

Tests 11.2-11.6.*	Requirements for application	If this is true...	Then we conclude...
limit test for divergence	Any $a_n$	$\lim_{n \rightarrow \infty} a_n \neq 0$	$\sum a_n$ diverges
		$\lim_{n \rightarrow \infty} a_n = 0$	inconclusive
geo. series	$a_n = r^n$	$ r  < 1$	$\sum_{n=1}^{\infty} (r)^n$ converges to $\frac{r}{1-r}$
		$ r  \geq 1$	$\sum (r)^n$ diverges
p-series	$a_n = \frac{1}{n^p}$	$p > 1$	$\sum a_n$ converges
		$p \leq 1$	$\sum a_n$ diverges
integral test	$a_n = f(n); f(x) > 0,$ continuous and decreasing on $[1, \infty)$	$\int_1^{\infty} f(x) dx$ converges	$\sum a_n$ converges
		$\int_1^{\infty} f(x) dx$ diverges	$\sum a_n$ diverges
comparison test	$a_n > 0$ known $b_n > 0$	$a_n \leq b_n, \sum b_n$ converges	$\sum a_n$ converges
		$a_n \geq b_n, \sum b_n$ diverges	$\sum a_n$ diverges
limit comparison test	$a_n > 0$ known $b_n > 0$	$\lim_{n \rightarrow \infty} \frac{a_n}{b_n} = L, 0 < L < \infty$ and $\sum b_n$ converges	$\sum a_n$ converges
		$\lim_{n \rightarrow \infty} \frac{a_n}{b_n} = L, 0 < L < \infty$ and $\sum b_n$ diverges	$\sum a_n$ diverges
		$\lim_{n \rightarrow \infty} \frac{a_n}{b_n} = 0 \text{ or } \infty, \text{ or DNE}$	inconclusive
alternating series	$a_n > 0$ $a_{n+1} \leq a_n$	$\lim_{n \rightarrow \infty} a_n = 0$	$\sum (-1)^n a_n$ converges
		other wise	inconclusive
* absolute convergence	Any $a_n$	$\sum_{n=1}^{\infty}  a_n $ converges	$\sum a_n$ converges
		$\sum_{n=1}^{\infty}  a_n $ diverges	inconclusive
combinations	Any $a_n, b_n, c \in \mathbb{R}$ $d \in \mathbb{R}$	$\sum a_n$ converges and $\sum b_n$ converges	$\sum (ca_n + db_n)$ converges

More Convergence testing	Requirements for application.	If this is true...	Then we conclude
Ratio test	Any, but useful with $n!$ and $x^n$ .	$\lim_{n \rightarrow \infty} \left  \frac{a_{n+1}}{a_n} \right  = L < 1$	$\sum_{n=1}^{\infty} a_n$ converges absolutely.
		$\lim_{n \rightarrow \infty} \left  \frac{a_{n+1}}{a_n} \right  = L > 1$	$\sum_{n=1}^{\infty} a_n$ diverges
		$\lim_{n \rightarrow \infty} \left  \frac{a_{n+1}}{a_n} \right  = 1$	inconclusive
Root test	Any, but useful when there's an overall power of $n$ .	$\lim_{n \rightarrow \infty}  a_n ^{\frac{1}{n}} = L < 1$	$\sum_{n=1}^{\infty} a_n$ converges absolutely
		$\lim_{n \rightarrow \infty}  a_n ^{\frac{1}{n}} = L > 1$	$\sum_{n=1}^{\infty} a_n$ diverges
		$\lim_{n \rightarrow \infty}  a_n ^{\frac{1}{n}} = 1$	inconclusive
Ratio test for power series	looks like: $\sum_{n=0}^{\infty} C_n x^n$ or $\sum_{n=0}^{\infty} C_n (x-a)^n$	Use Ratio test: same conclusion as above with $L < 1$ , but $L$ is a function of $x$ . Solve to find radius $R$ around $a$ .	
End points for power series	Plug in $a+R$ and $a-R$ get $\sum C_n R^n$ and $\sum C_n (-R)^n$	use any of: <u>alt. series test</u> , <u>lim test for divergence</u> , <u>geometric series</u> , or <u>p-series</u> to decide which endpoint(s) converge/diverge.	