

Constraining primordial non-Gaussianity with  
cosmological observatoion

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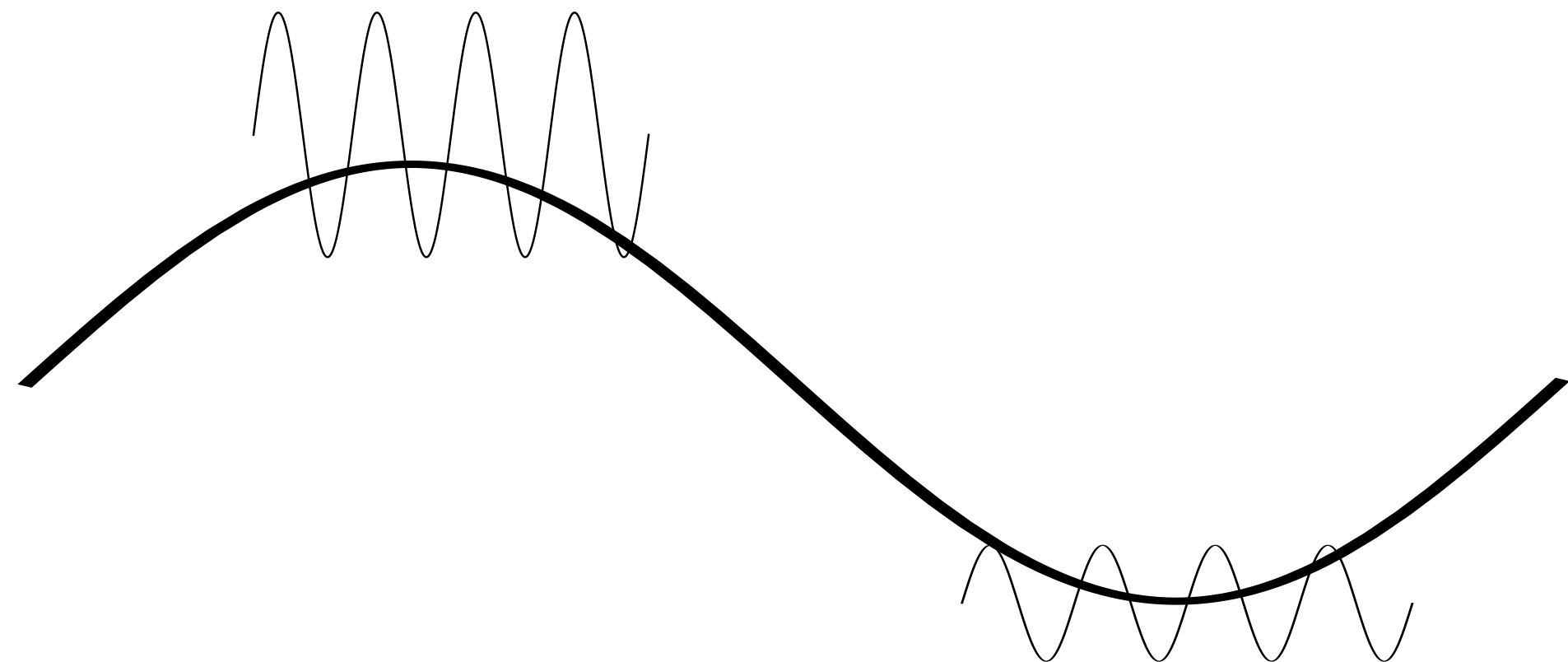
Planck 2015

$$\phi = \phi_G + f_{\text{NL}}(\phi_G^2 - \langle \phi_G^2 \rangle)$$

$$B_\phi(k_1, k_2, k_3)$$

Independent shape

$$f_{\text{NL}}^{\text{local}} = 0.8 \pm 5.0, f_{\text{NL}}^{\text{equil}} = -4 \pm 43 \text{ and } f_{\text{NL}}^{\text{ortho}} = -26 \pm 21$$



$$b_{\text{E}} = b_{\text{L}} + 1$$

See also Dalal et al. 2008

# f\_NL Constraint:

- Peculiar velocity field data
- (Future) 21-cm intensity mapping
- (Future) Multi-tracer technique

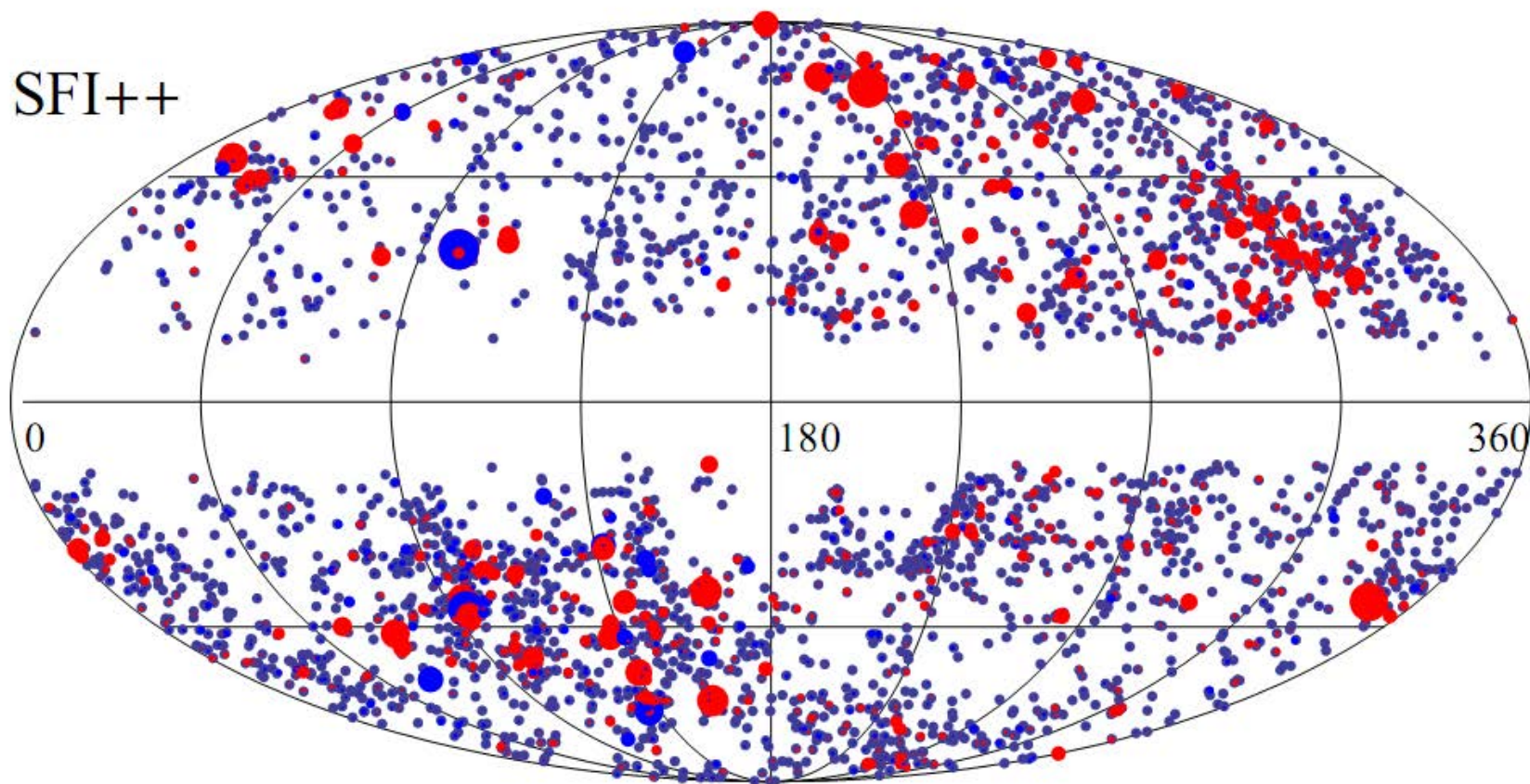
YZM, Douglas Scott, James E. Taylor, 2013, MNRAS

Yi-Chao Li and YZM, 2017, ArXiv: 1701.00221

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$$cz = H_0 r + v$$

# Linear perturbation theory: (Peebles 1971)

Linear bias factor:

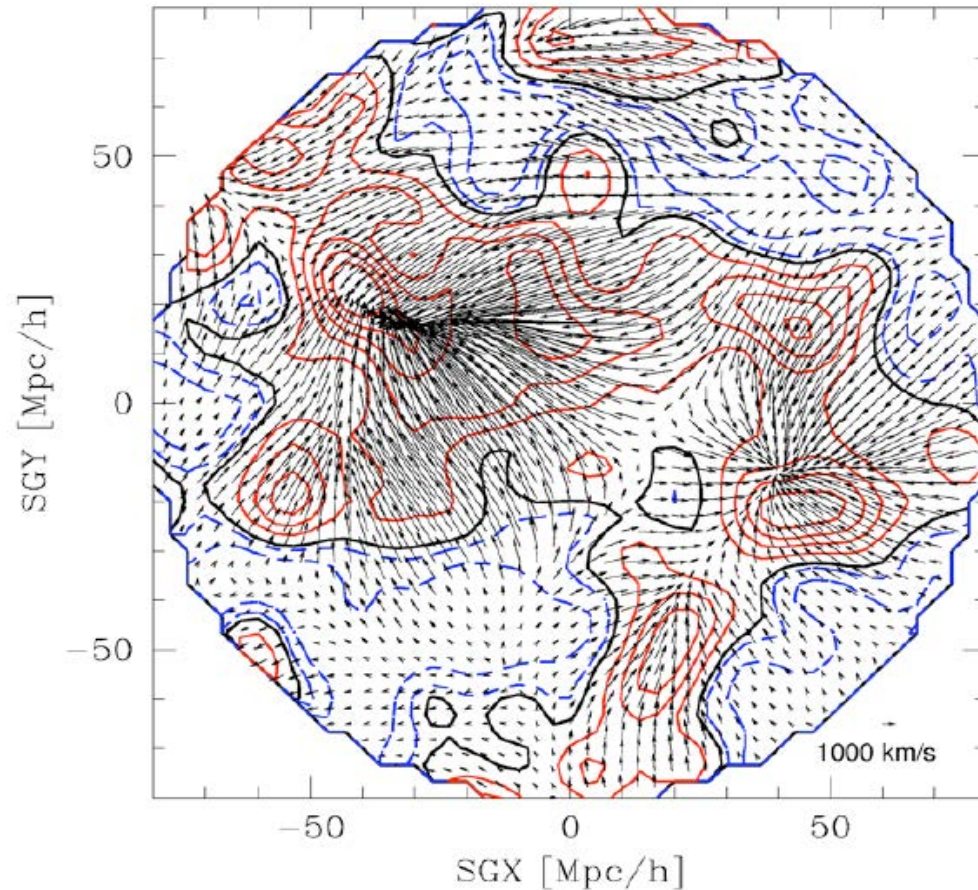
$$\vec{v}_g(\vec{x}) = \frac{H_0 f_0}{4\pi} \int d^3 \vec{x}' \delta_m(\vec{x}', t) \frac{(\vec{x}' - \vec{x})}{|\vec{x}' - \vec{x}|^3}$$

$$\delta_g = b \delta_m \quad f \equiv \frac{a}{D_1} \frac{dD_1}{da}$$

$$\vec{v}_g(\vec{x}) = \frac{H_0 \beta}{4\pi} \int d^3 \vec{x}' \delta_g(\vec{x}', t) \frac{(\vec{x}' - \vec{x})}{|\vec{x}' - \vec{x}|^3}$$

$$\beta = \frac{f_0}{b} = \frac{f_0}{(\sigma_8^{gal}/\sigma_8)}$$

$$\beta \sigma_8^{gal} = f_0 \sigma_8$$

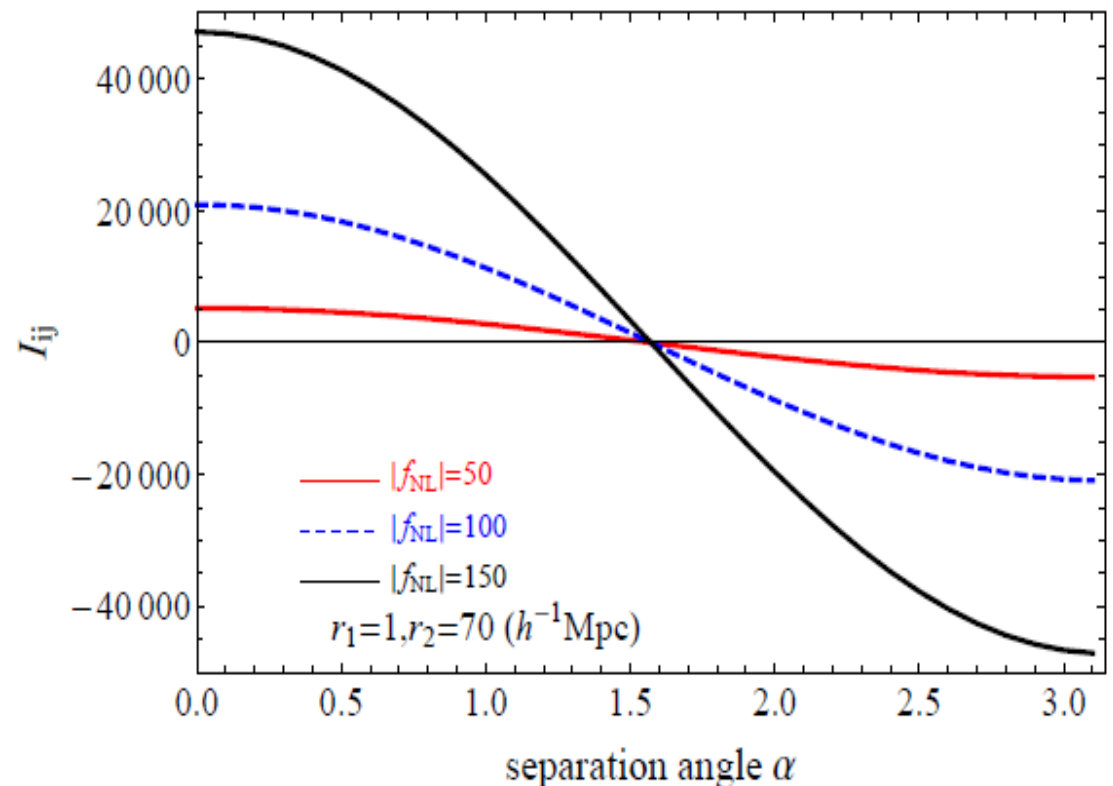


$$\begin{aligned} \mathbf{v}(\mathbf{r}) &= \frac{H_0 \beta}{4\pi} \int d^3 \mathbf{r}' \delta_g(\mathbf{r}') \frac{\mathbf{r}' - \mathbf{r}}{|\mathbf{r}' - \mathbf{r}|^3} \\ &- \frac{i H_0 (f/b)}{(2\pi)^3} \int d^3 \mathbf{k} (\Delta b(k)) \delta_m(\mathbf{k}) \frac{\mathbf{k}}{k^2} \exp(i\mathbf{k} \cdot \mathbf{r}) \end{aligned}$$

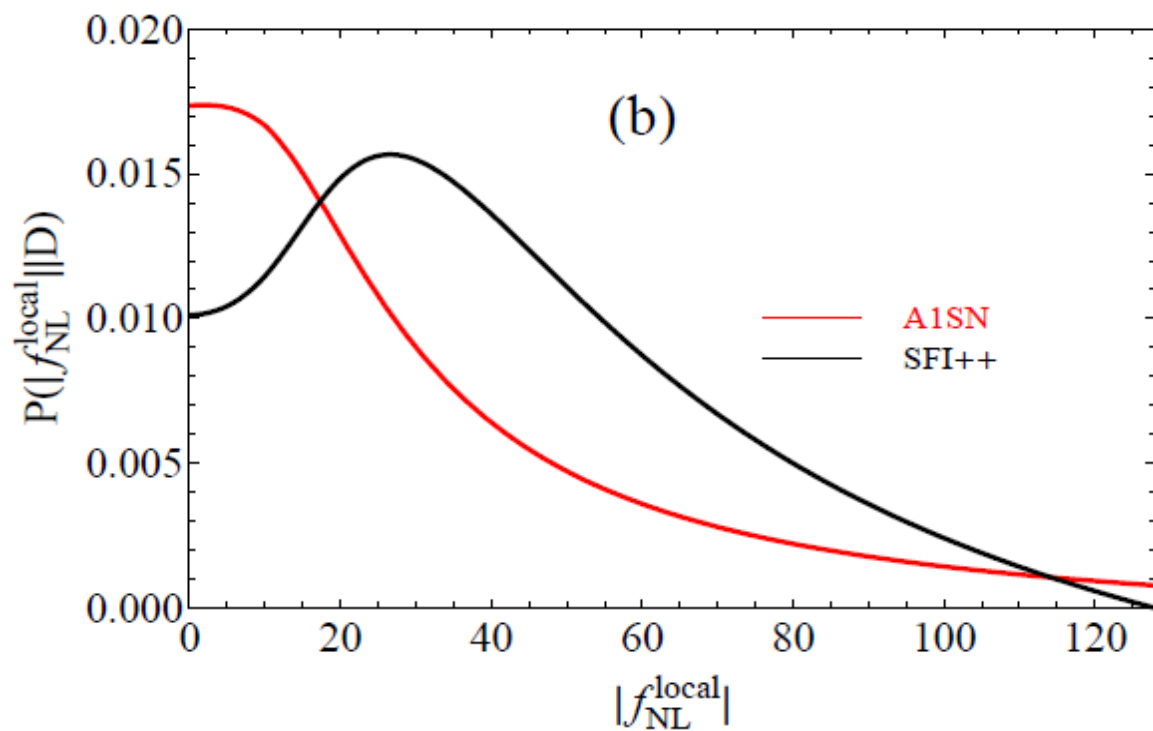
Dalal 2008:

$$\Delta b(k) = (b-1) f_{\text{NL}}^{\text{local}} A(k) \quad A(k) = \frac{3\delta_c(z)\Omega_m h^2}{k^2 T(k)} \left( \frac{H_0}{c} \right)^2$$

The extra term in the  $V(r)$  caused by non-Gaussianity will add more spatial correlation in the covariance matrix.







Data set	Model	$\beta$ value	$ f_{\text{NL}}^{\text{local}} $ value	$-\log L_{\min}$
A1SN	$\beta$ - $f_{\text{NL}}^{\text{local}}$	$0.53^{+0.15}_{-0.04}$	$0.0 \pm 25.7$	681.7
	$\beta$ -only	$0.65^{+0.07}_{-0.06}$		681.7
SFI++	$\beta$ - $f_{\text{NL}}^{\text{local}}$	$0.49^{+0.03}_{-0.05}$	$26.6 \pm 33.0$	14159.1
	$\beta$ -only	$0.49^{+0.04}_{-0.03}$		14159.1

(i) Radio sources from the NRAO VLA Sky Survey (NVSS), the quasar and MegaZ-LRG (DR7) catalogues of the SDSS, and the SDSS LRG redshift survey (Xia et al.(2011) found):

$$f_{\text{NL}}^{\text{local}} = 48 \pm 20 \text{ (1}\sigma\text{CL)}. \quad (8)$$

(ii) Photometric SDSS data (Nikoloudakis et al. (2013)):

$$f_{\text{NL}}^{\text{local}} < 120 \text{ (84\%)}. \quad (9)$$

(iii) SDSS-III (BOSS) DR9 (Ross et al. (2013)):

$$-45 < f_{\text{NL}}^{\text{local}} < 195 \text{ (2}\sigma\text{CL)}. \quad (10)$$

(iv) *Planck* CMB (2013):

$$-45 < f_{\text{NL}}^{\text{local}} = 2.7 \pm 5.8 \text{ (1}\sigma\text{CL)}. \quad (11)$$

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Comparing with  
others:

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No time to mention foreground analysis, see Richard Shaw's talk.



# Bias

$$b_{\text{HI}}^{\text{NG}}(z, k) = b_{\text{HI}}(z) + \Delta b_{\text{HI}}(z, k)$$

$$\Delta b_{\text{HI}}(z, k) = \frac{1}{\rho_{\text{HI}}(z)} \int_{M_{\text{min}}}^{M_{\text{max}}} dM \times \frac{dn}{dM}(M, z) M_{\text{HI}}(M) \Delta b(M, z, k) M, z),$$

$$\Delta b^{\text{MV}}(M, z, k) = 2f_{\text{NL}} \left( \frac{\delta_{\text{c}}^2(z)}{\sigma_{\text{D}}^2} \right) \frac{\mathcal{F}(k)}{\mathcal{M}_R(k)}$$

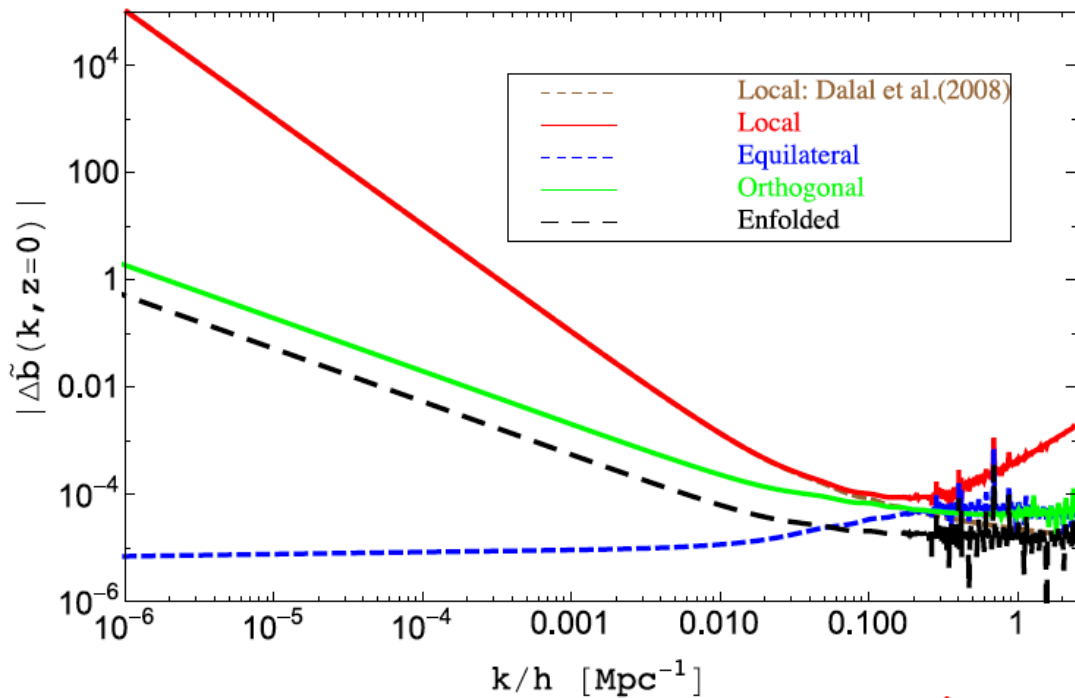
$$\mathcal{F}(k) = \frac{1}{16\pi^2 \sigma_R^2} \int dk_1 k_1^2 \mathcal{M}_R(k_1) \times \int_{-1}^1 d\mu \mathcal{M}_R(k_2) \frac{B_{\phi}(k_1, k_2, k)}{P_{\phi}(k)}$$

S. Matarrese and L. Verde, 2008

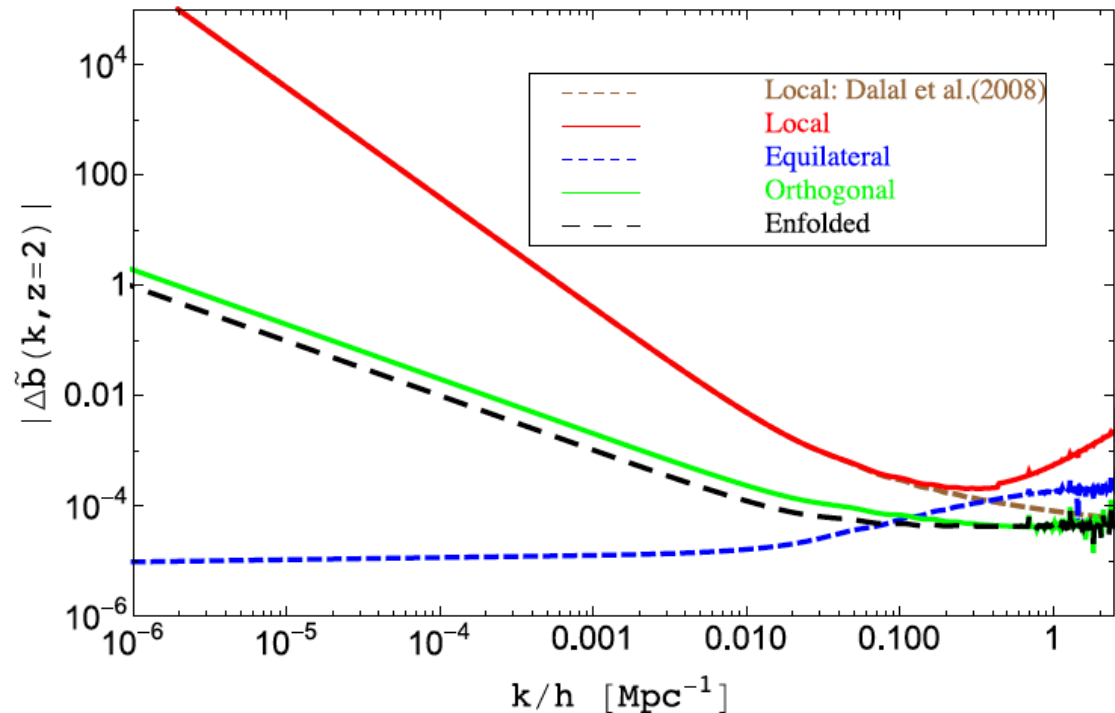
N. Dalal, et al., 2008

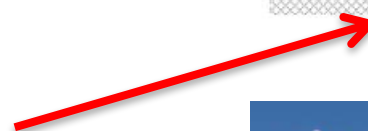
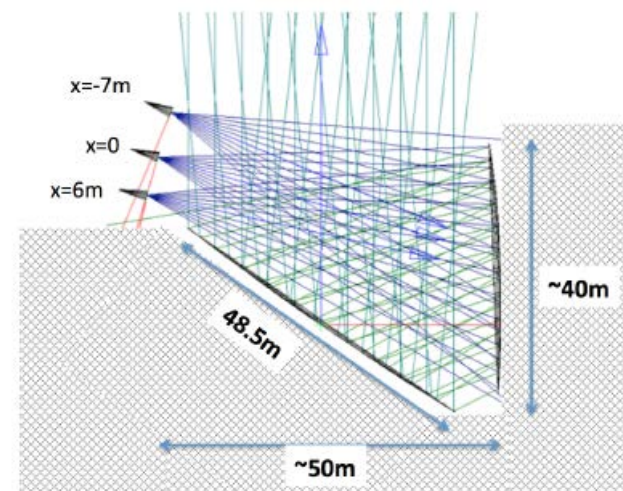
Y.-C. Li and YZM, 2017, ArXiv: 1701.00221

Yi-Chao Li and YZM, 2017,  
ArXiv: 1701.00221  
C. Fedeli et al., 2011,  
MNRAS



$$\begin{aligned}\Delta b(\text{Local}) &\sim k^{-2} \\ \Delta b(\text{Equilateral}) &\sim \text{const} \\ \Delta b(\text{Enfolded}) &\sim k^{-1} \\ \Delta b(\text{Orthogonal}) &\sim k^{-1}.\end{aligned}$$

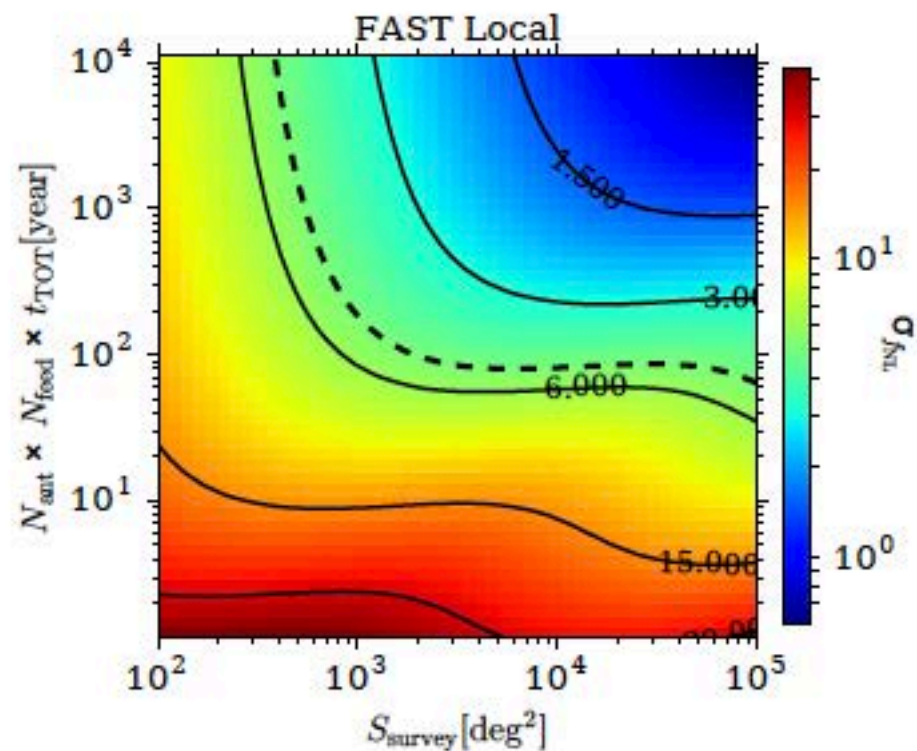
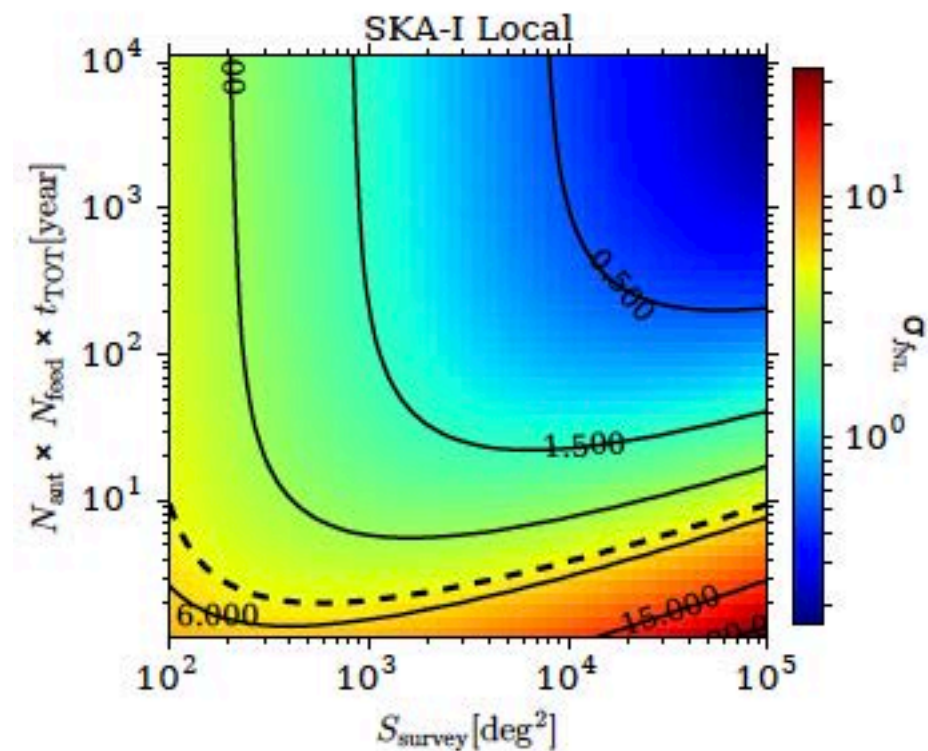




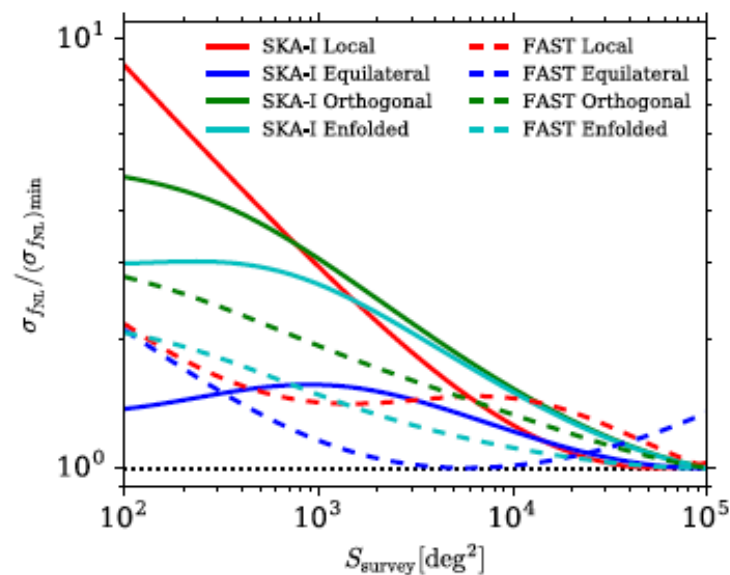
	FAST	SKA-I	BINGO
$\nu_{\min}$ [MHz]	1050	350	960
$\nu_{\max}$ [MHz]	1350	1050	1260
$\Delta\nu$ [MHz]	10	10	10
$n_\nu (n_z)$	30	70	30
$D_{\text{dish}}$ [m]	300	15	25
$N_{\text{ant}} \times N_{\text{feed}}$	$1 \times 19$	$190 \times 1$	$1 \times 60$
$t_{\text{TOT}}$ [yr]	1	1	1
$T_{\text{rec}}$ [K]	25	28	50
$S_{\text{survey}}$ [deg <sup>2</sup> ]	< 24000	< 25000	2500

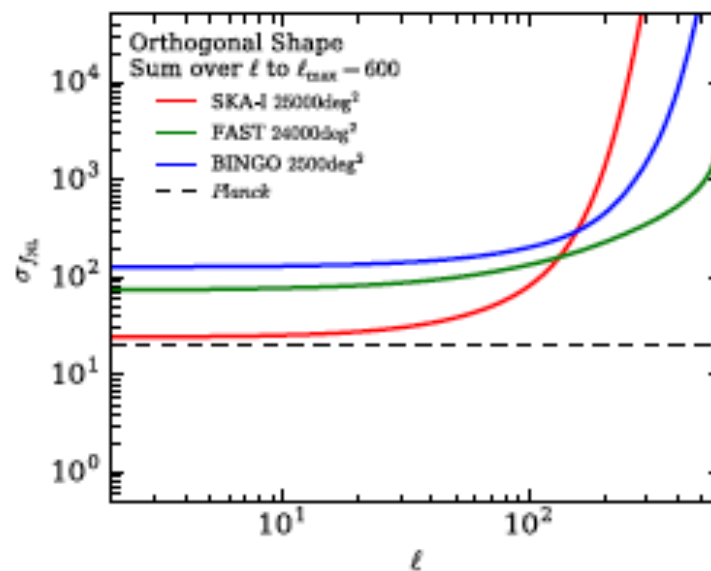
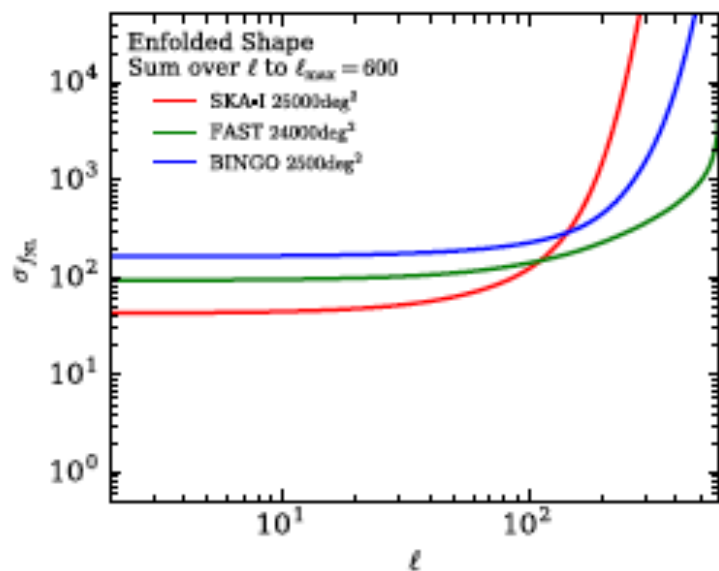
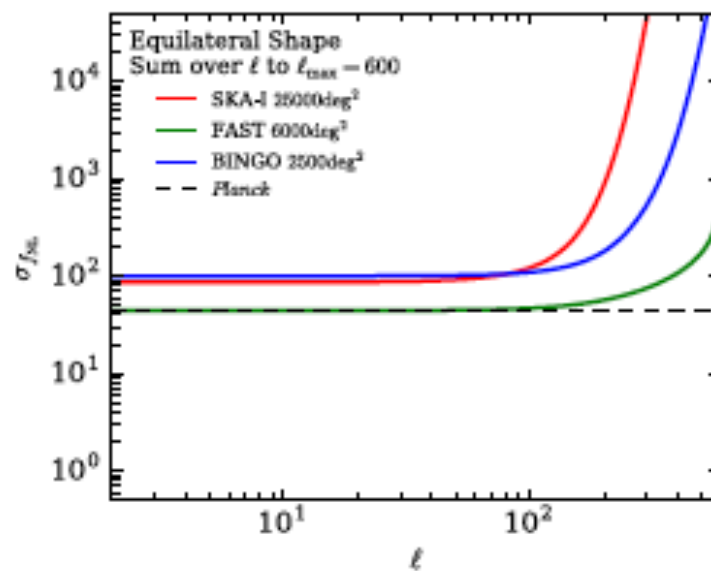
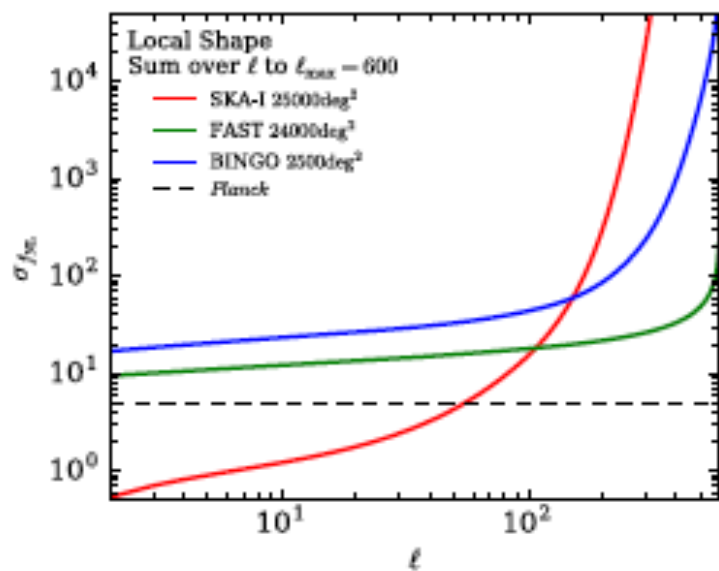






Yi-Chao Li and YZM, 2017,  
 ArXiv: 1701.00221  
 S. Camera, M. G. Santos, P.  
 G. Ferreira, and L.  
 Ferramacho, 2013, PRL





Yi-Chao Li and YZM, 2017,  
ArXiv: 1701.00221

		Current Configuration			Extensions		
	<i>Planck</i> 2015	FAST	SKA-I	BINGO	SKA-I 2yr <sup>†</sup>	FAST 2yr <sup>††</sup>	FAST low <sup>‡</sup>
Local	5	9.5	<b>0.54</b>	17	<b>0.43</b>	7.4	<b>1.6</b>
Equilateral	43	44	86	100	66	<b>32</b>	53
Orthogonal	21	75	25	128	<b>20</b>	59	39
Enfolded	–	94	43	164	36	70	64

<sup>†</sup> SKA-I with two-year observation; <sup>††</sup> FAST with two-year observation; <sup>‡</sup> FAST with low frequencies range from 350MHz to 1050MHz



Extended to 2-years, extended to 250 MHz receivers

Y.-C. Li and YZM, 2016, 1701.00221



# Conclusion

- Understanding the primordial fluctuation is a crucial way of understanding the initial condition of the Universe
- Besides the CMB measurement on bispectrum, the measurement from cosmic peculiar velocity field, and 21-cm intensity mapping can provide complementary constraints on  $f_{\text{NL}}$ .
- By using the extra correlation between residual velocity on different directions, we can constrain the local shape of  $f_{\text{NL}}$  to be less than 25.7 at 1-sigma CL.
- We forecasted that the future constraints on  $f_{\text{NL}}$  from single-dish intensity mapping method on large scales can be comparable with Planck satellite, provides a complementary method to access primordial non-Gaussianity.
- Complimentary method (e.g. Multi-tracer) has also been developed to overcome the cosmic variance problem, improving precision of  $f_{\text{NL}}$  measurements.

