

INTRODUCTION TO COMPUTER SYSTEMS

EX. 3 PEN AND PAPER

1 Overview

1.1 Confirmation of Concepts

1) Briefly describe the optimization methods presented below.

- a) Code Motion
- b) Strength Reduction
- c) Sharing of common subexpressions
- d) Remove Aliasing
- e) Function Inlining
- f) Loop Unrolling

2) Answer the following questions.

- a) Why can't the compiler move the procedure in the loop for optimization? Give two reasons.
- b) What are the limitations of optimizing the compiler? Give two things.

2 Code Optimization

2.1 Counting Instruction

1) Look at the given code and the corresponding assembly code, and answer the question.

*In the case of an instruction such as `jge`, it is considered to have been executed even if it is ignored because the conditions are not satisfied.

```
for(i=1;i<N+1;i++)  
    rlt += i;
```

```
        movl    $1, -4(%rbp)  
        jmp     .L2  
.L3:    movl    -4(%rbp), %eax  
        addl    %eax, -8(%rbp)  
        addl    $1, -4(%rbp)  
.L2:    movl    -20(%rbp), %eax  
        cmpl    -4(%rbp), %eax  
        jge     .L3
```

- a) if $N = 1$, How many instructions are executed?
- b) if $N = 3$, How many instructions are executed?
- c) Find a function for N that calculates the number of instructions executed for the natural number N .

2) The following is a C code representing two algorithms with different complexities for printing all partial sums of a first-order array, and the corresponding assembly code. Answer the questions.

1. $O(n^3)$ Algorithm

```
for(i=1;i<N+1;i++) {  
    for(j=0;j<N+1-i;j++) {  
        rlt = 0;  
        for(k=0;k<i;k++) {  
            rlt += arr[j+k];  
        }  
        //printf("%d\n", rlt);  
    }  
}
```

```

movl    $1, -4(%rbp)
jmp     .L2
.L7:
movl    $0, -8(%rbp)
jmp     .L3
.L6:
movl    $0, -16(%rbp)
movl    $0, -12(%rbp)
jmp     .L4
.L5:
movl    -8(%rbp), %edx
movl    -12(%rbp), %eax
addl    %edx, %eax
cltq
leaq    0(,%rax,4), %rdx
movq    -24(%rbp), %rax
addq    %rdx, %rax
movl    (%rax), %eax
addl    %eax, -16(%rbp)
addl    $1, -12(%rbp)
.L4:
movl    -12(%rbp), %eax
cmpl    -4(%rbp), %eax
jnl     .L5
addl    $1, -8(%rbp)
.L3:
movl    -28(%rbp), %eax
addl    $1, %eax
subl    -4(%rbp), %eax
cmpl    %eax, -8(%rbp)
jnl     .L6
addl    $1, -4(%rbp)
.L2:
movl    -28(%rbp), %eax
cmpl    -4(%rbp), %eax
jge     .L7

```

- if $N = 1$, How many instructions are executed?
- if $N = 3$, How many instructions are executed?
- Find a function for N that calculates the number of instructions executed for the natural number N .

2. $O(n^2)$ Algorithm

```

prefix[0] = 0;
for (i = 1; i < N+1; i++) {
    prefix[i] = prefix[i - 1] + arr[i-1];
}
for (i = 0; i < N; i++) {
    for (j = i; j < N; j++) {
        rlt = prefix[j + 1] - prefix[i];
        //printf("%d\n", rlt);
    }
}

```

```

movq    -32(%rbp), %rax
movl    $0, (%rax)
movl    $1, -4(%rbp)
jmp     .L2

.L3:
movl    -4(%rbp), %eax
cltq
salq    $2, %rax
leaq    -4(%rax), %rdx
movq    -32(%rbp), %rax
addq    %rdx, %rax
movl    (%rax), %ecx
movl    -4(%rbp), %eax
cltq
salq    $2, %rax
leaq    -4(%rax), %rdx
movq    -24(%rbp), %rax
addq    %rdx, %rax
movl    (%rax), %edx
movl    -4(%rbp), %eax
cltq
leaq    0(,%rax,4), %rsi
movq    -32(%rbp), %rax
addq    %rsi, %rax
addl    %ecx, %edx
movl    %edx, (%rax)
addl    $1, -4(%rbp)

.L2:
movl    -36(%rbp), %eax
cmpl    -4(%rbp), %eax
jge     .L3
movl    $0, -4(%rbp)
jmp     .L4

.L7:
movl    -4(%rbp), %eax
movl    %eax, -8(%rbp)
jmp     .L5

.L6:
movl    -8(%rbp), %eax
cltq
addq    $1, %rax
leaq    0(,%rax,4), %rdx
movq    -32(%rbp), %rax
addq    %rdx, %rax
movl    (%rax), %edx
movl    -4(%rbp), %eax
cltq
leaq    0(,%rax,4), %rcx
movq    -32(%rbp), %rax
addq    %rcx, %rax
movl    (%rax), %eax
subl    %eax, %edx
movl    %edx, -12(%rbp)
addl    $1, -8(%rbp)

```

```

.L5:
    movl    -8(%rbp), %eax
    cmpl    -36(%rbp), %eax
    jl      .L6
    addl    $1, -4(%rbp)

.L4:
    movl    -4(%rbp), %eax
    cmpl    -36(%rbp), %eax
    jl      .L7

```

- if $N = 1$, How many instructions are executed?
- if $N = 3$, How many instructions are executed?
- Find a function for N that calculates the number of instructions executed for the natural number N .
- Assuming that N is large enough, is an algorithm with complexity $O(n^2)$ more efficient than an algorithm with complexity $O(n^3)$ in terms of the number of instructions executed?

2.2 Strength Reduction

- Answer the questions using the table below.

* assume that y is integer.

Operation	Cycle
Integer add	1
Integer Multiply	4
Integer Divide	36
Floating-point add	3
Floating-point multiply	5
Floating-point divide	38

Table 1

- Which is faster, $y / 10$ or $y * 0.1$?
- Which is faster, $y / 0.1$ or $y * 10$?
- Calculate the total cycle to compute two expressions, $(y / 0.1) + (y * 0.1)$ and $(y * 10) + (y / 10)$. Compare and explain which is more efficient.

2.3 Other Methods

- Look at the code presented below and optimize it for the given optimization method.

- Use Code Motion & Remove Aliasing

```

for (i=0; i<100; i++) {
    for (j=0; j<100; j++)
        arr[i] += 5*j + i*i;
}

```

2. Use Function Inlining

```
int max(int a, int b) {  
    return (a > b) ? a : b;  
}  
a = max(x,y);
```

3. Use Loop Unrolling

```
for (i=0;i<3;i++)  
    ab[i] = i;
```

4. Use Sharing of common subexpressions

```
a = b * c - c * d;  
e = (b - d) * (b - d);
```