Discrete. Spring 20 Problems for Practice for Test 3. Also study the quizzes, and the previous two exams!

- 1. Given universe $\mathcal{U} = \{1, 2, 3, \dots, 107\}$; $A = \{7, 9, 10, 21, 25\}$; and $B = \{5, 4, 7, 10, 21\}$. Find the following:
 - $\bullet |\mathcal{P}(A)|$
 - The number of subsets of B of size 3.
 - $\bullet |A \cup B|$
 - $\bullet |\overline{A \cup B}|$
- 2. How many PIN's are there with 7 digits, no repeated digits?
- 3. How many PIN's are there with 4 digits, no repeated digits, and such that they obey the rule that: either the third digit is 0, the second digit is 2, or the last digit is 1? (more than one requirement can also be true.)
- 4. How many PIN's are there with 3 digits, repeated digits allowed, and such that the first digit is not 0 and the second digit is not 9?
- 5. How many ways can 7 students fill in the first row of 4 seats? (seated in order, leaving 3 students still standing.)
- 6. How many different committees of 4 people can be selected from a group of 10 people?
- 7. How many ways can 3 books be distributed to 7 shelves on a bookcase? (No ordering of the books on the shelves, just a loose pile.)
- 8. How many ways can we plan for 3 books to be placed on a bookcase with 7 shelves? (No books on the shelves yet, just the plan.)
- 9. How many ways are there to put 3 books on the 7 shelves of the bookcase in ordered rows?

How many ways can we plan for 3 books to be places on a bookcase with 7 shelves if at least one book must go on the top shelf? (No books yet, just the plan.)
How many ways are there to put 3 books on the 7 shelves of the bookcase in ordered rows if at least one book must go on the top shelf?
How many ways can 7 books be distributed to 3 shelves on a bookcase? (No ordering of the books on the shelves, just a loose pile.)
How many ways can we plan for 7 books to be placed on a bookcase with 3 shelves? (No books on the shelves yet, just the plan.)
How many ways are there to put 7 books on the 3 shelves of the bookcase in ordered rows?
How many ways can we plan for 7 books to be places on a bookcase with 3 shelves if at least two books must go on the top shelf? (No books yet, just the plan.)
How many ways are there to put 7 books on the 3 shelves of the bookcase in ordered rows if at least two books must go on the top shelf?