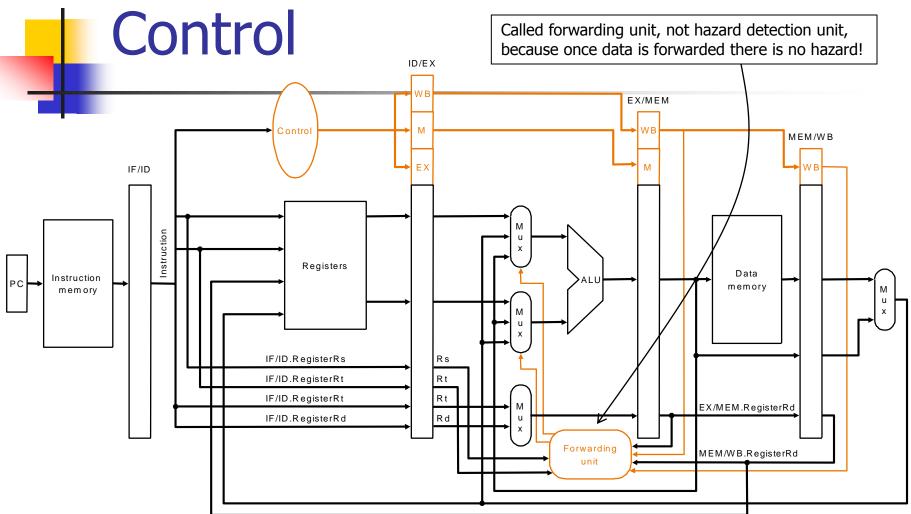
# Data Hazard: Detection and Forwarding

#### **MEM** hazard

```
MEM/WB.RegWrite
                                                      // if there is a write...
   and (MEM/WB.RegisterRd \neq 0)
                                                      // to a non-$0 register...
   and (EX/MEM.RegisterRd \neq ID/EX.RegisterRs)
                                                      // and not already a register match
                                                      // with earlier pipeline register...
  and ( MEM/WB.RegisterRd = ID/EX.RegisterRs ) ) // but match with later pipeline
                                                         register, then...
ForwardA = 01
if (
         MEM/WB.RegWrite
                                                      // if there is a write...
                                                      // to a non-$0 register...
   and (MEM/WB.RegisterRd \neq 0)
   and ( EX/MEM.RegisterRd \neq ID/EX.RegisterRt )
                                                      // and not already a register match
                                                      // with earlier pipeline register...
   and ( MEM/WB.RegisterRd = ID/EX.RegisterRt ) ) // but match with later pipeline
                                                         register, then...
ForwardB = 01
```

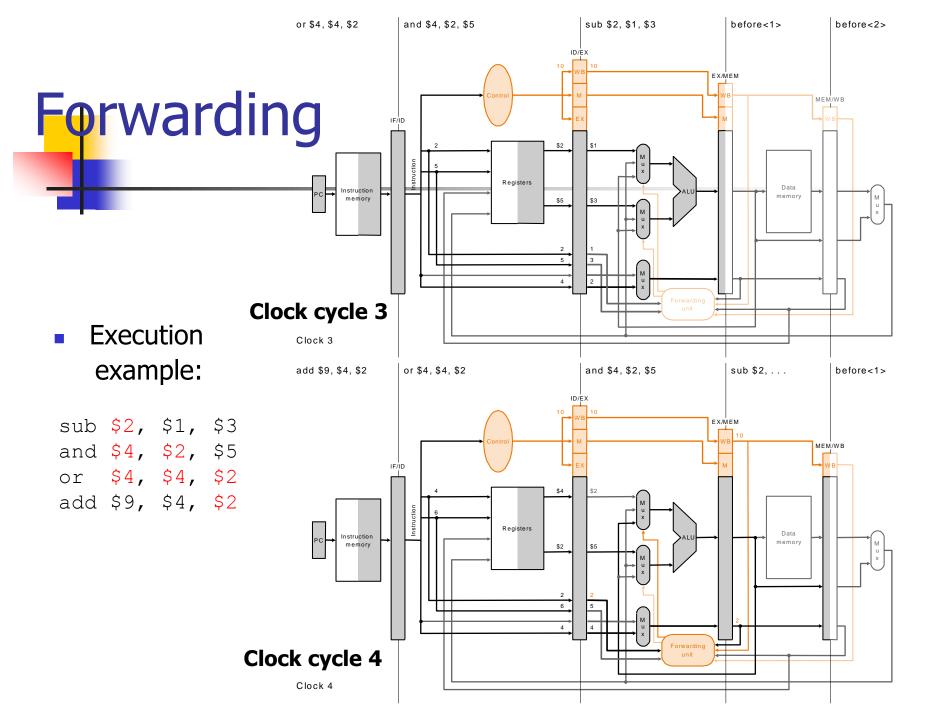
This check is necessary, e.g., for sequences such as add \$1, \$1, \$2; add \$1, \$1, \$3; add \$1, \$1, \$4; (array summing?), where an earlier pipeline (EX/MEM) register has more recent data

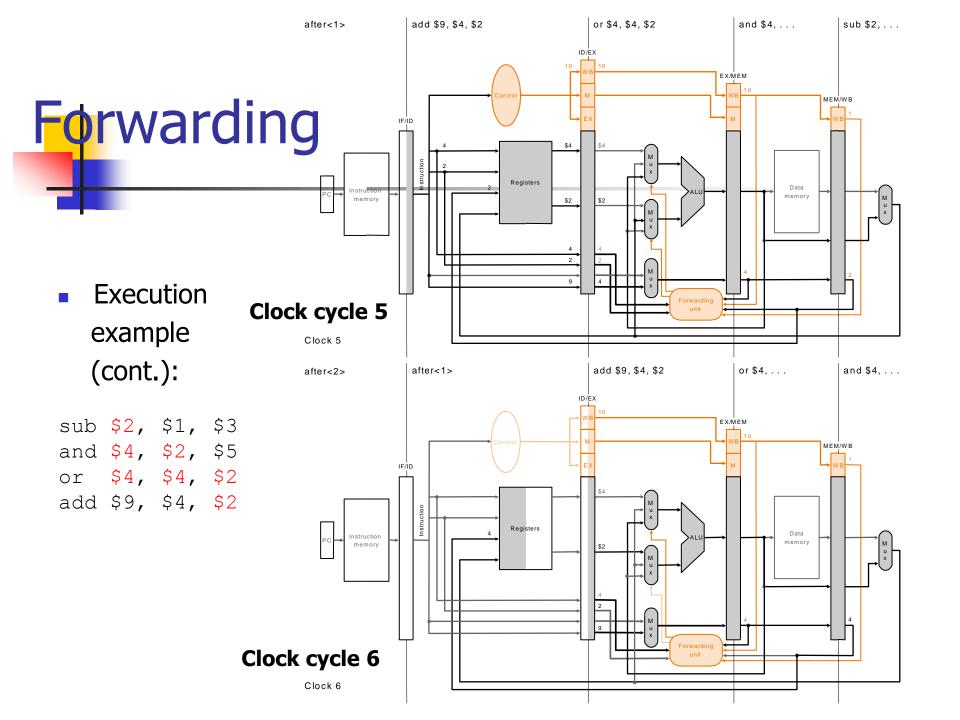
## Forwarding Hardware with



Datapath with forwarding hardware and control wires — certain details, e.g., branching hardware, are omitted to simplify the drawing

Note: so far we have only handled forwarding to R-type instructions...!



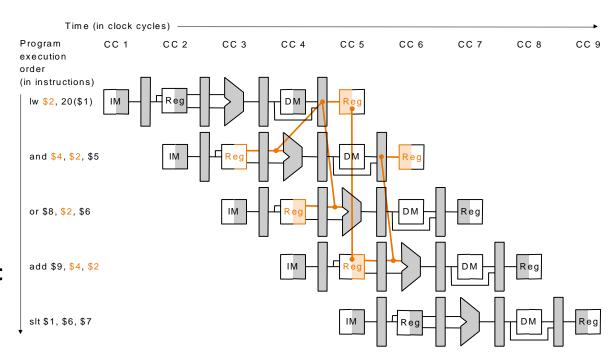


### Data Hazards and Stalls

Load word can still cause a hazard:

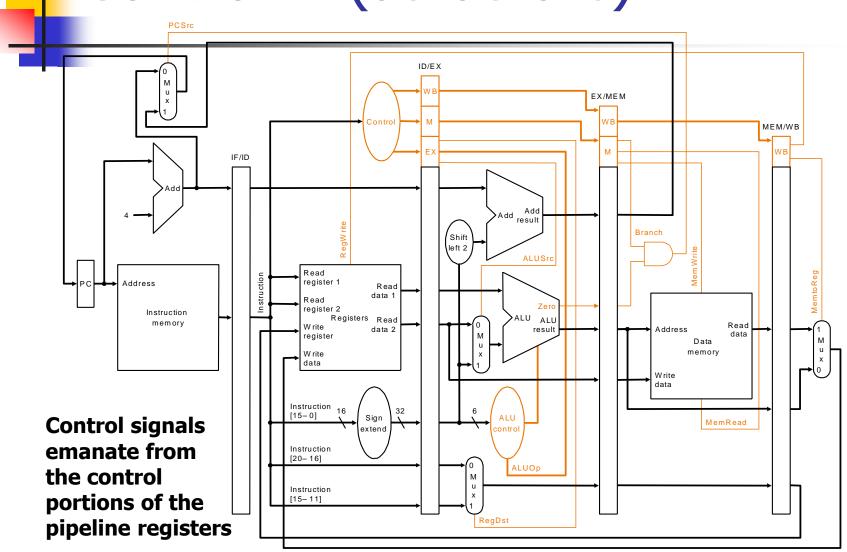
 an instruction tries to read a register following a load instruction that writes to the same register

As even a pipeline dependency goes backward in time forwarding will not solve the hazard



 therefore, we need a hazard detection unit to stall the pipeline after the load instruction

# Pipelined Datapath with Control II (as before)



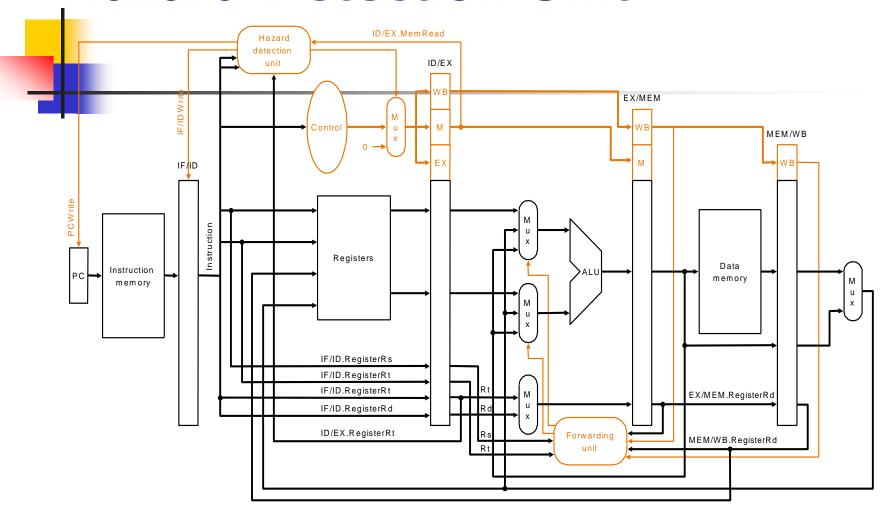
## Hazard Detection Logic to Stall

Hazard detection unit implements the following check if to stall

### Mechanics of Stalling

- If the check to stall verifies, then the pipeline needs to stall only 1 clock cycle after the load as after that the forwarding unit can resolve the dependency
- What the hardware does to stall the pipeline 1 cycle:
  - does not let the IF/ID register change (disable write!) this will cause the instruction in the ID stage to repeat, i.e., stall
  - therefore, the instruction, just behind, in the IF stage must be stalled as well – so hardware does not let the PC change (disable write!) – this will cause the instruction in the IF stage to repeat, i.e., stall
  - changes all the EX, MEM and WB control fields in the ID/EX
     pipeline register to 0, so effectively the instruction just behind
     the load becomes a nop a bubble is said to have been inserted
     into the pipeline
    - note that we cannot turn that instruction into an nop by 0ing all the bits in the instruction itself recall nop = 00...0 (32 bits) because it has already been decoded and control signals generated

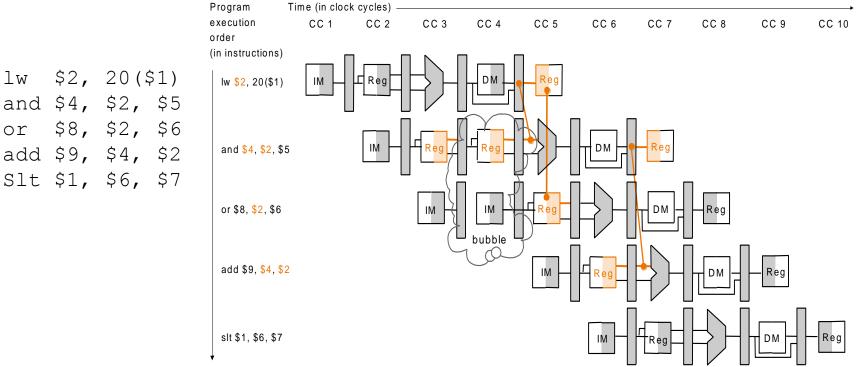
### Hazard Detection Unit



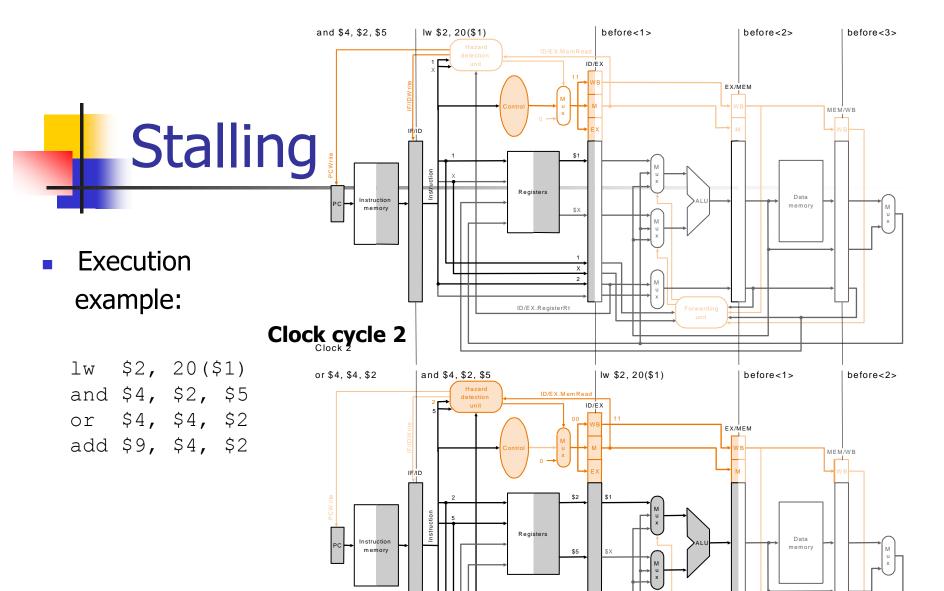
Datapath with forwarding hardware, the hazard detection unit and controls wires – certain details, e.g., branching hardware are omitted to simplify the drawing

## Stalling Resolves a Hazard

 Same instruction sequence as before for which forwarding by itself could not resolve the hazard:

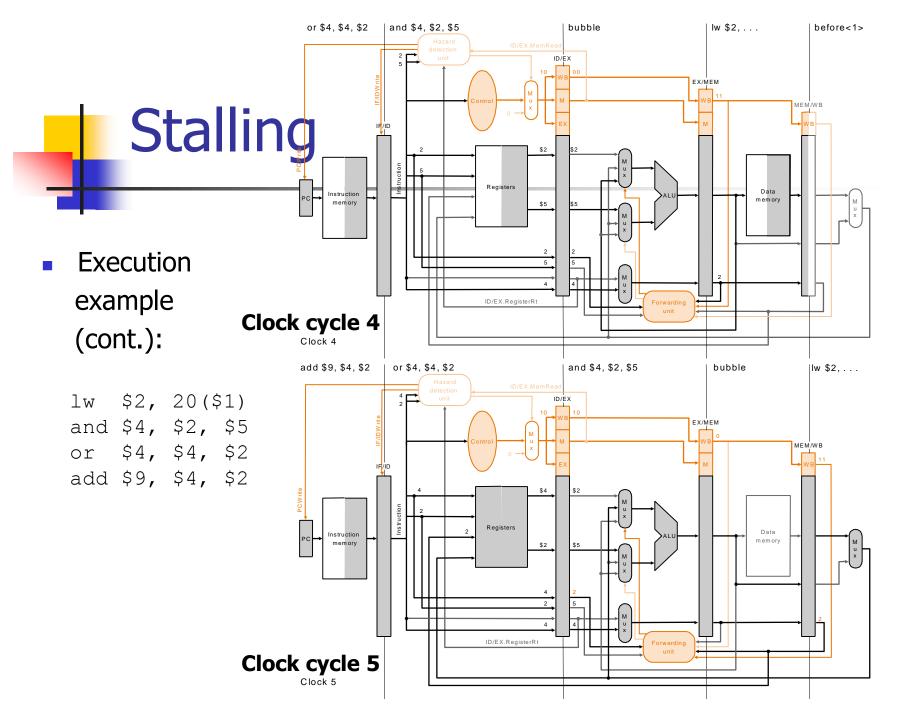


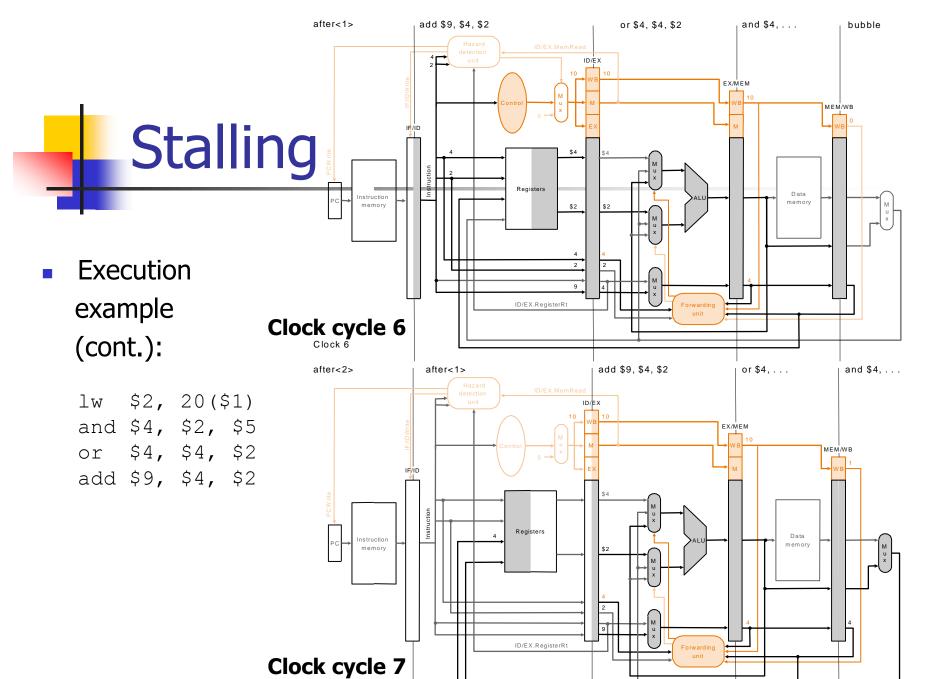
Hazard detection unit inserts a 1-cycle bubble in the pipeline, after which all pipeline register dependencies go forward so then the forwarding unit can handle them and there are no more hazards



Clock cycle 3

ID/EX.RegisterRt



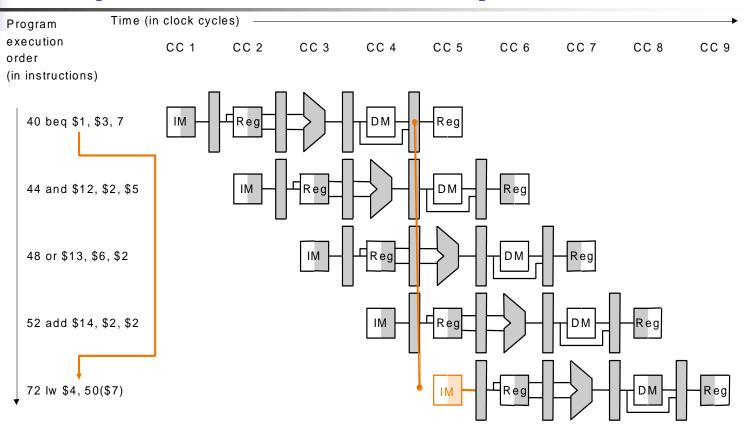


Clock 7

### Control (or Branch) Hazards

- Problem with branches in the pipeline we have so far is that the branch decision is not made till the MEM stage so what instructions, if at all, should we insert into the pipeline following the branch instructions?
- Possible solution: stall the pipeline till branch decision is known
  - not efficient, slow the pipeline significantly!
- Another solution: predict the branch outcome
  - e.g., always predict branch-not-taken continue with next sequential instructions
  - if the prediction is wrong have to flush the pipeline behind the branch – discard instructions already fetched or decoded – and continue execution at the branch target

# Predicting Branch-not-taken: Misprediction delay



The outcome of branch taken (prediction wrong) is decided only when beq is in the MEM stage, so the following three sequential instructions already in the pipeline have to be flushed and execution resumes at lw

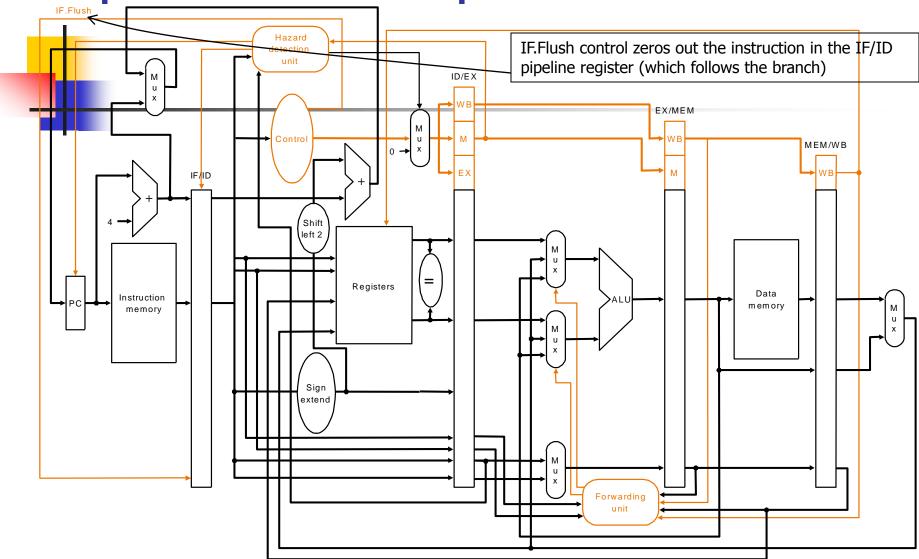
# Optimizing the Pipeline to Reduce Branch Delay

- Move the branch decision from the MEM stage (as in our current pipeline) earlier to the ID stage
  - calculating the branch target address involves moving the branch adder from the MEM stage to the ID stage – inputs to this adder, the PC value and the immediate fields are already available in the IF/ID pipeline register
  - calculating the branch decision is efficiently done, e.g., for equality test, by XORing respective bits and then ORing all the results and inverting, rather than using the ALU to subtract and then test for zero (when there is a carry delay)
    - with the more efficient equality test we can put it in the ID stage without significantly lengthening this stage – remember an objective of pipeline design is to keep pipeline stages balanced
  - we must correspondingly make additions to the forwarding and hazard detection units to forward to or stall the branch at the ID stage in case the branch decision depends on an earlier result



- Same strategy as for stalling on load-use data hazard...
- Zero out all the control values (or the instruction itself) in pipeline registers for the instructions following the branch that are already in the pipeline effectively turning them into nops so they are flushed
  - in the optimized pipeline, with branch decision made in the ID stage, we have to flush only one instruction in the IF stage – the branch delay penalty is then only one clock cycle

### Optimized Datapath for Branch



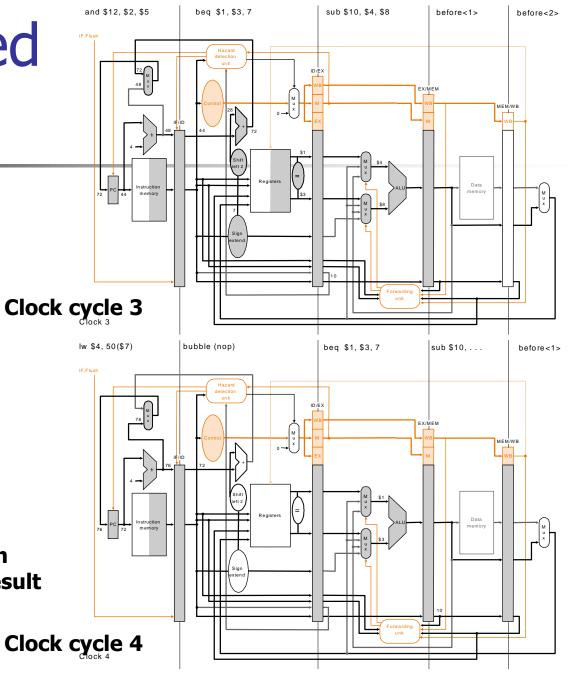
Branch decision is moved from the MEM stage to the ID stage — simplified drawing not showing enhancements to the forwarding and hazard detection units

## Pipelined Branch

Execution example:

36 sub \$10, \$4, \$8
40 beq \$1, \$3, 7
44 and \$12 \$2, \$5
48 or \$13 \$2, \$6
52 add \$14, \$4, \$2
56 slt \$15, \$6, \$7
...
72 lw \$4, 50(\$7)

Optimized pipeline with only one bubble as a result of the taken branch



## Simple Example: Comparing Performance

- Compare performance for single-cycle, multicycle, and pipelined datapaths using the gcc instruction mix
  - assume 2 ns for memory access, 2 ns for ALU operation, 1 ns for register read or write
  - assume gcc instruction mix 23% loads, 13% stores, 19% branches, 2% jumps, 43% ALU
  - for pipelined execution assume
    - 50% of the loads are followed immediately by an instruction that uses the result of the load
    - 25% of branches are mispredicted
    - branch delay on misprediction is 1 clock cycle
    - jumps always incur 1 clock cycle delay so their average time is 2 clock cycles

## Simple Example: Comparing Performance

- Single-cycle (p. 373): average instruction time 8 ns
- Multicycle (p. 397): average instruction time 8.04 ns
- Pipelined:
  - loads use 1 cc (clock cycle) when no load-use dependency and 2 cc when there is dependency – given 50% of loads are followed by dependency the average cc per load is 1.5
  - stores use 1 cc each
  - branches use 1 cc when predicted correctly and 2 cc when not given 25% misprediction average cc per branch is 1.25
  - jumps use 2 cc each
  - ALU instructions use 1 cc each
  - therefore, average CPI is
  - $1.5 \times 23\% + 1 \times 13\% + 1.25 \times 19\% + 2 \times 2\% + 1 \times 43\% = 1.18$
  - therefore, average instruction time is  $1.18 \times 2 = 2.36$  ns