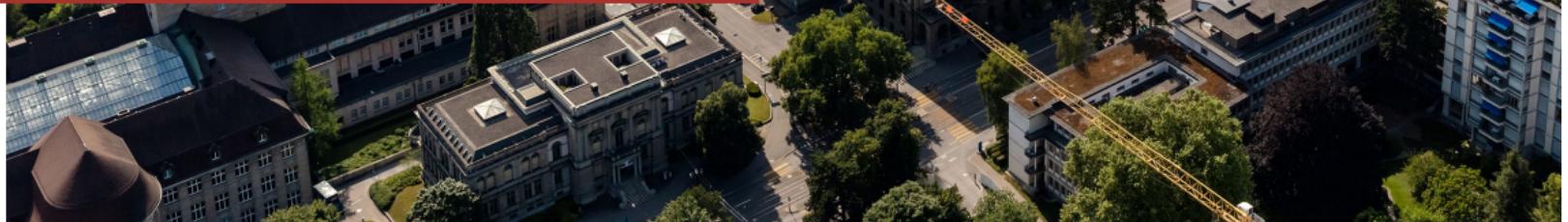
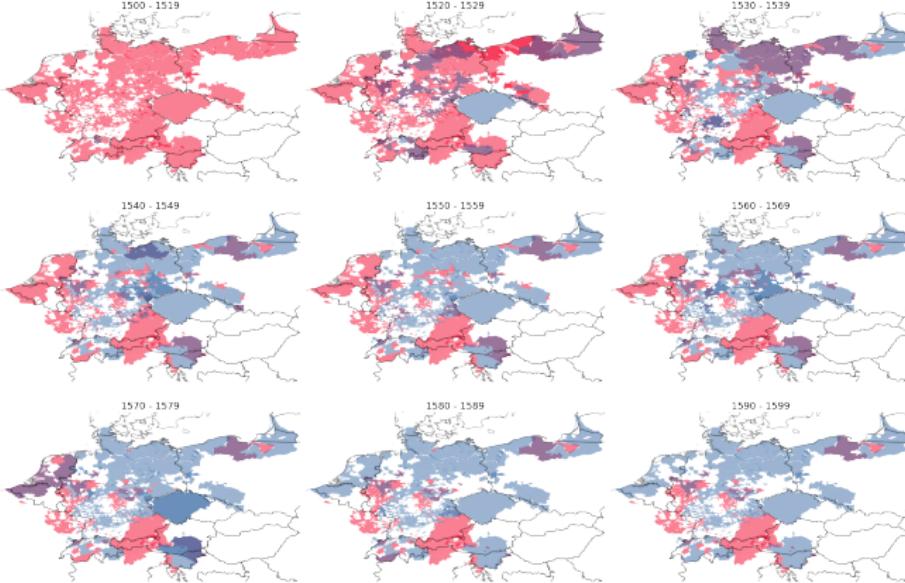


Path statistics for letter correspondence networks of the European Reformation

Ramona Roller
21st Juli 2023



The Adoption of Protestantism



- ▶ 16th-cent. Europe: Holy Roman Empire
- ▶ Territories become protestant
- ▶ Protestant ideas are transmitted

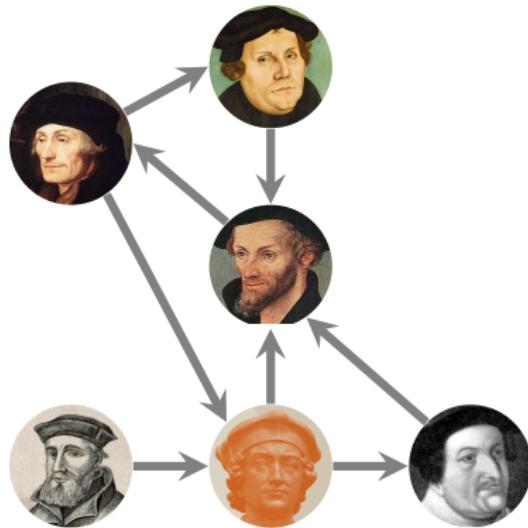
■ Catholic
■ Protestant

Research question

How can we characterise the transmission of protestant ideas?

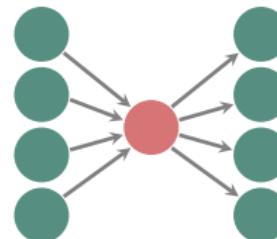
- ▶ Important reformers

Letter Correspondence Networks for the Transmission of Ideas

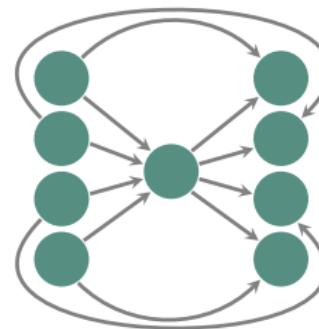


- ▶ Nodes: Reformers Edges: Letters
- ▶ $N_V: 3,000$ $N_E: 30,000$
- ✓ sending dates, locations
- ✗ Topics, receiving dates

➔ Use node betweenness to identify important reformers for the transmission of ideas

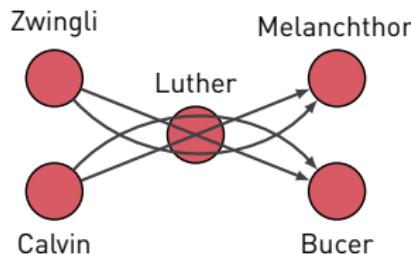
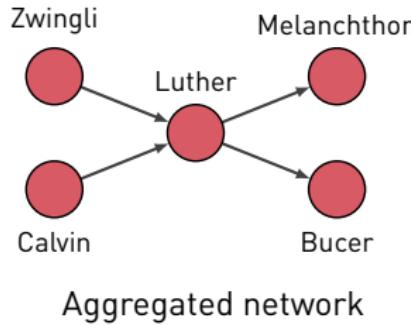


■ High betweenness ■ Low betweenness

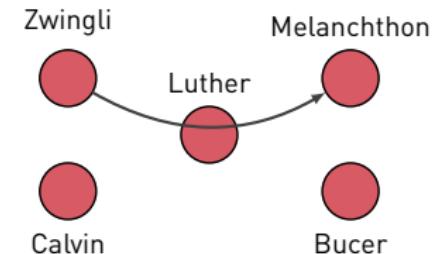
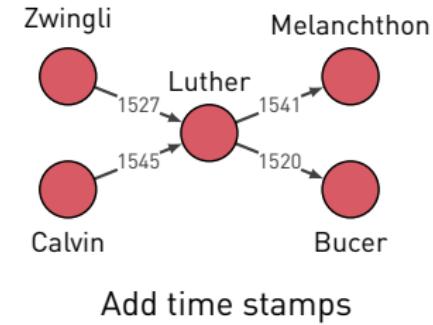


The Problem

Scholtes, Wider & Garas, 2016



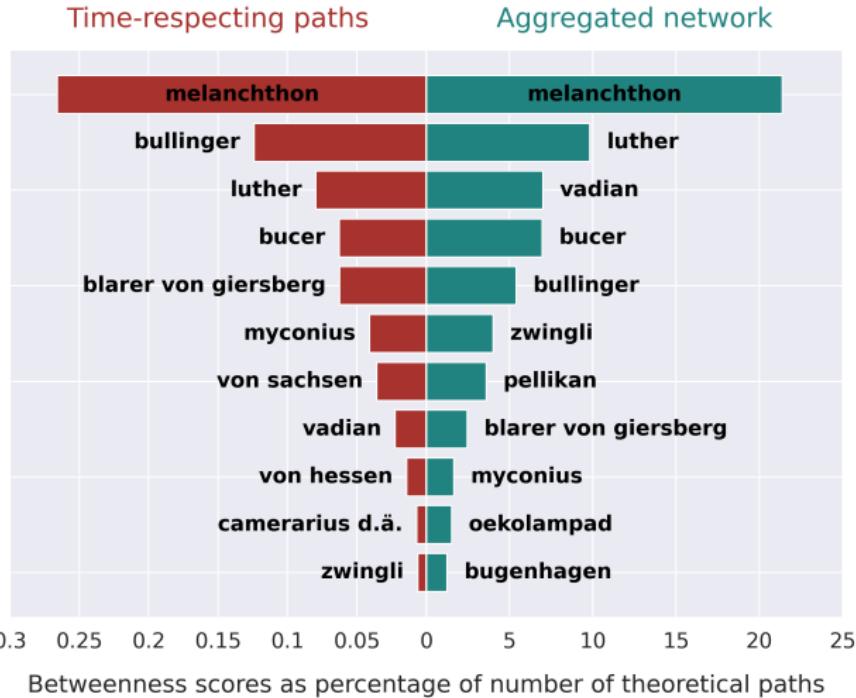
$$btw_{Luther} = 4$$



$$btw_{Luther} = 1$$

- In aggregated networks information can spread backwards in time
- Topological network measures in aggregated networks are biased

Results



- Melanchthon contributed most
- Aggregated network measures overestimate importance of reformers

Solutions: Account for Time

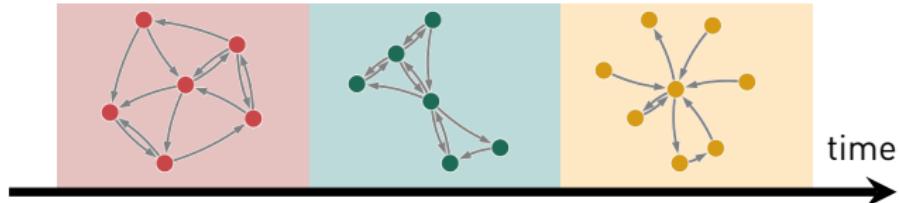
► Snapshots

- Automatic change points

Darst et al., 2016; Peixoto & Gauvin, 2018

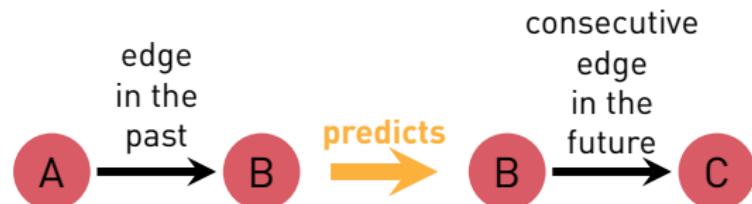
- Theoretical all of us, I assume

- Macro and meso scale



► Correlations between consecutive node pairs

- Time-respecting paths Pfitzner et al., 2013
- Micro scale

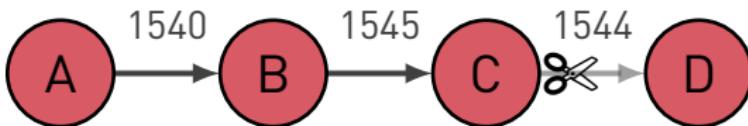


- ➔ Snapshots and time-respecting paths represent times at different scales: macro vs micro

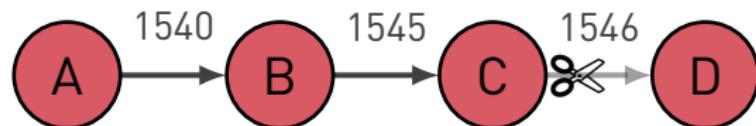
Time-respecting Paths

Pfitzner et al., 2013

- 1 Sequence of nodes that are connected by time-consecutive edges (**chronology**)..
- 2 ..with the inter-edge time being restricted by a lower (**minimum reaction time**) and an upper bound (**memory**)



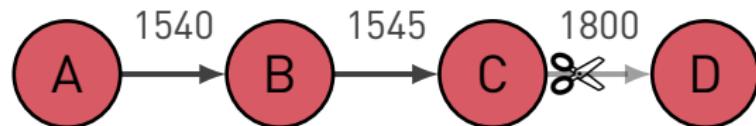
1. Chronology is broken



2a. Inter-edge time < minim reaction time

Assumptions

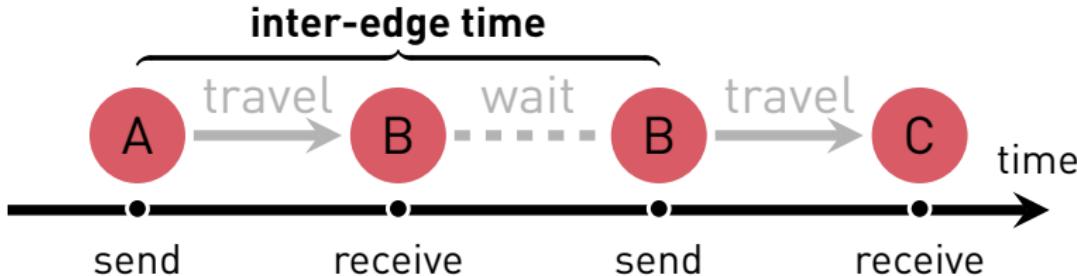
- 1 Time-consecutive edges deal with the same topic
- 2 Time scale is global



2b. Inter-edge time > memory

- Accounting for chronology is easy, choosing the correct inter-edge time is not
- Time scale at which temporal edges influence each other is unknown

Inter-edge Time for Letters



- ✓ Minimum inter-edge time: 1 day (min. reaction time)
- ✗ Maximum inter-edge time: δt (memory)

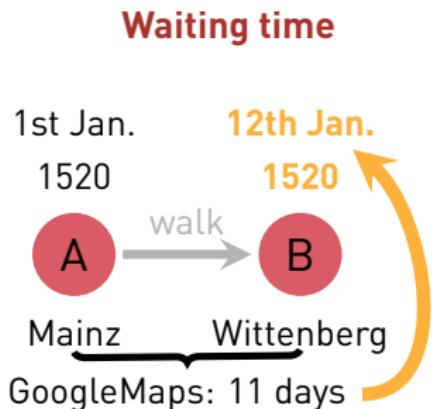
Real life

- ▶ Only waiting time is relevant
- ▶ Refresh memory: Repeatedly read letter
- ▶ Continuous waiting $\uparrow \rightarrow$ Forgetting \uparrow
- ➔ Estimating δt from data is hard

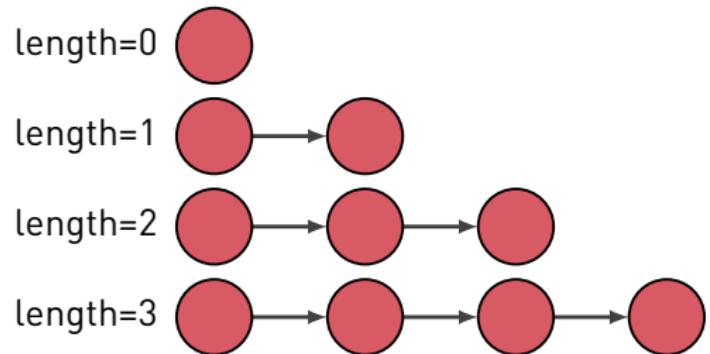
Data

- ▶ Missing receiving dates: cannot disentangle travel and waiting times
- ▶ No data on repeated reading
- ▶ Total waiting $\uparrow \rightarrow$ Forgetting \uparrow

Estimating δt from data

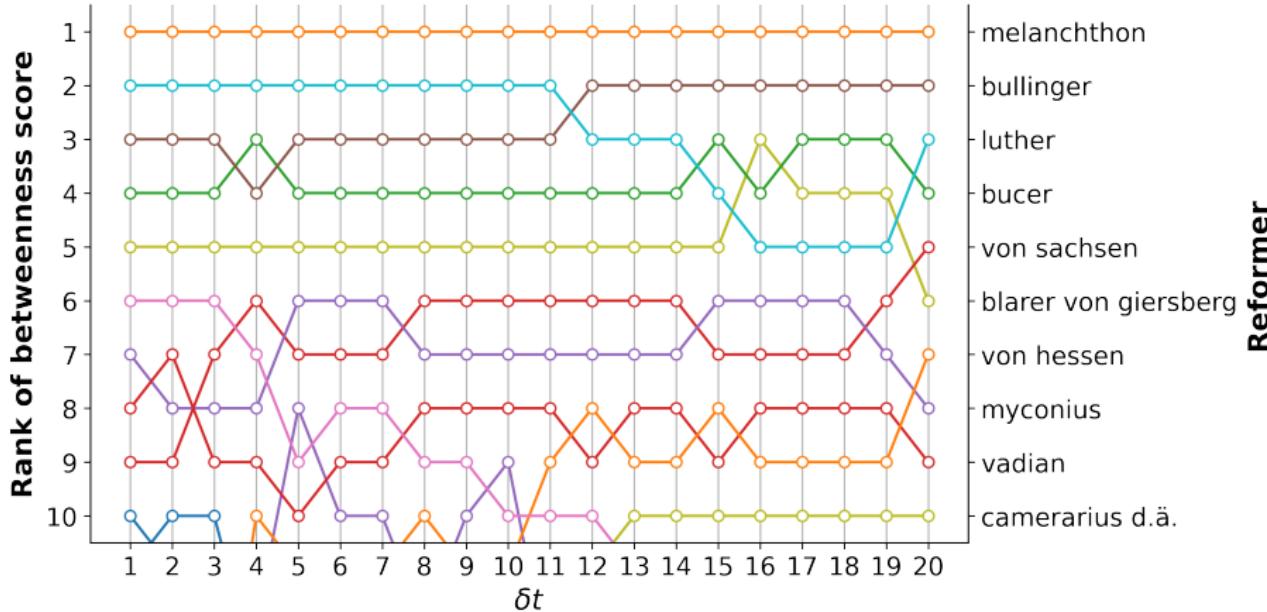


Path lengths Petrovic, Wagner & Scholtes, 2023



- ▶ $\delta t =$ typical (travel + waiting time)
- ▶ Keep 1% of reformers, 24% of edges
- ➔ Not representative to draw conclusion
- ➔ Sparseness poses problems to data-driven approaches
- ▶ Optimal δt : only one path length dominates
- ▶ No paths for some lengths → no variation for statistical inference
- ➔ Measure is not informative

Robustness Checks



- Robust result: Melanchthon is always the most important reformer
- But other reformers change their scores

Summary

- ▶ **Aggregated network ignore time**
 - ▶ Information spreads backwards in time
 - ▶ Biased topological network measures
- ▶ **Time-respecting paths**
 - ▶ Temporal ordering of edges
 - ▶ Challenge: parameter calibration (δt)
 - ▶ Calibration methods: problem with data sparseness
 - ▶ Strict assumptions
- ▶ **Outlook**
 - ▶ Validate topological paths with topic-based paths

