

Calculus II. Quiz 0. Name

Key

Time

Show all work on this page for full and/or partial credit. Use a calculator to find the decimal answer, rounded to two decimal places. Angles are always in radians for Calculus. Put a box around both answers!

For each problem, find $f(1)$ and $f'(1)$.

Example: $f(x) = 3 \sin 2x$

$$f(1) = 3 \sin(2 \cdot 1) = 2.73$$

$$f'(x) = 6 \cos 2x$$

$$f'(1) = 6 \cos(2 \cdot 1) = -2.50$$

1. $f(x) = \sin^2(\pi x)$

$$f(1) = \sin^2 \pi = \boxed{0} \quad f'(x) = \boxed{2 \sin(\pi x) \cos(\pi x) \pi} \quad f'(1) = \boxed{0}$$

2. $f(x) = \ln 3x - x^2$

$$f(1) = \ln 3 - 1 = \boxed{0.098} \approx \boxed{0.1}$$

$$f'(x) = \boxed{\frac{1}{3x} (3) - 2x} = \frac{1}{x} - 2x$$

$$f'(1) = \frac{1}{1} - 2 = \boxed{-1}$$

3. $f(x) = (\ln 3)x$

$$f(1) = (\ln 3) 1 = 1.098 \approx \boxed{1.10}$$

$$f'(x) = \boxed{\ln 3}$$

$$f'(1) = \ln 3 = 1.098 \approx \boxed{1.10}$$

4. $f(x) = 2^{x^3}$

$$f(1) = 2^1 = \boxed{2}$$

$$f'(x) = \boxed{2^{x^3} (\ln 2) (3x^2)}$$

$$f'(1) = 2^1 (\ln 2) 3 = \boxed{4.16}$$

5. $f(x) = (2^x)^3 = 2^{3x} = 8^x$

$$f(1) = (2^1)^3 = \boxed{8}$$

$$f'(x) = \boxed{3(2^x)^2 2^x \ln 2} = 3(\ln 2) 2^{3x}$$

$$f'(1) = 3 \cdot 2^2 \cdot 2 \ln 2 = \boxed{16.64}$$