1 ilpTest1

Initial Dictionary

$$\begin{array}{c|cccc} x_3 & 6 & -3x_1 - 2x_2 \\ x_4 & 0 & +3x_1 - 2x_2 \\ \hline z & 0 & +1x_2 \end{array}$$

No initialization required \rightarrow Proceed to Optimize Final dictionary after first LP relaxation solve:

$$\begin{array}{c|cccc} x_1 & 1 & -0.166667x_3 + 0.166667x_4 \\ x_2 & 1.5 & -0.25x_3 & -0.25x_4 \\ \hline z & 1.5 & -0.25x_3 & -0.25x_4 \\ \end{array}$$

After cutting plane is added

$$\begin{array}{c|cccc} x_1 & 1 & -0.166667x_3 + 0.166667x_4 \\ x_2 & 1.5 & -0.25x_3 & -0.25x_4 \\ x_5 & -0.5 & +0.25x_3 & +0.25x_4 \\ \hline z & 1.5 & -0.25x_3 & -0.25x_4 \\ \end{array}$$

Forming the dual dictionary:

The Final Dual Dictionary is:

$$\begin{array}{c|cccc} y_5 & 1 & +0.666667y_1 + 1y_2 - 4y_3 \\ y_4 & 0 & -0.333333y_1 & +1y_3 \\ \hline z & -1 & -0.666667y_1 - 1y_2 - 2y_3 \end{array}$$

Final primal dictionary obtained:

$$\begin{array}{c|ccccc} x_1 & 0.6666666666667 & -0.666667x_5 + 0.333333x_4 \\ x_2 & 1 & -1x_5 \\ x_3 & 2 & +4x_5 & -1x_4 \\ \hline z & 1 & -1x_5 \end{array}$$

After cutting plane is added

Forming the dual dictionary:

The Final Dual Dictionary is:

Final primal dictionary obtained:

$$\begin{array}{c|cccc} x_1 & 1 & -1x_5 + 0.5x_6 \\ x_2 & 1 & -1x_5 \\ x_3 & 1 & +5x_5 - 1.5x_6 \\ x_4 & 1 & -1x_5 + 1.5x_6 \\ \hline z & 1 & -1x_5 \end{array}$$

Done.

2 ilpTest2

Initial Dictionary

$$\begin{array}{c|cccc} x_4 & 10 & -1x_1 \\ x_5 & 10 & -1x_2 \\ x_6 & 10 & -1x_3 \\ x_7 & 1 & +2x_1-7x_2 \\ x_8 & 3 & -1x_1+2x_2-5x_3 \\ x_9 & 7 & -1x_1-1x_2+3x_3 \\ \hline z & 0 & +1x_1+1x_2-5x_3 \\ \end{array}$$

No initialization required \rightarrow Proceed to Optimize Final dictionary after first LP relaxation solve:

```
4.33333333333
                          +0.333333x_8 +0.666667x_9 -0.333333x_3
x_4
x_5
       8.6666666667
                          -0.333333x_8 + 0.333333x_9 - 2.666667x_3
             10
                                                          -1x_3
x_6
              3
                              -3x_8
                                            +1x_{9}
                                                         -18x_3
x_7
       5.66666666667
                          -0.333333x_8 - 0.666667x_9 + 0.3333333x_3
x_1
       1.33333333333
                          +0.333333x_8 -0.333333x_9 +2.666667x_3
x_2
                          +0.666667x_8 +0.333333x_9 +0.333333x_3
x_{10}
       -0.3333333333333
     -0.6666666666667
                          +0.333333x_8 +0.666667x_9 +0.666667x_3
x_{11}
      -0.66666666667
                          +0.333333x_8 +0.666667x_9 +0.666667x_3
x_{12}
       -0.3333333333333
                          +0.666667x_8 +0.333333x_9 +0.333333x_3
x_{13}
              7
                                            -1x_{9}
 z
```

Forming the dual dictionary:

The Final Dual Dictionary is:

```
5
                                                 -x_7
                                                               -1x_3
x_4
        8.42857142857
                              +0.285714x_{11}+0.142857x_7-0.285714x_3
x_5
               10
x_6
        0.428571428571
                              +1.285714x_{11} + 0.142857x_7 + 1.714286x_3
x_9
                                  -1x_{11}
                5
x_1
                                                               +1x_{3}
        1.57142857143
                              -0.285714x_{11} - 0.142857x_7 + 0.285714x_3
x_2
         1.14285714286
                              +0.428571x_{11} -0.285714x_7 -5.428571x_3
x_8
                              +0.714286x_{11} -0.142857x_7 -2.714286x_3
        0.571428571429
x_{10}
                                                 -x_7
     1.58603289232e - 17
                                  +1x_{11}
x_{12}
        0.571428571429
                              +0.714286x_{11} -0.142857x_7 -2.714286x_3
x_{13}
        6.57142857143
                              -1.285714x_{11} - 0.142857x_7 - 3.714286x_3
 z
```

```
+1x_{11}
x_4
                                                -x_7
x_5
        8.42857142857
                             +0.285714x_{11} +0.142857x_7 -0.285714x_3
x_6
               10
        0.428571428571
                             +1.285714x_{11} +0.142857x_7 +1.714286x_3
x_9
               5
                                 -1x_{11}
                                                 +x_7
                                                              +1x_{3}
x_1
        1.57142857143
                             -0.285714x_{11} - 0.142857x_7 + 0.285714x_3
x_2
                             +0.428571x_{11} -0.285714x_7 -5.428571x_3
        1.14285714286
x_8
        0.571428571429
                             +0.714286x_{11} -0.142857x_7 -2.714286x_3
x_{10}
     1.58603289232e - 17
                                                 -x_7
x_{12}
                             +0.714286x_{11} -0.142857x_7 -2.714286x_3
        0.571428571429
x_{13}
       -0.428571428571
                             +0.714286x_{11}+0.857143x_7+0.285714x_3
x_{14}
                             +0.714286x_{11}+0.857143x_7+0.285714x_3
       -0.428571428571
x_{15}
                             +0.285714x_{11} +0.142857x_7 +0.714286x_3
       -0.571428571429
x_{16}
       -0.142857142857
                             +0.571429x_{11} +0.285714x_7 +0.428571x_3
x_{17}
       -0.571428571429
                             +0.285714x_{11} +0.142857x_7 +0.714286x_3
x_{18}
       -0.571428571429
                             +0.285714x_{11} +0.142857x_7 +0.714286x_3
x_{19}
        6.57142857143
                             -1.285714x_{11} - 0.142857x_7 - 3.714286x_3
```

Forming the dual dictionary:

Note: we treat these as zero/integer. A floating pt. tolerance of 10^{-10} or so should be used to decide integrality.

x_4	5	$+1x_{11} - x_{16} - 1x_3$
x_5	9	$+1x_{16}-1x_3$
x_6	10	$-1x_{3}$
x_9	1	$+1x_{11}+1x_{16}+1x_3$
x_1	5	$-1x_{11} + x_{16} + 1x_3$
x_2	1	$-1x_{16} + 1x_3$
x_8	-4.4408920985e - 16	$+1x_{11} - 2x_{16} - 4x_3$
x_{10}	-1.11022302463e - 15	$+1x_{11}-1x_{16}-2x_3$
x_{12}	-1.11022302463e - 16	$+1x_{11} - x_{16} + x_3$
x_{13}	-7.77156117238e - 16	$+1x_{11}-1x_{16}-2x_3$
x_7	4	$-2x_{11} + 7x_{16} - 5x_3$
x_{15}	3	$-1x_{11} + 6x_{16} - 4x_3$
x_{14}	3	$-1x_{11} + 6x_{16} - 4x_3$
x_{17}	1	$+2x_{16}-1x_3$
x_{18}	1.11022302463e - 15	$+1x_{16} +x_3$
x_{19}	7.77156117238e - 16	$+x_{11} +1x_{16} +x_3$
\overline{z}	6	$-1x_{11} - 1x_{16} - 3x_3$

Done.

3 ilpTest3

Initial Dictionary

$$\begin{array}{c|cccc} x_4 & 10 & -1x_1 \\ x_5 & 10 & -1x_2 \\ x_6 & 10 & -1x_3 \\ x_7 & 1 & +2x_1+7x_2 \\ x_8 & 3 & +1x_1+2x_2-5x_3 \\ x_9 & 7 & +1x_1-1x_2+3x_3 \\ \hline z & 0 & -1x_1-1x_2+5x_3 \\ \end{array}$$

No initialization required \rightarrow Proceed to Optimize Final dictionary after first LP relaxation solve:

$$\begin{array}{c|cccc} x_4 & 10 & -1x_1 \\ x_2 & 10 & -1x_5 \\ x_6 & 5.4 & -0.2x_1 + 0.4x_5 + 0.2x_8 \\ x_7 & 71 & +2x_1 & -7x_5 \\ x_3 & 4.6 & +0.2x_1 - 0.4x_5 - 0.2x_8 \\ x_9 & 10.8 & +1.6x_1 - 0.2x_5 - 0.6x_8 \\ \hline z & 13 & -1x_5 & -1x_8 \\ \end{array}$$

Forming the dual dictionary:

Done.

4 ilpTest4

Initial Dictionary

$$\begin{array}{c|ccc} x_3 & 15 & -2x_1 - 2x_2 \\ x_4 & 5 & -2x_1 + 2x_2 \\ \hline z & -20 & +3x_1 + 4x_2 \end{array}$$

No initialization required \rightarrow Proceed to Optimize Final dictionary after first LP relaxation solve:

$$\begin{array}{c|cccc} x_2 & 7.5 & -1x_1 - 0.5x_3 \\ x_4 & 20 & -4x_1 & -1x_3 \\ \hline z & 10 & -1x_1 & -2x_3 \end{array}$$

After cutting plane is added

$$\begin{array}{c|cccc} x_2 & 7.5 & -1x_1 - 0.5x_3 \\ x_4 & 20 & -4x_1 & -1x_3 \\ x_5 & -0.5 & +0.5x_3 \\ \hline z & 10 & -1x_1 & -2x_3 \end{array}$$

Forming the dual dictionary:

$$\begin{array}{c|cccc} y_1 & 1 & +1y_2 & +4y_4 \\ y_3 & 2 & +0.5y_2 + 1y_4 -0.5y_5 \\ \hline z & -10 & -7.5y_2 -2y_4 +0.5y_5 \end{array}$$

The Final Dual Dictionary is:

Final primal dictionary obtained:

Done.

5 ilpTest5

Initial Dictionary

$$\begin{array}{c|cccc} x_3 & 15 & -2x_1 - 5x_2 \\ x_4 & 5 & -2x_1 + 2x_2 \\ \hline z & -20 & +3x_1 + 4x_2 \end{array}$$

No initialization required \rightarrow Proceed to Optimize Final dictionary after first LP relaxation solve:

$$\begin{array}{c|cccc} x_2 & 1.42857142857 & +0.142857x_4 -0.142857x_3 \\ x_1 & 3.92857142857 & -0.357143x_4 -0.142857x_3 \\ \hline z & -2.5 & -0.5x_4 & -1x_3 \end{array}$$

After cutting plane is added

Forming the dual dictionary:

The Final Dual Dictionary is:

Final primal dictionary obtained:

$$\begin{array}{c|cccc} x_2 & 1.8 & +0.4x_6 -0.2x_3 \\ x_1 & 3 & -1x_6 \\ x_4 & 2.6 & +2.8x_6 -0.4x_3 \\ x_5 & 1.8 & +2.4x_6 -0.2x_3 \\ \hline z & -3.8 & -1.4x_6 -0.8x_3 \end{array}$$

After cutting plane is added

$$\begin{array}{c|cccc} x_2 & 1.8 & +0.4x_6 -0.2x_3 \\ x_1 & 3 & -1x_6 \\ x_4 & 2.6 & +2.8x_6 -0.4x_3 \\ x_5 & 1.8 & +2.4x_6 -0.2x_3 \\ x_7 & -0.8 & +0.6x_6 +0.2x_3 \\ x_8 & -0.6 & +0.2x_6 +0.4x_3 \\ x_9 & -0.8 & +0.6x_6 +0.2x_3 \\ \hline z & -3.8 & -1.4x_6 -0.8x_3 \\ \hline \end{array}$$

Forming the dual dictionary:

The Final Dual Dictionary is:

Done.

6 ilpTest6

Initial Dictionary

 x_7 leaves

Problem is feasible Initialization phase yields a zero answer Final dictionary after first LP relaxation solve:

Done.

7 ilpTest7

Initial Dictionary

$$\begin{array}{c|cccc} x_3 & 15 & -4x_1 - 2x_2 \\ x_4 & 8 & -1x_1 - 2x_2 \\ x_5 & 5 & -1x_1 - 1x_2 \\ \hline z & 0 & +3x_1 + 2x_2 \\ \end{array}$$

No initialization required \rightarrow Proceed to Optimize Final dictionary after first LP relaxation solve:

$$\begin{array}{c|cccc} x_1 & 2.5 & -0.5x_3 + 1x_5 \\ x_4 & 0.5 & -0.5x_3 + 3x_5 \\ x_2 & 2.5 & +0.5x_3 - 2x_5 \\ \hline z & 12.5 & -0.5x_3 - 1x_5 \\ \end{array}$$

$$\begin{array}{c|cccc} x_1 & 2.5 & -0.5x_3 + 1x_5 \\ x_4 & 0.5 & -0.5x_3 + 3x_5 \\ x_2 & 2.5 & +0.5x_3 - 2x_5 \\ x_6 & -0.5 & +0.5x_3 \\ x_7 & -0.5 & +0.5x_3 \\ x_8 & -0.5 & +0.5x_3 \\ \hline z & 12.5 & -0.5x_3 - 1x_5 \\ \end{array}$$

Forming the dual dictionary:

The Final Dual Dictionary is:

Final primal dictionary obtained:

$$\begin{array}{c|cccc} x_1 & 2 & -1x_6 + 1x_5 \\ x_4 & - & -1x_6 + 3x_5 \\ x_2 & 3 & +1x_6 - 2x_5 \\ x_3 & 1 & +2x_6 \\ x_7 & - & +1x_6 \\ x_8 & - & +1x_6 \\ \hline z & 12 & -1x_6 - 1x_5 \\ \end{array}$$

Done.

8 ilpTest8

Initial Dictionary

No initialization required \rightarrow Proceed to Optimize Final dictionary after first LP relaxation solve:

```
1.53178905865
                       +0.144899x_1 +0.00345x_8 -1.103006x_3 -0.019221x_5
x_4
     83.9566288812
                       -65.058157x_1 + 0.522425x_8 + 42.830458x_3 - 0.624938x_5
x_6
     92.6490882208
                       +78.074914x_1 -0.045835x_8 +27.082799x_3 -0.601774x_5
x_7
                       -0.058896x_1 -0.013307x_8 +0.040168x_3 +0.002711x_5
    0.0916707737802
x_2
x_9
     153.806308526
                       -48.464268x_1 + 0.560375x_8 - 76.302612x_3 - 0.836373x_5
                       -5.945047x_1 -0.510596x_8 -79.255052x_3 -0.655249x_5
     67.2952193199
z
```

After cutting plane is added

```
+0.144899x_1 +0.00345x_8 -1.103006x_3 -0.019221x_5
       1.53178905865
x_4
       83.9566288812
                         -65.058157x_1 + 0.522425x_8 + 42.830458x_3 - 0.624938x_5
x_6
                         +78.074914x_1 -0.045835x_8 +27.082799x_3 -0.601774x_5
       92.6490882208
x_7
      0.0916707737802
                          -0.058896x_1 -0.013307x_8 +0.040168x_3 +0.002711x_5
x_2
                          -48.464268x_1 + 0.560375x_8 - 76.302612x_3 - 0.836373x_5
       153.806308526
x_9
      -0.53178905865
                          +0.855101x_1 +0.99655x_8 +0.103006x_3 +0.019221x_5
x_{10}
                          +0.058157x_1 +0.477575x_8 +0.169542x_3 +0.624938x_5
x_{11}
      -0.956628881222
                          +0.925086x_1 +0.045835x_8 +0.917201x_3 +0.601774x_5
x_{12}
      -0.649088220798
     -0.0916707737802
                          +0.058896x_1 +0.013307x_8 +0.959832x_3 +0.997289x_5
x_{13}
                          +0.464268x_1 +0.439625x_8 +0.302612x_3 +0.836373x_5
x_{14}
      -0.806308526368
                          -5.945047x_1 -0.510596x_8 -79.255052x_3 -0.655249x_5
       67.2952193199
```

Forming the dual dictionary:

The Final Dual Dictionary is:

```
1.51164658635
                          +0.130924x_1 +0.018474x_{10} -1.099598x_3 -0.031325x_{11}
x_4
                         -65.869076x_1 + 1.018474x_{10} + 42.900402x_3 - 1.031325x_{11}
x_6
      83.5116465863
      91.9397590361
                         +77.771084x_1 + 0.421687x_{10} + 27.204819x_3 - 0.975904x_{11}
x_7
                          -0.045783x_1 -0.015663x_{10} +0.040964x_3 +0.004819x_{11}
     0.0879518072289
x_2
      153.139759036
                         -49.428916x_1 + 1.221687x_{10} - 76.195181x_3 - 1.375904x_{11}
x_9
                          -0.869076x_1 +1.018474x_{10} -0.099598x_3 -0.031325x_{11}
      0.511646586345
x_8
      1.13975903614
                          +0.571084x_1 -0.778313x_{10} -0.195181x_3 +1.624096x_{11}
x_5
     0.0602409638554
                          +1.228916x_1 -0.421687x_{10} +0.795181x_3 +0.975904x_{11}
x_{12}
                          +0.616867x_1 -0.762651x_{10} +0.763855x_3 +1.619277x_{11}
x_{13}
      1.05180722892
      0.371887550201
                          +0.559839x_1 -0.203213x_{10} +0.095582x_3 +1.344578x_{11}
x_{14}
                          -5.875502x_1 -0.01004x_{10} -79.076305x_3 -1.048193x_{11}
      66.2871485944
 z
```

```
1.51164658635
                            +0.130924x_1 +0.018474x_{10} -1.099598x_3 -0.031325x_{11}
x_4
       83.5116465863
                           -65.869076x_1 + 1.018474x_{10} + 42.900402x_3 - 1.031325x_{11}
x_6
       91.9397590361
                           +77.771084x_1 + 0.421687x_{10} + 27.204819x_3 - 0.975904x_{11}
x_7
      0.0879518072289
                           -0.045783x_1 -0.015663x_{10} +0.040964x_3 +0.004819x_{11}
x_2
                           -49.428916x_1 + 1.221687x_{10} - 76.195181x_3 - 1.375904x_{11}
       153.139759036
x_9
                            -0.869076x_1 +1.018474x_{10} -0.099598x_3 -0.031325x_{11}
       0.511646586345
x_8
                            +0.571084x_1 -0.778313x_{10} -0.195181x_3 +1.624096x_{11}
       1.13975903614
x_5
      0.0602409638554
                            +1.228916x_1 -0.421687x_{10} +0.795181x_3 +0.975904x_{11}
x_{12}
       1.05180722892
                            +0.616867x_1 -0.762651x_{10} +0.763855x_3 +1.619277x_{11}
x_{13}
       0.371887550201
                            +0.559839x_1 -0.203213x_{10} +0.095582x_3 +1.344578x_{11}
x_{14}
      -0.511646586345
                            +0.869076x_1 +0.981526x_{10} +0.099598x_3 +0.031325x_{11}
x_{15}
                            +0.869076x_1 +0.981526x_{10} +0.099598x_3 +0.031325x_{11}
      -0.511646586345
x_{16}
                            +0.228916x_1 +0.578313x_{10} +0.795181x_3 +0.975904x_{11}
      -0.939759036145
x_{17}
      -0.0879518072289
                            +0.045783x_1 +0.015663x_{10} +0.959036x_3 +0.995181x_{11}
x_{18}
      -0.139759036145
                            +0.428916x_1 +0.778313x_{10} +0.195181x_3 +0.375904x_{11}
x_{19}
      -0.511646586345
                            +0.869076x_1 +0.981526x_{10} +0.099598x_3 +0.031325x_{11}
x_{20}
                            +0.428916x_1 +0.778313x_{10} +0.195181x_3 +0.375904x_{11}
x_{21}
      -0.139759036145
     -0.0602409638554
                           +0.771084x_1 +0.421687x_{10} +0.204819x_3 +0.024096x_{11}
x_{22}
                            +0.383133x_1 +0.762651x_{10} +0.236145x_3 +0.380723x_{11}
     -0.0518072289157
x_{23}
                            +0.440161x_1 +0.203213x_{10} +0.904418x_3 +0.655422x_{11}
x_{24}
      -0.371887550201
                            -5.875502x_1 -0.01004x_{10} -79.076305x_3 -1.048193x_{11}
       66.2871485944
z
```

Forming the dual dictionary:

```
5.01851851852
                                                                                                                     -0.175309y_4 + 63.997531y_6 - 79y_7 + 0.065432y_2 + 47.069136y_9 - 0.175309y_8 + 1
   y_1
                                                                                                                    -0.004938y_4 -0.57284y_6
                           0.462962962963
                                                                                                                                                                                                                                                                                                 +0.01358y_2
                                                                                                                                                                                                                                                                                                                                                                 -0.62716y_9 -1.004938y_8 + 0
y_{17}
                              78.22222222
                                                                                                                    +1.074074y_4 - 43.740741y_6 - 28y_7 - 0.037037y_2 + 75.074074y_9 + 0.074074y_8 + 10.074074y_8 
   y_3
                          0.61111111111111
                                                                                                                     +0.037037y_4 +1.62963y_6 +1y_7 -0.018519y_2 +2.037037y_9 +1.037037y_8 -1
y_{12}
                                                                                                                    z
                          -65.8888888889
```

```
1.51851851852
                          +0.175309x_1 +0.004938x_{17} -1.074074x_3 -0.037037x_{12}
x_4
      84.1481481481
                         -63.997531x_1 +0.57284x_{17} +43.740741x_3 -1.62963x_{12}
x_6
             92
                             +79x_{1}
                                                           +28x_{3}
                                                                          -1x_{12}
x_7
     0.0740740740741
                          -0.065432x_1 -0.01358x_{17} +0.037037x_3 +0.018519x_{12}
x_2
                         -47.069136x_1 +0.62716x_{17} -75.074074x_3 -2.037037x_{12}
      153.851851852
x_9
                          +0.175309x_1 +1.004938x_{17} -0.074074x_3 -1.037037x_{12}
      1.51851851852
x_8
                          -1.550617x_1 -0.076543x_{17} -1.518519x_3 +1.740741x_{12}
x_5
      0.962962962963
                          -0.82716x_1 +0.432099x_{17} -0.814815x_3 +0.592593x_{12}
      0.37037037037
x_{11}
      0.8888888889
                          -1.485185x_1 -0.062963x_{17} -0.555556x_3 +1.722222x_{12}
x_{13}
      0.666666666667
                          -0.755556x_1 +0.377778x_{17}
                                                            -1x_{3}
                                                                          +1x_{12}
x_{14}
             1
                                                            +x_3
                              +1x_{1}
                                            +1x_{17}
                                                                          -1x_{12}
x_{10}
      0.481481481481
                          +1.824691x_1 +0.995062x_{17} +0.074074x_3 -0.962963x_{12}
x_{16}
                          +1.824691x_1 +0.995062x_{17} +0.074074x_3 -0.962963x_{12}
      0.481481481481
x_{15}
      0.296296296296
                          -0.761728x_1 + 0.445679x_{17} + 0.148148x_3 + 0.574074x_{12}
x_{18}
      0.77777777778
                          +0.896296x_1 +0.940741x_{17} -0.1111111x_3 -0.555556x_{12}
x_{19}
      0.481481481481
                          +1.824691x_1 +0.995062x_{17} +0.074074x_3 -0.962963x_{12}
x_{20}
x_{21}
      0.77777777778
                          +0.896296x_1 +0.940741x_{17} -0.1111111x_3 -0.555556x_{12}
      0.37037037037
                          +1.17284x_1 +0.432099x_{17} +0.185185x_3 -0.407407x_{12}
x_{22}
                          +0.830864x_1 +0.92716x_{17} -0.074074x_3 -0.537037x_{12}
      0.851851851852
x_{23}
                          +0.101235x_1 +0.48642x_{17} +0.37037x_3 +0.185185x_{12}
x_{24}
     0.0740740740741
                          -5.018519x_1 -0.462963x_{17} -78.222222x_3 -0.611111x_{12}
      65.888888889
```

```
1.51851851852
                            +0.175309x_1 +0.004938x_{17} -1.074074x_3 -0.037037x_{12}
x_4
       84.1481481481
                           -63.997531x_1 + 0.57284x_{17} + 43.740741x_3 - 1.62963x_{12}
x_6
              92
                                                             +28x_{3}
x_7
                            -0.065432x_1 -0.01358x_{17} +0.037037x_3 +0.018519x_{12}
      0.0740740740741
x_2
       153.851851852
                           -47.069136x_1 +0.62716x_{17} -75.074074x_3 -2.037037x_{12}
x_9
                            +0.175309x_1 +1.004938x_{17} -0.074074x_3 -1.037037x_{12}
       1.51851851852
x_8
                            -1.550617x_1 -0.076543x_{17} -1.518519x_3 +1.740741x_{12}
       0.962962962963
x_5
                            -0.82716x_1 +0.432099x_{17} -0.814815x_3 +0.592593x_{12}
       0.37037037037
x_{11}
                            -1.485185x_1 -0.062963x_{17} -0.555556x_3 +1.722222x_{12}
x_{13}
       0.88888888889
       0.6666666666667
                            -0.755556x_1 + 0.377778x_{17}
                                                              -1x_3
                                                                            +1x_{12}
x_{14}
              1
                                +1x_1
                                              +1x_{17}
                                                              +x_3
                                                                             -1x_{12}
x_{10}
       0.481481481481
                            +1.824691x_1 +0.995062x_{17} +0.074074x_3 -0.962963x_{12}
x_{16}
       0.481481481481
                            +1.824691x_1 +0.995062x_{17} +0.074074x_3 -0.962963x_{12}
x_{15}
                            -0.761728x_1 + 0.445679x_{17} + 0.148148x_3 + 0.574074x_{12}
       0.296296296296
x_{18}
       0.77777777778
                            +0.896296x_1 +0.940741x_{17} -0.1111111x_3 -0.555556x_{12}
x_{19}
                            +1.824691x_1 +0.995062x_{17} +0.074074x_3 -0.962963x_{12}
       0.481481481481
x_{20}
                            +0.896296x_1 +0.940741x_{17} -0.1111111x_3 -0.555556x_{12}
x_{21}
       0.77777777778
                            +1.17284x_1 +0.432099x_{17} +0.185185x_3 -0.407407x_{12}
       0.37037037037
x_{22}
                            +0.830864x_1 +0.92716x_{17} -0.074074x_3 -0.537037x_{12}
       0.851851851852
x_{23}
      0.0740740740741
                            +0.101235x_1 +0.48642x_{17} +0.37037x_3 +0.185185x_{12}
x_{24}
                            +0.824691x_1 +0.995062x_{17} +0.074074x_3 +0.037037x_{12}
x_{25}
      -0.518518518519
                            +0.997531x_1 +0.42716x_{17} +0.259259x_3 +0.62963x_{12}
      -0.148148148148
x_{26}
      -0.0740740740741
                            +0.065432x_1 +0.01358x_{17} +0.962963x_3 +0.981481x_{12}
x_{27}
                            +0.069136x_1 +0.37284x_{17} +0.074074x_3 +0.037037x_{12}
      -0.851851851852
x_{28}
                            +0.824691x_1 +0.995062x_{17} +0.074074x_3 +0.037037x_{12}
      -0.518518518519
x_{29}
      -0.962962962963
                            +0.550617x_1 +0.076543x_{17} +0.518519x_3 +0.259259x_{12}
x_{30}
                            +0.82716x_1 +0.567901x_{17} +0.814815x_3 +0.407407x_{12}
       -0.37037037037
x_{31}
      -0.88888888889
                            +0.485185x_1 +0.062963x_{17} +0.555556x_3 +0.277778x_{12}
x_{32}
                            +0.755556x_1 +0.622222x_{17}
      -0.6666666666667
                                                              +x_3
x_{33}
                            +0.175309x_1 +0.004938x_{17} +0.925926x_3 +0.962963x_{12}
x_{34}
      -0.481481481481
                            +0.175309x_1 +0.004938x_{17} +0.925926x_3 +0.962963x_{12}
      -0.481481481481
x_{35}
                            +0.761728x_1 +0.554321x_{17} +0.851852x_3 +0.425926x_{12}
x_{36}
      -0.296296296296
x_{37}
      -0.77777777778
                            +0.103704x_1 +0.059259x_{17} +0.1111111x_3 +0.555556x_{12}
                            +0.175309x_1 +0.004938x_{17} +0.925926x_3 +0.962963x_{12}
x_{38}
      -0.481481481481
      -0.77777777778
                            +0.103704x_1 +0.059259x_{17} +0.1111111x_3 +0.555556x_{12}
x_{39}
       -0.37037037037
                            +0.82716x_1 +0.567901x_{17} +0.814815x_3 +0.407407x_{12}
x_{40}
                            +0.169136x_1 +0.07284x_{17} +0.074074x_3 +0.537037x_{12}
      -0.851851851852
x_{41}
                            +0.898765x_1 +0.51358x_{17} +0.62963x_3 +0.814815x_{12}
      -0.0740740740741
x_{42}
                            \overline{-5.018}519x_1 -0.462963x_{17} -78.222222x_3 -0.611111x_{12}
       65.888888889
 z
```

Forming the dual dictionary:

```
5.01851851852
                                                                                                                                                                                                                                                                                                                          -0.175309y_4 + 63.997531y_6 - 79y_7 + 0.065432y_2 + 47.069136y_9 - 0.175309y_8 + 10.065432y_2 + 47.069136y_9 - 0.175309y_8 + 10.065432y_9 + 10.06542y_9 + 10.06544y_9 + 10.0654y_9 + 10.0654y_9 + 10.0654y_9 + 10.0654y_9 + 10.0654y_9 + 10.
        y_1
                                                                         0.462962962963
                                                                                                                                                                                                                                                                                                                        -0.004938y_4 -0.57284y_6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              +0.01358y_2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          -0.62716y_9 -1.004938y_8+0
  y_{17}
                                                                                 78.222222222
                                                                                                                                                                                                                                                                                                                        +1.074074y_4 - 43.740741y_6 - 28y_7 - 0.037037y_2 + 75.074074y_9 + 0.074074y_8 + 1.074074y_8 + 1.0
        y_3
                                                                         0.61111111111111
                                                                                                                                                                                                                                                                                                                   +0.037037y_4 +1.62963y_6 +1y_7 -0.018519y_2 +2.037037y_9 +1.037037y_8 -1.037037y_8 +1.037037y_8 +1.03707y_8 +1
y_{12}
                                                                                                                                                                                                                                                                                                                     -65.8888888889
```

```
2.86600496278
                                                                                                                                                                                                           -0.205955y_4 + 63.724566y_6 - 80.230769y_7 + 0.047146y_2 + 46.459057y_9 + 1.58808y_7 + 0.047146y_2 + 46.459057y_9 + 1.58808y_7 + 0.047146y_7 + 0.047146y_8 + 0.047146y_8
      y_1
                                                                                                                                                                                                        0.220843672457
  y_{15}
                                                                                                                                                                                                           76.5583126551
      y_3
                                                  3.17741935484
                                                                                                                                                                                                           +0.096774y_4 +3.225806y_6 +3y_7 -0.016129y_2 +4.290323y_9 +0.19354y_6 +0.096774y_4 +3.225806y_6 +0.096774y_6 +0.000774y_6 +0.000774y_6 +0.000774y_6 +0.000740y_6 +0.000740y_
y_{30}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           -89y_7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  -0.096774y_2 - 149.258065y_9 - 0.8387
                                                   -62.935483871
                                                                                                                                                                                                      -1.419355y_4 - 80.645161y_6
           z
```

```
1.41935483871
                              +0.205955x_1 +0.012407x_{15} -1.024814x_3 -0.096774x_{30}
x_4
                              -63.724566x_1 + 0.823821x_{15} + 45.352357x_3 - 3.225806x_{30}
x_6
        80.6451612903
               89
                             +80.230769x_1 +0.230769x_{15} +29.538462x_3
x_7
       0.0967741935484
                              -0.047146x_1 -0.014888x_{15} +0.029777x_3 +0.016129x_{30}
x_2
        149.258064516
                             -46.459057x_1 + 0.960298x_{15} - 72.920596x_3 - 4.290323x_{30}
x_9
                              -1.588089x_1 +1.024814x_{15} -0.049628x_3 -0.193548x_{30}
        0.838709677419
x_8
                              -3.461538x_1 -0.461538x_{15} -4.076923x_3
                6
x_5
                              -2.863524x_1 +0.200993x_{15} -2.401985x_3 +3.032258x_{30}
         3.1935483871
x_{11}
                              -3.414392x_1 -0.44665x_{15} -3.1067x_3 +4.983871x_{30}
        5.90322580645
x_{13}
        4.58064516129
                              -3.129032x_1 +0.064516x_{15} -3.129032x_3 +4.096774x_{30}
x_{14}
                              -1.104218x_1 +0.282878x_{15} -0.565757x_3 +1.193548x_{30}
        0.161290322581
x_{28}
      2.6645352591e - 15
                                   +x_1
                                                 +1x_{15}
x_{16}
                                                                 -x_3
        0.41935483871
                              -0.794045x_1 +1.012407x_{15} -0.024814x_3 -0.096774x_{30}
x_{10}
                              -2.816377x_1 +0.215881x_{15} -1.431762x_3 +3.016129x_{30}
        3.09677419355
x_{18}
         1.38709677419
                              -1.265509x_1 +0.863524x_{15} -0.727047x_3 +1.064516x_{30}
x_{19}
     1.11022302463e - 16
x_{20}
                                                 +1x_{15}
                                                                 +x_3
x_{21}
                              -1.265509x_1 +0.863524x_{15} -0.727047x_3 +1.064516x_{30}
        1.38709677419
        0.193548387097
                              +0.367246x_1 +0.431762x_{15} +0.136476x_3 +0.032258x_{30}
x_{22}
        1.48387096774
                              -1.312655x_1 +0.848635x_{15} -0.69727x_3 +1.080645x_{30}
x_{23}
         1.8064516129
                              -1.598015x_1 +0.337469x_{15} -0.674938x_3 +1.967742x_{30}
x_{24}
                              -3.024814x_1 +0.781638x_{15} -1.563275x_3 +2.903226x_{30}
x_{17}
        2.41935483871
        2.77419354839
                              -1.069479x_1 + 0.188586x_{15} -1.377171x_3 +3.129032x_{30}
x_{26}
                3
                              -1.230769x_1 -0.230769x_{15} -1.538462x_3
                                                                               +3x_{30}
x_{12}
                2
                              -2.230769x_1 +0.769231x_{15} -1.538462x_3
                                                                               +3x_{30}
x_{25}
                2
                              -2.230769x_1 +0.769231x_{15} -1.538462x_3
x_{29}
        2.90322580645
                              -1.183623x_1 -0.215881x_{15} -0.568238x_3 +2.983871x_{30}
x_{27}
         2.22580645161
                               -1.39206x_1 +0.349876x_{15} -0.699752x_3 +2.870968x_{30}
x_{31}
       0.0967741935484
                              -0.047146x_1 -0.014888x_{15} +0.029777x_3 +1.016129x_{30}
x_{32}
                              -1.126551x_1 + 0.486352x_{15} -0.972705x_3 +1.806452x_{30}
        0.838709677419
x_{33}
                              -1.024814x_1 -0.218362x_{15} -0.563275x_3 +2.903226x_{30}
        2.41935483871
x_{34}
                              -1.024814x_1 -0.218362x_{15} -0.563275x_3 +2.903226x_{30}
        2.41935483871
x_{35}
                              -1.439206x_1 +0.334988x_{15} -0.669975x_3 +2.887097x_{30}
x_{36}
        2.32258064516
        1.03225806452
                              -0.759305x_1 -0.081886x_{15} -0.836228x_3 +1.83871x_{30}
x_{37}
        2.41935483871
                              -1.024814x_1 -0.218362x_{15} -0.563275x_3 +2.903226x_{30}
x_{38}
        1.03225806452
                              -0.759305x_1 -0.081886x_{15} -0.836228x_3 +1.83871x_{30}
x_{39}
        2.22580645161
                               -1.39206x_1 +0.349876x_{15} -0.699752x_3 +2.870968x_{30}
x_{40}
        0.935483870968
                              -0.712159x_1 -0.066998x_{15} -0.866005x_3 +1.822581x_{30}
x_{41}
        3.61290322581
                              -1.657568x_1 +0.2134x_{15} -1.426799x_3 +3.935484x_{30}
x_{42}
         62.935483871
                              -2.866005x_1 -0.220844x_{15} -76.558313x_3 -3.177419x_{30}
 z
```

0.4109549997

```
1.41935483871
                              +0.205955x_1 +0.012407x_{15} -1.024814x_3 -0.096774x_{30}
x_4
                              -63.724566x_1 + 0.823821x_{15} + 45.352357x_3 - 3.225806x_{30}
x_6
         80.6451612903
               89
                             +80.230769x_1 +0.230769x_{15} +29.538462x_3
x_7
       0.0967741935484
                              -0.047146x_1 -0.014888x_{15} +0.029777x_3 +0.016129x_{30}
x_2
        149.258064516
                              -46.459057x_1 + 0.960298x_{15} - 72.920596x_3 - 4.290323x_{30}
x_9
        0.838709677419
                              -1.588089x_1 +1.024814x_{15} -0.049628x_3 -0.193548x_{30}
x_8
                              -3.461538x_1 -0.461538x_{15} -4.076923x_3
                6
x_5
                                                                               +5x_{30}
                              -2.863524x_1 +0.200993x_{15} -2.401985x_3 +3.032258x_{30}
         3.1935483871
x_{11}
                              -3.414392x_1 -0.44665x_{15} -3.1067x_3 +4.983871x_{30}
x_{13}
        5.90322580645
         4.58064516129
                              -3.129032x_1 +0.064516x_{15} -3.129032x_3 +4.096774x_{30}
x_{14}
                              -1.104218x_1 +0.282878x_{15} -0.565757x_3 +1.193548x_{30}
        0.161290322581
x_{28}
      2.6645352591e - 15
                                   +x_1
                                                 +1x_{15}
x_{16}
                                                                 -x_3
        0.41935483871
                              -0.794045x_1 +1.012407x_{15} -0.024814x_3 -0.096774x_{30}
x_{10}
                              -2.816377x_1 + 0.215881x_{15} -1.431762x_3 +3.016129x_{30}
        3.09677419355
x_{18}
         1.38709677419
                              -1.265509x_1 + 0.863524x_{15} -0.727047x_3 +1.064516x_{30}
x_{19}
     1.11022302463e - 16
x_{20}
                                                 +1x_{15}
                                                                 +x_3
x_{21}
         1.38709677419
                              -1.265509x_1 +0.863524x_{15} -0.727047x_3 +1.064516x_{30}
        0.193548387097
                              +0.367246x_1 +0.431762x_{15} +0.136476x_3 +0.032258x_{30}
x_{22}
        1.48387096774
                              -1.312655x_1 +0.848635x_{15} -0.69727x_3 +1.080645x_{30}
x_{23}
         1.8064516129
                              -1.598015x_1 +0.337469x_{15} -0.674938x_3 +1.967742x_{30}
x_{24}
                              -3.024814x_1 +0.781638x_{15} -1.563275x_3 +2.903226x_{30}
x_{17}
         2.41935483871
         2.77419354839
                              -1.069479x_1 + 0.188586x_{15} -1.377171x_3 +3.129032x_{30}
x_{26}
                3
                              -1.230769x_1 -0.230769x_{15} -1.538462x_3
x_{12}
                                                                               +3x_{30}
                2
                              -2.230769x_1 +0.769231x_{15} -1.538462x_3
x_{25}
                                                                               +3x_{30}
                2
                              -2.230769x_1 +0.769231x_{15} -1.538462x_3
x_{29}
         2.90322580645
                              -1.183623x_1 -0.215881x_{15} -0.568238x_3 +2.983871x_{30}
x_{27}
         2.22580645161
                               -1.39206x_1 +0.349876x_{15} -0.699752x_3 +2.870968x_{30}
x_{31}
       0.0967741935484
                              -0.047146x_1 -0.014888x_{15} +0.029777x_3 +1.016129x_{30}
x_{32}
        0.838709677419
                              -1.126551x_1 + 0.486352x_{15} -0.972705x_3 +1.806452x_{30}
x_{33}
        2.41935483871
                              -1.024814x_1 -0.218362x_{15} -0.563275x_3 +2.903226x_{30}
x_{34}
                              -1.024814x_1 -0.218362x_{15} -0.563275x_3 +2.903226x_{30}
        2.41935483871
x_{35}
                              -1.439206x_1 +0.334988x_{15} -0.669975x_3 +2.887097x_{30}
x_{36}
        2.32258064516
        1.03225806452
                              -0.759305x_1 -0.081886x_{15} -0.836228x_3 +1.83871x_{30}
x_{37}
x_{38}
         2.41935483871
                              -1.024814x_1 -0.218362x_{15} -0.563275x_3 +2.903226x_{30}
         1.03225806452
                              -0.759305x_1 -0.081886x_{15} -0.836228x_3 +1.83871x_{30}
x_{39}
         2.22580645161
                               -1.39206x_1 +0.349876x_{15} -0.699752x_3 +2.870968x_{30}
x_{40}
        0.935483870968
                              -0.712159x_1 -0.066998x_{15} -0.866005x_3 +1.822581x_{30}
x_{41}
        3.61290322581
                              -1.657568x_1 +0.2134x_{15} -1.426799x_3 +3.935484x_{30}
x_{42}
                              +0.794045x_1 +0.987593x_{15} +0.024814x_3 +0.096774x_{30}
x_{43}
        -0.41935483871
       -0.645161290323
                              +0.724566x_1 +0.176179x_{15} +0.647643x_3 +0.225806x_{30}
x_{44}
       -0.0967741935484
                              +0.047146x_1 +0.014888x_{15} +0.970223x_3 +0.983871x_{30}
x_{45}
       -0.258064516129
                              +0.459057x_1 +0.039702x_{15} +0.920596x_3 +0.290323x_{30}
x_{46}
       -0.838709677419
                              +0.588089x_1 +0.975186x_{15} +0.049628x_3 +0.193548x_{30}
x_{47}
                              +0.863524x_1 +0.799007x_{15} +0.401985x_3 +0.967742x_{30}
       -0.193548387097
x_{48}
                              +0.414392x_1 +0.44665x_{15}
x_{49}
       -0.903225806452
                                                             +0.1067x_3 +0.016129x_{30}
                              +0.129032x_1 +0.935484x_{15} +0.129032x_3 +0.903226x_{30}
        -0.58064516129
x_{50}
       -0.161290322581
                              +0.104218x_1 +0.717122x_{15} +0.565757x_3 +0.806452x_{30}
x_{51}
```

 $+0.704045_{\infty} +0.097502_{\infty} +0.094914_{\infty} +0.006774_{\infty}$

Forming the dual dictionary:

```
2.86600496278
           y_1
  0.220843672457
           y_{15}
           76.5583126551
y_3
                         +3y_7 -0.016129y_2 +4.290323y_9 +0.19354
  3.17741935484
           +0.096774y_4 +3.225806y_6
y_{30}
           -1.419355y_4 - 80.645161y_6
                          -89y_{7}
                               -0.096774y_2 - 149.258065y_9 - 0.8387
  -62.935483871
```

1 11101	primar dictionary obtain	ica.			
x_4	1.66666666667	$+0.5x_2$	$+0.333333x_{72}$	$-1.166667x_3$	$-0.166667x_{45}$
x_6	19.6666666667	$-621.5x_2$	$-132.666667x_{72}$	$+148.8333333x_3$	$+30.833333x_{45}$
x_7	170	$+657.5x_2$	$+159x_{72}$	$-86.5x_3$	$-42.5x_{45}$
x_1	1	$+8.5x_2$	$+2x_{72}$	$-1.5x_3$	$-0.5x_{45}$
x_9	106		$-99x_{72}$	$+6.5x_3$	$+21.5x_{45}$
x_8	2.66666666667	$-109x_2$	$-9.666667x_{72}$	$+8.3333333x_3$	$+3.333333x_{45}$
x_5	1	$+18.5x_2$	$-4x_{72}$	$-6.5x_3$	$+5.5x_{45}$
x_{11}	1		$-7x_{72}$	-	
x_{13}	1		$-4x_{72}$	$-5.5x_3$	
x_{14}	1.66666666667		$-6.666667x_{72}$	$-2.166667x_3$	$+5.833333x_{45}$
x_{28}	-1.69642078163e - 13		$-4x_{72}$		$+2.5x_{45}$
x_{16}	3.3333333333		$-6.333333x_{72}$	$+5.666667x_3$	$+2.666667x_{45}$
x_{10}	3		$-8x_{72}$	$+7x_{3}$	
x_{18}	1		$-7x_{72}$	$+1x_{3}$	$+5x_{45}$
x_{19}	3		$-8x_{72}$	$+5x_3$	
x_{20}	3.3333333333	_	$-6.333333x_{72}$		$+2.666667x_{45}$
x_{21}	3	_	$-8x_{72}$	-	$+4x_{45}$
x_{22}	2		$-2x_{72}$	$+2x_3$	$+1x_{45}$
x_{23}	3		$-8x_{72}$	$+5x_{3}$	$+4x_{45}$
x_{24}	1.33333333333		$-5.333333x_{72}$	$+1.666667x_3$	$+3.666667x_{45}$
x_{17}	2	_	$-11x_{72}$	$+4.5x_3$	$+6.5x_{45}$
x_{26}	2.33333333333		$-3.333333x_{72}$	$-1.833333x_3$	$+4.166667x_{45}$
x_{12}	1	$+14x_{2}$	$-1x_{72}$	$-4x_{3}$	$+3x_{45}$
x_{25}	2.33333333333	$-87.5x_2$	$-9.333333x_{72}$	$+3.166667x_3$	$+6.166667x_{45}$
x_{29}	2.33333333333	_	$-9.333333x_{72}$	$+3.166667x_3$	$+6.166667x_{45}$
x_{27}	1	$+13x_{2}$	$-1x_{72}$	$-3x_{3}$	$+3x_{45}$
x_{31}	2		$-5x_{72}$	$+0.5x_3$	$+4.5x_{45}$
x_{32}	1.94289029309e - 16	$+2x_2$	$-x_{72}$	$-1x_{3}$	
x_{33}	1.33333333333		$-5.333333x_{72}$	$+1.666667x_3$	$+3.666667x_{45}$
x_{34}	0.666666666667	$+14.5x_2$	$-0.666667x_{72}$	$-3.166667x_3$	$+2.8333333x_{45}$
x_{35}	0.666666666667	$+14.5x_2$		$-3.166667x_3$	$+2.8333333x_{45}$
x_{36}	2	_	$-5x_{72}$	-	$+4.5x_{45}$
x_{37}	-3.10307335383e - 14			$-2x_3$	
x_{38}	0.666666666667	$+14.5x_2$	•-	$-3.166667x_3$	$+2.833333x_{45}$
x_{39}	2.77555756156e - 16	$+3x_2$	$-1x_{72}$	$-2x_3$	$+2x_{45}$
x_{40}	2	$-41.5x_2$	$-5x_{72}$	$+0.5x_3$	$+4.5x_{45}$
x_{41}	-5.55111512313e - 17	$+2x_2$	$-1x_{72}$	$-2x_{3}$	$+2x_{45}$
x_{42}	2.66666666667	$-3x_2$	$-4.666667x_{72}$	$-1.666667x_3$	$+5.3333333x_{45}$
x_{15}	3.3333333333	$-93x_{2}$	$-6.333333x_{72}$	$+5.666667x_3$	$+2.666667x_{45}$
x_{43}	3.66666666667	$-85x_{2}$	$-4.666667x_{72}$	$+4.3333333x_3$	$+2.333333x_{45}$
x_{30}	1.38777878078e - 17	$+1x_{2}^{2}1$	$+x_{72}$	$-1x_{3}$	$+1x_{45}$
x_{44}	0.666666666667	$-1x_2$	$+0.333333x_{72}$	$+0.3333333x_3$	$+0.333333x_{45}$
x_{47}	3	$-85.5x_2$	$-5x_{72}$	$+4.5x_3$	$+2.5x_{45}$
x_{48}	3.33333333333	$-66x_2$	$-3.333333x_{72}$	$+2.666667x_3$	$+2.666667x_{45}$
x_{49}	1	$-38x_{2}$	$-2x_{72}$	$+2x_{3}$	$+1x_{45}$
x_{50}	2.66666666667	$-85x_{2}$	$-5.666667x_{72}$	$+4.3333333x_3$	$+3.333333x_{45}$
x_{51}	2.33333333333	$-65x_{2}$	$-4.333333x_{72}$	$+3.666667x_3$	$+2.666667x_{45}$
~	2 66666666667	85m-	4.666667 _m	$\pm 4.333332_{m_{-}}$	\pm 9 222222 $_{r}$

Aiter	cutting plane is added				
x_4	1.66666666667	$+0.5x_2$	$+0.333333x_{72}$	$-1.166667x_3$	$-0.166667x_{45}$
x_6	19.6666666667	$-621.5x_2$	$-132.666667x_{72}$	$+148.8333333x_3$	$+30.833333x_{45}$
x_7	170	$+657.5x_2$	$+159x_{72}$	$-86.5x_{3}$	$-42.5x_{45}$
x_1	1	$+8.5x_2$	$+2x_{72}$	$-1.5x_3$	$-0.5x_{45}$
x_9	106	$-488.5x_2$	$-99x_{72}$	$+6.5x_{3}$	$+21.5x_{45}$
x_8	2.66666666667	$-109x_2$	$-9.666667x_{72}$	$+8.3333333x_3$	$+3.333333x_{45}$
x_5	1	$+18.5x_2$	$-4x_{72}$	$-6.5x_{3}$	$+5.5x_{45}$
x_{11}	1	$-4x_2$		$+x_3$	$+5x_{45}$
x_{13}	1			$-5.5x_{3}$	$+5.5x_{45}$
x_{14}	1.66666666667	$-28.5x_2$	$-6.666667x_{72}$		
x_{28}	-1.69642078163e - 13	$-34.5x_2$	$-4x_{72}$	$+1.5x_3$	$+2.5x_{45}$
x_{16}	3.33333333333	$-93x_{2}$	$-6.333333x_{72}$	$+5.666667x_3$	$+2.666667x_{45}$
x_{10}	3	$-101x_2$	$-8x_{72}$	$+7x_{3}$	$+3x_{45}$
x_{18}	1	$-41x_{2}$	$-7x_{72}$	$+1x_{3}$	$+5x_{45}$
x_{19}	3	$-9x_{2}$	$-8x_{72}$	$+5x_{3}$	$+4x_{45}$
x_{20}	3.33333333333	$-93x_{2}$	$-6.333333x_{72}$		$+2.666667x_{45}$
x_{21}	3	$-9x_{2}$	$-8x_{72}$	$+5x_{3}$	$+4x_{45}$
x_{22}	$\overline{}$	$-37x_{2}$	$-2x_{72}$	$+2x_{3}$	$+1x_{45}$
x_{23}	3	$-89x_{2}$	$-8x_{72}$	$+5x_{3}$	$+4x_{45}$
x_{24}	1.33333333333	$-43x_{2}$	$-5.333333x_{72}$	$+1.666667x_3$	$+3.666667x_{45}$
x_{17}	$\overline{}$	$-95.5x_2$	$-11x_{72}$	$+4.5x_3$	$+6.5x_{45}$
x_{26}	2.33333333333	$-23.5x_2$	$-3.333333x_{72}$	$-1.833333x_3$	$+4.166667x_{45}$
x_{12}	1	$+14x_{2}$	$-1x_{72}$	$-4x_{3}$	$+3x_{45}$
x_{25}	2.33333333333	$-87.5x_2$	$-9.333333x_{72}$	$+3.166667x_3$	$+6.166667x_{45}$
x_{29}	2.33333333333	$-87.5x_2$	$-9.333333x_{72}$	$+3.166667x_3$	$+6.166667x_{45}$
x_{27}	1	$+13x_{2}$	$-1x_{72}$	$-3x_{3}$	$+3x_{45}$
x_{31}	$\overline{2}$	$-41.5x_2$	$-5x_{72}$	$+0.5x_3$	$+4.5x_{45}$
x_{32}	1.94289029309e - 16	$+2x_2$	$-x_{72}$	$-1x_{3}$	$+1x_{45}$
x_{33}	1.3333333333	$-53x_{2}$	$-5.333333x_{72}$	$+1.666667x_3$	$+3.666667x_{45}$
x_{34}	0.666666666667	$+14.5x_2$	$-0.666667x_{72}$	$-3.166667x_3$	$+2.8333333x_{45}$
x_{35}	0.666666666667	$+14.5x_2$	$-0.666667x_{72}$	$-3.166667x_3$	$+2.8333333x_{45}$
x_{36}	2	$-40.5x_2$	$-5x_{72}$	$+0.5x_3$	$+4.5x_{45}$
x_{37}	-3.10307335383e - 14	$+3x_2$	$-1x_{72}$	$-2x_{3}$	$+2x_{45}$
x_{38}	0.666666666667		$-0.666667x_{72}$	$-3.166667x_3$	$+2.833333x_{45}$
x_{39}	2.77555756156e - 16	$+3x_2$	$-1x_{72}$	$-2x_{3}$	$+2x_{45}$
x_{40}	2	$-41.5x_2$	$-5x_{72}$	$+0.5x_3$	$+4.5x_{45}$
x_{41}	-5.55111512313e - 17	$+2x_2$	$-1x_{72}$	$-2x_{3}$	$+2x_{45}$
x_{42}	2.66666666667	$-3x_2$	$-4.666667x_{72}$	$-1.666667x_3$	$+5.333333x_{45}$
x_{15}	3.3333333333	$-93x_{2}$	$-6.333333x_{72}$	$+5.666667x_3$	$+2.666667x_{45}$
x_{43}	3.66666666667	$-85x_{2}$	$-4.666667x_{72}$	$+4.3333333x_3$	$+2.333333x_{45}$
x_{30}	1.38777878078e - 17	+122	$+x_{72}$	$-1x_{3}$	$+1x_{45}$
x_{44}	0.666666666667	$-1x_2$	$+0.333333x_{72}$	$+0.3333333x_3$	$+0.333333x_{45}$
x_{47}	3	$-85.5x_2$	$-5x_{72}$	$+4.5x_3$	$+2.5x_{45}$
x_{48}	3.3333333333	$-66x_2$	$-3.333333x_{72}$	$+2.666667x_3$	$+2.666667x_{45}$
x_{49}	1	$-38x_{2}$	$-2x_{72}$	$+2x_{3}$	$+1x_{45}$
x_{50}	2.66666666667	$-85x_{2}$	$-5.666667x_{72}$	$+4.333333x_3$	$+3.333333x_{45}$
x_{51}	2.3333333333	$-65x_{2}$	$-4.333333x_{72}$	$+3.666667x_3$	$+2.666667x_{45}$
· · · ·	3 6666666667	85m-	1.666667 <i>x</i>	$+4.333333x^{**}$	$\pm 9.333332_{max}$

Forming the dual dictionary:

5 1706975

```
1.55859375
                              -1.789063x_2
                                             -0.277344x_{74} -0.539063x_3 -0.003906x_6
x_4
            1.765625
                               +8.15625x_2
                                             +3.109375x_{74}
                                                             -2.84375x_3 +0.015625x_6
x_{45}
         183.77734375
                             -132.601563x_2 - 17.246094x_{74} + 107.648437x_3 - 1.285156x_6
x_7
                                             -0.109375x_{74}
                                                             +0.84375x_3 -0.015625x_6
            1.234375
                               -1.15625x_2
x_1
          88.66015625
                              -37.023437x_2 -4.691406x_{74} -100.273438x_3 + 0.722656x_6
x_9
                              -54.851562x_2 +3.378906x_{74} -5.601562x_3 +0.089844x_6
          3.15234375
x_8
           8.4765625
                              +74.515625x_2 +14.210937x_{74} -23.984375x_3 +0.101562x_6
x_5
                              +20.304688x_2 +10.488281x_{74} -17.445312x_3 +0.105469x_6
          5.91796875
x_{11}
                              +73.515625x_2 +14.210937x_{74} -22.984375x_3 +0.101562x_6
x_{13}
           8.4765625
           8.2421875
                              +37.671875x_2 +13.320312x_{74} -21.828125x_3 +0.117187x_6
x_{14}
                              -2.953125x_2 +4.882812x_{74} -7.453125x_3 +0.054687x_6
           2.1796875
x_{28}
                              -53.585937x_2 +3.714844x_{74} -4.835937x_3 +0.066406x_6
           4.50390625
x_{16}
            3.828125
                              -54.21875x_2 +3.546875x_{74}
                                                             -5.21875x_3 +0.078125x_6
x_{10}
                              +19.304688x_2 +10.488281x_{74} -16.445312x_3 +0.105469x_6
           5.91796875
x_{18}
            5.59375
                               -35.0625x_2
                                              +6.65625x_{74}
                                                              -10.0625x_3
                                                                             +0.09375x_6
x_{19}
                                                             -4.835937x_3 +0.066406x_6
           4.50390625
                              -53.585938x_2 +3.714844x_{74}
x_{20}
                               -35.0625x_2
                                              +6.65625x_{74}
                                                              -10.0625x_3
            5.59375
                                                                             +0.09375x_6
x_{21}
           2.6484375
                              -23.265625x_2 +1.664062x_{74}
                                                             -1.765625x_3 +0.023437x_6
x_{22}
                               -34.0625x_2
                                                              -10.0625x_3
                                                                            +0.09375x_6
            5.59375
                                              +6.65625x_{74}
x_{23}
            4.828125
                              +1.78125x_2
                                             +7.546875x_{74}
                                                             -11.21875x_3 +0.078125x_6
x_{24}
                              -11.804687x_2 +12.261719x_{74} -19.054687x_3 +0.144531x_6
x_{17}
           7.33203125
            7.828125
                              +19.78125x_2 +10.546875x_{74} -15.21875x_3 +0.078125x_6
x_{26}
           5.73828125
                              +41.257813x_2 +8.605469x_{74} -12.992187x_3 +0.050781x_6
x_{12}
                              -11.171875x_2 + 12.429687x_{74} - 18.671875x_3 + 0.132812x_6
           8.0078125
x_{25}
                              -11.171875x_2 +12.429687x_{74} -18.671875x_3 +0.132812x_6
           8.0078125
x_{29}
           5.73828125
                              +40.257813x_2 +8.605469x_{74} -11.992187x_3 +0.050781x_6
x_{27}
           7.15234375
                              +9.148437x_2 +10.378906x_{74} -14.601562x_3 +0.089844x_6
x_{31}
            1.765625
                              +10.15625x_2
                                            +3.109375x_{74}
                                                             -3.84375x_3 +0.015625x_6
x_{32}
            4.828125
                               -8.21875x_2
                                             +7.546875x_{74} -11.21875x_3 +0.078125x_6
x_{33}
                                             +8.328125x_{74} -11.53125x_3 +0.046875x_6
            5.296875
                              +39.46875x_2
x_{34}
                                             +8.328125x_{74} -11.53125x_3 +0.046875x_6
            5.296875
                              +39.46875x_2
x_{35}
                              +10.148437x_2 +10.378906x_{74} -14.601562x_3 +0.089844x_6
x_{36}
           7.15234375
           2.97265625
                              +22.101563x_2 +5.496094x_{74} -8.148437x_3 +0.035156x_6
x_{37}
                              +39.46875x_2 +8.328125x_{74}
                                                             -11.53125x_3 +0.046875x_6
x_{38}
            5.296875
           2.97265625
                              +22.101562x_2 +5.496094x_{74} -8.148437x_3 +0.035156x_6
x_{39}
           7.15234375
                              +9.148437x_2 +10.378906x_{74} -14.601562x_3 +0.089844x_6
x_{40}
           2.97265625
                              +21.101562x_2 +5.496094x_{74} -8.148437x_3 +0.035156x_6
x_{41}
                              +26.515625x_2 +13.210937x_{74} -18.984375x_3 +0.101562x_6
           9.4765625
x_{42}
                              -53.585937x_2 +3.714844x_{74} -4.835937x_3 +0.066406x_6
x_{15}
           4.50390625
                              -52.953125x_2 +3.882812x_{74} -4.453125x_3 +0.054687x_6
           5.1796875
x_{43}
                              +9.13625x_2
            1.765625
                                             +3.109375x_{74}
                                                              -3.84375x_3 +0.015625x_6
x_{30}
                              -8.210937x_2 +1.277344x_{74} -0.460937x_3 +0.003906x_6
           1.44140625
x_{44}
          4.62109375
                              -51.164062x_2 +4.160156x_{74}
                                                             -4.914062x_3 +0.058594x_6
x_{47}
           6.1796875
                              -34.953125x_2 +5.882812x_{74} -6.453125x_3 +0.054687x_6
x_{48}
           1.6484375
                              -24.265625x_2 +1.664063x_{74}
                                                             -1.765625x_3 +0.023437x_6
x_{49}
           5.38671875
                              -42.007813x_2 +6.269531x_{74}
                                                             -7.757812x_3 +0.074219x_6
x_{50}
x_{51}
                              -31.164062x_2 +5.160156x_{74} -5.914062x_3 +0.058594x_6
           4.62109375
```

50 052125_m

19 0000102

4 459195~

10.054697~

5 1706975

```
1.55859375
                              -1.789063x_2
                                             -0.277344x_{74} -0.539063x_3 -0.003906x_6
x_4
x_{45}
            1.765625
                               +8.15625x_2
                                             +3.109375x_{74}
                                                             -2.84375x_3 +0.015625x_6
         183.77734375
                             -132.601563x_2 - 17.246094x_{74} + 107.648437x_3 - 1.285156x_6
x_7
                                             -0.109375x_{74}
                                                             +0.84375x_3 -0.015625x_6
            1.234375
                               -1.15625x_2
x_1
          88.66015625
                              -37.023437x_2 -4.691406x_{74} -100.273438x_3 +0.722656x_6
x_9
                              -54.851562x_2 +3.378906x_{74} -5.601562x_3 +0.089844x_6
          3.15234375
x_8
           8.4765625
                              +74.515625x_2 +14.210937x_{74} -23.984375x_3 +0.101562x_6
x_5
                             +20.304688x_2 +10.488281x_{74} -17.445312x_3 +0.105469x_6
          5.91796875
x_{11}
                             +73.515625x_2 +14.210937x_{74} -22.984375x_3 +0.101562x_6
x_{13}
           8.4765625
           8.2421875
                              +37.671875x_2 +13.320312x_{74} -21.828125x_3 +0.117187x_6
x_{14}
                              -2.953125x_2 +4.882812x_{74} -7.453125x_3 +0.054687x_6
           2.1796875
x_{28}
                              -53.585937x_2 +3.714844x_{74} -4.835937x_3 +0.066406x_6
           4.50390625
x_{16}
           3.828125
                              -54.21875x_2 +3.546875x_{74}
                                                             -5.21875x_3 +0.078125x_6
x_{10}
                              +19.304688x_2 +10.488281x_{74} -16.445312x_3 +0.105469x_6
           5.91796875
x_{18}
            5.59375
                               -35.0625x_2
                                              +6.65625x_{74}
                                                              -10.0625x_3
                                                                             +0.09375x_6
x_{19}
                                                             -4.835937x_3 +0.066406x_6
           4.50390625
                              -53.585938x_2 +3.714844x_{74}
x_{20}
                               -35.0625x_2
                                              +6.65625x_{74}
                                                              -10.0625x_3
            5.59375
                                                                             +0.09375x_6
x_{21}
           2.6484375
                              -23.265625x_2 +1.664062x_{74}
                                                             -1.765625x_3 +0.023437x_6
x_{22}
                               -34.0625x_2
                                                              -10.0625x_3
                                                                            +0.09375x_6
            5.59375
                                              +6.65625x_{74}
x_{23}
           4.828125
                              +1.78125x_2
                                             +7.546875x_{74}
                                                             -11.21875x_3 +0.078125x_6
x_{24}
                              -11.804687x_2 +12.261719x_{74} -19.054687x_3 +0.144531x_6
x_{17}
           7.33203125
           7.828125
                              +19.78125x_2 +10.546875x_{74} -15.21875x_3 +0.078125x_6
x_{26}
           5.73828125
                              +41.257813x_2 +8.605469x_{74} -12.992187x_3 +0.050781x_6
x_{12}
                              -11.171875x_2 + 12.429687x_{74} - 18.671875x_3 + 0.132812x_6
           8.0078125
x_{25}
                              -11.171875x_2 +12.429687x_{74} -18.671875x_3 +0.132812x_6
           8.0078125
x_{29}
           5.73828125
                              +40.257813x_2 +8.605469x_{74} -11.992187x_3 +0.050781x_6
x_{27}
           7.15234375
                              +9.148437x_2 +10.378906x_{74} -14.601562x_3 +0.089844x_6
x_{31}
           1.765625
                              +10.15625x_2
                                            +3.109375x_{74}
                                                             -3.84375x_3 +0.015625x_6
x_{32}
           4.828125
                               -8.21875x_2
                                             +7.546875x_{74} -11.21875x_3 +0.078125x_6
x_{33}
                                             +8.328125x_{74} -11.53125x_3 +0.046875x_6
           5.296875
                              +39.46875x_2
x_{34}
                                             +8.328125x_{74} -11.53125x_3 +0.046875x_6
           5.296875
                              +39.46875x_2
x_{35}
                              +10.148437x_2 +10.378906x_{74} -14.601562x_3 +0.089844x_6
x_{36}
           7.15234375
           2.97265625
                              +22.101563x_2 +5.496094x_{74} -8.148437x_3 +0.035156x_6
x_{37}
                              +39.46875x_2 +8.328125x_{74} -11.53125x_3 +0.046875x_6
x_{38}
           5.296875
           2.97265625
                              +22.101562x_2 +5.496094x_{74} -8.148437x_3 +0.035156x_6
x_{39}
           7.15234375
                              +9.148437x_2 +10.378906x_{74} -14.601562x_3 +0.089844x_6
x_{40}
           2.97265625
                              +21.101562x_2 +5.496094x_{74} -8.148437x_3 +0.035156x_6
x_{41}
                             +26.515625x_2 +13.210937x_{74} -18.984375x_3 +0.101562x_6
           9.4765625
x_{42}
                              -53.585937x_2 +3.714844x_{74} -4.835937x_3 +0.066406x_6
x_{15}
           4.50390625
                              -52.953125x_2 +3.882812x_{74} -4.453125x_3 +0.054687x_6
           5.1796875
x_{43}
                              +9.13625x_2
           1.765625
                                             +3.109375x_{74}
                                                             -3.84375x_3 +0.015625x_6
x_{30}
                              -8.210937x_2 +1.277344x_{74} -0.460937x_3 +0.003906x_6
           1.44140625
x_{44}
          4.62109375
                              -51.164062x_2 +4.160156x_{74}
                                                             -4.914062x_3 +0.058594x_6
x_{47}
           6.1796875
                              -34.953125x_2 +5.882812x_{74} -6.453125x_3 +0.054687x_6
x_{48}
                              -24.265625x_2 +1.664063x_{74}
                                                             -1.765625x_3 +0.023437x_6
x_{49}
           1.6484375
           5.38671875
                              -42.007813x_2 +6.269531x_{74}
                                                             -7.757812x_3 +0.074219x_6
x_{50}
                              -31.164062x_2 +5.160156x_{74} -5.914062x_3 +0.058594x_6
x_{51}
           4.62109375
```

50 052125_m

19 0000102

4 459195~

10.054697~

Forming the dual dictionary:

```
9
                                                                                                                                                                                                                                           -2y_{45}
                                                                                                                                                                                                                                                                                                          -74y_7 	 -y_2
                                                                                                                                                                                                                                                                                                                                                                                                                                                       +56y_{9}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          -1y_{74}
       y_1
                                                                                                                                         -0.071429y_4 + 0.071429y_{45} -1.5y_7 + 0.071429y_2 -5.071429y_9 -0.142857y_7
                                      0.571428571429
     y_{61}
                                                                                                                                          -0.142857y_4 + 11.142857y_{45} - 66y_7 + 0.142857y_2 + 21.857143y_9 + 2.714286y_7
                                        37.1428571429
       y_3
                                        39.2857142857
                                                                                                                                          +1.214286y_4 - 12.214286y_{45} + 37.5y_7 - 0.214286y_2 + 54.214286y_9 - 3.571429y_7 - 0.214286y_9 + 54.214286y_9 - 3.571429y_7 - 0.214286y_9 - 0.214286y_9
y_{110}
                                      -42.1428571429 -0.857143y_4 -6.142857y_{45} -71y_7 -0.142857y_2 -125.857143y_9 -0.714286y_7
```

9 95714995714

```
-x_1 +0.071429x_{61} +0.142857x_3 -1.214286x_{110}
          0.857142857143
x_4
x_{45}
          6.14285714286
                                  +2x_1 -0.071429x_{61} -11.142857x_3 +12.214286x_{110}
                 71
                                            +1.5x_{61}
                                                            +66x_{3}
x_7
          0.142857142857
                                  +x_1 -0.071429x_{61} -0.142857x_3 +0.214286x_{110}
x_2
          125.857142857
                                 -56x_1 + 5.071429x_{61} - 21.857143x_3 - 54.214286x_{110}
x_9
                                  +1x_1 +0.142857x_{61} -2.714286x_3 +3.571429x_{110}
          0.714285714286
x_{74}
          35.7142857143
                                  +7x_1 -2.857143x_{61} -64.714286x_3 +62.571429x_{110}
x_5
                 23
                                  +3x_{1}
                                            +0.5x_{61}
                                                             -4x_3
                                                                           +37.5x_{110}
x_{11}
           35.5714285714
                                  +7x_1 -2.785714x_{61} -63.571429x_3 +62.357143x_{110}
x_{13}
           30.5714285714
                                  +5x_1 -0.285714x_{61} -53.571429x_3 +50.857143x_{110}
x_{14}
                                  +1x_1 +1.142857x_{61} -15.714286x_3 +14.571429x_{110}
          8.71428571429
x_{28}
                                  -1x_1 + 4.642857x_{61} -1.714286x_3 -0.928571x_{110}
           3.71428571429
x_{16}
           3.57142857143
                                  -2x_1 + 4.714286x_{61} -0.571429x_3 -2.142857x_{110}
x_{10}
                                  +3x_1 +0.571429x_{61} -38.857143x_3 +37.285714x_{110}
          22.8571428571
x_{18}
           11.2857142857
                                  -x_1 +3.857143x_{61} -15.285714x_3 +12.428571x_{110}
x_{19}
           3.71428571429
                                  -1x_1 + 4.642857x_{61} -1.714286x_3 -0.928571x_{110}
x_{20}
                                  -x_1 +3.857143x_{61} -15.285714x_3 +12.428571x_{110}
          11.2857142857
x_{21}
                  2
                                  -x_1
                                             +2x_{61}
                                                             -1x_3
x_{22}
                                                                              -x_{110}
           11.4285714286
                                  -x_1 +3.785714x_{61} -15.428571x_3 +12.642857x_{110}
x_{23}
           15.4285714286
                                  +2x_1 +1.285714x_{61} -25.428571x_3 +24.142857x_{110}
x_{24}
x_{17}
           23.5714285714
                                  +2x_1 +3.214286x_{61} -38.571429x_3 +35.357143x_{110}
          23.1428571429
                                  +5x_1 +0.428571x_{61} -40.142857x_3 +38.714286x_{110}
x_{26}
                 21
                                            -1.5x_{61}
                                                            -38x_{3}
                                                                           +37.5x_{110}
x_{12}
           23.7142857143
                                  +3x_1 +3.142857x_{61} -39.714286x_3 +36.571429x_{110}
x_{25}
          23.7142857143
                                  +3x_1 +3.142857x_{61} -39.714286x_3 +36.571429x_{110}
x_{29}
           20.8571428571
                                  +5x_1 -1.428571x_{61} -36.857143x_3 +37.285714x_{110}
x_{27}
          21.5714285714
                                  +4x_1 +1.214286x_{61} -36.571429x_3 +35.357143x_{110}
x_{31}
           6.42857142857
                                  +2x_1 -0.214286x_{61} -12.428571x_3 +12.642857x_{110}
x_{32}
                 14
                                  +2x_1
                                             +2x_{61}
                                                             -24x_3
                                                                            +22x_{110}
x_{33}
           19.8571428571
                                  +5x_1 -1.428571x_{61} -35.857143x_3 +36.285714x_{110}
x_{34}
          19.8571428571
                                  +5x_1 -1.428571x_{61} -35.857143x_3 +36.285714x_{110}
x_{35}
                                  +4x_1 +1.142857x_{61} -36.714286x_3 +35.571429x_{110}
x_{36}
           21.7142857143
           12.2857142857
                                  +3x_1 -0.642857x_{61} -23.285714x_3 +22.928571x_{110}
x_{37}
x_{38}
           19.8571428571
                                  +5x_1 -1.428571x_{61} -35.857143x_3 +36.285714x_{110}
           12.2857142857
                                  +3x_1 -0.642857x_{61} -23.285714x_3 +22.928571x_{110}
x_{39}
           21.5714285714
                                  +4x_1 +1.214286x_{61} -36.571429x_3 +35.357143x_{110}
x_{40}
           12.1428571429
                                  +3x_1 -0.571429x_{61} -23.142857x_3 +22.714286x_{110}
x_{41}
                                  +6x_1 +0.428571x_{61} -50.142857x_3 +48.714286x_{110}
          29.1428571429
x_{42}
                                  -1x_1 + 4.642857x_{61} -1.714286x_3 -0.928571x_{110}
x_{15}
          3.71428571429
          3.85714285714
                                  -x_1 + 4.571429x_{61} - 2.857143x_3 + 0.285714x_{110}
x_{43}
          6.28571428571
                                  +2x_{1}^{27}-0.142857x_{61}-12.285714x_{3}+12.428571x_{110}
x_{30}
                                  +1x_1 +0.785714x_{61} -2.428571x_3 +2.642857x_{110}
           1.42857142857
x_{44}
                  4
                                            +4.5x_{61}
                                                             -4x_3
                                                                            +1.5x_{110}
x_{47}
          8.85714285714
                                  +2x_1 +3.571429x_{61} -12.857143x_3 +11.285714x_{110}
x_{48}
                                  -3x_1 + 4.785714x_{61} + 0.571429x_3 -3.357143x_{110}
x_8
           3.42857142857
                                  +1x_1 +4.214286x_{61} -12.571429x_3 +10.357143x_{110}
           8.57142857143
x_{50}
                                  +1x_1 +3.214286x_{61} -10.571429x_3 +9.357143x_{110}
x_{51}
           7.57142857143
```

± 4.571.490∞

 $9.957149_{\infty} + 0.995714_{\odot}$

9 9571/199571/

```
-x_1 +0.071429x_{61} +0.142857x_3 -1.214286x_{110}
          0.857142857143
x_4
x_{45}
          6.14285714286
                                  +2x_1 -0.071429x_{61} -11.142857x_3 +12.214286x_{110}
                 71
                                            +1.5x_{61}
                                                            +66x_{3}
x_7
          0.142857142857
                                  +x_1 -0.071429x_{61} -0.142857x_3 +0.214286x_{110}
x_2
          125.857142857
                                 -56x_1 + 5.071429x_{61} - 21.857143x_3 - 54.214286x_{110}
x_9
                                  +1x_1 +0.142857x_{61} -2.714286x_3 +3.571429x_{110}
          0.714285714286
x_{74}
          35.7142857143
                                  +7x_1 -2.857143x_{61} -64.714286x_3 +62.571429x_{110}
x_5
                 23
                                  +3x_{1}
                                            +0.5x_{61}
                                                             -4x_3
                                                                           +37.5x_{110}
x_{11}
           35.5714285714
                                  +7x_1 -2.785714x_{61} -63.571429x_3 +62.357143x_{110}
x_{13}
           30.5714285714
                                  +5x_1 -0.285714x_{61} -53.571429x_3 +50.857143x_{110}
x_{14}
                                  +1x_1 +1.142857x_{61} -15.714286x_3 +14.571429x_{110}
          8.71428571429
x_{28}
          3.71428571429
                                  -1x_1 + 4.642857x_{61} - 1.714286x_3 - 0.928571x_{110}
x_{16}
          3.57142857143
                                  -2x_1 + 4.714286x_{61} -0.571429x_3 -2.142857x_{110}
x_{10}
                                  +3x_1 +0.571429x_{61} -38.857143x_3 +37.285714x_{110}
          22.8571428571
x_{18}
           11.2857142857
                                  -x_1 +3.857143x_{61} -15.285714x_3 +12.428571x_{110}
x_{19}
           3.71428571429
                                  -1x_1 + 4.642857x_{61} -1.714286x_3 -0.928571x_{110}
x_{20}
                                  -x_1 +3.857143x_{61} -15.285714x_3 +12.428571x_{110}
           11.2857142857
x_{21}
x_{22}
                  2
                                  -x_1
                                             +2x_{61}
                                                             -1x_3
                                                                              -x_{110}
           11.4285714286
                                  -x_1 +3.785714x_{61} -15.428571x_3 +12.642857x_{110}
x_{23}
           15.4285714286
                                  +2x_1 +1.285714x_{61} -25.428571x_3 +24.142857x_{110}
x_{24}
x_{17}
           23.5714285714
                                  +2x_1 +3.214286x_{61} -38.571429x_3 +35.357143x_{110}
           23.1428571429
                                  +5x_1 +0.428571x_{61} -40.142857x_3 +38.714286x_{110}
x_{26}
                 21
                                            -1.5x_{61}
                                                            -38x_{3}
                                                                           +37.5x_{110}
x_{12}
          23.7142857143
                                  +3x_1 +3.142857x_{61} -39.714286x_3 +36.571429x_{110}
x_{25}
          23.7142857143
                                  +3x_1 +3.142857x_{61} -39.714286x_3 +36.571429x_{110}
x_{29}
           20.8571428571
                                  +5x_1 -1.428571x_{61} -36.857143x_3 +37.285714x_{110}
x_{27}
          21.5714285714
                                  +4x_1 +1.214286x_{61} -36.571429x_3 +35.357143x_{110}
x_{31}
           6.42857142857
                                  +2x_1 -0.214286x_{61} -12.428571x_3 +12.642857x_{110}
x_{32}
                 14
                                  +2x_1
                                             +2x_{61}
                                                             -24x_3
                                                                            +22x_{110}
x_{33}
           19.8571428571
                                  +5x_1 -1.428571x_{61} -35.857143x_3 +36.285714x_{110}
x_{34}
          19.8571428571
                                  +5x_1 -1.428571x_{61} -35.857143x_3 +36.285714x_{110}
x_{35}
                                  +4x_1 +1.142857x_{61} -36.714286x_3 +35.571429x_{110}
x_{36}
           21.7142857143
          12.2857142857
                                  +3x_1 -0.642857x_{61} -23.285714x_3 +22.928571x_{110}
x_{37}
x_{38}
           19.8571428571
                                  +5x_1 -1.428571x_{61} -35.857143x_3 +36.285714x_{110}
           12.2857142857
                                  +3x_1 -0.642857x_{61} -23.285714x_3 +22.928571x_{110}
x_{39}
          21.5714285714
                                  +4x_1 +1.214286x_{61} -36.571429x_3 +35.357143x_{110}
x_{40}
           12.1428571429
                                  +3x_1 -0.571429x_{61} -23.142857x_3 +22.714286x_{110}
x_{41}
                                  +6x_1 +0.428571x_{61} -50.142857x_3 +48.714286x_{110}
          29.1428571429
x_{42}
                                  -1x_1 + 4.642857x_{61} -1.714286x_3 -0.928571x_{110}
x_{15}
          3.71428571429
          3.85714285714
                                  -x_1 + 4.571429x_{61} - 2.857143x_3 + 0.285714x_{110}
x_{43}
          6.28571428571
                                  +2x_{1}^{28}-0.142857x_{61}-12.285714x_{3}+12.428571x_{110}
x_{30}
                                  +1x_1 +0.785714x_{61} -2.428571x_3 +2.642857x_{110}
           1.42857142857
x_{44}
                  4
                                  -x_1
                                            +4.5x_{61}
                                                             -4x_3
                                                                            +1.5x_{110}
x_{47}
          8.85714285714
                                  +2x_1 +3.571429x_{61} -12.857143x_3 +11.285714x_{110}
x_{48}
                                  -3x_1 + 4.785714x_{61} + 0.571429x_3 -3.357143x_{110}
x_8
          3.42857142857
                                  +1x_1 +4.214286x_{61} -12.571429x_3 +10.357143x_{110}
           8.57142857143
x_{50}
                                  +1x_1 +3.214286x_{61} -10.571429x_3 +9.357143x_{110}
x_{51}
           7.57142857143
```

1 4 571 490 m

 $9.957149_{\infty} + 0.995714_{\odot}$

Forming the dual dictionary:

primal	dictionary obtained:	
x_4	1	$-1x_1 +1x_{209} -x_3 -2x_{110}$
x_{45}	6	$+3x_1$ $-1x_{209}$ $-11x_3+13x_{110}$
x_7	74	$+53x_1 +21x_{209} +63x_3 -54x_{110}$
x_2	1.02279296144e - 14	$+1x_1$ $-1x_{209}$ $+x_3$ $+1x_{110}$
x_9	136	$-127x_1 + 71x_{209} - 32x_3 - 11x_{110}$
x_{74}	1	$-1x_1 + 2x_{209} - 3x_3 + 2x_{110}$
x_5	30	$+47x_1$ $-4x_{209}$ $-59x_3 + 94x_{110}$
x_{11}	24	$-4x_1 +7x_{209} -41x_3 +32x_{110}$
x_{13}	30	$+46x_1 -39x_{209} -58x_3 +93x_{110}$
x_{14}	30	$+9x_1$ $-4x_{209}$ $-53x_3 + 54x_{110}$
x_{28}	11	$-15x_1 + 16x_{209} - 18x_3 + 2x_{110}$
x_{16}	13	$-66x_1 + 65x_{209} - 11x_3 - 52x_{110}$
x_{10}	13	$-68x_1 + 66x_{209} - 1x_3 - 54x_{110}$
x_{18}	24	$-5x_1 + 8x_{209} - 4x_3 + 31x_{110}$
x_{19}	19	$-54x_1 + 54x_{209} - 23x_3 - 3x_{110}$
$\begin{vmatrix} x_{13} \\ x_{20} \end{vmatrix}$	13	$-66x_1 + 65x_{209} - 11x_3 - 52x_{110}$
$\begin{bmatrix} x_{20} \\ x_{21} \end{bmatrix}$	19	$-54x_1 + 54x_{209} - 23x_3 - 3x_{110}$
$\begin{bmatrix} x_{21} \\ x_{22} \end{bmatrix}$	6	$-28x_1 + 28x_{209} - 5x_3 - 22x_{110}$
$\begin{bmatrix} x_{23} \\ x_{23} \end{bmatrix}$	19	$-53x_1 + 53x_{209} - 23x_3 - 29x_{110}$
$\begin{bmatrix} x_{23} \\ x_{24} \end{bmatrix}$	18	$-16x_1 + 18x_{209} - 28x_3 + 1x_{110}$
$\begin{bmatrix} x_{17} \\ x_{17} \end{bmatrix}$	30	$-43x_1 + 45x_{209} - 45x_3 + x_{110}$
x_{26}	24	$-1x_1 + 6x_{209} - 41x_3 + 34x_{110}$
$\begin{vmatrix} x_{12} \end{vmatrix}$	18	$+26x_1$ $-21x_{209}$ $-35x_3$ $+54x_{110}$
x_{25}	30	$-41x_1 + 44x_{209} - 46x_3 + 2x_{110}$
x_{29}	30	$-41x_1 + 44x_{209} - 46x_3 + 2x_{110}$
x_{27}	18	$+25x_1$ $-2x_{209}$ $-34x_3 +53x_{110}$
x_{31}	24	$-13x_1 + 17x_{209} - 39x_3 + 22x_{110}$
x_{32}	6	$+5x_1$ $-3x_{209}$ $-12x_3+15x_{110}$
x_{33}	18	$-26x_1 + 28x_{209} - 28x_3 + x_{110}$
x_{34}	17	$+25x_1$ $-2x_{209}$ $-33x_3+52x_{110}$
x_{35}	17	$+25x_1$ $-2x_{209}$ $-33x_3+52x_{110}$
x_{36}	24	$-12x_1 + 16x_{209} - 39x_3 + 23x_{110}$
x_{37}	11	$+12x_1$ $-9x_{209}$ $-22x_3$ $+3x_{110}$
x_{38}	17	$+25x_1$ $-2x_{209}$ $-33x_3+52x_{110}$
x_{39}	11	$+12x_1$ $-9x_{209}$ $-22x_3$ $+3x_{110}$
x_{40}	24	$-13x_1 +17x_{209} -39x_3 +22x_{110}$
x_{41}	11	$+11x_1$ $-8x_{209}$ $-22x_3+29x_{110}$
x_{42}	30	$+x_1 +6x_{209} -51x_3 +44x_{110}$
x_{15}	13	$-66x_1 +65x_{209} -11x_3 -52x_{110}$
x_{43}	13	$-64x_1 +64x_{209} -12x_3 -5x_{110}$
x_{30}	6	$30+4x_1 -2x_{209} -12x_3 + 14x_{110}$
x_{44}	3	$-1x_1 +11x_{209} -4x_3 -6x_{110}$
x_{47}	13	$-63x_1 +63x_{209} -13x_3 -48x_{110}$
x_{48}	16	$-48x_1 +5x_{209} -2x_3 -28x_{110}$
x_8	13	$-7x_1 +67x_{209} -9x_3 -56x_{110}$
x_{50}	17	$-58x_1 + 59x_{209} - 21x_3 - 36x_{110}$
x_{51}	14	$-44x_1 + 45x_{209} - 17x_3 - 26x_{110}$
· · · ·	12	64x + 64x = 12x = 5x = 5

Done.

9 ilpTest9

Initial Dictionary

$$\begin{array}{c|cccc} x_1 & 1.2 & -3.1x_2 + 4.3x_3 - 0.5x_5 \\ x_4 & 1 & -1x_2 & +1x_3 & -1x_5 \\ x_6 & 2.5 & +1.3x_2 - 2.1x_3 & +1x_5 \\ \hline z & 0 & -1.2x_2 - 2.3x_3 - 2.1x_5 \end{array}$$

No initialization required \rightarrow Proceed to Optimize Final dictionary after first LP relaxation solve:

$$\begin{array}{c|ccccc} x_1 & 1.2 & -3.1x_2 + 4.3x_3 - 0.5x_5 \\ x_4 & 1 & -1x_2 & +1x_3 & -1x_5 \\ x_6 & 2.5 & +1.3x_2 - 2.1x_3 & +1x_5 \\ \hline z & 0 & -1.2x_2 - 2.3x_3 - 2.1x_5 \end{array}$$

After cutting plane is added

$$\begin{array}{c|ccccc} x_1 & 1.2 & -3.1x_2 + 4.3x_3 - 0.5x_5 \\ x_4 & 1 & -1x_2 & +1x_3 & -1x_5 \\ x_6 & 2.5 & +1.3x_2 - 2.1x_3 & +1x_5 \\ x_7 & -0.2 & +0.1x_2 + 0.7x_3 + 0.5x_5 \\ x_8 & -0.5 & +0.7x_2 + 0.1x_3 \\ \hline z & 0 & -1.2x_2 - 2.3x_3 - 2.1x_5 \\ \end{array}$$

Forming the dual dictionary:

```
0.0180722891566
                       +0.783133x_8 +0.144578x_1 +0.572289x_5
     0.530120481928
                       -0.361446x_8 + 0.240964x_1 - 0.879518x_5
x_4
     2.93975903614
                       -0.277108x_8 - 0.481928x_1 + 0.759036x_5
x_6
    0.213855421687
                       +0.933735x_8 +0.210843x_1 +0.105422x_5
x_3
                       +1.295181x_8 -0.03012x_1 -0.01506x_5
     0.683734939759
x_2
    -1.31234939759
                       -3.701807x_8 - 0.448795x_1 - 2.324398x_5
```

After cutting plane is added

```
0.0180722891566
x_7
                          +0.783133x_8 +0.144578x_1 +0.572289x_5
      0.530120481928
                          -0.361446x_8 + 0.240964x_1 - 0.879518x_5
x_4
       2.93975903614
                          -0.277108x_8 - 0.481928x_1 + 0.759036x_5
x_6
      0.213855421687
                          +0.933735x_8 +0.210843x_1 +0.105422x_5
x_3
      0.683734939759
                          +1.295181x_8 -0.03012x_1 -0.01506x_5
x_2
     -0.0180722891566
                          +0.216867x_8 +0.855422x_1 +0.427711x_5
x_9
                          +0.361446x_8 +0.759036x_1 +0.879518x_5
      -0.530120481928
x_{10}
     -0.939759036145
                          +0.277108x_8 +0.481928x_1 +0.240964x_5
x_{11}
                          +0.066265x_8 +0.789157x_1 +0.894578x_5
x_{12}
      -0.213855421687
                          +0.704819x_8 +0.03012x_1 +0.01506x_5
     -0.683734939759
x_{13}
      -1.31234939759
                          -3.701807x_8 - 0.448795x_1 - 2.324398x_5
 z
```

Forming the dual dictionary:

```
5.00909090909
                                                                                                                                                                                                                                                                                               -1.018182y_7 + 0.727273y_4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            y_{13}
                                                                                                                                                                                                                                                                                             -0.236364y_7 - 0.545455y_4 + 1y_6 - 0.363636y_3 + 0.181818y_2 - 2.127273y_1 - 1.8y_9 - 0.181818y_2 - 0.1818184y_2 - 0.18
                                                                0.618181818182
y_{11}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          -1y_{6}
                                                                                                                                              2.1
                                                                                                                                                                                                                                                                                                                                       -0.5y_7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   +1y_4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  -y_3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                +0.5y_1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             +y_2
      y_5
                                                                                                                                                                                                                                                                                               -0.936364y_7 - 0.545455y_4 - 2y_6 - 1.363636y_3 - 1.818182y_2 - 1.427273y_1 - 1.4y_9 - 1.818182y_2 - 1.427273y_1 - 1.4y_9 - 1.818182y_2 - 1.81818444y_2 - 1.8181844y_2 - 1.8181844y_2 - 1.818184y_2 - 1.818184y_2 - 1.818184y_2 - 1.818184y_2 
                                                                      5.31818181818
```

```
0.936363636364
                          +1.018182x_{13} +0.236364x_{11} +0.5x_5
x_7
      0.545454545455
                          -0.727273x_{13} + 0.545455x_{11} -1x_5
x_4
              2
                                              -1x_{11}
                                                           +1x_{5}
x_6
      1.36363636364
                          +1.181818x_{13} +0.363636x_{11} +x_5
x_3
      1.81818181818
                          +1.909091x_{13} - 0.181818x_{11}
x_2
      1.42727272727
                          -0.836364x_{13} + 2.127273x_{11} - 0.5x_5
x_1
             1.4
                             -0.4x_{13}
                                             +1.8x_{11}
x_9
                          -0.109091x_{13} + 1.581818x_{11} + 0.5x_5
      0.881818181818
x_{10}
      0.972727272727
                          -0.563636x_{13} + 1.672727x_{11} + 0.5x_5
x_{12}
                          +1.454545x_{13} -0.090909x_{11} -x_5
      0.909090909091
x_8
     -5.31818181818
                          -5.009091x_{13} - 0.618182x_{11} - 2.1x_5
```

After cutting plane is added

```
0.936363636364
                           +1.018182x_{13} +0.236364x_{11} +0.5x_5
x_7
x_4
       0.545454545455
                           -0.727273x_{13} + 0.545455x_{11} -1x_5
               2
                                                           +1x_{5}
                                               -1x_{11}
x_6
       1.36363636364
                           +1.181818x_{13} +0.363636x_{11} +x_5
x_3
                           +1.909091x_{13} - 0.181818x_{11} \quad -x_5
       1.818181818
x_2
                           -0.836364x_{13} + 2.127273x_{11} - 0.5x_5
       1.42727272727
x_1
              1.4
                               -0.4x_{13}
                                              +1.8x_{11}
x_9
                           -0.109091x_{13} + 1.581818x_{11} + 0.5x_5
       0.881818181818
x_{10}
       0.972727272727
                           -0.563636x_{13} + 1.672727x_{11} + 0.5x_5
x_{12}
                           +1.454545x_{13} -0.090909x_{11} -x_5
       0.909090909091
x_8
                           +0.981818x_{13}+0.763636x_{11}+0.5x_5
      -0.936363636364
x_{14}
      -0.5454545454545
                           +0.727273x_{13}+0.454545x_{11}+1x_{5}
x_{15}
      -0.363636363636
                           +0.818182x_{13}+0.636364x_{11}+1x_5
x_{16}
x_{17}
      -0.818181818182
                           +0.090909x_{13} +0.181818x_{11} +x_5
x_{18}
      -0.427272727273
                           +0.836364x_{13}+0.872727x_{11}+0.5x_5
             -0.4
                               +0.4x_{13}
                                              +0.2x_{11}
                                                           +1x_{5}
x_{19}
      -0.881818181818
                           +0.109091x_{13} +0.418182x_{11} +0.5x_5
x_{20}
      -0.972727272727
                           +0.563636x_{13}+0.327273x_{11}+0.5x_5
x_{21}
      -0.909090909091
                           +0.545455x_{13}+0.090909x_{11}+x_5
x_{22}
                           -5.009091x_{13} - 0.618182x_{11} - 2.1x_5
      -5.31818181818
```

Forming the dual dictionary:

The Final Dual Dictionary is:

	2.0	112 125 1245 1055
x_7	3.9	$+1.3x_{22} +3.4x_{17} +0.5x_6$
x_4	3.77475828373e - 15	$-1x_{22}$ $-2x_{17}$ $-1x_6$
x_5	2	$-1x_{22}$ $+6x_{17}$ $+1x_6$
x_3	4	$+2x_{22}$ $+1x_{17}$ $+x_6$
x_2	3	$+4x_{22}$ $-3x_{17}$
x_1	8.1	$-3.3x_{22} + 10.6x_{17} - 0.5x_6$
x_9	8.2	$-2.6x_{22} + 11.2x_{17} + x_6$
x_{10}	8.1	$-2.3x_{22} + 12.6x_{17} + 0.5x_6$
x_{12}	8.1	$-3.3x_{22} + 13.6x_{17} + 0.5x_6$
x_8	2	$+3x_{22}$ $-2x_{17}$
x_{11}	4	$-1x_{22}$ $+6x_{17}$ $-x_6$
x_{15}	4	$-x_{22}$ $+8x_{17}$ $+1x_6$
x_{16}	5	$-x_{22}$ $+9x_{17}$ $+1x_6$
x_{14}	4.1	$+0.7x_{22} +6.6x_{17} +0.5x_6$
x_{18}	4.9	$+0.3x_{22} +7.4x_{17} +0.5x_6$
x_{19}	2.8	$-0.4x_{22} +6.8x_{17} +1x_6$
x_{20}	1.9	$-0.7x_{22} +5.4x_{17} +0.5x_6$
x_{21}	1.9	$+0.3x_{22} +4.4x_{17} +0.5x_6$
x_{13}	1	$+2x_{22}$ $-1x_{17}$
\overline{z}	-17	$-7.3x_{22} - 11.3x_{17} - 2.1x_6$

x_7	3.9	$+1.3x_{22} +3.4x_{17} +0.5x_6$
x_4	3.77475828373e - 15	$-1x_{22}$ $-2x_{17}$ $-1x_6$
x_5	2	$-1x_{22}$ $+6x_{17}$ $+1x_6$
x_3	4	$+2x_{22}$ $+1x_{17}$ $+x_{6}$
x_2	3	$+4x_{22}$ $-3x_{17}$
x_1	8.1	$-3.3x_{22} + 10.6x_{17} - 0.5x_6$
x_9	8.2	$-2.6x_{22} + 11.2x_{17} + x_6$
x_{10}	8.1	$-2.3x_{22} + 12.6x_{17} + 0.5x_6$
x_{12}	8.1	$-3.3x_{22} + 13.6x_{17} + 0.5x_6$
x_8	$\overline{2}$	$+3x_{22}$ $-2x_{17}$
x_{11}	4	$-1x_{22} +6x_{17} -x_6$
x_{15}	4	$-x_{22}$ $+8x_{17}$ $+1x_6$
x_{16}	5	$-x_{22}$ $+9x_{17}$ $+1x_6$
x_{14}	4.1	$+0.7x_{22} +6.6x_{17} +0.5x_{6}$
x_{18}	4.9	$+0.3x_{22} +7.4x_{17} +0.5x_6$
x_{19}	2.8	$-0.4x_{22} +6.8x_{17} +1x_6$
x_{20}	1.9	$-0.7x_{22} +5.4x_{17} +0.5x_6$
x_{21}	1.9	$+0.3x_{22} +4.4x_{17} +0.5x_6$
x_{13}	1	$+2x_{22}$ $-1x_{17}$
x_{23}	-0.9	$+0.7x_{22} +0.6x_{17} +0.5x_6$
x_{24}	-0.1	$+0.3x_{22} +0.4x_{17} +0.5x_6$
x_{25}	-0.2	$+0.6x_{22} +0.8x_{17} +1x_6$
x_{26}	-0.1	$+0.3x_{22} +0.4x_{17} +0.5x_6$
x_{27}	-0.1	$+0.3x_{22} +0.4x_{17} +0.5x_6$
x_{28}	-0.1	$+0.3x_{22} +0.4x_{17} +0.5x_6$
x_{29}	-0.9	$+0.7x_{22} +0.6x_{17} +0.5x_6$
x_{30}	-0.8	$+0.4x_{22} +0.2x_{17} +x_6$
x_{31}	-0.9	$+0.7x_{22} +0.6x_{17} +0.5x_6$
x_{32}	-0.9	$+0.7x_{22} +0.6x_{17} +0.5x_6$
z	-17	$-7.3x_{22} - 11.3x_{17} - 2.1x_6$

Forming the dual dictionary:

Unbounded Dictionary! The Final Dual Dictionary is:

Dual is unbounded Primal is therefore infeasible

Problem is ILP infeasible Could not find an integer point Done.

10 ilpTest10

Initial Dictionary

 x_7 leaves

Problem is feasible Initialization phase yields a zero answer Final dictionary after first LP relaxation solve:

```
9.375
                -3.4625x_2
                             +5.2875x_3
                                           +1.375x_7
x_4
       6.3
               -3.328571x_2 + 4.328571x_3 + 1.285714x_7
x_5
      5.575
              -3.705357x_2 + 5.830357x_3 + 0.803571x_7
x_6
      0.75
              -0.267857x_2 + 0.517857x_3 + 0.178571x_7
x_1
      4.65
              +1.003571x_2 +0.246429x_3 +0.464286x_7
x_8
              -1.326786x_2 -3.248214x_3 +0.017857x_7
      3.775
x_9
     -0.375
               +0.4625x_2
                            +0.7125x_3
                                           +0.625x_7
x_{10}
      -0.3
              +0.328571x_2 +0.671429x_3 +0.714286x_7
x_{11}
     -0.575
              +0.705357x_2 +0.169643x_3 +0.196429x_7
x_{12}
      -0.75
              +0.267857x_2 +0.482143x_3 +0.821429x_7
x_{13}
     -0.65
              +0.996429x_2+0.753571x_3+0.535714x_7
x_{14}
     -0.775
              +0.326786x_2 +0.248214x_3 +0.982143x_7
x_{15}
      -0.45
              -1.739286x_2 -0.610714x_3 -0.107143x_7
```

Forming the dual dictionary:

x_4	13.4	$-8.4x_2$	$+4.1x_3$	$+7x_{12}$
x_5	10.0636363636	$-7.945455x_2$	$+3.218182x_3$	$+6.545455x_{12}$
x_6	7.927272727	$-6.590909x_2$	$+5.136364x_3$	$+4.090909x_{12}$
x_1	1.27272727273	$-0.909091x_2$	$+0.363636x_3$	$+0.909091x_{12}$
x_8	6.00909090909	$-0.663636x_2$	$-0.154545x_3$	$+2.363636x_{12}$
x_9	3.82727272727	$-1.390909x_2$	$-3.263636x_3$	$+0.090909x_{12}$
x_7	2.92727272727	$-3.590909x_2$	$-0.863636x_3$	$+5.090909x_{12}$
x_{11}	1.79090909091	$-2.236364x_2$	$+0.054545x_3$	$+3.636364x_{12}$
x_{10}	1.45454545455	$-1.781818x_2$	$+0.172727x_3$	$+3.181818x_{12}$
x_{13}	1.65454545455	$-2.681818x_2$	$-0.227273x_3$	$+4.181818x_{12}$
x_{14}	0.918181818182	$-0.927273x_2$	$+0.290909x_3$	$+2.727273x_{12}$
x_{15}	2.1	$-3.2x_2$	$-0.6x_3$	$+5x_{12}$
\overline{z}	-0.763636363636	$-1.354545x_2$	$-0.518182x_3$	$-0.545455x_{12}$

```
x_4
              13.4
                                -8.4x_2
                                              +4.1x_3
                                                             +7x_{12}
x_5
        10.0636363636
                             -7.945455x_2 + 3.218182x_3 + 6.545455x_{12}
        7.92727272727
                             -6.590909x_2 + 5.136364x_3 + 4.090909x_{12}
x_6
        1.27272727273
                             -0.909091x_2 + 0.363636x_3 + 0.909091x_{12}
x_1
                             -0.663636x_2 -0.154545x_3 +2.363636x_{12}
        6.00909090909
x_8
                             -1.390909x_2 -3.263636x_3 +0.090909x_{12}
        3.82727272727
x_9
                             -3.590909x_2 - 0.863636x_3 + 5.090909x_{12}
x_7
        2.92727272727
        1.79090909091
                             -2.236364x_2 + 0.054545x_3 + 3.636364x_{12}
x_{11}
        1.45454545455
                             -1.781818x_2 + 0.172727x_3 + 3.181818x_{12}
x_{10}
        1.65454545455
                             -2.681818x_2 -0.227273x_3 +4.181818x_{12}
x_{13}
        0.918181818182
                             -0.927273x_2 + 0.290909x_3 + 2.727273x_{12}
x_{14}
               2.1
                                -3.2x_2
                                              -0.6x_{3}
                                                             +5x_{12}
x_{15}
                                              +0.9x_3
              -0.4
                                +0.4x_2
                                                              +1x_{12}
x_{16}
      -0.063636363636364
                             +0.945455x_2 +0.781818x_3 +0.454545x_{12}
x_{17}
       -0.927272727273
                             +0.590909x_2 +0.863636x_3 +0.909091x_{12}
x_{18}
       -0.272727272727
                             +0.909091x_2 +0.636364x_3 +0.090909x_{12}
x_{19}
x_{20}
      -0.00909090909091
                             +0.663636x_2 +0.154545x_3 +0.636364x_{12}
       -0.827272727273
                             +0.390909x_2 +0.263636x_3 +0.909091x_{12}
x_{21}
                             +0.590909x_2 +0.863636x_3 +0.909091x_{12}
       -0.927272727273
x_{22}
                             +0.236364x_2 +0.945455x_3 +0.363636x_{12}
x_{23}
       -0.790909090909
       -0.454545454545
                             +0.781818x_2 +0.827273x_3 +0.818182x_{12}
x_{24}
       -0.654545454545
                             +0.681818x_2 +0.227273x_3 +0.818182x_{12}
x_{25}
                             +0.927273x_2 +0.709091x_3 +0.272727x_{12}
x_{26}
       -0.918181818182
              -0.1
                                +0.2x_2
                                              +0.6x_3
x_{27}
                                                             +1x_{12}
                             -1.354545x_2 -0.518182x_3 -0.545455x_{12}
       -0.763636363636
 z
```

Forming the dual dictionary:

```
x_4
       21.9714285714
                          -14.071429x_2 + 3.285714x_{26} + 6.714286x_{21}
       17.4238095238
                          -12.457143x_2 + 2.095238x_{26} + 6.571429x_{21}
x_5
       15.8507936508
                          -13.428571x_2 + 6.269841x_{26} + 2.619048x_{21}
x_6
       1.15873015873
                          -0.814286x_2 +0.968254x_{26} +0.809524x_{21}
x_{16}
       7.26666666667
                              -0.6x_2
                                          -1.333333x_{26}
                                                             +3x_{21}
x_8
                           -2.771429x_2 -3.714286x_{26} +6.714286x_{21}
       5.07142857143
x_7
                           -1.428571x_2 +0.15873x_{26} +0.952381x_{21}
x_1
       2.20634920635
x_{11}
       4.03650793651
                           -2.514286x_2 -1.587302x_{26} +4.47619x_{21}
       3.55238095238
                           -2.185714x_2 -1.190476x_{26} +3.857143x_{21}
x_{10}
                           -2.628571x_2 -2.285714x_{26} + 5.285714x_{21}
       3.92857142857
x_{13}
       2.86825396825
                           -1.457143x_2 -0.793651x_{26} +3.238095x_{21}
x_{14}
                           -2.714286x_2 -3.253968x_{26} +6.47619x_{21}
       4.46984126984
x_{15}
                                         -5.222222x_{26} + 1.666667x_{21}
      0.41111111111111
                              +2.8x_2
x_9
       1.04126984127
                           -0.085714x_2 +1.031746x_{26} +0.190476x_{21}
x_{17}
       1.06349206349
                           -1.285714x_2 +1.587302x_{26} -0.47619x_{21}
x_3
      0.538095238095
                           -0.571429x_2 +0.952381x_{26} +0.714286x_{21}
x_{18}
      0.538095238095
                           +0.428571x_2 -0.047619x_{26} +0.714286x_{21}
x_{20}
      0.601587301587
                           -0.057143x_2 -0.460317x_{26} + 1.238095x_{21}
x_{12}
                           -0.571429x_2 +0.952381x_{26} +0.714286x_{21}
      0.538095238095
x_{22}
                           +0.085714x_2 +0.968254x_{26} -0.190476x_{21}
x_{19}
       0.45873015873
                           -0.328571x_2 +0.936508x_{26} +0.619048x_{21}
       0.91746031746
x_{24}
     0.0793650793651
                          +0.342857x_2 -0.015873x_{26} +0.904762x_{21}
x_{25}
                                          +1.333333x_{26}
x_{23}
      0.4333333333333
      1.13968253968
                           -0.628571x_2 +0.492063x_{26} +0.952381x_{21}
x_{27}
                           -0.657143x_2 -0.571429x_{26} -0.428571x_{21}
      -1.64285714286
 z
```

```
21.9714285714
                            -14.071429x_2 + 3.285714x_{26} + 6.714286x_{21}
x_4
                            -12.457143x_2 + 2.095238x_{26} + 6.571429x_{21}
x_5
        17.4238095238
x_6
        15.8507936508
                            -13.428571x_2 + 6.269841x_{26} + 2.619048x_{21}
                             -0.814286x_2 +0.968254x_{26} +0.809524x_{21}
        1.15873015873
x_{16}
        7.26666666667
                                -0.6x_2
                                            -1.333333x_{26}
                                                                +3x_{21}
x_8
                             -2.771429x_2 -3.714286x_{26} +6.714286x_{21}
        5.07142857143
x_7
                             -1.428571x_2 +0.15873x_{26} +0.952381x_{21}
        2.20634920635
x_1
        4.03650793651
                             -2.514286x_2 -1.587302x_{26} +4.47619x_{21}
x_{11}
                             -2.185714x_2 -1.190476x_{26} +3.857143x_{21}
        3.55238095238
x_{10}
        3.92857142857
                             -2.628571x_2 -2.285714x_{26} + 5.285714x_{21}
x_{13}
                             -1.457143x_2 -0.793651x_{26} +3.238095x_{21}
        2.86825396825
x_{14}
        4.46984126984
                             -2.714286x_2 -3.253968x_{26} +6.47619x_{21}
x_{15}
       0.41111111111111
                                +2.8x_2
                                            -5.222222x_{26} + 1.666667x_{21}
x_9
                             -0.085714x_2 +1.031746x_{26} +0.190476x_{21}
        1.04126984127
x_{17}
        1.06349206349
                             -1.285714x_2 +1.587302x_{26} -0.47619x_{21}
x_3
x_{18}
       0.538095238095
                             -0.571429x_2 +0.952381x_{26} +0.714286x_{21}
x_{20}
       0.538095238095
                             +0.428571x_2 -0.047619x_{26} +0.714286x_{21}
       0.601587301587
                             -0.057143x_2 -0.460317x_{26} + 1.238095x_{21}
x_{12}
       0.538095238095
                             -0.571429x_2 +0.952381x_{26} +0.714286x_{21}
x_{22}
        0.45873015873
                             +0.085714x_2 +0.968254x_{26} -0.190476x_{21}
x_{19}
x_{24}
        0.91746031746
                             -0.328571x_2 +0.936508x_{26} +0.619048x_{21}
                             +0.342857x_2 -0.015873x_{26} +0.904762x_{21}
       0.0793650793651
x_{25}
       0.4333333333333
                                            +1.333333x_{26}
x_{23}
        1.13968253968
                             -0.628571x_2 +0.492063x_{26} +0.952381x_{21}
x_{27}
                             +0.071429x_2 +0.714286x_{26} +0.285714x_{21}
       -0.971428571429
x_{28}
       -0.42380952381
                             +0.457143x_2 +0.904762x_{26} +0.428571x_{21}
x_{29}
      -0.850793650794
                             +0.428571x_2 +0.730159x_{26} +0.380952x_{21}
x_{30}
       -0.15873015873
                             +0.814286x_2 +0.031746x_{26} +0.190476x_{21}
x_{31}
      -0.2666666666667
                                +0.6x_2
                                            +0.333333x_{26}
x_{32}
      -0.0714285714286
                             +0.771429x_2 +0.714286x_{26} +0.285714x_{21}
x_{33}
      -0.206349206349
                             +0.428571x_2 +0.84127x_{26} +0.047619x_{21}
x_{34}
                             +0.514286x_2 +0.587302x_{26} +0.52381x_{21}
x_{35}
      -0.0365079365079
      -0.552380952381
                             +0.185714x_2 +0.190476x_{26} +0.142857x_{21}
x_{36}
x_{37}
      -0.928571428571
                             +0.628571x_2 +0.285714x_{26} +0.714286x_{21}
      -0.868253968254
                             +0.457143x_2 +0.793651x_{26} +0.761905x_{21}
x_{38}
      -0.469841269841
                             +0.714286x_2 +0.253968x_{26} +0.52381x_{21}
x_{39}
                                            +0.222222x_{26}+0.333333x_{21}
      -0.4111111111111
                                +0.2x_2
x_{40}
      -0.0412698412698
                             +0.085714x_2 +0.968254x_{26} +0.809524x_{21}
x_{41}
                             +0.285714x_2 +0.412698x_{26} +0.47619x_{21}
x_{42}
      -0.0634920634921
x_{43}
      -0.538095238095
                             +0.571429x_2 +0.047619x_{26} +0.285714x_{21}
      -0.538095238095
                             +0.574429x_2 +0.047619x_{26} +0.285714x_{21}
x_{44}
      -0.601587301587
                             +0.057143x_2 +0.460317x_{26} +0.761905x_{21}
x_{45}
      -0.538095238095
                             +0.571429x_2 +0.047619x_{26} +0.285714x_{21}
x_{46}
                             +0.914286x_2 +0.031746x_{26} +0.190476x_{21}
       -0.45873015873
x_{47}
                             +0.328571x_2 +0.063492x_{26} +0.380952x_{21}
x_{48}
       -0.91746031746
      -0.0793650793651
                             +0.657143x_2 +0.015873x_{26} +0.095238x_{21}
x_{49}
x_{50}
      -0.4333333333333
                                 +1x_2
                                            +0.666667x_{26}
                                                                 +x_{21}
```

69957

10.507027~

0.120600520602

y_{32}	-1.02140518266e - 14	$+17y_{4}$	$+2y_{5}$	$-8.333333y_6$	$+0.333333y_{16}$	$+16y_{8}$	$+38y_{7}$	+3.333333
y_{36}	3	$-47y_{4}$	$-46y_{5}$	$-18.333333y_6$	$-5.666667y_{16}$	$-21y_{8}$	$-47y_{7}$	-6.666667
y_2	0.1	$+12.6y_4$	$+9y_{5}$	$+21.833333y_6$	$+1.666667y_{16}$	$-5.1y_{8}$	$-11.3y_7$	+0.666667
\overline{z}	3.3	$-43.4y_4$	$-37.5y_{5}$	$-28.2y_6$	$-4.2y_{16}$	$-14.6y_{8}$	$-20.9y_7$	$-5y_1$

x_4	43.4	$-17x_{32}$	$+47x_{36}$	$-12.6x_2$
x_5	37.5	$-2x_{32}$	$+46x_{36}$	$-9x_{2}$
x_6	28.2	$+8.333333x_{32}$	$+18.333333x_{36}$	$-21.833333x_2$
x_{16}	4.2	$-0.333333x_{32}$	$+5.666667x_{36}$	$-1.666667x_2$
x_8	14.6	$-16x_{32}$	$+21x_{36}$	$+5.1x_2$
x_7	20.9	$-38x_{32}$	$+47x_{36}$	$+11.3x_2$
x_1	5	$-3.333333x_{32}$	$+6.666667x_{36}$	$-0.666667x_2$
x_{11}	15.3	$-22.666667x_{32}$	$+31.333333x_{36}$	$+5.266667x_2$
x_{10}	13.4	$-19x_{32}$	$+27x_{36}$	$+4.2x_2$
x_{13}	16.9	$-28x_{32}$	$+37x_{36}$	$+7.3x_2$
x_{14}	11.3	$-15.3333333x_{32}$	$+22.666667x_{36}$	$+3.533333x_2$
x_{15}	20	$-35.666667x_{32}$	$+45.3333333x_{36}$	$+10.266667x_2$
x_{21}	2.8	$-4x_{32}$	$+7x_{36}$	$+1.1x_2$
x_{17}	2.4		$+1.333333x_{36}$	
x_3	1	$+6.666667x_{32}$	$-3.333333x_{36}$	$-4.666667x_2$
x_{18}	3.3	$-x_{32}$		
x_{20}	2.5		$+5x_{36}$	
x_{12}	3.7		$+8.666667x_{36}$	-
x_{22}	3.3	$-x_{32}$		
x_{19}	0.7			$-1.866667x_2$
x_{24}	3.4		$+4.3333333x_{36}$	$-1.333333x_2$
x_{25}	2.6		$+6.333333x_{36}$	$+1.366667x_2$
x_{23}	1.5	$+4x_{32}$		$-3.4x_2$
x_{27}	4.2		$+6.666667x_{36}$	$-0.466667x_2$
x_{26}	0.8	_	$-x_{36}$	-
x_{29}	1.5	$+1x_{32}$		
x_{30}	0.8	-	$+2.666667x_{36}$	
x_{31}	0.4	_	$+1.333333x_{36}$	$+0.966667x_2$
x_9	0.9		$+11.666667x_{36}$	=
x_{33}	1.3		$+2x_{36}$	
x_{34}	0.6	-	$+0.333333x_{36}$	
x_{35}	1.9		$+3.666667x_{36}$	
x_{28}	0.4		$+2x_{36}$	
x_{37}	1.3	$-2x_{32}$	$+5x_{36}$	$+0.9x_2$
x_{38}	1.9	$-0.666667x_{32}$	$+5.3333333x_{36}$	$-0.133333x_2$
x_{39}	1.2	$-1.3333333x_{32}$	$+3.666667x_{36}$	$+0.833333x_2$
x_{40}	0.7	$-0.666667x_{32}$	$+2.333333x_{36}$	$+0.166667x_2$
x_{41}	3	$-0.3333333x_{32}$	$+5.666667x_{36}$	$-0.766667x_2$
x_{42}	1.6	$-0.666667x_{32}$	$+3.333333x_{36}$	$+0.066667x_2$
x_{43}	0.3	$-1x_{32}$	$+2x_{36}$	$+0.8x_2$
x_{44}	0.3	$-1x_{32}^{32}$	$+2x_{36}$	$+0.8x_{2}$
x_{45}	1.9	$-1.666667x_{32}$	$+5.3333333x_{36}$	$+0.066667x_2$
x_{46}	0.3	$-1x_{32}$	$+2x_{36}$	$+0.8x_2$
x_{47}	0.1	$-0.666667x_{32}$	$+1.3333333x_{36}$	$+1.066667x_2$
$\begin{bmatrix} x_{48} \\ x_{48} \end{bmatrix}$	0.2	$-1.3333333x_{32}$	$+2.666667x_{36}$	$+0.6333333x_2$
$\begin{bmatrix} x_{49} \\ x_{49} \end{bmatrix}$	0.2	$-0.3333333x_{32}$	$+0.666667x_{36}$	$+0.7333333x_2$
- 1	0.099999999999	$+2x_{32}$	$-x_{36}$	$-0.2x_2$
<u>~-</u> .	0.4	+ 1 222222 <i>m</i>	⊤U 333333 [∞]	0.2333332

Aiter	utting plane is added			
x_4	43.4	$-17x_{32}$	$+47x_{36}$	$-12.6x_2$
x_5	37.5	$-2x_{32}$	$+46x_{36}$	$-9x_{2}$
x_6	28.2	$+8.3333333x_{32}$	$+18.333333x_{36}$	$-21.833333x_2\\$
x_{16}	4.2	$-0.3333333x_{32}$	$+5.666667x_{36}$	$-1.666667x_2$
x_8	14.6	$-16x_{32}$	$+21x_{36}$	$+5.1x_2$
x_7	20.9	$-38x_{32}$	$+47x_{36}$	$+11.3x_2$
x_1	5	$-3.3333333x_{32}$	$+6.666667x_{36}$	$-0.666667x_2$
x_{11}	15.3	$-22.666667x_{32}$	$+31.333333x_{36}$	$+5.266667x_2$
x_{10}	13.4	$-19x_{32}$	$+27x_{36}$	$+4.2x_2$
x_{13}	16.9	$-28x_{32}$	$+37x_{36}$	$+7.3x_2$
x_{14}	11.3	$-15.333333x_{32}$	$+22.666667x_{36}$	$+3.5333333x_2$
x_{15}	20	$-35.666667x_{32}$	$+45.3333333x_{36}$	$+10.266667x_2$
x_{21}	2.8	$-4x_{32}$	$+7x_{36}$	$+1.1x_2$
x_{17}	2.4	$+2.3333333x_{32}$	$+1.3333333x_{36}$	$-1.733333x_2$
x_3	1	$+6.666667x_{32}$	$-3.333333x_{36}$	$-4.666667x_2$
x_{18}	3.3	$-x_{32}$	$+5x_{36}$	$-1.5x_2$
x_{20}	2.5	$-3x_{32}$	$+5x_{36}$	$+1.3x_2$
x_{12}	3.7	$-6.333333x_{32}$	$+8.666667x_{36}$	$+2.133333x_2$
x_{22}	3.3	$-x_{32}$	$+5x_{36}$	$-1.5x_2$
x_{19}	0.7	$+3.666667x_{32}$	$-1.333333x_{36}$	$-1.866667x_2$
x_{24}	3.4	$+0.3333333x_{32}$	$+4.3333333x_{36}$	$-1.333333x_2$
x_{25}	2.6	$-3.666667x_{32}$	$+6.3333333x_{36}$	$+1.366667x_2$
x_{23}	1.5	$+4x_{32}$	$-x_{36}$	$-3.4x_2$
x_{27}	4.2	$-2.333333x_{32}$	$+6.666667x_{36}$	$-0.466667x_2$
x_{26}	0.8	$+3x_{32}$	$-x_{36}$	$-1.8x_2$
x_{29}	1.5	$+1x_{32}$	$+3x_{36}$	$-0.7x_2$
x_{30}	0.8	$+0.666667x_{32}$	$+2.666667x_{36}$	$-0.466667x_2$
x_{31}	0.4	$-0.666667x_{32}$	$+1.3333333x_{36}$	$+0.966667x_2$
x_9	0.9	$-22.333333x_{32}$	$+11.666667x_{36}$	$+14.033333x_2$
x_{33}	1.3	$+1x_{32}$	$+2x_{36}$	$-0.2x_2$
x_{34}	0.6	$+2.3333333x_{32}$	$+0.333333x_{36}$	$-1.033333x_2$
x_{35}	1.9	$-0.333333x_{32}$	$+3.666667x_{36}$	$+0.033333x_2$
x_{28}	0.4	$+1x_{32}$	$+2x_{36}$	$-0.9x_2$
x_{37}	1.3	$-2x_{32}$	$+5x_{36}$	$+0.9x_2$
x_{38}	1.9	$-0.666667x_{32}$	$+5.3333333x_{36}$	$-0.133333x_2$
x_{39}	1.2	$-1.333333x_{32}$	$+3.666667x_{36}$	$+0.833333x_2$
x_{40}	0.7	$-0.666667x_{32}$	$+2.333333x_{36}$	$+0.166667x_2$
x_{41}	3	$-0.333333x_{32}$	$+5.666667x_{36}$	$-0.766667x_2$
x_{42}	1.6	$-0.666667x_{32}$	$+3.333333x_{36}$	$+0.066667x_2$
x_{43}	0.3	$-1x_{32}$	$+2x_{36}$	$+0.8x_2$
x_{44}	0.3	$-1x_{32}^{44}$	$+2x_{36}$	$+0.8x_2$
x_{45}	1.9	$-1.666667x_{32}$	$+5.3333333x_{36}$	$+0.066667x_2$
x_{46}	0.3	$-1x_{32}$	$+2x_{36}$	$+0.8x_2$
x_{47}	0.1	$-0.666667x_{32}$	$+1.333333x_{36}$	$+1.066667x_2$
x_{48}	0.2	$-1.333333x_{32}$	$+2.666667x_{36}$	$+0.633333x_2$
x_{49}	0.2	$-0.333333x_{32}$	$+0.666667x_{36}$	$+0.733333x_2$
x_{50}	0.0999999999999	$+2x_{32}$	$-x_{36}$	$-0.2x_2$
œ	0.4	$\pm 1.222222_{max}$	$\pm 0.333332x_{res}$	$0.033333m^2$

y_{32}	-1.02140518266e - 14	$+17y_{4}$	$+2y_{5}$	$-8.333333y_6$	$+0.333333y_{16}$	$+16y_{8}$	$+38y_{7}$	+3.333333
y_{36}	3	$-47y_{4}$	$-46y_{5}$	$-18.333333y_6$	$-5.666667y_{16}$	$-21y_{8}$	$-47y_{7}$	-6.666667
y_2	0.1	$+12.6y_4$	$+9y_{5}$	$+21.833333y_6$	$+1.666667y_{16}$	$-5.1y_{8}$	$-11.3y_7$	+0.666667
z	3.3	$-43.4y_4$	$-37.5y_5$	$-28.2y_{6}$	$-4.2y_{16}$	$-14.6y_{8}$	$-20.9y_7$	$-5y_1$

y_{82}	2.74025289779	$+0.771075y_4 +0.026344y_1 -0.026344y_1 -0.0026344y_1 -0.00264y_1 -0.00$	$-0.961538y_3$	$-2.270021y_{16} - 1.08$	$1665y_8 + 1.43098$
y_6	0.00885142255005	$-0.862381y_4 - 0.077977y_1 - 0.0000000000000000000000000000000000$	$-0.153846y_3$	$-0.100738y_{16} + 0.04$	$1728y_8 - 0.715701$
y_{13}	0.00263435194942	$-0.863804y_4 - 0.142255y_1 - 0.0000000000000000000000000000000000$	$+0.192308y_3$	$-0.041886y_{16} -0.55$	$9009y_8 - 0.927292$
\overline{z}	3.82794520548	$-4.251233y_4 - 0.389041y_1$	$-0.2y_3$	$-1.332329y_{16} -6.65$	$3973y_8 - 1.216712$

1 65616420256

```
4.25123287671
                           -0.771075x_{82} + 0.862381x_6 + 0.863804x_{13}
x_4
       0.38904109589
x_1
                           -0.026344x_{82} + 0.077977x_6 + 0.142255x_{13}
             0.2
                          +0.961538x_{82} +0.153846x_6 -0.192308x_{13}
x_3
       1.33232876712
                          +2.270021x_{82} +0.100738x_6 +0.041886x_{13}
x_{16}
       6.65397260274
                           +1.081665x_{82} -0.041728x_6 +0.559009x_{13}
x_8
       1.21671232877
                           -1.43098x_{82} +0.715701x_6 +0.927292x_{13}
x_5
                          +1.158325x_{82} -0.008641x_6 +0.045047x_{13}
      0.0298630136986
x_{48}
      0.580547945205
                          +0.366702x_{82} +0.034563x_6 +0.81981x_{13}
x_{11}
                          +0.668335x_{82} +0.041728x_6 +0.690991x_{13}
x_{10}
       0.74602739726
x_7
      0.189041095891
                           -0.987882x_{82} -0.075869x_6 +1.334563x_{13}
       1.45561643836
                          +1.489463x_{82} +0.031191x_6 +0.556902x_{13}
x_{14}
      0.0682191780822
                           -0.307165x_{82} -0.05079x_6 +1.258693x_{13}
x_{15}
      0.687397260274
                          +1.565859x_{82} +0.005058x_6 +0.144362x_{13}
x_{21}
                          +2.381981x_{82} +0.069336x_6 -0.062698x_{13}
       2.21890410959
x_{17}
x_{32}
       1.23917808219
                          +1.488409x_{82} -0.00569x_6 -0.037408x_{13}
       1.07945205479
                          +2.402529x_{82} +0.088514x_6 +0.026344x_{13}
x_{18}
       1.77068493151
                          +1.573762x_{82} -0.018335x_6 +0.101686x_{13}
x_{20}
      0.808219178082
                          +0.885142x_{82} -0.020021x_6 +0.220232x_{13}
x_{12}
       1.07945205479
                          +2.402529x_{82} +0.088514x_6 +0.026344x_{13}
x_{22}
       1.61917808219
                          +1.873024x_{82} +0.055848x_6 -0.114331x_{13}
x_{19}
                          +2.535037x_{82} +0.076291x_6 +0.010801x_{13}
x_{24}
       1.82657534247
                           +1.82824x_{82} -0.011591x_6 +0.127503x_{13}
       1.32054794521
x_{25}
      0.131780821918
                          +1.537935x_{82} +0.127713x_6 -0.104847x_{13}
x_{23}
                          +1.721812x_{82} +0.063435x_6 +0.102213x_{13}
        1.2002739726
x_{27}
       1.16904109589
                          +2.127503x_{82} +0.062592x_6 -0.088514x_{13}
x_{26}
       1.77890410959
                          +3.189673x_{82} +0.038567x_6 -0.024236x_{13}
x_{29}
       1.06191780822
                          +2.706533x_{82} +0.028662x_6 -0.015279x_{13}
x_{30}
       1.52410958904
                           +1.42334x_{82} -0.033087x_6 +0.013962x_{13}
x_{31}
                           -4.864067x_{82} -0.44236x_{6} +0.665964x_{13}
      0.660547945206
x_9
                          +2.968915x_{82} +0.012013x_6 -0.032139x_{13}
       2.39506849315
x_{33}
       1.60712328767
                          +2.420969x_{82} +0.03393x_6 -0.073235x_{13}
x_{34}
                          +2.737619x_{82} +0.016649x_{6} +0.01686x_{13}
       1.96684931507
x_{35}
       0.11397260274
                          +0.870126x_{82} +0.004426x_6 +0.001317x_{13}
x_{36}
       1.06575342466
                          +2.542677x_{82} -0.006322x_6 +0.069547x_{13}
x_{37}
       1.43369863014
                          +3.475237x_{82} +0.033298x_6 +0.03372x_{13}
x_{38}
       1.51589041096
                          +2.288198x_{82} -0.013066x_6 +0.04373x_{13}
x_{39}
      0.449863013699
                          +1.254478x_{82} +0.006744x_6 +0.025817x_{13}
x_{40}
                          +3.438883x_{82} +0.060906x_6 +0.030032x_{13}
       1.80657534247
x_{41}
                           +1.994731x_{82} +0.015595x_6 +0.028451x_{13}
x_{42}
       1.27780821918
                           +1.290832x_{82} -0.020864x_6 +0.029505x_{13}
x_{43}
       0.77698630137
       0.77698630137
                          +1.290862x_{82} -0.020864x_6 +0.029505x_{13}
x_{44}
      0.566575342466
                          +2.246575x_{82} +0.030137x_6 +0.068493x_{13}
x_{45}
       0.77698630137
                          +1.290832x_{82} -0.020864x_6 +0.029505x_{13}
x_{46}
                           +1.553214x_{82} -0.037513x_6 +0.012645x_{13}
       1.4101369863
x_{47}
                          +0.909115x_{82} -0.03098x_6 -0.00922x_{13}
      0.402191780822
x_{57}
       1.22712328767
                          +1.036354x_{82} -0.027608x_6 +0.003688x_{13}
x_{49}
                          +2.717071x_{82} -0.002529x_6 -0.072181x_{13}
x_{50}
       2.20630136986
```

 $\pm 1.071540_{\infty} \pm 0.004915_{\infty}$

```
4.25123287671
                             -0.771075x_{82} + 0.862381x_6 + 0.863804x_{13}
x_4
        0.38904109589
                             -0.026344x_{82} + 0.077977x_6 + 0.142255x_{13}
x_1
               0.2
                             +0.961538x_{82} +0.153846x_6 -0.192308x_{13}
x_3
                             +2.270021x_{82} +0.100738x_6 +0.041886x_{13}
        1.33232876712
x_{16}
        6.65397260274
                             +1.081665x_{82} -0.041728x_6 +0.559009x_{13}
x_8
         1.21671232877
                              -1.43098x_{82} +0.715701x_6 +0.927292x_{13}
x_5
                             +1.158325x_{82} -0.008641x_6 +0.045047x_{13}
       0.0298630136986
x_{48}
                             +0.366702x_{82} +0.034563x_6 +0.81981x_{13}
        0.580547945205
x_{11}
                             +0.668335x_{82} +0.041728x_6 +0.690991x_{13}
        0.74602739726
x_{10}
        0.189041095891
                             -0.987882x_{82} -0.075869x_6 +1.334563x_{13}
x_7
                             +1.489463x_{82} +0.031191x_6 +0.556902x_{13}
        1.45561643836
x_{14}
       0.0682191780822
                             -0.307165x_{82} -0.05079x_6 +1.258693x_{13}
x_{15}
        0.687397260274
                             +1.565859x_{82} +0.005058x_6 +0.144362x_{13}
x_{21}
                             +2.381981x_{82} +0.069336x_6 -0.062698x_{13}
        2.21890410959
x_{17}
        1.23917808219
                             +1.488409x_{82} -0.00569x_6 -0.037408x_{13}
x_{32}
                             +2.402529x_{82} +0.088514x_6 +0.026344x_{13}
        1.07945205479
x_{18}
                             +1.573762x_{82} -0.018335x_6 +0.101686x_{13}
        1.77068493151
x_{20}
        0.808219178082
                             +0.885142x_{82} -0.020021x_6 +0.220232x_{13}
x_{12}
        1.07945205479
                             +2.402529x_{82} +0.088514x_6 +0.026344x_{13}
x_{22}
        1.61917808219
                             +1.873024x_{82} +0.055848x_6 -0.114331x_{13}
x_{19}
                             +2.535037x_{82} +0.076291x_6 +0.010801x_{13}
x_{24}
        1.82657534247
                             +1.82824x_{82} -0.011591x_6 +0.127503x_{13}
        1.32054794521
x_{25}
        0.131780821918
                             +1.537935x_{82} +0.127713x_6 -0.104847x_{13}
x_{23}
                             +1.721812x_{82} +0.063435x_6 +0.102213x_{13}
         1.2002739726
x_{27}
                             +2.127503x_{82} +0.062592x_6 -0.088514x_{13}
         1.16904109589
x_{26}
         1.77890410959
                             +3.189673x_{82} +0.038567x_6 -0.024236x_{13}
x_{29}
        1.06191780822
                             +2.706533x_{82} +0.028662x_6 -0.015279x_{13}
x_{30}
        1.52410958904
                              +1.42334x_{82} -0.033087x_6 +0.013962x_{13}
x_{31}
                             -4.864067x_{82} -0.44236x_6 +0.665964x_{13}
        0.660547945206
x_9
                             +2.968915x_{82} +0.012013x_6 -0.032139x_{13}
        2.39506849315
x_{33}
        1.60712328767
                             +2.420969x_{82} +0.03393x_6 -0.073235x_{13}
x_{34}
                             +2.737619x_{82} +0.016649x_6 +0.01686x_{13}
x_{35}
         1.96684931507
        0.11397260274
                             +0.870126x_{82} +0.004426x_6 +0.001317x_{13}
x_{36}
                             +2.542677x_{82} -0.006322x_6 +0.069547x_{13}
        1.06575342466
x_{37}
        1.43369863014
                             +3.475237x_{82} +0.033298x_6 +0.03372x_{13}
x_{38}
        1.51589041096
                             +2.288198x_{82} -0.013066x_6 +0.04373x_{13}
x_{39}
        0.449863013699
                             +1.254478x_{82} +0.006744x_6 +0.025817x_{13}
x_{40}
                             +3.438883x_{82} +0.060906x_6 +0.030032x_{13}
        1.80657534247
x_{41}
                             +1.994731x_{82} +0.015595x_6 +0.028451x_{13}
x_{42}
        1.27780821918
                             +1.290832x_{82} -0.020864x_6 +0.029505x_{13}
        0.77698630137
x_{43}
        0.77698630137
                             +1.29 832x_{82} -0.020864x_6 +0.029505x_{13}
x_{44}
                             +2.246575x_{82} +0.030137x_6 +0.068493x_{13}
        0.566575342466
x_{45}
        0.77698630137
                             +1.290832x_{82} -0.020864x_6 +0.029505x_{13}
x_{46}
                             +1.553214x_{82} -0.037513x_6 +0.012645x_{13}
         1.4101369863
x_{47}
                             +0.909115x_{82} -0.03098x_6 -0.00922x_{13}
        0.402191780822
x_{57}
        1.22712328767
                             +1.036354x_{82} -0.027608x_6 +0.003688x_{13}
x_{49}
x_{50}
                             +2.717071x_{82} -0.002529x_6 -0.072181x_{13}
        2.20630136986
         1 65616499956
                              \pm 1.071540_{\infty} \pm 0.004215_{\infty}
```

71111101	arctionary obtained.	
x_4	41.925	$-26.25x_{87} + 1.3x_3 + 38.5x_{187}$
x_1	5.25	$-2.5x_{87}$ $-x_3$ $+5x_{187}$
x_6	22.075	$-23.75x_{87} + 3.5x_3 + 22.5x_{187}$
x_{16}	6.075	$+4.25x_{87} +0.5x_3 +5.5x_{187}$
x_8	18.9	$+2x_{87}$ $-1.1x_3$ $+13x_{187}$
x_5	36.6	$-25x_{87}$ $+0.6x_3$ $+36x_{187}$
x_{48}	1.65	$+3.5x_{87}$ $-x_3$ $+2x_{187}$
x_{11}	19.8	$-3x_{87}$ $-1.4x_3$ $+2x_{187}$
x_{10}	17.475	$-1.75x_{87}$ $-1.1x_3 + 17.5x_{187}$
x_7	27.45	$-6.5x_{87}$ $-2.9x_3$ $+28x_{187}$
x_{14}	15.55	$+1.5x_{87}$ $-0.8x_3$ $+15x_{187}$
x_{15}	26.675	$-4.75x_{87}$ $-2.6x_3 + 27.5x_{187}$
x_{21}	5.1	$+4x_{87}$ $-0.1x_3$ $+5x_{187}$
x_{17}	4.025	$+5.75x_{87} +0.6x_3 +2.5x_{187}$
x_{32}	1.325	$+4.75x_{87} +0.2x_3 +0.5x_{187} +0.5x_{187}$
	5.3	$+5x_{87}$ $+0.5x_3$ $+5x_{187}$
x_{18}	4.725	$+4.75x_{87} -0.1x_3 +3.5x_{187} +0.00x_3 +3.5x_{187}$
x_{20}	5.875	$+2.25x_{87} -0.4x_3 +5.5x_{187} +2.25x_{87} -0.4x_3 +5.5x_{187}$
x_{12}	5.3	$+5x_{87}$ $+0.5x_3$ $+5x_{187}$
x_{22}	1.625	$+3x_{87} +0.5x_3 +3x_{187} +4.75x_{87} +0.6x_3 +0.5x_{187}$
x_{19}		
x_{24}	5.525	$+5.75x_{87} +0.5x_3 +4.5x_{187}$
x_{25}	5.175	$+5.25x_{87} -0.1x_3 +4.5x_{187}$
x_{23}	1.7	$+2x_{87}$ $+0.8x_3$ $+2x_{187}$
x_{27}	6.075	$+3.25x_{87} +0.2x_3 +5.5x_{187}$
x_{26}	2.075	$+5.25x_{87} +0.6x_3 +1.5x_{187}$
x_{29}	4.325	$+8.75x_{87} +0.5x_3 +3.5x_{187}$
x_{30}	3.25	$+7.5x_{87} +0.4x_3 +3x_{187}$
x_{31}	2.1	$+5x_{87}$ $-x_3$ $+1x_{187}$
x_{110}	1.075	$+1.25x_{87}$ $-x_3$ $+1.5x_{187}$
x_{33}	4.025	$+8.75x_{87} +0.4x_3 +2.5x_{187}$
x_{34}	2.425	$+6.75x_{87} +0.5x_3 +1.5x_{187}$
x_{35}	4.625	$+7.75x_{87} +0.3x_3 +3.5x_{187}$
x_{36}	0.85	$+2.5x_{87} +0.1x_3 +1x_{187}$
x_{37}	4.25	$+7.5x_{87} +0.1x_3 +4x_{187}$
x_{38}	5.35	$+9.5x_{87} +0.4x_3 +5x_{187}$
x_{39}	3.8	$+7x_{87}$ $+0.1x_3$ $+3x_{187}$
x_{40}	2.05	$+3.5x_{87} +0.1x_3 +2x_{187}$
x_{41}	6.225	$+8.75x_{87} +0.5x_3 +5.5x_{187}$
x_{42}	3.65	$+5.5x_{87} +0.2x_3 +3x_{187}$
x_{43}	1.875	$+4.25x_{87}$ $-x_3$ $+1.5x_{187}$
x_{44}	1.875	$49 + 4.25x_{87} - x_3 + 1.5x_{187}$
x_{45}	4.325	$+5.75x_{87} +0.2x_3 +4.5x_{187}$
x_{46}	1.875	$+4.25x_{87}$ $-x_3$ $+1.5x_{187}$
x_{47}	1.95	$+5.5x_{87}$ $-x_3$ $+1x_{187}$
x_{57}	0.15	$+3.5x_{87}$ $+x_3$ $+x_{187}$
x_{49}	1.425	$+3.75x_{87}$ $-x_3$ $+0.5x_{187}$
x_{50}	2.45	$+8.5x_{87}$ $+0.4x_3$ $+1x_{187}$
· · ·	9.1	$+6x_{} + 0.3x_{} + 1x_{}$

x_4	41.925	$-26.25x_{87} + 1.3x_3 + 38.5x_{187}$
x_1	5.25	$-2.5x_{87}$ $-x_3$ $+5x_{187}$
x_6	22.075	$-23.75x_{87} + 3.5x_3 + 22.5x_{187}$
x_{16}	6.075	$+4.25x_{87} +0.5x_3 +5.5x_{187}$
x_8	18.9	$+2x_{87}$ $-1.1x_3$ $+13x_{187}$
x_5	36.6	$-25x_{87}$ $+0.6x_3$ $+36x_{187}$
x_{48}	1.65	$+3.5x_{87}$ $-x_3$ $+2x_{187}$
x_{11}	19.8	$-3x_{87}$ $-1.4x_3$ $+2x_{187}$
x_{10}	17.475	$-1.75x_{87}$ $-1.1x_3 + 17.5x_{187}$
x_7	27.45	$-6.5x_{87}$ $-2.9x_3$ $+28x_{187}$
x_{14}	15.55	$+1.5x_{87}$ $-0.8x_3$ $+15x_{187}$
x_{15}	26.675	$-4.75x_{87}$ $-2.6x_3 + 27.5x_{187}$
x_{21}	5.1	$+4x_{87}$ $-0.1x_3$ $+5x_{187}$
x_{17}	4.025	$+5.75x_{87} +0.6x_3 +2.5x_{187}$
x_{32}	1.325	$+4.75x_{87} +0.2x_3 +0.5x_{187}$
x_{18}	5.3	$+5x_{87} +0.5x_3 +5x_{187}$
x_{20}	4.725	$+4.75x_{87} -0.1x_3 +3.5x_{187}$
x_{12}	5.875	$+2.25x_{87} -0.4x_3 +5.5x_{187}$
x_{22}	5.3	$+5x_{87} +0.5x_3 +5x_{187}$
x_{19}	1.625	$+4.75x_{87} +0.6x_3 +0.5x_{187}$
x_{24}	5.525	$+5.75x_{87} +0.5x_3 +4.5x_{187}$
x_{25}	5.175	$+5.25x_{87} -0.1x_3 +4.5x_{187}$
	1.7	$+2x_{87}$ $+0.8x_3$ $+2x_{187}$
x_{23}	6.075	$+3.25x_{87} +0.2x_3 +5.5x_{187}$
x_{27}	2.075	$+5.25x_{87} +0.2x_3 +5.5x_{187} +5.25x_{87} +0.6x_3 +1.5x_{187}$
x_{26}	4.325	$+8.75x_{87} +0.5x_3 +1.5x_{187} +8.75x_{87} +0.5x_3 +3.5x_{187}$
x_{29}	3.25	
x_{30}	2.1	$+7.5x_{87}$ $+0.4x_3$ $+3x_{187}$
x_{31}	$\frac{2.1}{1.075}$	$+5x_{87}$ $-x_3$ $+1x_{187}$
x_{110}		$+1.25x_{87}$ $-x_3$ $+1.5x_{187}$
x_{33}	4.025	$+8.75x_{87} +0.4x_3 +2.5x_{187}$
x_{34}	2.425	$+6.75x_{87} +0.5x_3 +1.5x_{187}$
x_{35}	4.625	$+7.75x_{87} +0.3x_3 +3.5x_{187}$
x_{36}	0.85	$+2.5x_{87} +0.1x_3 +1x_{187}$
x_{37}	4.25	$+7.5x_{87}$ $+0.1x_3$ $+4x_{187}$
x_{38}	5.35	$+9.5x_{87}$ $+0.4x_3$ $+5x_{187}$
x_{39}	3.8	$+7x_{87}$ $+0.1x_3$ $+3x_{187}$
x_{40}	2.05	$+3.5x_{87} +0.1x_3 +2x_{187}$
x_{41}	6.225	$+8.75x_{87} +0.5x_3 +5.5x_{187}$
x_{42}	3.65	$+5.5x_{87}$ $+0.2x_3$ $+3x_{187}$
x_{43}	1.875	$+4.25x_{87}$ $-x_3$ $+1.5x_{187}$
x_{44}	1.875	$50 + 4.25x_{87} - x_3 + 1.5x_{187}$
x_{45}	4.325	$+5.75x_{87} +0.2x_3 +4.5x_{187}$
x_{46}	1.875	$+4.25x_{87}$ $-x_3$ $+1.5x_{187}$
x_{47}	1.95	$+5.5x_{87}$ $-x_3$ $+1x_{187}$
x_{57}	0.15	$+3.5x_{87}$ $+x_3$ $+x_{187}$
x_{49}	1.425	$+3.75x_{87}$ $-x_3$ $+0.5x_{187}$
x_{50}	2.45	$+8.5x_{87}$ $+0.4x_3$ $+1x_{187}$
œ	9.1	$+6x_{} + 0.3x_{} + 1x_{}$

Unbounded Dictionary! The Final Dual Dictionary is:

Dual is unbounded Primal is therefore infeasible Problem is ILP infeasible Could not find an integer point Done.