(1) Find the eigenvalues and eigenspaces for:  $T: \mathcal{P}^3 \to \mathcal{P}^3$  where  $T(f) = x^2(f'')$  (multiplying by  $x^2$  after taking the second derivative.) Start by finding a matrix representation. Eigenspaces should be spans of polynomials.

(2) Find the eigenvalues and eigenspaces for:  $T: \mathcal{P}^3 \to \mathcal{P}^3$  where T(f) = ((x+1)f)' (multiplying by x+1 and then taking the derivative.) Eigenspaces should be spans of polynomials.