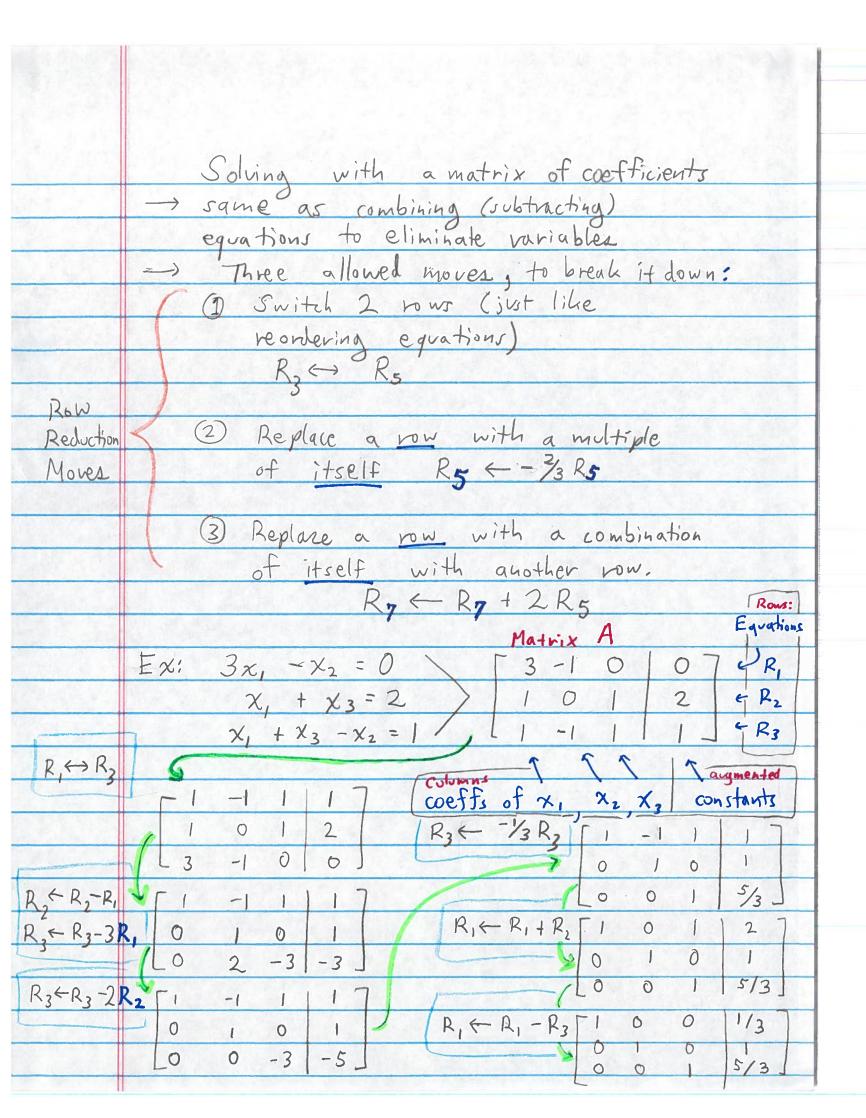
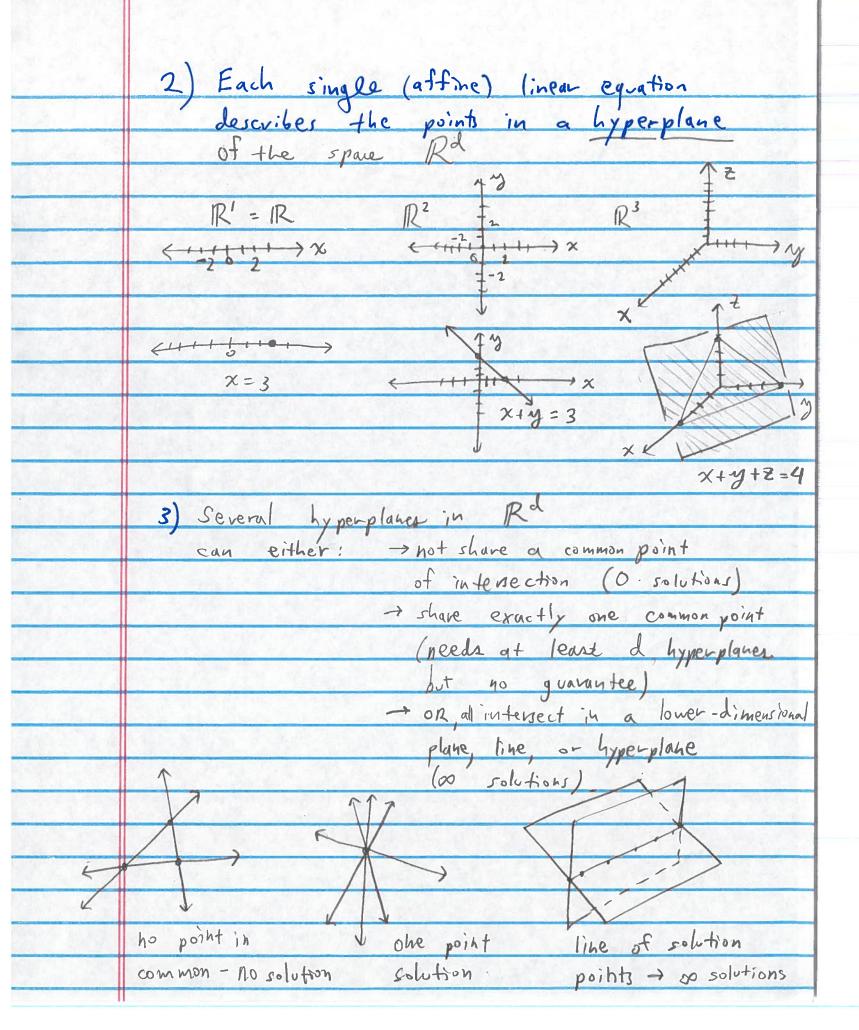
Linear Algebra Chp. 1 3,5,-1, =,1 scalar coefficients system $\begin{cases} 3x + 5y - 7 = 2 \\ x, y, t = 5 \end{cases}$ variables $\Rightarrow x - y = 0$ $y + \frac{1}{2}z = 1$ equations *affine scalar constants homogeneous linear equation linear equation (2 3x, - x2 = 0 homogeneous (Alternate scalar variables $\chi_1 + \chi_3 = 0$ 5 ys km of linear $\chi_1 + \chi_2 - \chi_2 = 0$ equations

Solve: 5 imultaneous solution (x_1, x_2, x_3) (1) Subtract equations: $x_1 + x_3 = 0$ $-(x_1 + x_3 - x_2 = 0)$ $\Rightarrow (x_2 = 0)$ (2) Substitute back: $3x_1 - 0 = 0$ $0 + x_3 = 0$ $\Rightarrow (x_1 = 0)$ $(x_1, x_2, x_3) = (0,0,0)$ makes all 3 + nve.





Goal # 1: be able to look at equations of know what the picture is, and vice versa: look at the picture and know things about the equations. Two lines in 12: crossing = different sloper parallel = same slope ex: $y = \frac{2}{3}x + 1$, $y = \frac{2}{3}x - 5$ 3y - 2x = 3, 3y - 2x = -5Slope = coefficients Three lives in IR2: 9 different pictures lines: Four Five lines: Six lines: In general n lines? 37,830 Seven lines: - open research 4,134,940 Eight lines: question. Un known Nine lines:

Back to solution me thod: matrix Amxn has on columns Recall, from a system of (affine) linear equations we write a matrix (augmented) of scalar coefficients and solve using [row reduction moves.] Two matrices are now equivalent, ArB, when you get from A to B by now reduction moves. of B with a ll "O"s before it in its now and and all "O"s above and below, in its column The now reduced echelon form of A (r.r.e.f.) is a matrix BrA where each row of B is either all O's or has a pirot 1 and the pirots in earlier (higher) rows are in earlier (Further left) columns, and "O" rows are at bottom. ex; → If A~B in rine.f, a privat column of A) is a column of A where that column in B has a pint

a system is solved when its matrix A of wefficients is put in r.r.e.f. B (the moves are also done on the augmented column of constants, but that column doesn't have to be in rire.f.) Then the virie, f. B is returned to equations as follows: · each column corresponds to an original variable x, y, z or x, x2, x3, x4,... (except the augment column, which is constants). · each pinot in B is a determined. variable of the solution: it will be on the left of an equation. · each non-pirot column of Bis a free variable, it can be any real number. ex: B (augment) 0100-2053 $\chi_1 = \chi_1$ (free!) 0001103 1/4 -> - x2-2x5+5x7 = 3 00000000 $\chi_3 = \chi_3$ (free!) X X X X X X -> x4 + x5 + 3x7 = 1/4 piwts Xs = Xs (free 1) X6 = X6 (free!) Next we solve $\chi_1 = \chi_7$ (free!) the non-free (Trive free)

(uviubles = 5 dimensional equations, one for each pirot.

	$\rightarrow x_i = x_i$	
	$\chi_2 = 3 + 2\chi_5 - 5\chi_7$ This is	the
à à E		eneval solution.
		e 00 solution
		ince choosing
		a for the free
	$\chi_7 = \chi_7$ wriables gives a specific solution.	
	Specific solution example:	
	x=0 < pick any!	2,=0
	$\chi_2 = ? \leftarrow find: 3 + 2(-2) - 5(0) = -1$	$\chi_2 = -1$
EL LO	X3=1 < pick any!	χ ₃ =
	$\chi_{4} = ? \leftarrow +ind: \frac{1}{4} - (-2) - 3(0) = \frac{9}{4}$	X4 = 9/4
	$\chi_{s}=-2 \leftarrow pick any!$	$\chi_s = -2$
	x6 = 3 ← pick any!	χ ₆ = 3
	$\chi_7 = 0 \leftarrow pick any!$	X7 = 0
	+ Other possibilities:	
	· only one unique solution: when every	
	column is a pivot column, and any now in B of	
	"O" i ends in an augment of O in that row,	
	· Zero solutions: when there is a row	
	of "O"s in B but the augment	
	column is not 0 in that row,	
	B	
	ex: [01000200]	
	00000005	no solution

So now we know some facts to conclude: has only one solution (x,y) This set of lines ...it has a matrix A3xz, (3 equations 2 variables) (with a extra augmented column) and together they now reduce to rire.f. B, (with augment), that has 2 pirots (both columns) and a now of "0" = (with 0 in augment) This set of lines > has no solutions! 111 50 it has a matrix Ayx2 (4 equations, 2 mrs) (with an extra augment column) which row reduces to r.r.e.f. B, (with augment) that has at least one now of "O's, with a nonzero entry in the augment of that row. ... And, it does have 2 pirots. Why? Just pick two crossing lines to be two rows. One solution!