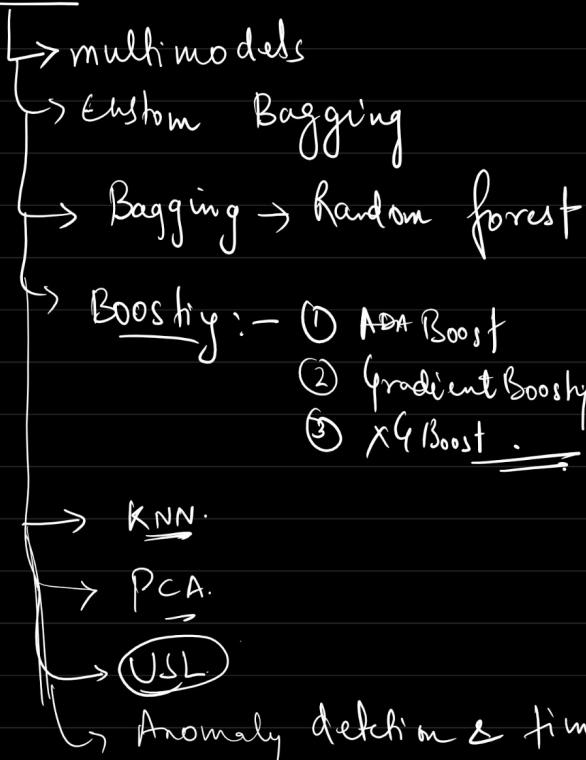


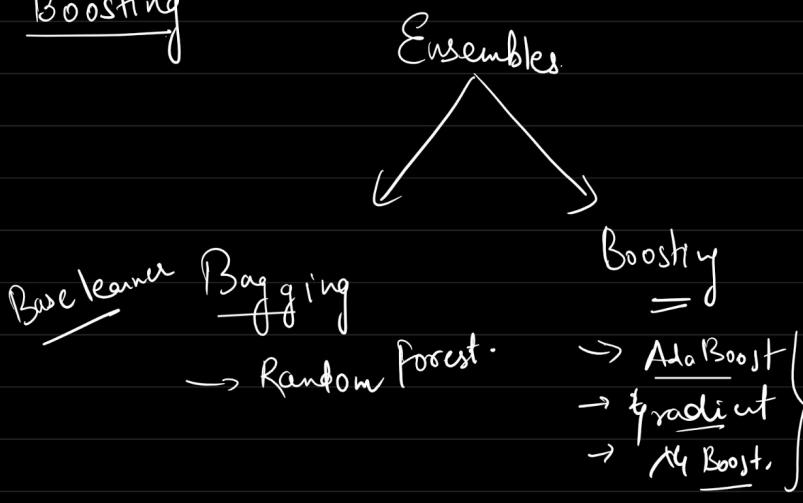
Reg.

Classification

Ensembles



* Boosting

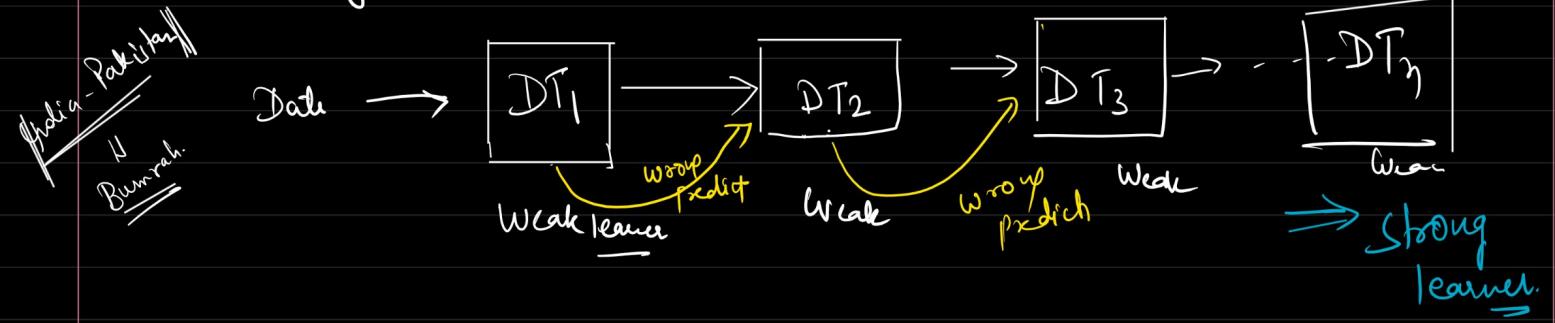


Bagging : Base learner
(Decision Trees)

Bootstrap aggregation

Boosting : - weak learners
(Decision trees)

* Boosting (Boost over)



* Weak Learner → Model is very simple and not powerful from data.

Analogy
 → Football
 → One shot

* Principle of Boosting : → Build a first model on training data and then build a second model to rectify the errors present in this first model.

Bagging

→ Classification: Voting
 → Regression: Average

Boosting

$M_1 \rightarrow M_2 \rightarrow M_3 \dots M_n$

 $\alpha_1 M_1 + \alpha_2 M_2 + \dots + \alpha_n M_n$

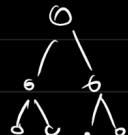
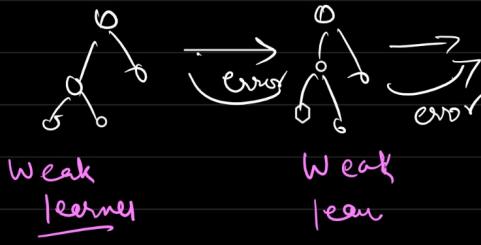
$\alpha_1, \alpha_2, \dots, \alpha_n$ are weights

* AdaBoost (Adaptive Boosting)

* Work both for classification & regression

Yann LeCun and Robert Schapire in 1995.

* Boosting →



* Bagging → reduces variance
 * Boosting → reduces bias.

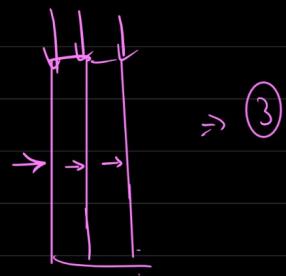
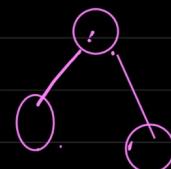
* AdaBoost → Concept of boosting

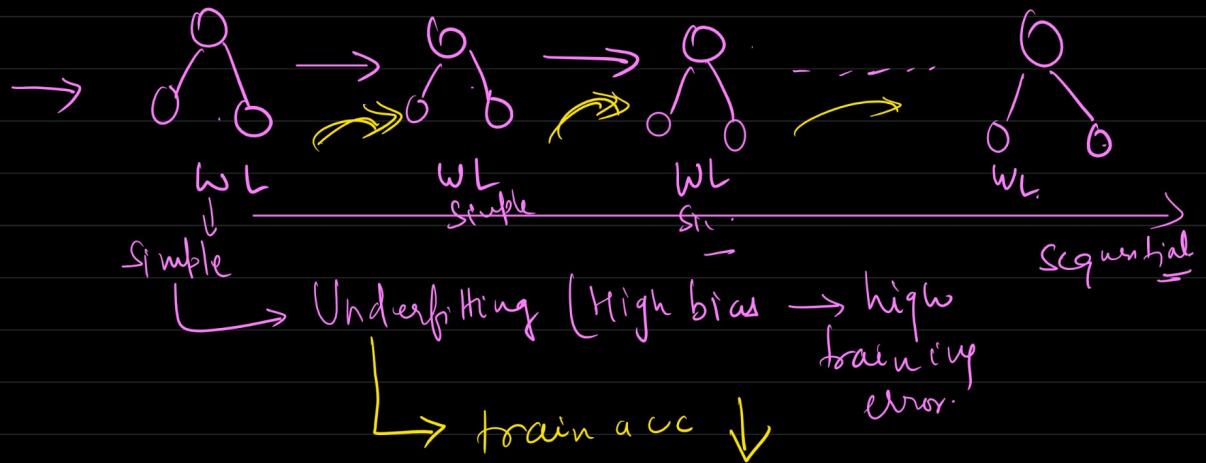
* Decision Stumps

A decision

tree with

only one level of depth.



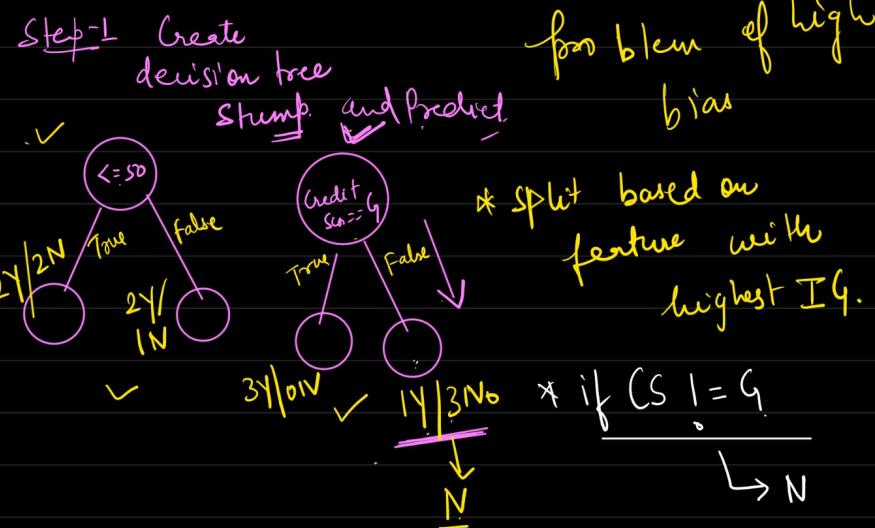


Each individual DT is a high bias model but error is transferred to next model leading to low bias at an over all level.

* Mathematical explanation of AdaBoost

→ AdaBoost solves the problem of high bias

	Salary	Credit score	Approval
B	$\leq 50k$	B	No
G	$\leq 50k$	G	Yes
G	$\leq 50k$	G	Yes
B	$> 50k$	B	No
G	$> 50k$	G	Yes
N	$> 50k$	N	Yes
N	$\leq 50k$	N	No



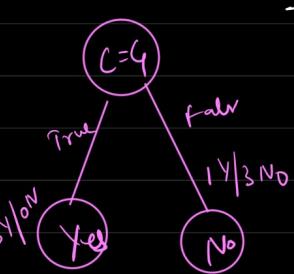
	Salary	Credit score	Approval	Wi
B	$\leq 50k$	B	No	1/7
G	$\leq 50k$	G	Yes	1/7
G	$\leq 50k$	G	Yes	1/7
B	$> 50k$	B	No	1/7
G	$> 50k$	G	Yes	1/7
N	$> 50k$	N	Yes	1/7
N	$\leq 50k$	N	No	1/7

Step-2 Assign equal weights to all the dp

Step-3 - Total Error & Performance of Stump.

$$\text{Total Error} = 1/7$$

(Sum of wts of misclassified dp's) * Performance of Stump:-



K boosting production fn

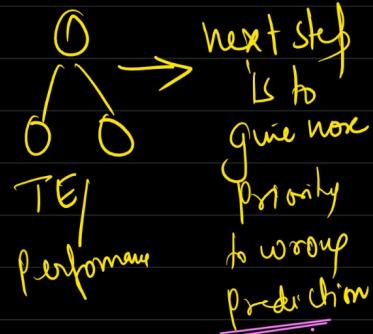
$$f = \alpha_1 M_1 + \alpha_2 M_2 + \dots + \alpha_m M_m$$

↑
0.896

$$\frac{1}{2} \ln \left[\frac{1 - TE}{TE} \right]$$

$$\frac{1}{2} \ln \left[1 - \frac{1}{e} \right]$$

$$= \frac{1}{2} \ln [6] \approx 0.896$$



* Performance of individual stump (model) will be considered as weight for that specific model.

Step-4 → Give more

wts to incorrect classified dp & lesser wt to correct datapoint

* For correct classification → performance of stump

$$Wt_{new} = \frac{Wt_{old} * e}{e}$$

* for incorrect classification

+ performance of stump.

$$e = 2.73$$

$$Wt_{new} = Wt_{old} * e$$

Salary	Credit score	Approval	Wt	updated wt	Normalized wt	Bin assignmt
$\leq 50k$	B	No	$\frac{1}{7}$	0.058	0.083	$0 - 0.083$
$\leq 50k$	G	Yes	$\frac{1}{7}$	0.058	0.083	$0.08 - 0.16$
$> 50k$	G	Yes	$\frac{1}{7}$	0.058	0.08	$0.16 - 0.24$
$> 50k$	B	No	$\frac{1}{7}$	0.058	0.08	$0.24 - 0.32$
$> 50k$	G	Yes	$\frac{1}{7}$	0.058	0.08	$0.32 - 0.40$
$> 50k$	N	Yes	$\frac{1}{7}$	0.349	0.5007	$0.40 - 0.90$
$\leq 50k$	N	No	$\frac{1}{7}$	0.058	0.08	$0.90 - 0.98$

$$\text{Correct} \rightarrow \frac{1}{7} \times e = \underline{0.0896}$$

$$\text{Incorrect} = \frac{1}{7} e^+ = \underline{0.349}$$

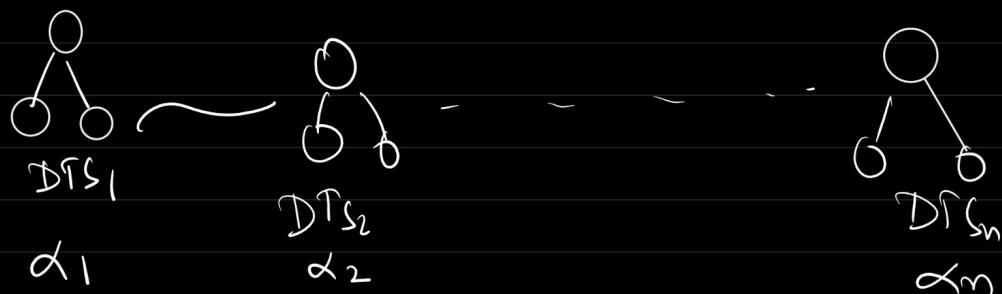
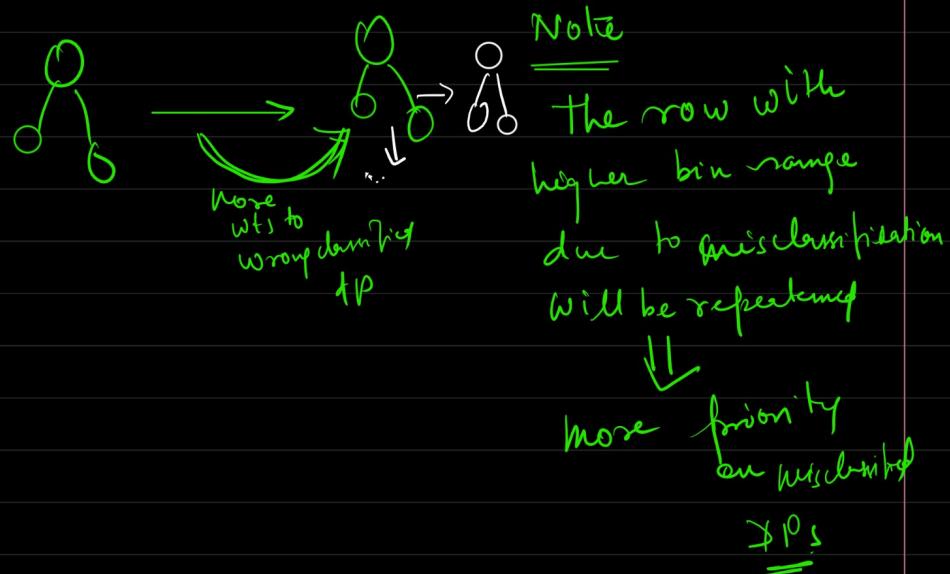
$$\text{normalizing} = \frac{\text{updated wt}}{\text{total updated wt}}$$

$$\sum \text{ total } \underline{0.697} \approx 1$$

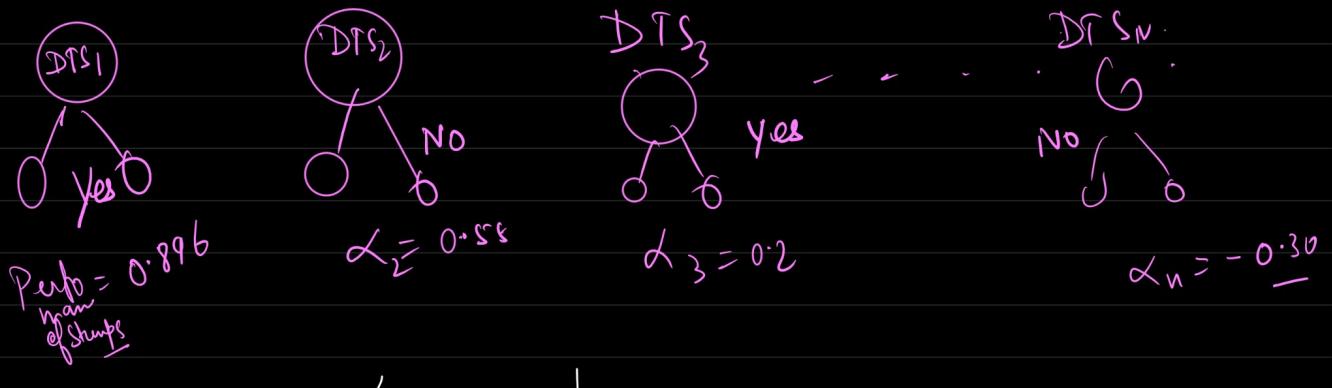


$$0 - \underline{0.08} \quad 0.16$$

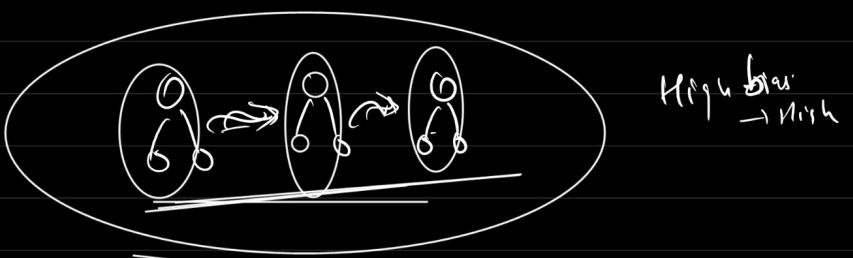
Age	Credit score	Approval	wt	Updated wt	Normalized wt	Bin assignment	Random nos (0 to 0.98)	
<=50k	B	No	1/7	0.058	0.083	0-0.083	→ 0.3	↓
<=50k	G	Yes	1/7	0.058	0.083	0.08-0.16	→ 0.4	↑
>50k	G	Yes	1/7	0.058	0.08	0.16-0.24	→ 0.4	↑
>50k	B	No	1/7	0.058	0.08	0.24-0.32	→ 0.5	↑
>50k	G	Yes	1/7	0.058	0.08	0.32-0.40	→ 0.4	↑
① & ② >50k	N	Yes	1/7	0.349	0.5007	0.40-0.9	→ 0.1	↑
<50k	N	No	1/7	0.058	0.08	0.90-0.98	→ 0.9	↑
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* Final prediction



$$\begin{aligned}
 f &= \alpha_1(M_1) + \alpha_2(M_2) + \alpha_3(M_3) + \dots + \alpha_n(M_n) \\
 &= \cancel{0.896}(\text{Yes}) + \cancel{0.55}(\text{No}) + \cancel{0.25}(\text{Yes}) + \dots + \cancel{-0.30}(\text{No}) \\
 &= \cancel{1.15}(\text{Yes}) + \cancel{0.25}(\text{No}) \\
 \text{Final prediction} &\Rightarrow \underline{\text{Yes}}
 \end{aligned}$$



Adaboost Regressor

→ All the steps will be same except instead of Information gain, you will use Variance reduction to select the decision stump during prediction.

$$f = \alpha_1 m_1 + \alpha_2 m_2 + \dots + \alpha_n m_n$$