Simulation and analysis of the production of the Higgs boson in pp collisions using PYTHIA and ROOT

Proyecto Física Computacional

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 - A simple analysis of the Higgs
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 - $\blacksquare H \rightarrow c\bar{c}$
- Conclusions and remarks
- Acknowledgments

Introduction and motivations

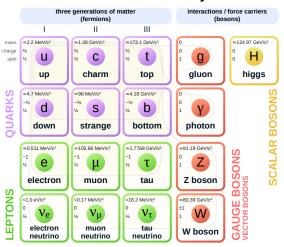
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- In the SM, the building blocks of matter are the fermions, which are comprised of quarks and leptons.
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- All the elementary particles acquire mass through their interaction with the **Higgs field**.

Standard Model of Elementary Particles



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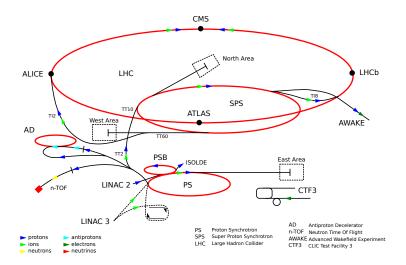
- The SM doesn't predict the value of the masses of the elementary particles, including the Higgs boson mass.
- The particles masses are considered parameters to be determined experimentally.
- The range of possible values for the Higgs boson are all bellow the 1 TeV.
- The data taken from the LEP and SLC colliders, the Tevatron, and other experiments predicted the Higgs boson mass in the range 90 GeV − 152 GeV at the 95% confidence level (CL).

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- The CMS experiment excluded at 95% CL masses from 127 to 600 GeV. The ATLAS experiment excluded also at 95% CL masses in the ranges 111.4 116.4, 119.4 122.1, and $129.2 541 \ GeV$.
- In 2012, the ATLAS and CMS collaborations reported an excess of events between 2σ and 3σ near 125~GeV.



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- This decay channels correspond to: $H \to \gamma \gamma$, $H \to ZZ \to 4l$, $H \to WW \to lvlv$, $H \to \tau \tau$, and $H \to bb$, where l stand for e^- and μ^- .

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- In particular, the CMS publication focused on the observation in five decay channels in the low-mass range from 110 to 145 GeV.
- This decay channels correspond to: $H \to \gamma \gamma$, $H \to ZZ \to 4l$, $H \to WW \to lvlv$, $H \to \tau \tau$, and $H \to bb$, where l stand for e^- and μ^- .
- The channels with the highest sensitivity for discovering the SM Higgs boson with a mass near 125 GeV are $H \to \gamma \gamma$ and $H \to ZZ \to 4l$.

Theoretical framework

■ ROOT is an object-oriented C++ framework aimed at solving the data analysis challenges of high-energy physics.

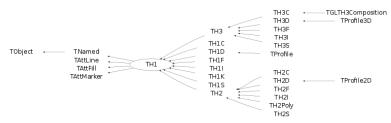
ROOT'

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- The ROOT framework has a lot of libraries which contains several classes.
- Among the libraries we have libraries for histograms, graphs, fitting, mathematical functions, etc.
- An example of how the classes are organized is shown bellow for the histogram library:



The class hierarchy of histogram classes

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- It focuses on centre-of-mass energies greater than about 10 GeV.
- It comprises a coherent set of physics models for the evolution from a few-body high-energy ('hard') scattering process to a complex multihadronic final state.
- The particles are produced in vacuum, but also can be added external detector effects to the simulation.

■ Specifically, PYTHIA is a general-purpuse event generator for high-energy particle collition, rewritten from scratch in C++.

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- PYTHIA can be run standalone, but it can also interfaced with a set of other libraries.
- Among the libraries we have AlpGen, MadGraph, PowHeg, FastJet and ROOT.
- For this project we are interested only in ROOT.

A simple PYTHIA algorithm

Let's make a simple ${\tt PYTHIA}$ algorithm. Indeed, go to the directory

```
> cd pythia8303/examples
```

In such directory, create the file mymainO1.cc. Once the file is created, modify the Makefile located in the same directory:

Now, in the file mymain01.cc add the following lines of code:

```
Pythia pythia;
pythia.readString("HiggsSM:all = on");
pythia.readString("Beams:eCM = 13000.");
pythia.readString("Next:numberShowEvent = 2");
pythia.init();
```

```
for (int iEvent = 0; iEvent < number_of_events; ++</pre>
      iEvent)
2 {
      pythia.next();
3
      Int_t ie = 0;
4
      for (Int_t i = 0; i < pythia.event.size(); ++i)</pre>
5
      {
6
           if (pythia.event[i].id() == 11)
7
           {
8
               ie = i;
9
               m_e_histogram -> Fill(pythia.event[ie].m()
      );
11
13 }
```

```
for (int iEvent = 0; iEvent < number_of_events; ++</pre>
      iEvent)
2 {
      pythia.next();
3
      Int_t imu = 0;
4
       for (Int_t i = 0; i < pythia.event.size(); ++i)</pre>
5
       {
6
            else if (pythia.event[i].id() == 13)
7
       {
8
           imu = i;
9
           m_mu_histogram -> Fill(pythia.event[imu].m());
10
11
12
13 }
```

Finally, to compile the algorithm write the following commands in the terminal shell

```
> make mymain01
2 ./mymain01 > myout01
```

This will generate the following output:

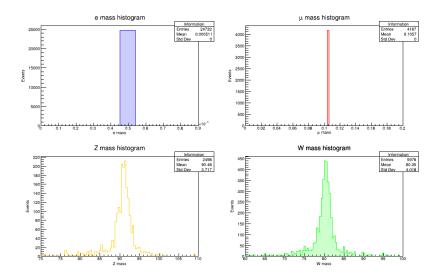
```
76 *----- PYTHIA Process Initialization
77
78
     We collide p+ with p+ at a CM energy of 1.300e+04 GeV
79
80
81
82
     Subprocess
                                                    Code
                                                             Estimated
83
                                                              max (mb)
84
85
86
   | f fbar -> H (SM)
                                                     901 |
                                                             9.030e-09
     q q \rightarrow H (SM)
                                                     902
                                                             2.524e-07
   | gamma gamma -> H (SM)
                                                     903
                                                             8.477e-12
90 | f fbar -> H0 Z0 (SM)
                                                     904 I
                                                             5.187e-09
   | f fbar -> H0 W+- (SM)
                                                             9.431e-09
                                                     905
   | f f' -> H0 f f'(Z0 Z0 fusion) (SM)
                                                     906 I
                                                             1.835e-08
   | f 1 f 2 -> H0 f 3 f 4 (W+ W- fusion) (SM)
                                                             4.832e-08
                                                     907 I
   l q q -> H t tbar (SM)
                                                             5.102e-08
                                                     908 I
95
   | q qbar -> H t tbar (SM)
                                                     909 I
                                                             2.603e-08
96
97 *----- End PYTHIA Process Initialization ------
```

```
127 ----- PYTHIA Info Listing ------
128
129 Beam A: id = 2212, pz = 6.500e+03, e = 6.500e+03, m = 9.383e-01.
130 Beam B: id = 2212. pz = -6.500e+03. e = 6.500e+03. m = 9.383e-01.
131
132 In 1: id = 21, x = 1.508e-03, pdf = 2.813e+01 at 02 = 1.562e+04.
133 In 2: id = 21. x = 6.131e-02. pdf = 1.561e+00 at same 02.
134
135 Subprocess g g -> H (SM) with code 902 is 2 -> 1.
136 It has sHat = 1.562e+04.
       alphaEM = 7.846e-03, alphaS = 1.238e-01 at Q2 = 1.562e+04.
137
138
139 Impact parameter b = 6.777e-01 gives enhancement factor = 1.643e+00.
140 Max pT scale for MPI = 1.300e+04, ISR = 1.300e+04, FSR = 1.300e+04.
141 Number of MPI = 5, ISR = 12, FSRproc = 54, FSRreson = 12.
142
143 ----- End PYTHIA Info Listing -----
```

46															
47	no	id	name	status	MO	thers	daughters		colours		p_x	P_Y	p_z	e	m
48	0	90	(system)	-11	0	0	0	0	0	0	0.000	0.000	0.000	13000.000	13000.
49	1	2212	(p+)	-12	0	0	3	0	0	0	0.000	0.000	6500.000	6500.000	θ.
50	2	2212	(p+)	-12	0	0	4	Θ	0	0	0.000	0.000	-6500.000	6500.000	θ.
51	3	21	(g)	-21	1	0	5	Θ	101	102	0.000	0.000	9.802	9.802	θ.
52	4	21	(g)	-21	2	0	5	Θ	102	101	0.000	0.000	-398.531	398.531	θ.
53	5	25	(h0)	-22	3	4	6	7	0	0	0.000	0.000	-388.730	408.333	124.
54	6	4	c	23	5	0	0	0	103	0	49.441	8.740	-315.857	319.826	1.
55	7	-4	cbar	23	5	0	Θ	Θ	0	103	-49.441	-8.740	-72.873	88.507	1.
56				Charge su	m:	0.000		Moi	mentum	sum:	0.000	0.000	-388.730	408.333	124

160		PYTHIA	Event Listing	(complete	event)										
161															
162	no	id	name	status		hers	daugh			lours	p_x	P_y	p_z	e	m
163	0	98	(system)	-11	0	9	Θ	0	Θ	0	0.000	0.000	0.000	13000.000	13000.000
164	1	2212	(p+)	-12	Θ	Θ	276	0	θ	0	0.000	0.000	6500.000	6500.000	0.938
165	2	2212	(p+)	-12	0	0	271	0	0	0	0.000	0.000	-6500.000	6500.000	0.938
166	3	21	(g)	-21	6	0	5	0	101	102	0.000	0.000	9.802	9.802	0.000
167	4	21	(g)	-21	7	7	5	0	102	101	0.000	0.000	-398.531	398.531	0.000
168	5	25	(h0)	-22	3	4	8	8	0	0	0.000	0.000	-388.730	408.333	124.999
169	6	21	(g)	-41	10	10	9	3	101	104	0.000	0.000	38.246	38.246	0.000
170	7	21	(g)	-42	11	9	4	4	182	101	-0.000	-0.000	-398.531	398.531	0.000
171	8	25	(h0)	-44	5	5	12	12	0	0	44.676	28.554	-358.914	383.739	124.999
172	9	21	(g)	-43	6	0	13	13	102	104	-44.676	-28.554	-1.371	53.039	0.000
173	10	21	(g)	-42	15	15	6	6	101	104	0.000	-0.000	38.246	38.246	0.000
174	11	21	(g)	-41	16	9	14	7	102	105	-0.000	0.000	-446.740	446.740	0.000
175	12	25	(h0)	-44	8	8	17	17	θ	0	44.664	40.774	-390.060	414.040	124.999
176	13	21	(g)	-44	9	9	18	18	102	104	-44.677	-27.658	-6.023	52.889	0.000
177	14	21	(g)	-43	11	0	19	19	101	105	0.013	-13.116	-12.411	18.057	0.000
178	15	21	(g)	-42	21	0	10	10	101	104	-0.000	-0.000	38.246	38.246	0.000
179	16	21	(g)	-41	22	22	20	11	186	105	0.000	0.000	-722.639	722.639	0.000
180	17	25	(h0)	-44	12	12	23	23	Θ	0	37.479	31.810	-393.439	415.735	124.999
181	18	21	(g)	-44	13	13	24	24	182	104	-45.203	-28.315	-5.647	53.637	0.000
182	19	21	(g)	-44	14	14	25	25	101	105	-0.259	-13.455	-12.376	18.283	0.000
183	20	21	(g)	-43	16	0	26	26	186	102	7.983	9.960	-272.931	273.229	0.000
184	21	21	(g)	-41	34	34	27	15	107	104	-0.000	0.000	59.555	59.555	0.000
185	22	21	(g)	-42	35	0	16	16	186	105	-0.000	-0.000	-722.639	722.639	0.000
186	23	25	(h0)	-44	17	17	36	36	Θ	0	35.355	30.136	-386.750	409.095	124.999
187	24	21	(g)	-44	18	18	37	37	182	104	-49.775	-31.919	-12.300	60.396	0.000
188	25	21	(g)	-44	19	19	28	29	181	105	-0.822	-13.899	-13.412	19.333	0.000
189	26	21	(g)	-44	20	20	39	39	186	102	7.955	9.938	-270.832	271.131	0.00
190	27	21	(g)	-43	21	0	30	30	107	101	7.287	5.744	20.211	22.239	0.000
191	28	21	(g)	-51	25	0	38	38	108	105	-0.160	-16.166	-4.996	16.921	0.000

1893	*	PYTHIA Error and Warning Messages Statistics*
1894	1	
1895	times	message
1896	1	I I
1897	19	Error in Pythia::next: hadronLevel failed; try again
1898	15	Error in StringFragmentation::fragment: stuck in joining
1899	4	Error in StringFragmentation::fragmentToJunction: caught in junction flavour loop
1900	2	Warning in HadronWidths::pickMasses: angular momentum and running widths not used
1901	4	Warning in PhaseSpace2to2tauyz::trialKin: maximum for cross section violated
1902	1	Warning in Pythia::check: energy-momentum not quite conserved
1903	5	Warning in Pythia::check: not quite matched particle energy/momentum/mass
1904	2	Warning in SimpleSpaceShower::pT2nextQCD: small daughter PDF
1905	4	Warning in SimpleSpaceShower::pT2nextQCD: weight above unity
1906	1 7	Warning in SimpleTimeShower::findMEcorr: ME weight above PS one
1907	1	Warning in SimpleTimeShower::pTnext: negative dipole mass.
1908	71	Warning in StringFragmentation::fragmentToJunction: bad convergence junction rest frame
1909	1	I and the second se
1910	*	End PYTHIA Error and Warning Messages Statistics



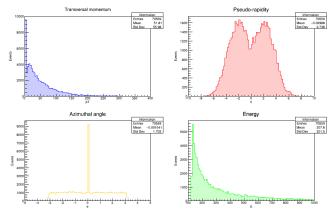
Results

A simple analysis of the Higgs

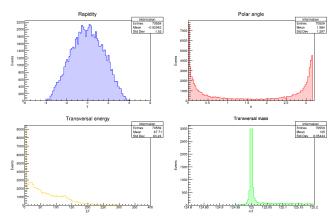
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A simple analysis of the Higgs

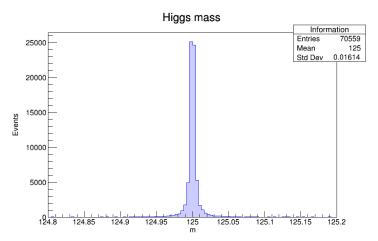
- Before to show the main analysis of this project let's study in first place the kinematical variables associated with the Higgs boson.
- Indeed, the histogram for the variables p_T , η , ϕ and E have the form



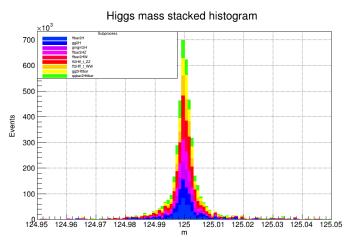
■ Furthermore, the histogram for the variables y, θ , E_T and m_T have the form



• On the other hand, the mass of the Higgs boson have the following distribution:



■ Finally, the production of the Higgs boson due to the processes $f\bar{f} \to H^0$, $gg \to H^0$, $\gamma\gamma \to H^0$, $f\bar{f} \to H^0Z^0$, $f\bar{f} \to H^0W^{\pm}$, $ff' \to H^0ff'$, $f_1f_2 \to H^0f_3f_4$, $gg \to H^0t\bar{t}$ and $q\bar{q} \to H^0t\bar{t}$ is shown in the stacked mass histogram



$H \to \gamma \gamma$

■ In the $H \to \gamma \gamma$ channel we made a search of the diphoton mass $m_{\gamma\gamma}$ in the range 110-150 GeV.

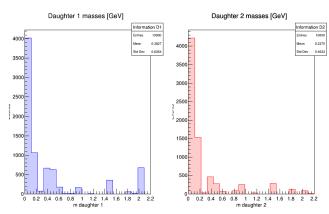
$H \rightarrow \gamma \gamma$

- In the $H \to \gamma \gamma$ channel we made a search of the diphoton mass $m_{\gamma\gamma}$ in the range 110-150 GeV.
- The diphoton mass receive contributions from a large irreducible background from quantum chromodynamics.

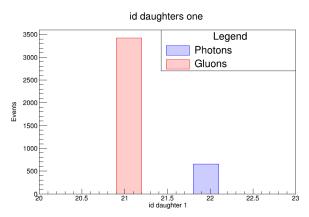
$H \to \gamma \gamma$

- In the $H \to \gamma \gamma$ channel we made a search of the diphoton mass $m_{\gamma\gamma}$ in the range 110-150 GeV.
- The diphoton mass receive contributions from a large irreducible background from quantum chromodynamics.
- The channel $H \to \gamma \gamma$ is one of the most promising channels in the search of the SM Higgs boson in low mass range.

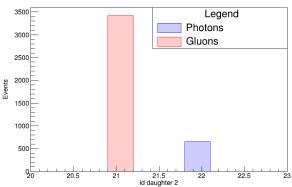
Now, let's try to reconstruct the SM Higgs boson in the $H \to \gamma \gamma$ channel. Indeed, the distribution of the masses of the all possibles daughter (according to PYTHIA) of the SM Higgs boson is



■ From the above histogram, we see that the majority of the events corresponds to daughter that are massless. Indeed, by doing a histogram of the ID of the daughters that are massless we get





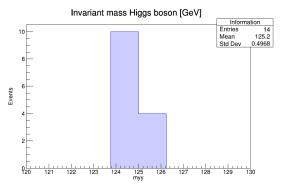


■ From above we see that we have daughters that correspond to photons and gluons. However, we are interested only on the photon daughters.

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- In this way, by using the formula

$$m_{\gamma\gamma} = \sqrt{2p_{T,1}p_{T,2}\left(\cosh\left(\eta_1 - \eta_2\right) - \cos\left(\phi_1 - \phi_2\right)\right)},$$
 (1)

we get the following histogram for the diphoton mass:



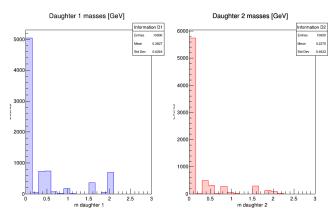
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- When the Higgs boson was discovered, this particle was measured in the decay channel $\gamma\gamma$, ZZ, WW and $\tau\tau$.
- However, one of the highest priorities of the LHC is the measurement of the coupling of the H boson with other SM particles.
- Recently, ATLAS and CMS reported the coupling of the H boson with the quarks t and b.
- Thus, the next objetive is the measurement of the coupling of H with second generation quarks (c and s).

■ Now, let's analyse the decay $H \to c\bar{c}$ by using the PYTHIA simulator. Indeed, again we have that the mass of the possible daughters are distributed according to the following histogram:

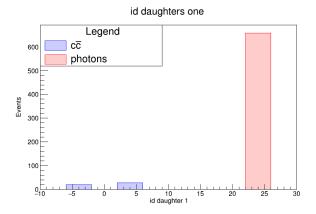


■ From the previous histogram we have that there is a very low production of daughters between the mass range 1-1.5 GeV, where the charm quark is located.

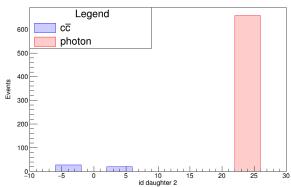
- From the previous histogram we have that there is a very low production of daughters between the mass range 1-1.5 GeV, where the charm quark is located.
- This is expected, because the branching fraction for the decay $H \to c\bar{c}$ is $0.0288^{+0.0016}_{-0.0006}$. This says that the coupling of the Higgs to the quarks $c\bar{c}$ is very weak.

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- Indeed, the coupling of the Higgs with the third generation quarks $b\bar{b}$ is much strong.

■ In this way, by making a histogram with the ID of the produced charm quarks we get



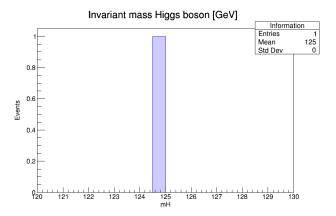
id daughters two



■ Finally, by using the center-of-mass formula for a 2—body decay process

$$M = \sqrt{m_1^2 + m_2^2 + 2(E_1 E_2 - \vec{p_1} \cdot \vec{p_2})},$$
 (2)

we get the following histogram



Conclusions and remarks

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- The simulations were made with 10000 pp collisions. However, we can go further with more collisions by using computational clusters (e.g. LXPLUS).

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The references for this work can be finded in the project document.

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