

3. Find the tangent slope to $y = \frac{7^x}{\sin(e^x)}$ at $x = 3$.

$$m = \frac{\sin(e^3)7^3 \ln 7 - 7^3 \cos(e^3)(e^3)}{\sin^2(e^3)}$$

4. Find the tangent line to the curve given by $xy + y = 7^x$ at $(x, y) = (0, 1)$.

$$y = ((\ln 7) - 1)x + 1$$

5. Find the linearization $L(x)$ to $f(x) = x^3 + 4x$ at $x_1 = 1$. Use it to approximate $f(1.01)$. Also give the differentials dx and dy .

$$\begin{aligned} L(x) &= 7(x - 1) + 5 \\ f(1.01) &\approx L(1.01) = 7(0.01) + 5 = 5.07 \\ dx &= 0.01; \quad dy = 7(0.01) = 0.07 \end{aligned}$$

6. Estimate $\ln(1.01)$ and $\ln(0.98)$ using linearization at $x = 1$.

$$\begin{aligned} L(x) &= x - 1 \\ \ln(1.01) &\approx L(1.01) = 0.01 \\ \ln(0.98) &\approx L(0.98) = -0.02 \end{aligned}$$

7. A particle is moving along the curve given by $xy + 1 = 2y^3e^{(x-1)}$. At the point (1,1) the x -coordinate is increasing at the rate 5 m/s. Find the rate of change in the y -coordinate.

$$y' = -1$$

8. A light on a 3 ft pole shines on a 1 inch mouse running away at 2 ft/s. How fast is the tip of the mouse shadow moving when it is 4 ft away?

$$y' = \frac{72}{35} \text{ ft/s}$$

9. A cylindrical tank with radius 5 m is being filled at a rate of $3 \text{ m}^3/\text{min}$. How fast is the height of the water increasing?

$$h' = \frac{3}{25\pi} \text{ m/min}$$