

# 1 ilpTest1

Initial Dictionary

$$\begin{array}{c|cc} x_3 & 6 & -3x_1 - 2x_2 \\ x_4 & 0 & +3x_1 - 2x_2 \\ \hline z & 0 & +1x_2 \end{array}$$

No initialization required → Proceed to Optimize.

Final dictionary after first LP relaxation solve:

$$\begin{array}{c|ccc} x_1 & 1 & -0.166667x_3 + 0.166667x_4 & \\ x_2 & 1.5 & -0.25x_3 & -0.25x_4 \\ \hline z & 1.5 & -0.25x_3 & -0.25x_4 \end{array}$$

After cutting plane is added

$$\begin{array}{c|ccc} x_1 & 1 & -0.166667x_3 + 0.166667x_4 & \\ x_2 & 1.5 & -0.25x_3 & -0.25x_4 \\ x_4 & -0.5 & +0.25x_3 & +0.25x_4 \\ \hline z & 1.5 & -0.25x_3 & -0.25x_4 \end{array}$$

Forming the dual dictionary:

$$\begin{array}{c|cccc} y_3 & 0.25 & +0.166667y_1 + 0.25y_2 - 0.25y_4 & & \\ y_4 & 0.25 & -0.166667y_1 + 0.25y_2 - 0.25y_4 & & \\ \hline z & -1.5 & -1y_1 & -1.5y_2 & +0.5y_4 \end{array}$$

The Final Dual Dictionary is:

$$\begin{array}{c|ccc} y_4 & 1 & +0.666667y_1 + 1y_2 - 4y_3 & \\ y_4 & 0 & -0.333333y_1 & +1y_3 \\ \hline z & -1 & -0.666667y_1 - 1y_2 - 2y_3 & \end{array}$$

Final primal dictionary obtained:

$$\begin{array}{c|ccc} x_1 & 0.666666666667 & -0.666667x_4 + 0.333333x_4 & \\ x_2 & 1 & -1x_4 & \\ x_3 & 2 & +4x_4 & -1x_4 \\ \hline z & 1 & -1x_4 & \end{array}$$

After cutting plane is added

$$\begin{array}{c|cc}
 x_1 & 0.666666666667 & -0.666667x_4 + 0.333333x_4 \\
 x_2 & 1 & -1x_4 \\
 x_3 & 2 & +4x_4 & -1x_4 \\
 x_5 & -0.666666666667 & +0.666667x_4 + 0.666667x_4 \\
 \hline
 z & 1 & -1x_4
 \end{array}$$

Forming the dual dictionary:

$$\begin{array}{c|ccc}
 y_4 & 1 & +0.666667y_1 + 1y_2 - 4y_3 - 0.666667y_5 \\
 y_4 & 0 & -0.333333y_1 & +1y_3 - 0.666667y_5 \\
 \hline
 z & -1 & -0.666667y_1 - 1y_2 - 2y_3 + 0.666667y_5
 \end{array}$$

The Final Dual Dictionary is:

$$\begin{array}{c|ccccc}
 y_4 & 1 & +1y_1 & +1y_2 & -5y_3 & +1y_4 \\
 y_5 & 0 & -0.5y_1 & & +1.5y_3 & -1.5y_4 \\
 \hline
 z & -1 & -1y_1 & -1y_2 & -1y_3 & -1y_4
 \end{array}$$

Final primal dictionary obtained:

$$\begin{array}{c|cc}
 x_1 & 1 & -1x_4 + 0.5x_5 \\
 x_2 & 1 & -1x_4 \\
 x_3 & 1 & +5x_4 - 1.5x_5 \\
 x_4 & 1 & -1x_4 + 1.5x_5 \\
 \hline
 z & 1 & -1x_4
 \end{array}$$

Final Answer: 1

## 2 ilpTest2

Initial Dictionary

$$\begin{array}{c|ccc}
 x_4 & 10 & -1x_1 & \\
 x_5 & 10 & & -1x_2 \\
 x_6 & 10 & & -1x_3 \\
 x_7 & 1 & +2x_1 - 7x_2 & \\
 x_8 & 3 & -1x_1 + 2x_2 - 5x_3 & \\
 x_9 & 7 & -1x_1 - 1x_2 + 3x_3 & \\
 \hline
 z & 0 & +1x_1 + 1x_2 - 5x_3 &
 \end{array}$$

No initialization required → Proceed to Optimize.

Final dictionary after first LP relaxation solve:

|       |              |  |
|-------|--------------|--|
| $x_4$ | 4.3333333333 | $+0.333333x_8 + 0.666667x_9 - 0.333333x_3$ |
| $x_5$ | 8.6666666667 | $-0.333333x_8 + 0.333333x_9 - 2.666667x_3$ |
| $x_6$ | 10           | $-1x_3$                                    |
| $x_7$ | 3            | $-3x_8 + 1x_9 - 18x_3$                     |
| $x_1$ | 5.6666666667 | $-0.333333x_8 - 0.666667x_9 + 0.333333x_3$ |
| $x_2$ | 1.3333333333 | $+0.333333x_8 - 0.333333x_9 + 2.666667x_3$ |
| $z$   | 7            | $-1x_9 - 2x_3$                             |

After cutting plane is added

|          |                   |  |
|----------|-------------------|--|
| $x_4$    | 4.3333333333      | $+0.333333x_8 + 0.666667x_9 - 0.333333x_3$ |
| $x_5$    | 8.6666666667      | $-0.333333x_8 + 0.333333x_9 - 2.666667x_3$ |
| $x_6$    | 10                | $-1x_3$                                    |
| $x_7$    | 3                 | $-3x_8 + 1x_9 - 18x_3$                     |
| $x_1$    | 5.6666666667      | $-0.333333x_8 - 0.666667x_9 + 0.333333x_3$ |
| $x_2$    | 1.3333333333      | $+0.333333x_8 - 0.333333x_9 + 2.666667x_3$ |
| $x_9$    | $-0.333333333333$ | $+0.666667x_8 + 0.333333x_9 + 0.333333x_3$ |
| $x_{10}$ | $-0.666666666667$ | $+0.333333x_8 + 0.666667x_9 + 0.666667x_3$ |
| $x_{11}$ | $-0.666666666667$ | $+0.333333x_8 + 0.666667x_9 + 0.666667x_3$ |
| $x_{12}$ | $-0.333333333333$ | $+0.666667x_8 + 0.333333x_9 + 0.333333x_3$ |
| $z$      | 7                 | $-1x_9 - 2x_3$                             |

Forming the dual dictionary:

|       |    |  |
|-------|----|--|
| $y_8$ | -0 | $-0.333333y_4 + 0.333333y_5 + 3y_7 + 0.333333y_1 - 0.333333y_2 - 0.666667y_9 - 0.333333y_{10}$         |
| $y_9$ | 1  | $-0.666667y_4 - 0.333333y_5 - 1y_7 + 0.666667y_1 + 0.333333y_2 - 0.333333y_9 - 0.666667y_{10}$         |
| $y_3$ | 2  | $+0.333333y_4 + 2.666667y_5 + 1y_6 + 18y_7 - 0.333333y_1 - 2.666667y_2 - 0.333333y_9 - 0.666667y_{10}$ |
| $z$   | -7 | $-4.333333y_4 - 8.666667y_5 - 10y_6 - 3y_7 - 5.666667y_1 - 1.333333y_2 + 0.333333y_9 + 0.666667y_{10}$ |

The Final Dual Dictionary is:

|          |                |   |
|----------|----------------|---|
| $y_{10}$ | 1.28571428571  | $-1y_4 - 0.285714y_5 - 1.285714y_9 + 1y_1 + 0.285714y_2 - 0.428571y_8 - 0.714285714$            |
| $y_7$    | 0.142857142857 | $+0y_4 - 0.142857y_5 - 0.142857y_9 - 0y_1 + 0.142857y_2 + 0.285714y_8 + 0.142857142857$         |
| $y_3$    | 3.71428571429  | $+1y_4 + 0.285714y_5 + 1y_6 - 1.714286y_9 - 1y_1 - 0.285714y_2 + 5.428571y_8 + 2.71428571429$   |
| $z$      | -6.57142857143 | $-5y_4 - 8.428571y_5 - 10y_6 - 0.428571y_9 - 5y_1 - 1.571429y_2 - 1.142857y_8 - 0.571428571429$ |

Final primal dictionary obtained:

|          |                       |                   |                |                |
|----------|-----------------------|-------------------|----------------|----------------|
| $x_4$    | 5                     | $+1x_{10}$        | $-0x_7$        | $-1x_3$        |
| $x_5$    | 8.42857142857         | $+0.285714x_{10}$ | $+0.142857x_7$ | $-0.285714x_3$ |
| $x_6$    | 10                    |                   |                | $-1x_3$        |
| $x_9$    | 0.428571428571        | $+1.285714x_{10}$ | $+0.142857x_7$ | $+1.714286x_3$ |
| $x_1$    | 5                     | $-1x_{10}$        | $+0x_7$        | $+1x_3$        |
| $x_2$    | 1.57142857143         | $-0.285714x_{10}$ | $-0.142857x_7$ | $+0.285714x_3$ |
| $x_8$    | 1.14285714286         | $+0.428571x_{10}$ | $-0.285714x_7$ | $-5.428571x_3$ |
| $x_9$    | 0.571428571429        | $+0.714286x_{10}$ | $-0.142857x_7$ | $-2.714286x_3$ |
| $x_{11}$ | $1.58603289232e - 17$ | $+1x_{10}$        | $-0x_7$        | $-0x_3$        |
| $x_{12}$ | 0.571428571429        | $+0.714286x_{10}$ | $-0.142857x_7$ | $-2.714286x_3$ |
| $z$      | 6.57142857143         | $-1.285714x_{10}$ | $-0.142857x_7$ | $-3.714286x_3$ |

After cutting plane is added

|          |                       |                   |                |                |
|----------|-----------------------|-------------------|----------------|----------------|
| $x_4$    | 5                     | $+1x_{10}$        | $-0x_7$        | $-1x_3$        |
| $x_5$    | 8.42857142857         | $+0.285714x_{10}$ | $+0.142857x_7$ | $-0.285714x_3$ |
| $x_6$    | 10                    |                   |                | $-1x_3$        |
| $x_9$    | 0.428571428571        | $+1.285714x_{10}$ | $+0.142857x_7$ | $+1.714286x_3$ |
| $x_1$    | 5                     | $-1x_{10}$        | $+0x_7$        | $+1x_3$        |
| $x_2$    | 1.57142857143         | $-0.285714x_{10}$ | $-0.142857x_7$ | $+0.285714x_3$ |
| $x_8$    | 1.14285714286         | $+0.428571x_{10}$ | $-0.285714x_7$ | $-5.428571x_3$ |
| $x_9$    | 0.571428571429        | $+0.714286x_{10}$ | $-0.142857x_7$ | $-2.714286x_3$ |
| $x_{11}$ | $1.58603289232e - 17$ | $+1x_{10}$        | $-0x_7$        | $-0x_3$        |
| $x_{12}$ | 0.571428571429        | $+0.714286x_{10}$ | $-0.142857x_7$ | $-2.714286x_3$ |
| $x_{13}$ | $-0.428571428571$     | $+0.714286x_{10}$ | $+0.857143x_7$ | $+0.285714x_3$ |
| $x_{14}$ | $-0.428571428571$     | $+0.714286x_{10}$ | $+0.857143x_7$ | $+0.285714x_3$ |
| $x_{15}$ | $-0.571428571429$     | $+0.285714x_{10}$ | $+0.142857x_7$ | $+0.714286x_3$ |
| $x_{16}$ | $-0.142857142857$     | $+0.571429x_{10}$ | $+0.285714x_7$ | $+0.428571x_3$ |
| $x_{17}$ | $-0.571428571429$     | $+0.285714x_{10}$ | $+0.142857x_7$ | $+0.714286x_3$ |
| $x_{18}$ | $-0.571428571429$     | $+0.285714x_{10}$ | $+0.142857x_7$ | $+0.714286x_3$ |
| $z$      | 6.57142857143         | $-1.285714x_{10}$ | $-0.142857x_7$ | $-3.714286x_3$ |

Forming the dual dictionary:

|          |                  |                               |   |
|----------|------------------|-------------------------------|---|
| $y_{10}$ | 1.28571428571    | $-1y_4 - 0.285714y_5$         | $-1.285714y_9 + 1y_1 + 0.285714y_2 - 0.428571y_8 - 0.714286y_3$ |
| $y_7$    | 0.142857142857   | $+0y_4 - 0.142857y_5$         | $-0.142857y_9 - 0y_1 + 0.142857y_2 + 0.285714y_8 + 0.142857y_3$ |
| $y_3$    | 3.71428571429    | $+1y_4 + 0.285714y_5 + 1y_6$  | $-1.714286y_9 - 1y_1 - 0.285714y_2 + 5.428571y_8 + 2.714286y_3$ |
| $z$      | $-6.57142857143$ | $-5y_4 - 8.428571y_5 - 10y_6$ | $-0.428571y_9 - 5y_1 - 1.571429y_2 - 1.142857y_8 - 0.571429y_3$ |

The Final Dual Dictionary is:

|          |    |                        |  |   |      |
|----------|----|------------------------|--|---|------|
| $y_{10}$ | 1  | $-1y_4$                | $-1y_9 + 1y_1$   | $-1y_8 - 1y_9 - 1y_{11} - 1y_{12} + 2y_7 + 1y_{14} + 1y_{13}$ | $-0$ |
| $y_{15}$ | 1  | $+0y_4 - 1y_5$         | $-1y_9 - 0y_1 + 1y_2 + 2y_8 + 1y_9 + 0y_{11} + 1y_{12} - 7y_7 - 6y_{14} - 6y_{13} - 2y_{16} - 1y_{17} - 1$ |   |      |
| $y_3$    | 3  | $+1y_4 + 1y_5 + 1y_6$  | $-1y_9 - 1y_1 - 1y_2 + 4y_8 + 2y_9 - 0y_{11} + 2y_{12} + 5y_7 + 4y_{14} + 4y_{13} + 1y_{16} - 0y_{17} - 0$ |   |      |
| $z$      | -6 | $-5y_4 - 9y_5 - 10y_6$ | $-1y_9 - 5y_1 - 1y_2 + 0y_8 + 0y_9 + 0y_{11} + 0y_{12} - 4y_7 - 3y_{14} - 3y_{13} - 1y_{16} - 0y_{17} - 0$ |   |      |

Final primal dictionary obtained:

Note: We need to set tolerances small enough to recognize  $10^{-16}$  as zero.

|          |                        |                             |
|----------|------------------------|-----------------------------|
| $x_4$    | 5                      | $+1x_{10} - 0x_{15} - 1x_3$ |
| $x_5$    | 9                      | $+1x_{15} - 1x_3$           |
| $x_6$    | 10                     | $-1x_3$                     |
| $x_9$    | 1                      | $+1x_{10} + 1x_{15} + 1x_3$ |
| $x_1$    | 5                      | $-1x_{10} + 0x_{15} + 1x_3$ |
| $x_2$    | 1                      | $-1x_{15} + 1x_3$           |
| $x_8$    | $-4.4408920985e - 16$  | $+1x_{10} - 2x_{15} - 4x_3$ |
| $x_9$    | $-1.11022302463e - 15$ | $+1x_{10} - 1x_{15} - 2x_3$ |
| $x_{11}$ | $-1.11022302463e - 16$ | $+1x_{10} - 0x_{15} + 0x_3$ |
| $x_{12}$ | $-7.77156117238e - 16$ | $+1x_{10} - 1x_{15} - 2x_3$ |
| $x_7$    | 4                      | $-2x_{10} + 7x_{15} - 5x_3$ |
| $x_{14}$ | 3                      | $-1x_{10} + 6x_{15} - 4x_3$ |
| $x_{13}$ | 3                      | $-1x_{10} + 6x_{15} - 4x_3$ |
| $x_{16}$ | 1                      | $+2x_{15} - 1x_3$           |
| $x_{17}$ | $1.11022302463e - 15$  | $+1x_{15} + 0x_3$           |
| $x_{18}$ | $7.77156117238e - 16$  | $+0x_{10} + 1x_{15} + 0x_3$ |
| $z$      | 6                      | $-1x_{10} - 1x_{15} - 3x_3$ |

Done.

Final Answer: 6

### 3 ilpTest3

Initial Dictionary

|       |    |                       |
|-------|----|-----------------------|
| $x_4$ | 10 | $-1x_1$               |
| $x_5$ | 10 | $-1x_2$               |
| $x_6$ | 10 | $-1x_3$               |
| $x_7$ | 1  | $+2x_1 + 7x_2$        |
| $x_8$ | 3  | $+1x_1 + 2x_2 - 5x_3$ |
| $x_9$ | 7  | $+1x_1 - 1x_2 + 3x_3$ |
| $z$   | 0  | $-1x_1 - 1x_2 + 5x_3$ |

No initialization required → Proceed to Optimize.

Final dictionary after first LP relaxation solve:

|       |      |                             |         |         |
|-------|------|-----------------------------|---------|---------|
| $x_4$ | 10   | $-1x_1$                     |         |         |
| $x_2$ | 10   |                             | $-1x_5$ |         |
| $x_6$ | 5.4  | $-0.2x_1 + 0.4x_5 + 0.2x_8$ |         |         |
| $x_7$ | 71   | $+2x_1 - 7x_5$              |         |         |
| $x_3$ | 4.6  | $+0.2x_1 - 0.4x_5 - 0.2x_8$ |         |         |
| $x_9$ | 10.8 | $+1.6x_1 - 0.2x_5 - 0.6x_8$ |         |         |
| $z$   | 13   |                             | $-1x_5$ | $-1x_8$ |

After cutting plane is added

|          |      |                             |         |         |
|----------|------|-----------------------------|---------|---------|
| $x_4$    | 10   | $-1x_1$                     |         |         |
| $x_2$    | 10   |                             | $-1x_5$ |         |
| $x_6$    | 5.4  | $-0.2x_1 + 0.4x_5 + 0.2x_8$ |         |         |
| $x_7$    | 71   | $+2x_1 - 7x_5$              |         |         |
| $x_3$    | 4.6  | $+0.2x_1 - 0.4x_5 - 0.2x_8$ |         |         |
| $x_9$    | 10.8 | $+1.6x_1 - 0.2x_5 - 0.6x_8$ |         |         |
| $x_9$    | -0.4 | $+0.2x_1 + 0.6x_5 + 0.8x_8$ |         |         |
| $x_{10}$ | -0.6 | $+0.8x_1 + 0.4x_5 + 0.2x_8$ |         |         |
| $x_{11}$ | -0.8 | $+0.4x_1 + 0.2x_5 + 0.6x_8$ |         |         |
| $z$      | 13   |                             | $-1x_5$ | $-1x_8$ |

Forming the dual dictionary:

|       |     |   |   |
|-------|-----|---|---|
| $y_1$ | -0  | $+1y_4$   | $+0.2y_6 - 2y_7 - 0.2y_3 - 1.6y_9 - 0.2y_9 - 0.8y_{10} - 0.4y_{11}$ |
| $y_5$ | 1   | $+1y_2 - 0.4y_6 + 7y_7 + 0.4y_3 + 0.2y_9 - 0.6y_9 - 0.4y_{10} - 0.2y_{11}$            |   |
| $y_8$ | 1   | $-0.2y_6 + 0.2y_3 + 0.6y_9 - 0.8y_9 - 0.2y_{10} - 0.6y_{11}$                          |   |
| $z$   | -13 | $-10y_4 - 10y_2 - 5.4y_6 - 71y_7 - 4.6y_3 - 10.8y_9 + 0.4y_9 + 0.6y_{10} + 0.8y_{11}$ |   |

The Final Dual Dictionary is:

|       |     |  |  |
|-------|-----|--|--|
| $y_9$ | -0  | $+5y_4$  | $+1y_6 - 10y_7 - 1y_3 - 8y_9 - 5y_1 - 4y_{10} - 2y_{11}$ |
| $y_5$ | 1   | $-3y_4 + 1y_2 - 1y_6 + 13y_7 + 1y_3 + 5y_9 + 3y_1 + 2y_{10} + 1y_{11}$   |  |
| $y_8$ | 1   | $-4y_4 - 1y_6 + 8y_7 + 1y_3 + 7y_9 + 4y_1 + 3y_{10} + 1y_{11}$           |  |
| $z$   | -13 | $-8y_4 - 10y_2 - 5y_6 - 75y_7 - 5y_3 - 14y_9 - 2y_1 - 1y_{10} + 0y_{11}$ |  |

Final primal dictionary obtained:

$$\begin{array}{c|ccc}
 x_4 & 8 & -5x_9 & +3x_5 & +4x_8 \\
 x_2 & 10 & & -1x_5 & \\
 x_6 & 5 & -1x_9 & +1x_5 & +1x_8 \\
 x_7 & 75 & +10x_9 & -13x_5 & -8x_8 \\
 x_3 & 5 & +1x_9 & -1x_5 & -1x_8 \\
 x_9 & 14 & +8x_9 & -5x_5 & -7x_8 \\
 x_1 & 2 & +5x_9 & -3x_5 & -4x_8 \\
 x_{10} & 1 & +4x_9 & -2x_5 & -3x_8 \\
 x_{11} & -1.99840144433e - 15 & +2x_9 & -1x_5 & -1x_8 \\
 \hline
 z & 13 & & -1x_5 & -1x_8
 \end{array}$$

Done.

final Answer: 13

## 4 ilpTest4

Initial Dictionary

$$\begin{array}{c|cc}
 x_3 & 15 & -2x_1 - 2x_2 \\
 x_4 & 5 & -2x_1 + 2x_2 \\
 \hline
 z & -20 & +3x_1 + 4x_2
 \end{array}$$

No initialization required → Proceed to Optimize.

Final dictionary after first LP relaxation solve:

$$\begin{array}{c|ccc}
 x_2 & 7.5 & -1x_1 & -0.5x_3 \\
 x_4 & 20 & -4x_1 & -1x_3 \\
 \hline
 z & 10 & -1x_1 & -2x_3
 \end{array}$$

After cutting plane is added

$$\begin{array}{c|ccc}
 x_2 & 7.5 & -1x_1 & -0.5x_3 \\
 x_4 & 20 & -4x_1 & -1x_3 \\
 x_4 & -0.5 & & +0.5x_3 \\
 \hline
 z & 10 & -1x_1 & -2x_3
 \end{array}$$

Forming the dual dictionary:

$$\begin{array}{c|cccc}
 y_1 & 1 & +1y_2 & +4y_4 & \\
 y_3 & 2 & +0.5y_2 & +1y_4 & -0.5y_4 \\
 \hline
 z & -10 & -7.5y_2 & -20y_4 & +0.5y_4
 \end{array}$$

The Final Dual Dictionary is:

$$\begin{array}{c|ccc} y_1 & 1 & +1y_2 & +4y_4 \\ y_4 & 4 & +1y_2 & +2y_4 -2y_3 \\ \hline z & -8 & -7y_2 -19y_4 -1y_3 & \end{array}$$

Final primal dictionary obtained:

$$\begin{array}{c|ccc} x_2 & 7 & -1x_1 -1x_4 & \\ x_4 & 19 & -4x_1 -2x_4 & \\ x_3 & 1 & +2x_4 & \\ \hline z & 8 & -1x_1 -4x_4 & \end{array}$$

Done.

final answer: 8

## 5 ilpTest5

Initial Dictionary

$$\begin{array}{c|ccc} x_3 & 15 & -2x_1 -5x_2 & \\ x_4 & 5 & -2x_1 +2x_2 & \\ \hline z & -20 & +3x_1 +4x_2 & \end{array}$$

No initialization required → Proceed to Optimize.

Final dictionary after first LP relaxation solve:

$$\begin{array}{c|ccc} x_2 & 1.42857142857 & +0.142857x_4 -0.142857x_3 & \\ x_1 & 3.92857142857 & -0.357143x_4 -0.142857x_3 & \\ \hline z & -2.5 & -0.5x_4 & -1x_3 \end{array}$$

After cutting plane is added

$$\begin{array}{c|ccc} x_2 & 1.42857142857 & +0.142857x_4 -0.142857x_3 & \\ x_1 & 3.92857142857 & -0.357143x_4 -0.142857x_3 & \\ x_4 & -0.428571428571 & +0.857143x_4 +0.142857x_3 & \\ x_5 & -0.928571428571 & +0.357143x_4 +0.142857x_3 & \\ \hline z & -2.5 & -0.5x_4 & -1x_3 \end{array}$$

Forming the dual dictionary:

$$\begin{array}{c|ccc} y_4 & 0.5 & -0.142857y_2 +0.357143y_1 -0.857143y_4 -0.357143y_5 & \\ y_3 & 1 & +0.142857y_2 +0.142857y_1 -0.142857y_4 -0.142857y_5 & \\ \hline z & 2.5 & -1.428571y_2 -3.928571y_1 +0.428571y_4 +0.928571y_5 & \end{array}$$



The Final Dual Dictionary is:

$$\begin{array}{c|ccc}
y_5 & 1.4 & -0.4y_2 + 1y_1 - 2.8y_4 - 2.4y_4 & \\
y_3 & 0.8 & +0.2y_2 & +0.4y_4 + 0.2y_4 \\
\hline
z & 3.8 & -1.8y_2 - 3y_1 - 2.6y_4 - 1.8y_4 & 
\end{array}$$

Final primal dictionary obtained:

$$\begin{array}{c|ccc}
x_2 & 1.8 & +0.4x_5 - 0.2x_3 & \\
x_1 & 3 & -1x_5 & \\
x_4 & 2.6 & +2.8x_5 - 0.4x_3 & \\
x_4 & 1.8 & +2.4x_5 - 0.2x_3 & \\
\hline
z & -3.8 & -1.4x_5 - 0.8x_3 & 
\end{array}$$

After cutting plane is added

$$\begin{array}{c|ccc}
x_2 & 1.8 & +0.4x_5 - 0.2x_3 & \\
x_1 & 3 & -1x_5 & \\
x_4 & 2.6 & +2.8x_5 - 0.4x_3 & \\
x_4 & 1.8 & +2.4x_5 - 0.2x_3 & \\
x_6 & -0.8 & +0.6x_5 + 0.2x_3 & \\
x_7 & -0.6 & +0.2x_5 + 0.4x_3 & \\
x_8 & -0.8 & +0.6x_5 + 0.2x_3 & \\
\hline
z & -3.8 & -1.4x_5 - 0.8x_3 & 
\end{array}$$

Forming the dual dictionary:

$$\begin{array}{c|ccccccc}
y_5 & 1.4 & -0.4y_2 + 1y_1 - 2.8y_4 - 2.4y_4 - 0.6y_6 - 0.2y_7 - 0.6y_8 & \\
y_3 & 0.8 & +0.2y_2 & +0.4y_4 + 0.2y_4 - 0.2y_6 - 0.4y_7 - 0.2y_8 & \\
\hline
z & 3.8 & -1.8y_2 - 3y_1 - 2.6y_4 - 1.8y_4 + 0.8y_6 + 0.6y_7 + 0.8y_8 & 
\end{array}$$

The Final Dual Dictionary is:

$$\begin{array}{c|ccc}
y_6 & 2 & -1y_2 + 2y_1 - 6y_4 - 5y_4 - 2y_5 + 1y_3 - 1y_8 & \\
y_7 & 1 & +1y_2 - 1y_1 + 4y_4 + 3y_4 + 1y_5 - 3y_3 - 0y_8 & \\
\hline
z & 6 & -2y_2 - 2y_1 - 5y_4 - 4y_4 - 1y_5 - 1y_3 + 0y_8 & 
\end{array}$$

Final primal dictionary obtained:

$$\begin{array}{c|ccc}
x_2 & & 2 & +1x_6 - 1x_7 \\
x_1 & & 2 & -2x_6 + 1x_7 \\
x_4 & & 5 & +6x_6 - 4x_7 \\
x_4 & & 4 & +5x_6 - 3x_7 \\
x_5 & & 1 & +2x_6 - 1x_7 \\
x_3 & & 1 & -1x_6 + 3x_7 \\
x_8 & -9.71445146547e - 16 & & +1x_6 + 0x_7 \\
\hline
z & & -6 & -2x_6 - 1x_7
\end{array}$$

Done.

Final answer: -6

## 6 ilpTest6

Initial Dictionary

$$\begin{array}{c|cccccc}
 x_7 & -1 & +1x_1 & +1x_2 & & & \\
 x_8 & -1 & +1x_1 & +1x_2 & & & +1x_6 \\
 x_9 & -1 & & & +1x_3 & +1x_4 & \\
 x_{10} & -1 & & & +1x_3 & +1x_4 & +1x_5 \\
 x_{11} & -1 & & & & +1x_4 & +1x_5 & +1x_6 \\
 x_{12} & -1 & & +1x_2 & & & +1x_5 & +1x_6 \\
 \hline
 z & 0 & -1x_1 & -1x_2 & -1x_3 & -1x_4 & -1x_5 & -1x_6
 \end{array}$$

$x_7$  leaves

Problem is feasible. Initialization phase yields a zero answer. Final dictionary after first LP relaxation solve:

$$\begin{array}{c|cccc}
 x_2 & 1 & & +1x_{12} & -1x_5 & -1x_6 \\
 x_8 & 0 & & & +1x_6 & +1x_7 \\
 x_1 & 0 & & -1x_{12} & +1x_5 & +1x_6 & +1x_7 \\
 x_{10} & 0 & +1x_9 & & +1x_5 & & \\
 x_3 & 0 & +1x_9 & -1x_{11} & +1x_5 & +1x_6 & \\
 x_4 & 1 & & +1x_{11} & -1x_5 & -1x_6 & \\
 \hline
 z & -2 & -1x_9 & & -1x_5 & -1x_6 & -1x_7
 \end{array}$$

Done.

Final Answer: -2

## 7 ilpTest7

Initial Dictionary

$$\begin{array}{c|cc}
 x_3 & 15 & -4x_1 - 2x_2 \\
 x_4 & 8 & -1x_1 - 2x_2 \\
 x_5 & 5 & -1x_1 - 1x_2 \\
 \hline
 z & 0 & +3x_1 + 2x_2
 \end{array}$$

No initialization required → Proceed to Optimize.

Final dictionary after first LP relaxation solve:

$$\begin{array}{c|cc}
x_1 & 2.5 & -0.5x_3 + 1x_5 \\
x_4 & 0.5 & -0.5x_3 + 3x_5 \\
x_2 & 2.5 & +0.5x_3 - 2x_5 \\
\hline
z & 12.5 & -0.5x_3 - 1x_5
\end{array}$$

After cutting plane is added

$$\begin{array}{c|cc}
x_1 & 2.5 & -0.5x_3 + 1x_5 \\
x_4 & 0.5 & -0.5x_3 + 3x_5 \\
x_2 & 2.5 & +0.5x_3 - 2x_5 \\
x_5 & -0.5 & +0.5x_3 \\
x_6 & -0.5 & +0.5x_3 \\
x_7 & -0.5 & +0.5x_3 \\
\hline
z & 12.5 & -0.5x_3 - 1x_5
\end{array}$$

Forming the dual dictionary:

$$\begin{array}{c|ccccccc}
y_3 & 0.5 & +0.5y_1 & +0.5y_4 & -0.5y_2 & -0.5y_5 & -0.5y_6 & -0.5y_7 \\
y_5 & 1 & -1y_1 & -3y_4 & +2y_2 & & & \\
\hline
z & -12.5 & -2.5y_1 & -0.5y_4 & -2.5y_2 & +0.5y_5 & +0.5y_6 & +0.5y_7
\end{array}$$

The Final Dual Dictionary is:

$$\begin{array}{c|cccc}
y_5 & 1 & +1y_1 & +1y_4 & -1y_2 & -2y_3 & -1y_6 & -1y_7 \\
y_5 & 1 & -1y_1 & -3y_4 & +2y_2 & & & \\
\hline
z & -12 & -2y_1 & & -3y_2 & -1y_3 & & 
\end{array}$$

Final primal dictionary obtained:

$$\begin{array}{c|cc}
x_1 & 2 & -1x_5 + 1x_5 \\
x_4 & -0 & -1x_5 + 3x_5 \\
x_2 & 3 & +1x_5 - 2x_5 \\
x_3 & 1 & +2x_5 \\
x_6 & -0 & +1x_5 \\
x_7 & -0 & +1x_5 \\
\hline
z & 12 & -1x_5 - 1x_5
\end{array}$$

Done.

Final Answer: 12

## 8 ilpTest8

Initial Dictionary

|       |    |                                  |
|-------|----|----------------------------------|
| $x_5$ | 84 | $+7x_1 - 14x_2 - 59x_3 - 54x_4$  |
| $x_6$ | 44 | $-71x_1 - 32x_2 + 75x_3 + 28x_4$ |
| $x_7$ | 41 | $+74x_1 + 12x_2 + 63x_3 + 33x_4$ |
| $x_8$ | 24 | $-3x_1 - 78x_2 - 9x_3 - 11x_4$   |
| $x_9$ | 97 | $-56x_1 - 32x_2 - 32x_3 + 39x_4$ |
| $z$   | 0  | $-9x_1 + 49x_2 - 36x_3 + 41x_4$  |

No initialization required → Proceed to Optimize.

Final dictionary after first LP relaxation solve:

|       |                 |  |
|-------|-----------------|--|
| $x_4$ | 1.53178905865   | $+0.144899x_1 + 0.003450x_8 - 1.103006x_3 - 0.019221x_5$   |
| $x_6$ | 83.9566288812   | $-65.058157x_1 + 0.522425x_8 + 42.830458x_3 - 0.624938x_5$ |
| $x_7$ | 92.6490882208   | $+78.074914x_1 - 0.045835x_8 + 27.082799x_3 - 0.601774x_5$ |
| $x_2$ | 0.0916707737802 | $-0.058896x_1 - 0.013307x_8 + 0.040168x_3 + 0.002711x_5$   |
| $x_9$ | 153.806308526   | $-48.464268x_1 + 0.560375x_8 - 76.302612x_3 - 0.836373x_5$ |
| $z$   | 67.2952193199   | $-5.945047x_1 - 0.510596x_8 - 79.255052x_3 - 0.655249x_5$  |

After cutting plane is added

|          |                  |  |
|----------|------------------|--|
| $x_4$    | 1.53178905865    | $+0.144899x_1 + 0.003450x_8 - 1.103006x_3 - 0.019221x_5$   |
| $x_6$    | 83.9566288812    | $-65.058157x_1 + 0.522425x_8 + 42.830458x_3 - 0.624938x_5$ |
| $x_7$    | 92.6490882208    | $+78.074914x_1 - 0.045835x_8 + 27.082799x_3 - 0.601774x_5$ |
| $x_2$    | 0.0916707737802  | $-0.058896x_1 - 0.013307x_8 + 0.040168x_3 + 0.002711x_5$   |
| $x_9$    | 153.806308526    | $-48.464268x_1 + 0.560375x_8 - 76.302612x_3 - 0.836373x_5$ |
| $x_9$    | -0.53178905865   | $+0.855101x_1 + 0.996550x_8 + 0.103006x_3 + 0.019221x_5$   |
| $x_{10}$ | -0.956628881222  | $+0.058157x_1 + 0.477575x_8 + 0.169542x_3 + 0.624938x_5$   |
| $x_{11}$ | -0.649088220798  | $+0.925086x_1 + 0.045835x_8 + 0.917201x_3 + 0.601774x_5$   |
| $x_{12}$ | -0.0916707737802 | $+0.058896x_1 + 0.013307x_8 + 0.959832x_3 + 0.997289x_5$   |
| $x_{13}$ | -0.806308526368  | $+0.464268x_1 + 0.439625x_8 + 0.302612x_3 + 0.836373x_5$   |
| $z$      | 67.2952193199    | $-5.945047x_1 - 0.510596x_8 - 79.255052x_3 - 0.655249x_5$  |

Forming the dual dictionary:

|       |                |  |
|-------|----------------|--|
| $y_1$ | 5.94504682109  | $-0.144899y_4 + 65.058157y_6 - 78.074914y_7 + 0.058896y_2 + 48.464268y_9 - 0.85510$  |
| $y_8$ | 0.510596352883 | $-0.003450y_4 - 0.522425y_6 + 0.045835y_7 + 0.013307y_2 - 0.560375y_9 - 0.99655$     |
| $y_3$ | 79.2550517496  | $+1.103006y_4 - 42.830458y_6 - 27.082799y_7 - 0.040168y_2 + 76.302612y_9 - 0.10300$  |
| $y_5$ | 0.655248891079 | $+0.019221y_4 + 0.624938y_6 + 0.601774y_7 - 0.002711y_2 + 0.836373y_9 - 0.01922$     |
| $z$   | -67.2952193199 | $-1.531789y_4 - 83.956629y_6 - 92.649088y_7 - 0.091671y_2 - 153.806309y_9 + 0.53178$ |

The Final Dual Dictionary is:

|          |                 |  |
|----------|-----------------|--|
| $y_1$    | 5.87550200803   | $-0.130924y_4 + 65.869076y_6 - 77.771084y_7 + 0.045783y_2 + 49.428916y_9 + 0.869076y_3$  |
| $y_9$    | 0.0100401606426 | $-0.018474y_4 - 1.018474y_6 - 0.421687y_7 + 0.015663y_2 - 1.221687y_9 - 1.018474y_3$     |
| $y_3$    | 79.0763052209   | $+1.099598y_4 - 42.900402y_6 - 27.204819y_7 - 0.040964y_2 + 76.195181y_9 + 0.099598y_1$  |
| $y_{10}$ | 1.04819277108   | $+0.031325y_4 + 1.031325y_6 + 0.975904y_7 - 0.004819y_2 + 1.375904y_9 + 0.031325y_1$     |
| $z$      | -66.2871485944  | $-1.511647y_4 - 83.511647y_6 - 91.939759y_7 - 0.087952y_2 - 153.139759y_9 - 0.511647y_3$ |

Final primal dictionary obtained:

|          |                 |   |
|----------|-----------------|---|
| $x_4$    | 1.51164658635   | $+0.130924x_1 + 0.018474x_9 - 1.099598x_3 - 0.031325x_{10}$   |
| $x_6$    | 83.5116465863   | $-65.869076x_1 + 1.018474x_9 + 42.900402x_3 - 1.031325x_{10}$ |
| $x_7$    | 91.9397590361   | $+77.771084x_1 + 0.421687x_9 + 27.204819x_3 - 0.975904x_{10}$ |
| $x_2$    | 0.0879518072289 | $-0.045783x_1 - 0.015663x_9 + 0.040964x_3 + 0.004819x_{10}$   |
| $x_9$    | 153.139759036   | $-49.428916x_1 + 1.221687x_9 - 76.195181x_3 - 1.375904x_{10}$ |
| $x_8$    | 0.511646586345  | $-0.869076x_1 + 1.018474x_9 - 0.099598x_3 - 0.031325x_{10}$   |
| $x_5$    | 1.13975903614   | $+0.571084x_1 - 0.778313x_9 - 0.195181x_3 + 1.624096x_{10}$   |
| $x_{11}$ | 0.0602409638554 | $+1.228916x_1 - 0.421687x_9 + 0.795181x_3 + 0.975904x_{10}$   |
| $x_{12}$ | 1.05180722892   | $+0.616867x_1 - 0.762651x_9 + 0.763855x_3 + 1.619277x_{10}$   |
| $x_{13}$ | 0.371887550201  | $+0.559839x_1 - 0.203213x_9 + 0.095582x_3 + 1.344578x_{10}$   |
| $z$      | 66.2871485944   | $-5.875502x_1 - 0.010040x_9 - 79.076305x_3 - 1.048193x_{10}$  |

After cutting plane is added

|          |                  |                  |                 |                  |                    |
|----------|------------------|------------------|-----------------|------------------|--------------------|
| $x_4$    | 1.51164658635    | +0.130924 $x_1$  | +0.018474 $x_9$ | -1.099598 $x_3$  | -0.031325 $x_{10}$ |
| $x_6$    | 83.5116465863    | -65.869076 $x_1$ | +1.018474 $x_9$ | +42.900402 $x_3$ | -1.031325 $x_{10}$ |
| $x_7$    | 91.9397590361    | +77.771084 $x_1$ | +0.421687 $x_9$ | +27.204819 $x_3$ | -0.975904 $x_{10}$ |
| $x_2$    | 0.0879518072289  | -0.045783 $x_1$  | -0.015663 $x_9$ | +0.040964 $x_3$  | +0.004819 $x_{10}$ |
| $x_9$    | 153.139759036    | -49.428916 $x_1$ | +1.221687 $x_9$ | -76.195181 $x_3$ | -1.375904 $x_{10}$ |
| $x_8$    | 0.511646586345   | -0.869076 $x_1$  | +1.018474 $x_9$ | -0.099598 $x_3$  | -0.031325 $x_{10}$ |
| $x_5$    | 1.13975903614    | +0.571084 $x_1$  | -0.778313 $x_9$ | -0.195181 $x_3$  | +1.624096 $x_{10}$ |
| $x_{11}$ | 0.0602409638554  | +1.228916 $x_1$  | -0.421687 $x_9$ | +0.795181 $x_3$  | +0.975904 $x_{10}$ |
| $x_{12}$ | 1.05180722892    | +0.616867 $x_1$  | -0.762651 $x_9$ | +0.763855 $x_3$  | +1.619277 $x_{10}$ |
| $x_{13}$ | 0.371887550201   | +0.559839 $x_1$  | -0.203213 $x_9$ | +0.095582 $x_3$  | +1.344578 $x_{10}$ |
| $x_{14}$ | -0.511646586345  | +0.869076 $x_1$  | +0.981526 $x_9$ | +0.099598 $x_3$  | +0.031325 $x_{10}$ |
| $x_{15}$ | -0.511646586345  | +0.869076 $x_1$  | +0.981526 $x_9$ | +0.099598 $x_3$  | +0.031325 $x_{10}$ |
| $x_{16}$ | -0.939759036145  | +0.228916 $x_1$  | +0.578313 $x_9$ | +0.795181 $x_3$  | +0.975904 $x_{10}$ |
| $x_{17}$ | -0.0879518072289 | +0.045783 $x_1$  | +0.015663 $x_9$ | +0.959036 $x_3$  | +0.995181 $x_{10}$ |
| $x_{18}$ | -0.139759036145  | +0.428916 $x_1$  | +0.778313 $x_9$ | +0.195181 $x_3$  | +0.375904 $x_{10}$ |
| $x_{19}$ | -0.511646586345  | +0.869076 $x_1$  | +0.981526 $x_9$ | +0.099598 $x_3$  | +0.031325 $x_{10}$ |
| $x_{20}$ | -0.139759036145  | +0.428916 $x_1$  | +0.778313 $x_9$ | +0.195181 $x_3$  | +0.375904 $x_{10}$ |
| $x_{21}$ | -0.0602409638554 | +0.771084 $x_1$  | +0.421687 $x_9$ | +0.204819 $x_3$  | +0.024096 $x_{10}$ |
| $x_{22}$ | -0.0518072289157 | +0.383133 $x_1$  | +0.762651 $x_9$ | +0.236145 $x_3$  | +0.380723 $x_{10}$ |
| $x_{23}$ | -0.371887550201  | +0.440161 $x_1$  | +0.203213 $x_9$ | +0.904418 $x_3$  | +0.655422 $x_{10}$ |
| $z$      | 66.2871485944    | -5.875502 $x_1$  | -0.010040 $x_9$ | -79.076305 $x_3$ | -1.048193 $x_{10}$ |

Forming the dual dictionary:

|          |                 |                 |                  |                  |                 |                   |                 |
|----------|-----------------|-----------------|------------------|------------------|-----------------|-------------------|-----------------|
| $y_1$    | 5.87550200803   | -0.130924 $y_4$ | +65.869076 $y_6$ | -77.771084 $y_7$ | +0.045783 $y_2$ | +49.428916 $y_9$  | +0.869076 $y_3$ |
| $y_9$    | 0.0100401606426 | -0.018474 $y_4$ | -1.018474 $y_6$  | -0.421687 $y_7$  | +0.015663 $y_2$ | -1.221687 $y_9$   | -1.018474 $y_3$ |
| $y_3$    | 79.0763052209   | +1.099598 $y_4$ | -42.900402 $y_6$ | -27.204819 $y_7$ | -0.040964 $y_2$ | +76.195181 $y_9$  | +0.099598 $y_3$ |
| $y_{10}$ | 1.04819277108   | +0.031325 $y_4$ | +1.031325 $y_6$  | +0.975904 $y_7$  | -0.004819 $y_2$ | +1.375904 $y_9$   | +0.031325 $y_3$ |
| $z$      | -66.2871485944  | -1.511647 $y_4$ | -83.511647 $y_6$ | -91.939759 $y_7$ | -0.087952 $y_2$ | -153.139759 $y_9$ | -0.511647 $y_3$ |

The Final Dual Dictionary is:

|          |                |                 |                  |           |                 |                   |                 |                    |
|----------|----------------|-----------------|------------------|-----------|-----------------|-------------------|-----------------|--------------------|
| $y_1$    | 5.01851851852  | -0.175309 $y_4$ | +63.997531 $y_6$ | -79 $y_7$ | +0.065432 $y_2$ | +47.069136 $y_9$  | -0.175309 $y_3$ | +1.018474 $y_{10}$ |
| $y_{16}$ | 0.462962962963 | -0.004938 $y_4$ | -0.572840 $y_6$  |           | +0.013580 $y_2$ | -0.627160 $y_9$   | -1.004938 $y_3$ | +0.010040 $y_{10}$ |
| $y_3$    | 78.2222222222  | +1.074074 $y_4$ | -43.740741 $y_6$ | -28 $y_7$ | -0.037037 $y_2$ | +75.074074 $y_9$  | +0.074074 $y_3$ | +1.031325 $y_{10}$ |
| $y_{11}$ | 0.611111111111 | +0.037037 $y_4$ | +1.629630 $y_6$  | +1 $y_7$  | -0.018519 $y_2$ | +2.037037 $y_9$   | +1.037037 $y_3$ | -1.048193 $y_{10}$ |
| $z$      | -65.8888888889 | -1.518519 $y_4$ | -84.148148 $y_6$ | -92 $y_7$ | -0.074074 $y_2$ | -153.851852 $y_9$ | -1.518519 $y_3$ | -0.010040 $y_{10}$ |

Final primal dictionary obtained:

|          |                 |                 |                   |                 |                   |
|----------|-----------------|-----------------|-------------------|-----------------|-------------------|
| $x_4$    | 1.51851851852   | $+0.175309x_1$  | $+0.004938x_{16}$ | $-1.074074x_3$  | $-0.037037x_{11}$ |
| $x_6$    | 84.1481481481   | $-63.997531x_1$ | $+0.572840x_{16}$ | $+43.740741x_3$ | $-1.629630x_{11}$ |
| $x_7$    | 92              | $+79x_1$        |                   | $+28x_3$        | $-1x_{11}$        |
| $x_2$    | 0.0740740740741 | $-0.065432x_1$  | $-0.013580x_{16}$ | $+0.037037x_3$  | $+0.018519x_{11}$ |
| $x_9$    | 153.851851852   | $-47.069136x_1$ | $+0.627160x_{16}$ | $-75.074074x_3$ | $-2.037037x_{11}$ |
| $x_8$    | 1.51851851852   | $+0.175309x_1$  | $+1.004938x_{16}$ | $-0.074074x_3$  | $-1.037037x_{11}$ |
| $x_5$    | 0.962962962963  | $-1.550617x_1$  | $-0.076543x_{16}$ | $-1.518519x_3$  | $+1.740741x_{11}$ |
| $x_{10}$ | 0.37037037037   | $-0.827160x_1$  | $+0.432099x_{16}$ | $-0.814815x_3$  | $+0.592593x_{11}$ |
| $x_{12}$ | 0.888888888889  | $-1.485185x_1$  | $-0.062963x_{16}$ | $-0.555556x_3$  | $+1.722222x_{11}$ |
| $x_{13}$ | 0.666666666667  | $-0.755556x_1$  | $+0.377778x_{16}$ | $-1x_3$         | $+1x_{11}$        |
| $x_9$    | 1               | $+1x_1$         | $+1x_{16}$        | $+0x_3$         | $-1x_{11}$        |
| $x_{15}$ | 0.481481481481  | $+1.824691x_1$  | $+0.995062x_{16}$ | $+0.074074x_3$  | $-0.962963x_{11}$ |
| $x_{14}$ | 0.481481481481  | $+1.824691x_1$  | $+0.995062x_{16}$ | $+0.074074x_3$  | $-0.962963x_{11}$ |
| $x_{17}$ | 0.296296296296  | $-0.761728x_1$  | $+0.445679x_{16}$ | $+0.148148x_3$  | $+0.574074x_{11}$ |
| $x_{18}$ | 0.777777777778  | $+0.896296x_1$  | $+0.940741x_{16}$ | $-0.111111x_3$  | $-0.555556x_{11}$ |
| $x_{19}$ | 0.481481481481  | $+1.824691x_1$  | $+0.995062x_{16}$ | $+0.074074x_3$  | $-0.962963x_{11}$ |
| $x_{20}$ | 0.777777777778  | $+0.896296x_1$  | $+0.940741x_{16}$ | $-0.111111x_3$  | $-0.555556x_{11}$ |
| $x_{21}$ | 0.37037037037   | $+1.172840x_1$  | $+0.432099x_{16}$ | $+0.185185x_3$  | $-0.407407x_{11}$ |
| $x_{22}$ | 0.851851851852  | $+0.830864x_1$  | $+0.927160x_{16}$ | $-0.074074x_3$  | $-0.537037x_{11}$ |
| $x_{23}$ | 0.0740740740741 | $+0.101235x_1$  | $+0.486420x_{16}$ | $+0.370370x_3$  | $+0.185185x_{11}$ |
| $z$      | 65.8888888889   | $-5.018519x_1$  | $-0.462963x_{16}$ | $-78.222222x_3$ | $-0.611111x_{11}$ |

After cutting plane is added

|          |                    |                 |                   |                 |                   |
|----------|--------------------|-----------------|-------------------|-----------------|-------------------|
| $x_4$    | 1.51851851852      | $+0.175309x_1$  | $+0.004938x_{16}$ | $-1.074074x_3$  | $-0.037037x_{11}$ |
| $x_6$    | 84.1481481481      | $-63.997531x_1$ | $+0.572840x_{16}$ | $+43.740741x_3$ | $-1.629630x_{11}$ |
| $x_7$    | 92                 | $+79x_1$        |                   | $+28x_3$        | $-1x_{11}$        |
| $x_2$    | 0.0740740740741    | $-0.065432x_1$  | $-0.013580x_{16}$ | $+0.037037x_3$  | $+0.018519x_{11}$ |
| $x_9$    | 153.851851852      | $-47.069136x_1$ | $+0.627160x_{16}$ | $-75.074074x_3$ | $-2.037037x_{11}$ |
| $x_8$    | 1.51851851852      | $+0.175309x_1$  | $+1.004938x_{16}$ | $-0.074074x_3$  | $-1.037037x_{11}$ |
| $x_5$    | 0.962962962963     | $-1.550617x_1$  | $-0.076543x_{16}$ | $-1.518519x_3$  | $+1.740741x_{11}$ |
| $x_{10}$ | 0.37037037037      | $-0.827160x_1$  | $+0.432099x_{16}$ | $-0.814815x_3$  | $+0.592593x_{11}$ |
| $x_{12}$ | 0.888888888889     | $-1.485185x_1$  | $-0.062963x_{16}$ | $-0.555556x_3$  | $+1.722222x_{11}$ |
| $x_{13}$ | 0.666666666667     | $-0.755556x_1$  | $+0.377778x_{16}$ | $-1x_3$         | $+1x_{11}$        |
| $x_9$    | 1                  | $+1x_1$         | $+1x_{16}$        | $+0x_3$         | $-1x_{11}$        |
| $x_{15}$ | 0.481481481481     | $+1.824691x_1$  | $+0.995062x_{16}$ | $+0.074074x_3$  | $-0.962963x_{11}$ |
| $x_{14}$ | 0.481481481481     | $+1.824691x_1$  | $+0.995062x_{16}$ | $+0.074074x_3$  | $-0.962963x_{11}$ |
| $x_{17}$ | 0.296296296296     | $-0.761728x_1$  | $+0.445679x_{16}$ | $+0.148148x_3$  | $+0.574074x_{11}$ |
| $x_{18}$ | 0.777777777778     | $+0.896296x_1$  | $+0.940741x_{16}$ | $-0.111111x_3$  | $-0.555556x_{11}$ |
| $x_{19}$ | 0.481481481481     | $+1.824691x_1$  | $+0.995062x_{16}$ | $+0.074074x_3$  | $-0.962963x_{11}$ |
| $x_{20}$ | 0.777777777778     | $+0.896296x_1$  | $+0.940741x_{16}$ | $-0.111111x_3$  | $-0.555556x_{11}$ |
| $x_{21}$ | 0.37037037037      | $+1.172840x_1$  | $+0.432099x_{16}$ | $+0.185185x_3$  | $-0.407407x_{11}$ |
| $x_{22}$ | 0.851851851852     | $+0.830864x_1$  | $+0.927160x_{16}$ | $-0.074074x_3$  | $-0.537037x_{11}$ |
| $x_{23}$ | 0.0740740740741    | $+0.101235x_1$  | $+0.486420x_{16}$ | $+0.370370x_3$  | $+0.185185x_{11}$ |
| $x_{24}$ | $-0.518518518519$  | $+0.824691x_1$  | $+0.995062x_{16}$ | $+0.074074x_3$  | $+0.037037x_{11}$ |
| $x_{25}$ | $-0.148148148148$  | $+0.997531x_1$  | $+0.427160x_{16}$ | $+0.259259x_3$  | $+0.629630x_{11}$ |
| $x_{26}$ | $-0.0740740740741$ | $+0.065432x_1$  | $+0.013580x_{16}$ | $+0.962963x_3$  | $+0.981481x_{11}$ |
| $x_{27}$ | $-0.851851851852$  | $+0.069136x_1$  | $+0.372840x_{16}$ | $+0.074074x_3$  | $+0.037037x_{11}$ |
| $x_{28}$ | $-0.518518518519$  | $+0.824691x_1$  | $+0.995062x_{16}$ | $+0.074074x_3$  | $+0.037037x_{11}$ |
| $x_{29}$ | $-0.962962962963$  | $+0.550617x_1$  | $+0.076543x_{16}$ | $+0.518519x_3$  | $+0.259259x_{11}$ |
| $x_{30}$ | $-0.37037037037$   | $+0.827160x_1$  | $+0.567901x_{16}$ | $+0.814815x_3$  | $+0.407407x_{11}$ |
| $x_{31}$ | $-0.888888888889$  | $+0.485185x_1$  | $+0.062963x_{16}$ | $+0.555556x_3$  | $+0.277778x_{11}$ |
| $x_{32}$ | $-0.666666666667$  | $+0.755556x_1$  | $+0.622222x_{16}$ | $+0x_3$         |                   |
| $x_{33}$ | $-0.481481481481$  | $+0.175309x_1$  | $+0.004938x_{16}$ | $+0.925926x_3$  | $+0.962963x_{11}$ |
| $x_{34}$ | $-0.481481481481$  | $+0.175309x_1$  | $+0.004938x_{16}$ | $+0.925926x_3$  | $+0.962963x_{11}$ |
| $x_{35}$ | $-0.296296296296$  | $+0.761728x_1$  | $+0.554321x_{16}$ | $+0.851852x_3$  | $+0.425926x_{11}$ |
| $x_{36}$ | $-0.777777777778$  | $+0.103704x_1$  | $+0.059259x_{16}$ | $+0.111111x_3$  | $+0.555556x_{11}$ |
| $x_{37}$ | $-0.481481481481$  | $+0.175309x_1$  | $+0.004938x_{16}$ | $+0.925926x_3$  | $+0.962963x_{11}$ |
| $x_{38}$ | $-0.777777777778$  | $+0.103704x_1$  | $+0.059259x_{16}$ | $+0.111111x_3$  | $+0.555556x_{11}$ |
| $x_{39}$ | $-0.37037037037$   | $+0.827160x_1$  | $+0.567901x_{16}$ | $+0.814815x_3$  | $+0.407407x_{11}$ |
| $x_{40}$ | $-0.851851851852$  | $+0.169136x_1$  | $+0.072840x_{16}$ | $+0.074074x_3$  | $+0.537037x_{11}$ |
| $x_{41}$ | $-0.0740740740741$ | $+0.898765x_1$  | $+0.513580x_{16}$ | $+0.629630x_3$  | $+0.814815x_{11}$ |
| $z$      | 65.8888888889      | $-5.018519x_1$  | $-0.462963x_{16}$ | $-78.222222x_3$ | $-0.611111x_{11}$ |



Forming the dual dictionary:

|          |                |   |
|----------|----------------|---|
| $y_1$    | 5.01851851852  | $-0.175309y_4 + 63.997531y_6 - 79y_7 + 0.065432y_2 + 47.069136y_9 - 0.175309y_8 + 1$  |
| $y_{16}$ | 0.462962962963 | $-0.004938y_4 - 0.572840y_6 + 0.013580y_2 - 0.627160y_9 - 1.004938y_8 + 0$            |
| $y_3$    | 78.2222222222  | $+1.074074y_4 - 43.740741y_6 - 28y_7 - 0.037037y_2 + 75.074074y_9 + 0.074074y_8 + 1$  |
| $y_{11}$ | 0.611111111111 | $+0.037037y_4 + 1.629630y_6 + 1y_7 - 0.018519y_2 + 2.037037y_9 + 1.037037y_8 - 1$     |
| $z$      | -65.8888888889 | $-1.518519y_4 - 84.148148y_6 - 92y_7 - 0.074074y_2 - 153.851852y_9 - 1.518519y_8 - 0$ |

The Final Dual Dictionary is:

|          |                |   |
|----------|----------------|---|
| $y_1$    | 2.86600496278  | $-0.205955y_4 + 63.724566y_6 - 80.230769y_7 + 0.047146y_2 + 46.459057y_9 + 1.58808$ |
| $y_{14}$ | 0.220843672457 | $-0.012407y_4 - 0.823821y_6 - 0.230769y_7 + 0.014888y_2 - 0.960298y_9 - 1.02481$    |
| $y_3$    | 76.5583126551  | $+1.024814y_4 - 45.352357y_6 - 29.538462y_7 - 0.029777y_2 + 72.920596y_9 + 0.04962$ |
| $y_{29}$ | 3.17741935484  | $+0.096774y_4 + 3.225806y_6 + 3y_7 - 0.016129y_2 + 4.290323y_9 + 0.19354$           |
| $z$      | -62.935483871  | $-1.419355y_4 - 80.645161y_6 - 89y_7 - 0.096774y_2 - 149.258065y_9 - 0.83871$       |

Final primal dictionary obtained:

|          |                       |                 |                   |                 |                   |
|----------|-----------------------|-----------------|-------------------|-----------------|-------------------|
| $x_4$    | 1.41935483871         | $+0.205955x_1$  | $+0.012407x_{14}$ | $-1.024814x_3$  | $-0.096774x_{29}$ |
| $x_6$    | 80.6451612903         | $-63.724566x_1$ | $+0.823821x_{14}$ | $+45.352357x_3$ | $-3.225806x_{29}$ |
| $x_7$    | 89                    | $+80.230769x_1$ | $+0.230769x_{14}$ | $+29.538462x_3$ | $-3x_{29}$        |
| $x_2$    | 0.0967741935484       | $-0.047146x_1$  | $-0.014888x_{14}$ | $+0.029777x_3$  | $+0.016129x_{29}$ |
| $x_9$    | 149.258064516         | $-46.459057x_1$ | $+0.960298x_{14}$ | $-72.920596x_3$ | $-4.290323x_{29}$ |
| $x_8$    | 0.838709677419        | $-1.588089x_1$  | $+1.024814x_{14}$ | $-0.049628x_3$  | $-0.193548x_{29}$ |
| $x_5$    | 6                     | $-3.461538x_1$  | $-0.461538x_{14}$ | $-4.076923x_3$  | $+5x_{29}$        |
| $x_{10}$ | 3.1935483871          | $-2.863524x_1$  | $+0.200993x_{14}$ | $-2.401985x_3$  | $+3.032258x_{29}$ |
| $x_{12}$ | 5.90322580645         | $-3.414392x_1$  | $-0.446650x_{14}$ | $-3.1067x_3$    | $+4.983871x_{29}$ |
| $x_{13}$ | 4.58064516129         | $-3.129032x_1$  | $+0.064516x_{14}$ | $-3.129032x_3$  | $+4.096774x_{29}$ |
| $x_{27}$ | 0.161290322581        | $-1.104218x_1$  | $+0.282878x_{14}$ | $-0.565757x_3$  | $+1.193548x_{29}$ |
| $x_{15}$ | $2.6645352591e - 15$  | $+0x_1$         | $+1x_{14}$        | $-0x_3$         |                   |
| $x_9$    | 0.41935483871         | $-0.794045x_1$  | $+1.012407x_{14}$ | $-0.024814x_3$  | $-0.096774x_{29}$ |
| $x_{17}$ | 3.09677419355         | $-2.816377x_1$  | $+0.215881x_{14}$ | $-1.431762x_3$  | $+3.016129x_{29}$ |
| $x_{18}$ | 1.38709677419         | $-1.265509x_1$  | $+0.863524x_{14}$ | $-0.727047x_3$  | $+1.064516x_{29}$ |
| $x_{19}$ | $1.11022302463e - 16$ | $-0x_1$         | $+1x_{14}$        | $+0x_3$         | $-0x_{29}$        |
| $x_{20}$ | 1.38709677419         | $-1.265509x_1$  | $+0.863524x_{14}$ | $-0.727047x_3$  | $+1.064516x_{29}$ |
| $x_{21}$ | 0.193548387097        | $+0.367246x_1$  | $+0.431762x_{14}$ | $+0.136476x_3$  | $+0.032258x_{29}$ |
| $x_{22}$ | 1.48387096774         | $-1.312655x_1$  | $+0.848635x_{14}$ | $-0.697270x_3$  | $+1.080645x_{29}$ |
| $x_{23}$ | 1.8064516129          | $-1.598015x_1$  | $+0.337469x_{14}$ | $-0.674938x_3$  | $+1.967742x_{29}$ |
| $x_{16}$ | 2.41935483871         | $-3.024814x_1$  | $+0.781638x_{14}$ | $-1.563275x_3$  | $+2.903226x_{29}$ |
| $x_{25}$ | 2.77419354839         | $-1.069479x_1$  | $+0.188586x_{14}$ | $-1.377171x_3$  | $+3.129032x_{29}$ |
| $x_{11}$ | 3                     | $-1.230769x_1$  | $-0.230769x_{14}$ | $-1.538462x_3$  | $+3x_{29}$        |
| $x_{24}$ | 2                     | $-2.230769x_1$  | $+0.769231x_{14}$ | $-1.538462x_3$  | $+3x_{29}$        |
| $x_{28}$ | 2                     | $-2.230769x_1$  | $+0.769231x_{14}$ | $-1.538462x_3$  | $+3x_{29}$        |
| $x_{26}$ | 2.90322580645         | $-1.183623x_1$  | $-0.215881x_{14}$ | $-0.568238x_3$  | $+2.983871x_{29}$ |
| $x_{30}$ | 2.22580645161         | $-1.392060x_1$  | $+0.349876x_{14}$ | $-0.699752x_3$  | $+2.870968x_{29}$ |
| $x_{31}$ | 0.0967741935484       | $-0.047146x_1$  | $-0.014888x_{14}$ | $+0.029777x_3$  | $+1.016129x_{29}$ |
| $x_{32}$ | 0.838709677419        | $-1.126551x_1$  | $+0.486352x_{14}$ | $-0.972705x_3$  | $+1.806452x_{29}$ |
| $x_{33}$ | 2.41935483871         | $-1.024814x_1$  | $-0.218362x_{14}$ | $-0.563275x_3$  | $+2.903226x_{29}$ |
| $x_{34}$ | 2.41935483871         | $-1.024814x_1$  | $-0.218362x_{14}$ | $-0.563275x_3$  | $+2.903226x_{29}$ |
| $x_{35}$ | 2.32258064516         | $-1.439206x_1$  | $+0.334988x_{14}$ | $-0.669975x_3$  | $+2.887097x_{29}$ |
| $x_{36}$ | 1.03225806452         | $-0.759305x_1$  | $-0.081886x_{14}$ | $-0.836228x_3$  | $+1.838710x_{29}$ |
| $x_{37}$ | 2.41935483871         | $-1.024814x_1$  | $-0.218362x_{14}$ | $-0.563275x_3$  | $+2.903226x_{29}$ |
| $x_{38}$ | 1.03225806452         | $-0.759305x_1$  | $-0.081886x_{14}$ | $-0.836228x_3$  | $+1.838710x_{29}$ |
| $x_{39}$ | 2.22580645161         | $-1.392060x_1$  | $+0.349876x_{14}$ | $-0.699752x_3$  | $+2.870968x_{29}$ |
| $x_{40}$ | 0.935483870968        | $-0.712159x_1$  | $-0.066998x_{14}$ | $-0.866005x_3$  | $+1.822581x_{29}$ |
| $x_{41}$ | 3.61290322581         | $-1.657568x_1$  | $+0.2134x_{14}$   | $-1.426799x_3$  | $+3.935484x_{29}$ |
| $z$      | 62.935483871          | $-2.866005x_1$  | $-0.220844x_{14}$ | $-76.558313x_3$ | $-3.177419x_{29}$ |

After cutting plane is added

|          |                       |                 |                   |                 |                   |
|----------|-----------------------|-----------------|-------------------|-----------------|-------------------|
| $x_4$    | 1.41935483871         | $+0.205955x_1$  | $+0.012407x_{14}$ | $-1.024814x_3$  | $-0.096774x_{29}$ |
| $x_6$    | 80.6451612903         | $-63.724566x_1$ | $+0.823821x_{14}$ | $+45.352357x_3$ | $-3.225806x_{29}$ |
| $x_7$    | 89                    | $+80.230769x_1$ | $+0.230769x_{14}$ | $+29.538462x_3$ | $-3x_{29}$        |
| $x_2$    | 0.0967741935484       | $-0.047146x_1$  | $-0.014888x_{14}$ | $+0.029777x_3$  | $+0.016129x_{29}$ |
| $x_9$    | 149.258064516         | $-46.459057x_1$ | $+0.960298x_{14}$ | $-72.920596x_3$ | $-4.290323x_{29}$ |
| $x_8$    | 0.838709677419        | $-1.588089x_1$  | $+1.024814x_{14}$ | $-0.049628x_3$  | $-0.193548x_{29}$ |
| $x_5$    | 6                     | $-3.461538x_1$  | $-0.461538x_{14}$ | $-4.076923x_3$  | $+5x_{29}$        |
| $x_{10}$ | 3.1935483871          | $-2.863524x_1$  | $+0.200993x_{14}$ | $-2.401985x_3$  | $+3.032258x_{29}$ |
| $x_{12}$ | 5.90322580645         | $-3.414392x_1$  | $-0.446650x_{14}$ | $-3.1067x_3$    | $+4.983871x_{29}$ |
| $x_{13}$ | 4.58064516129         | $-3.129032x_1$  | $+0.064516x_{14}$ | $-3.129032x_3$  | $+4.096774x_{29}$ |
| $x_{27}$ | 0.161290322581        | $-1.104218x_1$  | $+0.282878x_{14}$ | $-0.565757x_3$  | $+1.193548x_{29}$ |
| $x_{15}$ | $2.6645352591e - 15$  | $+0x_1$         | $+1x_{14}$        | $-0x_3$         |                   |
| $x_9$    | 0.41935483871         | $-0.794045x_1$  | $+1.012407x_{14}$ | $-0.024814x_3$  | $-0.096774x_{29}$ |
| $x_{17}$ | 3.09677419355         | $-2.816377x_1$  | $+0.215881x_{14}$ | $-1.431762x_3$  | $+3.016129x_{29}$ |
| $x_{18}$ | 1.38709677419         | $-1.265509x_1$  | $+0.863524x_{14}$ | $-0.727047x_3$  | $+1.064516x_{29}$ |
| $x_{19}$ | $1.11022302463e - 16$ | $-0x_1$         | $+1x_{14}$        | $+0x_3$         | $-0x_{29}$        |
| $x_{20}$ | 1.38709677419         | $-1.265509x_1$  | $+0.863524x_{14}$ | $-0.727047x_3$  | $+1.064516x_{29}$ |
| $x_{21}$ | 0.193548387097        | $+0.367246x_1$  | $+0.431762x_{14}$ | $+0.136476x_3$  | $+0.032258x_{29}$ |
| $x_{22}$ | 1.48387096774         | $-1.312655x_1$  | $+0.848635x_{14}$ | $-0.697270x_3$  | $+1.080645x_{29}$ |
| $x_{23}$ | 1.8064516129          | $-1.598015x_1$  | $+0.337469x_{14}$ | $-0.674938x_3$  | $+1.967742x_{29}$ |
| $x_{16}$ | 2.41935483871         | $-3.024814x_1$  | $+0.781638x_{14}$ | $-1.563275x_3$  | $+2.903226x_{29}$ |
| $x_{25}$ | 2.77419354839         | $-1.069479x_1$  | $+0.188586x_{14}$ | $-1.377171x_3$  | $+3.129032x_{29}$ |
| $x_{11}$ | 3                     | $-1.230769x_1$  | $-0.230769x_{14}$ | $-1.538462x_3$  | $+3x_{29}$        |
| $x_{24}$ | 2                     | $-2.230769x_1$  | $+0.769231x_{14}$ | $-1.538462x_3$  | $+3x_{29}$        |
| $x_{28}$ | 2                     | $-2.230769x_1$  | $+0.769231x_{14}$ | $-1.538462x_3$  | $+3x_{29}$        |
| $x_{26}$ | 2.90322580645         | $-1.183623x_1$  | $-0.215881x_{14}$ | $-0.568238x_3$  | $+2.983871x_{29}$ |
| $x_{30}$ | 2.22580645161         | $-1.392060x_1$  | $+0.349876x_{14}$ | $-0.699752x_3$  | $+2.870968x_{29}$ |
| $x_{31}$ | 0.0967741935484       | $-0.047146x_1$  | $-0.014888x_{14}$ | $+0.029777x_3$  | $+1.016129x_{29}$ |
| $x_{32}$ | 0.838709677419        | $-1.126551x_1$  | $+0.486352x_{14}$ | $-0.972705x_3$  | $+1.806452x_{29}$ |
| $x_{33}$ | 2.41935483871         | $-1.024814x_1$  | $-0.218362x_{14}$ | $-0.563275x_3$  | $+2.903226x_{29}$ |
| $x_{34}$ | 2.41935483871         | $-1.024814x_1$  | $-0.218362x_{14}$ | $-0.563275x_3$  | $+2.903226x_{29}$ |
| $x_{35}$ | 2.32258064516         | $-1.439206x_1$  | $+0.334988x_{14}$ | $-0.669975x_3$  | $+2.887097x_{29}$ |
| $x_{36}$ | 1.03225806452         | $-0.759305x_1$  | $-0.081886x_{14}$ | $-0.836228x_3$  | $+1.838710x_{29}$ |
| $x_{37}$ | 2.41935483871         | $-1.024814x_1$  | $-0.218362x_{14}$ | $-0.563275x_3$  | $+2.903226x_{29}$ |
| $x_{38}$ | 1.03225806452         | $-0.759305x_1$  | $-0.081886x_{14}$ | $-0.836228x_3$  | $+1.838710x_{29}$ |
| $x_{39}$ | 2.22580645161         | $-1.392060x_1$  | $+0.349876x_{14}$ | $-0.699752x_3$  | $+2.870968x_{29}$ |
| $x_{40}$ | 0.935483870968        | $-0.712159x_1$  | $-0.066998x_{14}$ | $-0.866005x_3$  | $+1.822581x_{29}$ |
| $x_{41}$ | 3.61290322581         | $-1.657568x_1$  | $+0.2134x_{14}$   | $-1.426799x_3$  | $+3.935484x_{29}$ |
| $x_{42}$ | $-0.41935483871$      | $+0.794045x_1$  | $+0.987593x_{14}$ | $+0.024814x_3$  | $+0.096774x_{29}$ |
| $x_{43}$ | $-0.645161290323$     | $+0.724566x_1$  | $+0.176179x_{14}$ | $+0.647643x_3$  | $+0.225806x_{29}$ |
| $x_{44}$ | $-0.0967741935484$    | $+0.047146x_1$  | $+0.014888x_{14}$ | $+0.970223x_3$  | $+0.983871x_{29}$ |
| $x_{45}$ | $-0.258064516129$     | $+0.459057x_1$  | $+0.039702x_{14}$ | $+0.920596x_3$  | $+0.290323x_{29}$ |
| $x_{46}$ | $-0.838709677419$     | $+0.588089x_1$  | $+0.975186x_{14}$ | $+0.049628x_3$  | $+0.193548x_{29}$ |
| $x_{47}$ | $-0.193548387097$     | $+0.863524x_1$  | $+0.799007x_{14}$ | $+0.401985x_3$  | $+0.967742x_{29}$ |
| $x_{48}$ | $-0.903225806452$     | $+0.414392x_1$  | $+0.446650x_{14}$ | $+0.1067x_3$    | $+0.016129x_{29}$ |
| $x_{49}$ | $-0.58064516129$      | $+0.129032x_1$  | $+0.935484x_{14}$ | $+0.129032x_3$  | $+0.903226x_{29}$ |
| $x_{50}$ | $-0.161290322581$     | $+0.104218x_1$  | $+0.717122x_{14}$ | $+0.565757x_3$  | $+0.806452x_{29}$ |
| $x_{51}$ | $-0.41935483871$      | $+0.794045x_1$  | $+0.987593x_{14}$ | $+0.024814x_3$  | $+0.096774x_{29}$ |

Forming the dual dictionary:

|          |                |   |
|----------|----------------|---|
| $y_1$    | 2.86600496278  | $-0.205955y_4 + 63.724566y_6 - 80.230769y_7 + 0.047146y_2 + 46.459057y_9 + 1.58808$ |
| $y_{14}$ | 0.220843672457 | $-0.012407y_4 - 0.823821y_6 - 0.230769y_7 + 0.014888y_2 - 0.960298y_9 - 1.02481$    |
| $y_3$    | 76.5583126551  | $+1.024814y_4 - 45.352357y_6 - 29.538462y_7 - 0.029777y_2 + 72.920596y_9 + 0.04962$ |
| $y_{29}$ | 3.17741935484  | $+0.096774y_4 + 3.225806y_6 + 3y_7 - 0.016129y_2 + 4.290323y_9 + 0.19354$           |
| $z$      | -62.935483871  | $-1.419355y_4 - 80.645161y_6 - 89y_7 - 0.096774y_2 - 149.258065y_9 - 0.83871$       |

The Final Dual Dictionary is:

|          |                |   |
|----------|----------------|---|
| $y_2$    | 7              | $-0.5y_4 + 621.5y_6 - 657.5y_7 - 8.5y_1 + 488.5y_9 + 109y_8 - 18.5y_5 +$            |
| $y_{71}$ | 4.3333333333   | $-0.333333y_4 + 132.666667y_6 - 159y_7 - 2y_1 + 99y_9 + 9.666667y_8 + 4y_5 +$       |
| $y_3$    | 70.3333333333  | $+1.166667y_4 - 148.833333y_6 + 86.5y_7 + 1.5y_1 - 6.5y_9 - 8.333333y_8 + 6.5y_5 -$ |
| $y_{44}$ | 2.3333333333   | $+0.166667y_4 - 30.833333y_6 + 42.5y_7 + 0.5y_1 - 21.5y_9 - 3.333333y_8 - 5.5y_5 -$ |
| $z$      | -59.3333333333 | $-1.666667y_4 - 19.666667y_6 - 170y_7 - 1y_1 - 106y_9 - 2.666667y_8 - 1y_5 -$       |

Final primal dictionary obtained:

|          |                        |             |                     |                  |                    |
|----------|------------------------|-------------|---------------------|------------------|--------------------|
| $x_4$    | 1.6666666667           | $+0.5x_2$   | $+0.333333x_{71}$   | $-1.166667x_3$   | $-0.166667x_{44}$  |
| $x_6$    | 19.6666666667          | $-621.5x_2$ | $-132.666667x_{71}$ | $+148.833333x_3$ | $+30.833333x_{44}$ |
| $x_7$    | 170                    | $+657.5x_2$ | $+159x_{71}$        | $-86.5x_3$       | $-42.5x_{44}$      |
| $x_1$    | 1                      | $+8.5x_2$   | $+2x_{71}$          | $-1.5x_3$        | $-0.5x_{44}$       |
| $x_9$    | 106                    | $-488.5x_2$ | $-99x_{71}$         | $+6.5x_3$        | $+21.5x_{44}$      |
| $x_8$    | 2.6666666667           | $-109x_2$   | $-9.666667x_{71}$   | $+8.333333x_3$   | $+3.333333x_{44}$  |
| $x_5$    | 1                      | $+18.5x_2$  | $-4x_{71}$          | $-6.5x_3$        | $+5.5x_{44}$       |
| $x_{10}$ | 1                      | $-40x_2$    | $-7x_{71}$          | $+0x_3$          | $+5x_{44}$         |
| $x_{12}$ | 1                      | $+17.5x_2$  | $-4x_{71}$          | $-5.5x_3$        | $+5.5x_{44}$       |
| $x_{13}$ | 1.6666666667           | $-28.5x_2$  | $-6.666667x_{71}$   | $-2.166667x_3$   | $+5.833333x_{44}$  |
| $x_{27}$ | $-1.69642078163e - 13$ | $-34.5x_2$  | $-4x_{71}$          | $+1.5x_3$        | $+2.5x_{44}$       |
| $x_{15}$ | 3.3333333333           | $-93x_2$    | $-6.333333x_{71}$   | $+5.666667x_3$   | $+2.666667x_{44}$  |
| $x_9$    | 3                      | $-101x_2$   | $-8x_{71}$          | $+7x_3$          | $+3x_{44}$         |
| $x_{17}$ | 1                      | $-41x_2$    | $-7x_{71}$          | $+1x_3$          | $+5x_{44}$         |
| $x_{18}$ | 3                      | $-90x_2$    | $-8x_{71}$          | $+5x_3$          | $+4x_{44}$         |
| $x_{19}$ | 3.3333333333           | $-93x_2$    | $-6.333333x_{71}$   | $+5.666667x_3$   | $+2.666667x_{44}$  |
| $x_{20}$ | 3                      | $-90x_2$    | $-8x_{71}$          | $+5x_3$          | $+4x_{44}$         |
| $x_{21}$ | 2                      | $-37x_2$    | $-2x_{71}$          | $+2x_3$          | $+1x_{44}$         |
| $x_{22}$ | 3                      | $-89x_2$    | $-8x_{71}$          | $+5x_3$          | $+4x_{44}$         |
| $x_{23}$ | 1.3333333333           | $-43x_2$    | $-5.333333x_{71}$   | $+1.666667x_3$   | $+3.666667x_{44}$  |
| $x_{16}$ | 2                      | $-95.5x_2$  | $-11x_{71}$         | $+4.5x_3$        | $+6.5x_{44}$       |
| $x_{25}$ | 2.3333333333           | $-23.5x_2$  | $-3.333333x_{71}$   | $-1.833333x_3$   | $+4.166667x_{44}$  |
| $x_{11}$ | 1                      | $+14x_2$    | $-1x_{71}$          | $-4x_3$          | $+3x_{44}$         |
| $x_{24}$ | 2.3333333333           | $-87.5x_2$  | $-9.333333x_{71}$   | $+3.166667x_3$   | $+6.166667x_{44}$  |
| $x_{28}$ | 2.3333333333           | $-87.5x_2$  | $-9.333333x_{71}$   | $+3.166667x_3$   | $+6.166667x_{44}$  |
| $x_{26}$ | 1                      | $+13x_2$    | $-1x_{71}$          | $-3x_3$          | $+3x_{44}$         |
| $x_{30}$ | 2                      | $-41.5x_2$  | $-5x_{71}$          | $+0.5x_3$        | $+4.5x_{44}$       |
| $x_{31}$ | $1.94289029309e - 16$  | $+2x_2$     | $-0x_{71}$          | $-1x_3$          | $+1x_{44}$         |
| $x_{32}$ | 1.3333333333           | $-53x_2$    | $-5.333333x_{71}$   | $+1.666667x_3$   | $+3.666667x_{44}$  |
| $x_{33}$ | 0.6666666667           | $+14.5x_2$  | $-0.666667x_{71}$   | $-3.166667x_3$   | $+2.833333x_{44}$  |
| $x_{34}$ | 0.6666666667           | $+14.5x_2$  | $-0.666667x_{71}$   | $-3.166667x_3$   | $+2.833333x_{44}$  |
| $x_{35}$ | 2                      | $-40.5x_2$  | $-5x_{71}$          | $+0.5x_3$        | $+4.5x_{44}$       |
| $x_{36}$ | $-3.10307335383e - 14$ | $+3x_2$     | $-1x_{71}$          | $-2x_3$          | $+2x_{44}$         |
| $x_{37}$ | 0.6666666667           | $+14.5x_2$  | $-0.666667x_{71}$   | $-3.166667x_3$   | $+2.833333x_{44}$  |
| $x_{38}$ | $2.77555756156e - 16$  | $+3x_2$     | $-1x_{71}$          | $-2x_3$          | $+2x_{44}$         |
| $x_{39}$ | 2                      | $-41.5x_2$  | $-5x_{71}$          | $+0.5x_3$        | $+4.5x_{44}$       |
| $x_{40}$ | $-5.55111512313e - 17$ | $+2x_2$     | $-1x_{71}$          | $-2x_3$          | $+2x_{44}$         |
| $x_{41}$ | 2.6666666667           | $-30x_2$    | $-4.666667x_{71}$   | $-1.666667x_3$   | $+5.333333x_{44}$  |
| $x_{14}$ | 3.3333333333           | $-93x_2$    | $-6.333333x_{71}$   | $+5.666667x_3$   | $+2.666667x_{44}$  |
| $x_{42}$ | 3.6666666667           | $-85x_2$    | $-4.666667x_{71}$   | $+4.333333x_3$   | $+2.333333x_{44}$  |
| $x_{29}$ | $1.38777878078e - 17$  | $+1x_2$     | $+0x_{71}$          | $-1x_3$          | $+1x_{44}$         |
| $x_{43}$ | 0.6666666667           | $-10x_2$    | $+0.333333x_{71}$   | $+0.333333x_3$   | $+0.333333x_{44}$  |
| $x_{46}$ | 3                      | $-85.5x_2$  | $-5x_{71}$          | $+4.5x_3$        | $+2.5x_{44}$       |
| $x_{47}$ | 3.3333333333           | $-66x_2$    | $-3.333333x_{71}$   | $+2.666667x_3$   | $+2.666667x_{44}$  |
| $x_{48}$ | 1                      | $-38x_2$    | $-2x_{71}$          | $+2x_3$          | $+1x_{44}$         |
| $x_{49}$ | 2.6666666667           | $-85x_2$    | $-5.666667x_{71}$   | $+4.333333x_3$   | $+3.333333x_{44}$  |
| $x_{50}$ | 2.3333333333           | $-65x_2$    | $-4.333333x_{71}$   | $+3.666667x_3$   | $+2.666667x_{44}$  |
| $x_{51}$ | 3.6666666667           | $-85x_2$    | $-4.666667x_{71}$   | $+4.333333x_3$   | $+2.333333x_{44}$  |

After cutting plane is added

|          |                        |             |                     |                  |                    |
|----------|------------------------|-------------|---------------------|------------------|--------------------|
| $x_4$    | 1.66666666667          | $+0.5x_2$   | $+0.333333x_{71}$   | $-1.166667x_3$   | $-0.166667x_{44}$  |
| $x_6$    | 19.6666666667          | $-621.5x_2$ | $-132.666667x_{71}$ | $+148.833333x_3$ | $+30.833333x_{44}$ |
| $x_7$    | 170                    | $+657.5x_2$ | $+159x_{71}$        | $-86.5x_3$       | $-42.5x_{44}$      |
| $x_1$    | 1                      | $+8.5x_2$   | $+2x_{71}$          | $-1.5x_3$        | $-0.5x_{44}$       |
| $x_9$    | 106                    | $-488.5x_2$ | $-99x_{71}$         | $+6.5x_3$        | $+21.5x_{44}$      |
| $x_8$    | 2.66666666667          | $-109x_2$   | $-9.666667x_{71}$   | $+8.333333x_3$   | $+3.333333x_{44}$  |
| $x_5$    | 1                      | $+18.5x_2$  | $-4x_{71}$          | $-6.5x_3$        | $+5.5x_{44}$       |
| $x_{10}$ | 1                      | $-40x_2$    | $-7x_{71}$          | $+0x_3$          | $+5x_{44}$         |
| $x_{12}$ | 1                      | $+17.5x_2$  | $-4x_{71}$          | $-5.5x_3$        | $+5.5x_{44}$       |
| $x_{13}$ | 1.66666666667          | $-28.5x_2$  | $-6.666667x_{71}$   | $-2.166667x_3$   | $+5.833333x_{44}$  |
| $x_{27}$ | $-1.69642078163e - 13$ | $-34.5x_2$  | $-4x_{71}$          | $+1.5x_3$        | $+2.5x_{44}$       |
| $x_{15}$ | 3.33333333333          | $-93x_2$    | $-6.333333x_{71}$   | $+5.666667x_3$   | $+2.666667x_{44}$  |
| $x_9$    | 3                      | $-101x_2$   | $-8x_{71}$          | $+7x_3$          | $+3x_{44}$         |
| $x_{17}$ | 1                      | $-41x_2$    | $-7x_{71}$          | $+1x_3$          | $+5x_{44}$         |
| $x_{18}$ | 3                      | $-90x_2$    | $-8x_{71}$          | $+5x_3$          | $+4x_{44}$         |
| $x_{19}$ | 3.33333333333          | $-93x_2$    | $-6.333333x_{71}$   | $+5.666667x_3$   | $+2.666667x_{44}$  |
| $x_{20}$ | 3                      | $-90x_2$    | $-8x_{71}$          | $+5x_3$          | $+4x_{44}$         |
| $x_{21}$ | 2                      | $-37x_2$    | $-2x_{71}$          | $+2x_3$          | $+1x_{44}$         |
| $x_{22}$ | 3                      | $-89x_2$    | $-8x_{71}$          | $+5x_3$          | $+4x_{44}$         |
| $x_{23}$ | 1.33333333333          | $-43x_2$    | $-5.333333x_{71}$   | $+1.666667x_3$   | $+3.666667x_{44}$  |
| $x_{16}$ | 2                      | $-95.5x_2$  | $-11x_{71}$         | $+4.5x_3$        | $+6.5x_{44}$       |
| $x_{25}$ | 2.33333333333          | $-23.5x_2$  | $-3.333333x_{71}$   | $-1.833333x_3$   | $+4.166667x_{44}$  |
| $x_{11}$ | 1                      | $+14x_2$    | $-1x_{71}$          | $-4x_3$          | $+3x_{44}$         |
| $x_{24}$ | 2.33333333333          | $-87.5x_2$  | $-9.333333x_{71}$   | $+3.166667x_3$   | $+6.166667x_{44}$  |
| $x_{28}$ | 2.33333333333          | $-87.5x_2$  | $-9.333333x_{71}$   | $+3.166667x_3$   | $+6.166667x_{44}$  |
| $x_{26}$ | 1                      | $+13x_2$    | $-1x_{71}$          | $-3x_3$          | $+3x_{44}$         |
| $x_{30}$ | 2                      | $-41.5x_2$  | $-5x_{71}$          | $+0.5x_3$        | $+4.5x_{44}$       |
| $x_{31}$ | $1.94289029309e - 16$  | $+2x_2$     | $-0x_{71}$          | $-1x_3$          | $+1x_{44}$         |
| $x_{32}$ | 1.33333333333          | $-53x_2$    | $-5.333333x_{71}$   | $+1.666667x_3$   | $+3.666667x_{44}$  |
| $x_{33}$ | 0.66666666667          | $+14.5x_2$  | $-0.666667x_{71}$   | $-3.166667x_3$   | $+2.833333x_{44}$  |
| $x_{34}$ | 0.66666666667          | $+14.5x_2$  | $-0.666667x_{71}$   | $-3.166667x_3$   | $+2.833333x_{44}$  |
| $x_{35}$ | 2                      | $-40.5x_2$  | $-5x_{71}$          | $+0.5x_3$        | $+4.5x_{44}$       |
| $x_{36}$ | $-3.10307335383e - 14$ | $+3x_2$     | $-1x_{71}$          | $-2x_3$          | $+2x_{44}$         |
| $x_{37}$ | 0.66666666667          | $+14.5x_2$  | $-0.666667x_{71}$   | $-3.166667x_3$   | $+2.833333x_{44}$  |
| $x_{38}$ | $2.77555756156e - 16$  | $+3x_2$     | $-1x_{71}$          | $-2x_3$          | $+2x_{44}$         |
| $x_{39}$ | 2                      | $-41.5x_2$  | $-5x_{71}$          | $+0.5x_3$        | $+4.5x_{44}$       |
| $x_{40}$ | $-5.55111512313e - 17$ | $+2x_2$     | $-1x_{71}$          | $-2x_3$          | $+2x_{44}$         |
| $x_{41}$ | 2.66666666667          | $-30x_2$    | $-4.666667x_{71}$   | $-1.666667x_3$   | $+5.333333x_{44}$  |
| $x_{14}$ | 3.33333333333          | $-93x_2$    | $-6.333333x_{71}$   | $+5.666667x_3$   | $+2.666667x_{44}$  |
| $x_{42}$ | 3.66666666667          | $-85x_2$    | $-4.666667x_{71}$   | $+4.333333x_3$   | $+2.333333x_{44}$  |
| $x_{29}$ | $1.38777878078e - 17$  | $+12x_2$    | $+0x_{71}$          | $-1x_3$          | $+1x_{44}$         |
| $x_{43}$ | 0.66666666667          | $-10x_2$    | $+0.333333x_{71}$   | $+0.333333x_3$   | $+0.333333x_{44}$  |
| $x_{46}$ | 3                      | $-85.5x_2$  | $-5x_{71}$          | $+4.5x_3$        | $+2.5x_{44}$       |
| $x_{47}$ | 3.33333333333          | $-66x_2$    | $-3.333333x_{71}$   | $+2.666667x_3$   | $+2.666667x_{44}$  |
| $x_{48}$ | 1                      | $-38x_2$    | $-2x_{71}$          | $+2x_3$          | $+1x_{44}$         |
| $x_{49}$ | 2.66666666667          | $-85x_2$    | $-5.666667x_{71}$   | $+4.333333x_3$   | $+3.333333x_{44}$  |
| $x_{50}$ | 2.33333333333          | $-65x_2$    | $-4.333333x_{71}$   | $+3.666667x_3$   | $+2.666667x_{44}$  |
| $x_{51}$ | 3.66666666667          | $-85x_2$    | $-4.666667x_{71}$   | $+4.333333x_3$   | $+2.333333x_{44}$  |

Forming the dual dictionary:

|          |                  |                |                  |             |           |             |                |            |   |
|----------|------------------|----------------|------------------|-------------|-----------|-------------|----------------|------------|---|
| $y_2$    | 7                | $-0.5y_4$      | $+621.5y_6$      | $-657.5y_7$ | $-8.5y_1$ | $+488.5y_9$ | $+109y_8$      | $-18.5y_5$ | + |
| $y_{71}$ | 4.3333333333     | $-0.333333y_4$ | $+132.666667y_6$ | $-159y_7$   | $-2y_1$   | $+99y_9$    | $+9.666667y_8$ | $+4y_5$    | + |
| $y_3$    | 70.3333333333    | $+1.166667y_4$ | $-148.833333y_6$ | $+86.5y_7$  | $+1.5y_1$ | $-6.5y_9$   | $-8.333333y_8$ | $+6.5y_5$  | - |
| $y_{44}$ | 2.3333333333     | $+0.166667y_4$ | $-30.833333y_6$  | $+42.5y_7$  | $+0.5y_1$ | $-21.5y_9$  | $-3.333333y_8$ | $-5.5y_5$  | - |
| $z$      | $-59.3333333333$ | $-1.666667y_4$ | $-19.666667y_6$  | $-170y_7$   | $-1y_1$   | $-106y_9$   | $-2.666667y_8$ | $-1y_5$    | - |

The Final Dual Dictionary is:

|          |                |                |                   |                  |                |                  |                 |                |   |
|----------|----------------|----------------|-------------------|------------------|----------------|------------------|-----------------|----------------|---|
| $y_2$    | 13.9453125     | $+1.789063y_4$ | $-8.156250y_{44}$ | $+132.601563y_7$ | $+1.156250y_1$ | $+37.023437y_9$  | $+54.851562y_8$ | $+5.601562y_5$ | + |
| $y_{73}$ | 10.38671875    | $+0.277344y_4$ | $-3.109375y_{44}$ | $+17.246094y_7$  | $+0.109375y_1$ | $+4.691406y_9$   | $+3.378906y_8$  | $+0.378906y_5$ | + |
| $y_3$    | 65.6953125     | $+0.539063y_4$ | $+2.843750y_{44}$ | $-107.648437y_7$ | $-0.843750y_1$ | $+100.273438y_9$ | $+5.601562y_8$  | $+5.601562y_5$ | + |
| $y_6$    | 0.01953125     | $+0.003906y_4$ | $-0.015625y_{44}$ | $+1.285156y_7$   | $+0.015625y_1$ | $-0.722656y_9$   | $-0.089844y_8$  | $-0.089844y_5$ | - |
| $z$      | $-52.79296875$ | $-1.558594y_4$ | $-1.765625y_{44}$ | $-183.777344y_7$ | $-1.234375y_1$ | $-88.660156y_9$  | $-3.152344y_8$  | $-3.152344y_5$ | - |

Final primal dictionary obtained:

|          |              |                  |                    |                  |                |
|----------|--------------|------------------|--------------------|------------------|----------------|
| $x_4$    | 1.55859375   | $-1.789063x_2$   | $-0.277344x_{73}$  | $-0.539063x_3$   | $-0.003906x_6$ |
| $x_{44}$ | 1.765625     | $+8.156250x_2$   | $+3.109375x_{73}$  | $-2.843750x_3$   | $+0.015625x_6$ |
| $x_7$    | 183.77734375 | $-132.601563x_2$ | $-17.246094x_{73}$ | $+107.648437x_3$ | $-1.285156x_6$ |
| $x_1$    | 1.234375     | $-1.156250x_2$   | $-0.109375x_{73}$  | $+0.843750x_3$   | $-0.015625x_6$ |
| $x_9$    | 88.66015625  | $-37.023437x_2$  | $-4.691406x_{73}$  | $-100.273438x_3$ | $+0.722656x_6$ |
| $x_8$    | 3.15234375   | $-54.851562x_2$  | $+3.378906x_{73}$  | $-5.601562x_3$   | $+0.089844x_6$ |
| $x_5$    | 8.4765625    | $+74.515625x_2$  | $+14.210937x_{73}$ | $-23.984375x_3$  | $+0.101562x_6$ |
| $x_{10}$ | 5.91796875   | $+20.304688x_2$  | $+10.488281x_{73}$ | $-17.445312x_3$  | $+0.105469x_6$ |
| $x_{12}$ | 8.4765625    | $+73.515625x_2$  | $+14.210937x_{73}$ | $-22.984375x_3$  | $+0.101562x_6$ |
| $x_{13}$ | 8.2421875    | $+37.671875x_2$  | $+13.320312x_{73}$ | $-21.828125x_3$  | $+0.117187x_6$ |
| $x_{27}$ | 2.1796875    | $-2.953125x_2$   | $+4.882812x_{73}$  | $-7.453125x_3$   | $+0.054687x_6$ |
| $x_{15}$ | 4.50390625   | $-53.585937x_2$  | $+3.714844x_{73}$  | $-4.835937x_3$   | $+0.066406x_6$ |
| $x_9$    | 3.828125     | $-54.218750x_2$  | $+3.546875x_{73}$  | $-5.218750x_3$   | $+0.078125x_6$ |
| $x_{17}$ | 5.91796875   | $+19.304688x_2$  | $+10.488281x_{73}$ | $-16.445312x_3$  | $+0.105469x_6$ |
| $x_{18}$ | 5.59375      | $-35.0625x_2$    | $+6.656250x_{73}$  | $-10.0625x_3$    | $+0.093750x_6$ |
| $x_{19}$ | 4.50390625   | $-53.585938x_2$  | $+3.714844x_{73}$  | $-4.835937x_3$   | $+0.066406x_6$ |
| $x_{20}$ | 5.59375      | $-35.0625x_2$    | $+6.656250x_{73}$  | $-10.0625x_3$    | $+0.093750x_6$ |
| $x_{21}$ | 2.6484375    | $-23.265625x_2$  | $+1.664062x_{73}$  | $-1.765625x_3$   | $+0.023437x_6$ |
| $x_{22}$ | 5.59375      | $-34.0625x_2$    | $+6.656250x_{73}$  | $-10.0625x_3$    | $+0.093750x_6$ |
| $x_{23}$ | 4.828125     | $+1.781250x_2$   | $+7.546875x_{73}$  | $-11.218750x_3$  | $+0.078125x_6$ |
| $x_{16}$ | 7.33203125   | $-11.804687x_2$  | $+12.261719x_{73}$ | $-19.054687x_3$  | $+0.144531x_6$ |
| $x_{25}$ | 7.828125     | $+19.781250x_2$  | $+10.546875x_{73}$ | $-15.218750x_3$  | $+0.078125x_6$ |
| $x_{11}$ | 5.73828125   | $+41.257813x_2$  | $+8.605469x_{73}$  | $-12.992187x_3$  | $+0.050781x_6$ |
| $x_{24}$ | 8.0078125    | $-11.171875x_2$  | $+12.429687x_{73}$ | $-18.671875x_3$  | $+0.132812x_6$ |
| $x_{28}$ | 8.0078125    | $-11.171875x_2$  | $+12.429687x_{73}$ | $-18.671875x_3$  | $+0.132812x_6$ |
| $x_{26}$ | 5.73828125   | $+40.257813x_2$  | $+8.605469x_{73}$  | $-11.992187x_3$  | $+0.050781x_6$ |
| $x_{30}$ | 7.15234375   | $+9.148437x_2$   | $+10.378906x_{73}$ | $-14.601562x_3$  | $+0.089844x_6$ |
| $x_{31}$ | 1.765625     | $+10.156250x_2$  | $+3.109375x_{73}$  | $-3.843750x_3$   | $+0.015625x_6$ |
| $x_{32}$ | 4.828125     | $-8.218750x_2$   | $+7.546875x_{73}$  | $-11.218750x_3$  | $+0.078125x_6$ |
| $x_{33}$ | 5.296875     | $+39.468750x_2$  | $+8.328125x_{73}$  | $-11.531250x_3$  | $+0.046875x_6$ |
| $x_{34}$ | 5.296875     | $+39.468750x_2$  | $+8.328125x_{73}$  | $-11.531250x_3$  | $+0.046875x_6$ |
| $x_{35}$ | 7.15234375   | $+10.148437x_2$  | $+10.378906x_{73}$ | $-14.601562x_3$  | $+0.089844x_6$ |
| $x_{36}$ | 2.97265625   | $+22.101563x_2$  | $+5.496094x_{73}$  | $-8.148437x_3$   | $+0.035156x_6$ |
| $x_{37}$ | 5.296875     | $+39.468750x_2$  | $+8.328125x_{73}$  | $-11.531250x_3$  | $+0.046875x_6$ |
| $x_{38}$ | 2.97265625   | $+22.101562x_2$  | $+5.496094x_{73}$  | $-8.148437x_3$   | $+0.035156x_6$ |
| $x_{39}$ | 7.15234375   | $+9.148437x_2$   | $+10.378906x_{73}$ | $-14.601562x_3$  | $+0.089844x_6$ |
| $x_{40}$ | 2.97265625   | $+21.101562x_2$  | $+5.496094x_{73}$  | $-8.148437x_3$   | $+0.035156x_6$ |
| $x_{41}$ | 9.4765625    | $+26.515625x_2$  | $+13.210937x_{73}$ | $-18.984375x_3$  | $+0.101562x_6$ |
| $x_{14}$ | 4.50390625   | $-53.585937x_2$  | $+3.714844x_{73}$  | $-4.835937x_3$   | $+0.066406x_6$ |
| $x_{42}$ | 5.1796875    | $-52.953125x_2$  | $+3.882812x_{73}$  | $-4.453125x_3$   | $+0.054687x_6$ |
| $x_{29}$ | 1.765625     | $+9.156250x_2$   | $+3.109375x_{73}$  | $-3.843750x_3$   | $+0.015625x_6$ |
| $x_{43}$ | 1.44140625   | $-8.210937x_2$   | $+1.277344x_{73}$  | $-0.460937x_3$   | $+0.003906x_6$ |
| $x_{46}$ | 4.62109375   | $-51.164062x_2$  | $+4.160156x_{73}$  | $-4.914062x_3$   | $+0.058594x_6$ |
| $x_{47}$ | 6.1796875    | $-34.953125x_2$  | $+5.882812x_{73}$  | $-6.453125x_3$   | $+0.054687x_6$ |
| $x_{48}$ | 1.6484375    | $-24.265625x_2$  | $+1.664063x_{73}$  | $-1.765625x_3$   | $+0.023437x_6$ |
| $x_{49}$ | 5.38671875   | $-42.007813x_2$  | $+6.269531x_{73}$  | $-7.757812x_3$   | $+0.074219x_6$ |
| $x_{50}$ | 4.62109375   | $-31.164062x_2$  | $+5.160156x_{73}$  | $-5.914062x_3$   | $+0.058594x_6$ |
| $x_{51}$ | 5.1796875    | $-52.953125x_2$  | $+3.882812x_{73}$  | $-4.453125x_3$   | $+0.054687x_6$ |



After cutting plane is added

|          |              |                  |                    |                  |                |
|----------|--------------|------------------|--------------------|------------------|----------------|
| $x_4$    | 1.55859375   | $-1.789063x_2$   | $-0.277344x_{73}$  | $-0.539063x_3$   | $-0.003906x_6$ |
| $x_{44}$ | 1.765625     | $+8.156250x_2$   | $+3.109375x_{73}$  | $-2.843750x_3$   | $+0.015625x_6$ |
| $x_7$    | 183.77734375 | $-132.601563x_2$ | $-17.246094x_{73}$ | $+107.648437x_3$ | $-1.285156x_6$ |
| $x_1$    | 1.234375     | $-1.156250x_2$   | $-0.109375x_{73}$  | $+0.843750x_3$   | $-0.015625x_6$ |
| $x_9$    | 88.66015625  | $-37.023437x_2$  | $-4.691406x_{73}$  | $-100.273438x_3$ | $+0.722656x_6$ |
| $x_8$    | 3.15234375   | $-54.851562x_2$  | $+3.378906x_{73}$  | $-5.601562x_3$   | $+0.089844x_6$ |
| $x_5$    | 8.4765625    | $+74.515625x_2$  | $+14.210937x_{73}$ | $-23.984375x_3$  | $+0.101562x_6$ |
| $x_{10}$ | 5.91796875   | $+20.304688x_2$  | $+10.488281x_{73}$ | $-17.445312x_3$  | $+0.105469x_6$ |
| $x_{12}$ | 8.4765625    | $+73.515625x_2$  | $+14.210937x_{73}$ | $-22.984375x_3$  | $+0.101562x_6$ |
| $x_{13}$ | 8.2421875    | $+37.671875x_2$  | $+13.320312x_{73}$ | $-21.828125x_3$  | $+0.117187x_6$ |
| $x_{27}$ | 2.1796875    | $-2.953125x_2$   | $+4.882812x_{73}$  | $-7.453125x_3$   | $+0.054687x_6$ |
| $x_{15}$ | 4.50390625   | $-53.585937x_2$  | $+3.714844x_{73}$  | $-4.835937x_3$   | $+0.066406x_6$ |
| $x_9$    | 3.828125     | $-54.218750x_2$  | $+3.546875x_{73}$  | $-5.218750x_3$   | $+0.078125x_6$ |
| $x_{17}$ | 5.91796875   | $+19.304688x_2$  | $+10.488281x_{73}$ | $-16.445312x_3$  | $+0.105469x_6$ |
| $x_{18}$ | 5.59375      | $-35.0625x_2$    | $+6.656250x_{73}$  | $-10.0625x_3$    | $+0.093750x_6$ |
| $x_{19}$ | 4.50390625   | $-53.585938x_2$  | $+3.714844x_{73}$  | $-4.835937x_3$   | $+0.066406x_6$ |
| $x_{20}$ | 5.59375      | $-35.0625x_2$    | $+6.656250x_{73}$  | $-10.0625x_3$    | $+0.093750x_6$ |
| $x_{21}$ | 2.6484375    | $-23.265625x_2$  | $+1.664062x_{73}$  | $-1.765625x_3$   | $+0.023437x_6$ |
| $x_{22}$ | 5.59375      | $-34.0625x_2$    | $+6.656250x_{73}$  | $-10.0625x_3$    | $+0.093750x_6$ |
| $x_{23}$ | 4.828125     | $+1.781250x_2$   | $+7.546875x_{73}$  | $-11.218750x_3$  | $+0.078125x_6$ |
| $x_{16}$ | 7.33203125   | $-11.804687x_2$  | $+12.261719x_{73}$ | $-19.054687x_3$  | $+0.144531x_6$ |
| $x_{25}$ | 7.828125     | $+19.781250x_2$  | $+10.546875x_{73}$ | $-15.218750x_3$  | $+0.078125x_6$ |
| $x_{11}$ | 5.73828125   | $+41.257813x_2$  | $+8.605469x_{73}$  | $-12.992187x_3$  | $+0.050781x_6$ |
| $x_{24}$ | 8.0078125    | $-11.171875x_2$  | $+12.429687x_{73}$ | $-18.671875x_3$  | $+0.132812x_6$ |
| $x_{28}$ | 8.0078125    | $-11.171875x_2$  | $+12.429687x_{73}$ | $-18.671875x_3$  | $+0.132812x_6$ |
| $x_{26}$ | 5.73828125   | $+40.257813x_2$  | $+8.605469x_{73}$  | $-11.992187x_3$  | $+0.050781x_6$ |
| $x_{30}$ | 7.15234375   | $+9.148437x_2$   | $+10.378906x_{73}$ | $-14.601562x_3$  | $+0.089844x_6$ |
| $x_{31}$ | 1.765625     | $+10.156250x_2$  | $+3.109375x_{73}$  | $-3.843750x_3$   | $+0.015625x_6$ |
| $x_{32}$ | 4.828125     | $-8.218750x_2$   | $+7.546875x_{73}$  | $-11.218750x_3$  | $+0.078125x_6$ |
| $x_{33}$ | 5.296875     | $+39.468750x_2$  | $+8.328125x_{73}$  | $-11.531250x_3$  | $+0.046875x_6$ |
| $x_{34}$ | 5.296875     | $+39.468750x_2$  | $+8.328125x_{73}$  | $-11.531250x_3$  | $+0.046875x_6$ |
| $x_{35}$ | 7.15234375   | $+10.148437x_2$  | $+10.378906x_{73}$ | $-14.601562x_3$  | $+0.089844x_6$ |
| $x_{36}$ | 2.97265625   | $+22.101563x_2$  | $+5.496094x_{73}$  | $-8.148437x_3$   | $+0.035156x_6$ |
| $x_{37}$ | 5.296875     | $+39.468750x_2$  | $+8.328125x_{73}$  | $-11.531250x_3$  | $+0.046875x_6$ |
| $x_{38}$ | 2.97265625   | $+22.101562x_2$  | $+5.496094x_{73}$  | $-8.148437x_3$   | $+0.035156x_6$ |
| $x_{39}$ | 7.15234375   | $+9.148437x_2$   | $+10.378906x_{73}$ | $-14.601562x_3$  | $+0.089844x_6$ |
| $x_{40}$ | 2.97265625   | $+21.101562x_2$  | $+5.496094x_{73}$  | $-8.148437x_3$   | $+0.035156x_6$ |
| $x_{41}$ | 9.4765625    | $+26.515625x_2$  | $+13.210937x_{73}$ | $-18.984375x_3$  | $+0.101562x_6$ |
| $x_{14}$ | 4.50390625   | $-53.585937x_2$  | $+3.714844x_{73}$  | $-4.835937x_3$   | $+0.066406x_6$ |
| $x_{42}$ | 5.1796875    | $-52.953125x_2$  | $+3.882812x_{73}$  | $-4.453125x_3$   | $+0.054687x_6$ |
| $x_{29}$ | 1.765625     | $+9.156250x_2$   | $+3.109375x_{73}$  | $-3.843750x_3$   | $+0.015625x_6$ |
| $x_{43}$ | 1.44140625   | $-8.210937x_2$   | $+1.277344x_{73}$  | $-0.460937x_3$   | $+0.003906x_6$ |
| $x_{46}$ | 4.62109375   | $-51.164062x_2$  | $+4.160156x_{73}$  | $-4.914062x_3$   | $+0.058594x_6$ |
| $x_{47}$ | 6.1796875    | $-34.953125x_2$  | $+5.882812x_{73}$  | $-6.453125x_3$   | $+0.054687x_6$ |
| $x_{48}$ | 1.6484375    | $-24.265625x_2$  | $+1.664063x_{73}$  | $-1.765625x_3$   | $+0.023437x_6$ |
| $x_{49}$ | 5.38671875   | $-42.007813x_2$  | $+6.269531x_{73}$  | $-7.757812x_3$   | $+0.074219x_6$ |
| $x_{50}$ | 4.62109375   | $-31.164062x_2$  | $+5.160156x_{73}$  | $-5.914062x_3$   | $+0.058594x_6$ |
| $x_{51}$ | 5.1796875    | $-52.953125x_2$  | $+3.882812x_{73}$  | $-4.453125x_3$   | $+0.054687x_6$ |

Forming the dual dictionary:

|          |                |                |                   |                  |                |                  |            |
|----------|----------------|----------------|-------------------|------------------|----------------|------------------|------------|
| $y_2$    | 13.9453125     | $+1.789063y_4$ | $-8.156250y_{44}$ | $+132.601563y_7$ | $+1.156250y_1$ | $+37.023437y_9$  | $+54.8515$ |
| $y_{73}$ | 10.38671875    | $+0.277344y_4$ | $-3.109375y_{44}$ | $+17.246094y_7$  | $+0.109375y_1$ | $+4.691406y_9$   | $-3.37890$ |
| $y_3$    | 65.6953125     | $+0.539063y_4$ | $+2.843750y_{44}$ | $-107.648437y_7$ | $-0.843750y_1$ | $+100.273438y_9$ | $+5.60156$ |
| $y_6$    | 0.01953125     | $+0.003906y_4$ | $-0.015625y_{44}$ | $+1.285156y_7$   | $+0.015625y_1$ | $-0.722656y_9$   | $-0.08984$ |
| $z$      | $-52.79296875$ | $-1.558594y_4$ | $-1.765625y_{44}$ | $-183.777344y_7$ | $-1.234375y_1$ | $-88.660156y_9$  | $-3.15234$ |

The Final Dual Dictionary is:

|           |                  |                |                    |            |                |                  |                |
|-----------|------------------|----------------|--------------------|------------|----------------|------------------|----------------|
| $y_1$     | 9                | $+0y_4$        | $-2y_{44}$         | $-74y_7$   | $-0y_2$        | $+56y_9$         | $-1y_{73}$     |
| $y_{60}$  | 0.571428571429   | $-0.071429y_4$ | $+0.071429y_{44}$  | $-1.5y_7$  | $+0.071429y_2$ | $-5.071429y_9$   | $-0.142857y_7$ |
| $y_3$     | 37.1428571429    | $-0.142857y_4$ | $+11.142857y_{44}$ | $-66y_7$   | $+0.142857y_2$ | $+21.857143y_9$  | $+2.714286y_7$ |
| $y_{109}$ | 39.2857142857    | $+1.214286y_4$ | $-12.214286y_{44}$ | $+37.5y_7$ | $-0.214286y_2$ | $+54.214286y_9$  | $-3.571429y_7$ |
| $z$       | $-42.1428571429$ | $-0.857143y_4$ | $-6.142857y_{44}$  | $-71y_7$   | $-0.142857y_2$ | $-125.857143y_9$ | $-0.714286y_7$ |

Final primal dictionary obtained:

|          |                |   |
|----------|----------------|---|
| $x_4$    | 0.857142857143 | $-0x_1 + 0.071429x_{60} + 0.142857x_3 - 1.214286x_{109}$    |
| $x_{44}$ | 6.14285714286  | $+2x_1 - 0.071429x_{60} - 11.142857x_3 + 12.214286x_{109}$  |
| $x_7$    | 71             | $+74x_1 + 1.5x_{60} + 66x_3 - 37.5x_{109}$                  |
| $x_2$    | 0.142857142857 | $+0x_1 - 0.071429x_{60} - 0.142857x_3 + 0.214286x_{109}$    |
| $x_9$    | 125.857142857  | $-56x_1 + 5.071429x_{60} - 21.857143x_3 - 54.214286x_{109}$ |
| $x_{73}$ | 0.714285714286 | $+1x_1 + 0.142857x_{60} - 2.714286x_3 + 3.571429x_{109}$    |
| $x_5$    | 35.7142857143  | $+7x_1 - 2.857143x_{60} - 64.714286x_3 + 62.571429x_{109}$  |
| $x_{10}$ | 23             | $+3x_1 + 0.5x_{60} - 40x_3 + 37.5x_{109}$                   |
| $x_{12}$ | 35.5714285714  | $+7x_1 - 2.785714x_{60} - 63.571429x_3 + 62.357143x_{109}$  |
| $x_{13}$ | 30.5714285714  | $+5x_1 - 0.285714x_{60} - 53.571429x_3 + 50.857143x_{109}$  |
| $x_{27}$ | 8.71428571429  | $+1x_1 + 1.142857x_{60} - 15.714286x_3 + 14.571429x_{109}$  |
| $x_{15}$ | 3.71428571429  | $-1x_1 + 4.642857x_{60} - 1.714286x_3 - 0.928571x_{109}$    |
| $x_9$    | 3.57142857143  | $-2x_1 + 4.714286x_{60} - 0.571429x_3 - 2.142857x_{109}$    |
| $x_{17}$ | 22.8571428571  | $+3x_1 + 0.571429x_{60} - 38.857143x_3 + 37.285714x_{109}$  |
| $x_{18}$ | 11.2857142857  | $-0x_1 + 3.857143x_{60} - 15.285714x_3 + 12.428571x_{109}$  |
| $x_{19}$ | 3.71428571429  | $-1x_1 + 4.642857x_{60} - 1.714286x_3 - 0.928571x_{109}$    |
| $x_{20}$ | 11.2857142857  | $-0x_1 + 3.857143x_{60} - 15.285714x_3 + 12.428571x_{109}$  |
| $x_{21}$ | 2              | $-0x_1 + 2x_{60} - 1x_3 - 0x_{109}$                         |
| $x_{22}$ | 11.4285714286  | $-0x_1 + 3.785714x_{60} - 15.428571x_3 + 12.642857x_{109}$  |
| $x_{23}$ | 15.4285714286  | $+2x_1 + 1.285714x_{60} - 25.428571x_3 + 24.142857x_{109}$  |
| $x_{16}$ | 23.5714285714  | $+2x_1 + 3.214286x_{60} - 38.571429x_3 + 35.357143x_{109}$  |
| $x_{25}$ | 23.1428571429  | $+5x_1 + 0.428571x_{60} - 40.142857x_3 + 38.714286x_{109}$  |
| $x_{11}$ | 21             | $+5x_1 - 1.5x_{60} - 38x_3 + 37.5x_{109}$                   |
| $x_{24}$ | 23.7142857143  | $+3x_1 + 3.142857x_{60} - 39.714286x_3 + 36.571429x_{109}$  |
| $x_{28}$ | 23.7142857143  | $+3x_1 + 3.142857x_{60} - 39.714286x_3 + 36.571429x_{109}$  |
| $x_{26}$ | 20.8571428571  | $+5x_1 - 1.428571x_{60} - 36.857143x_3 + 37.285714x_{109}$  |
| $x_{30}$ | 21.5714285714  | $+4x_1 + 1.214286x_{60} - 36.571429x_3 + 35.357143x_{109}$  |
| $x_{31}$ | 6.42857142857  | $+2x_1 - 0.214286x_{60} - 12.428571x_3 + 12.642857x_{109}$  |
| $x_{32}$ | 14             | $+2x_1 + 2x_{60} - 24x_3 + 22x_{109}$                       |
| $x_{33}$ | 19.8571428571  | $+5x_1 - 1.428571x_{60} - 35.857143x_3 + 36.285714x_{109}$  |
| $x_{34}$ | 19.8571428571  | $+5x_1 - 1.428571x_{60} - 35.857143x_3 + 36.285714x_{109}$  |
| $x_{35}$ | 21.7142857143  | $+4x_1 + 1.142857x_{60} - 36.714286x_3 + 35.571429x_{109}$  |
| $x_{36}$ | 12.2857142857  | $+3x_1 - 0.642857x_{60} - 23.285714x_3 + 22.928571x_{109}$  |
| $x_{37}$ | 19.8571428571  | $+5x_1 - 1.428571x_{60} - 35.857143x_3 + 36.285714x_{109}$  |
| $x_{38}$ | 12.2857142857  | $+3x_1 - 0.642857x_{60} - 23.285714x_3 + 22.928571x_{109}$  |
| $x_{39}$ | 21.5714285714  | $+4x_1 + 1.214286x_{60} - 36.571429x_3 + 35.357143x_{109}$  |
| $x_{40}$ | 12.1428571429  | $+3x_1 - 0.571429x_{60} - 23.142857x_3 + 22.714286x_{109}$  |
| $x_{41}$ | 29.1428571429  | $+6x_1 + 0.428571x_{60} - 50.142857x_3 + 48.714286x_{109}$  |
| $x_{14}$ | 3.71428571429  | $-1x_1 + 4.642857x_{60} - 1.714286x_3 - 0.928571x_{109}$    |
| $x_{42}$ | 3.85714285714  | $-0x_1 + 4.571429x_{60} - 2.857143x_3 + 0.285714x_{109}$    |
| $x_{29}$ | 6.28571428571  | $+2x_1 - 0.142857x_{60} - 12.285714x_3 + 12.428571x_{109}$  |
| $x_{43}$ | 1.42857142857  | $+1x_1 + 0.785714x_{60} - 2.428571x_3 + 2.642857x_{109}$    |
| $x_{46}$ | 4              | $-0x_1 + 4.5x_{60} - 4x_3 + 1.5x_{109}$                     |
| $x_{47}$ | 8.85714285714  | $+2x_1 + 3.571429x_{60} - 12.857143x_3 + 11.285714x_{109}$  |
| $x_8$    | 3.42857142857  | $-3x_1 + 4.785714x_{60} + 0.571429x_3 - 3.357143x_{109}$    |
| $x_{49}$ | 8.57142857143  | $+1x_1 + 4.214286x_{60} - 12.571429x_3 + 10.357143x_{109}$  |
| $x_{50}$ | 7.57142857143  | $+1x_1 + 3.214286x_{60} - 10.571429x_3 + 9.357143x_{109}$   |
| $x_{51}$ | 3.85714285714  | $-0x_1 + 4.571429x_{60} - 2.857143x_3 + 0.285714x_{109}$    |

After cutting plane is added

|          |                |   |
|----------|----------------|---|
| $x_4$    | 0.857142857143 | $-0x_1 + 0.071429x_{60} + 0.142857x_3 - 1.214286x_{109}$    |
| $x_{44}$ | 6.14285714286  | $+2x_1 - 0.071429x_{60} - 11.142857x_3 + 12.214286x_{109}$  |
| $x_7$    | 71             | $+74x_1 + 1.5x_{60} + 66x_3 - 37.5x_{109}$                  |
| $x_2$    | 0.142857142857 | $+0x_1 - 0.071429x_{60} - 0.142857x_3 + 0.214286x_{109}$    |
| $x_9$    | 125.857142857  | $-56x_1 + 5.071429x_{60} - 21.857143x_3 - 54.214286x_{109}$ |
| $x_{73}$ | 0.714285714286 | $+1x_1 + 0.142857x_{60} - 2.714286x_3 + 3.571429x_{109}$    |
| $x_5$    | 35.7142857143  | $+7x_1 - 2.857143x_{60} - 64.714286x_3 + 62.571429x_{109}$  |
| $x_{10}$ | 23             | $+3x_1 + 0.5x_{60} - 40x_3 + 37.5x_{109}$                   |
| $x_{12}$ | 35.5714285714  | $+7x_1 - 2.785714x_{60} - 63.571429x_3 + 62.357143x_{109}$  |
| $x_{13}$ | 30.5714285714  | $+5x_1 - 0.285714x_{60} - 53.571429x_3 + 50.857143x_{109}$  |
| $x_{27}$ | 8.71428571429  | $+1x_1 + 1.142857x_{60} - 15.714286x_3 + 14.571429x_{109}$  |
| $x_{15}$ | 3.71428571429  | $-1x_1 + 4.642857x_{60} - 1.714286x_3 - 0.928571x_{109}$    |
| $x_9$    | 3.57142857143  | $-2x_1 + 4.714286x_{60} - 0.571429x_3 - 2.142857x_{109}$    |
| $x_{17}$ | 22.8571428571  | $+3x_1 + 0.571429x_{60} - 38.857143x_3 + 37.285714x_{109}$  |
| $x_{18}$ | 11.2857142857  | $-0x_1 + 3.857143x_{60} - 15.285714x_3 + 12.428571x_{109}$  |
| $x_{19}$ | 3.71428571429  | $-1x_1 + 4.642857x_{60} - 1.714286x_3 - 0.928571x_{109}$    |
| $x_{20}$ | 11.2857142857  | $-0x_1 + 3.857143x_{60} - 15.285714x_3 + 12.428571x_{109}$  |
| $x_{21}$ | 2              | $-0x_1 + 2x_{60} - 1x_3 - 0x_{109}$                         |
| $x_{22}$ | 11.4285714286  | $-0x_1 + 3.785714x_{60} - 15.428571x_3 + 12.642857x_{109}$  |
| $x_{23}$ | 15.4285714286  | $+2x_1 + 1.285714x_{60} - 25.428571x_3 + 24.142857x_{109}$  |
| $x_{16}$ | 23.5714285714  | $+2x_1 + 3.214286x_{60} - 38.571429x_3 + 35.357143x_{109}$  |
| $x_{25}$ | 23.1428571429  | $+5x_1 + 0.428571x_{60} - 40.142857x_3 + 38.714286x_{109}$  |
| $x_{11}$ | 21             | $+5x_1 - 1.5x_{60} - 38x_3 + 37.5x_{109}$                   |
| $x_{24}$ | 23.7142857143  | $+3x_1 + 3.142857x_{60} - 39.714286x_3 + 36.571429x_{109}$  |
| $x_{28}$ | 23.7142857143  | $+3x_1 + 3.142857x_{60} - 39.714286x_3 + 36.571429x_{109}$  |
| $x_{26}$ | 20.8571428571  | $+5x_1 - 1.428571x_{60} - 36.857143x_3 + 37.285714x_{109}$  |
| $x_{30}$ | 21.5714285714  | $+4x_1 + 1.214286x_{60} - 36.571429x_3 + 35.357143x_{109}$  |
| $x_{31}$ | 6.42857142857  | $+2x_1 - 0.214286x_{60} - 12.428571x_3 + 12.642857x_{109}$  |
| $x_{32}$ | 14             | $+2x_1 + 2x_{60} - 24x_3 + 22x_{109}$                       |
| $x_{33}$ | 19.8571428571  | $+5x_1 - 1.428571x_{60} - 35.857143x_3 + 36.285714x_{109}$  |
| $x_{34}$ | 19.8571428571  | $+5x_1 - 1.428571x_{60} - 35.857143x_3 + 36.285714x_{109}$  |
| $x_{35}$ | 21.7142857143  | $+4x_1 + 1.142857x_{60} - 36.714286x_3 + 35.571429x_{109}$  |
| $x_{36}$ | 12.2857142857  | $+3x_1 - 0.642857x_{60} - 23.285714x_3 + 22.928571x_{109}$  |
| $x_{37}$ | 19.8571428571  | $+5x_1 - 1.428571x_{60} - 35.857143x_3 + 36.285714x_{109}$  |
| $x_{38}$ | 12.2857142857  | $+3x_1 - 0.642857x_{60} - 23.285714x_3 + 22.928571x_{109}$  |
| $x_{39}$ | 21.5714285714  | $+4x_1 + 1.214286x_{60} - 36.571429x_3 + 35.357143x_{109}$  |
| $x_{40}$ | 12.1428571429  | $+3x_1 - 0.571429x_{60} - 23.142857x_3 + 22.714286x_{109}$  |
| $x_{41}$ | 29.1428571429  | $+6x_1 + 0.428571x_{60} - 50.142857x_3 + 48.714286x_{109}$  |
| $x_{14}$ | 3.71428571429  | $-1x_1 + 4.642857x_{60} - 1.714286x_3 - 0.928571x_{109}$    |
| $x_{42}$ | 3.85714285714  | $-0x_1 + 4.571429x_{60} - 2.857143x_3 + 0.285714x_{109}$    |
| $x_{29}$ | 6.28571428571  | $+2x_1 - 0.142857x_{60} - 12.285714x_3 + 12.428571x_{109}$  |
| $x_{43}$ | 1.42857142857  | $+1x_1 + 0.785714x_{60} - 2.428571x_3 + 2.642857x_{109}$    |
| $x_{46}$ | 4              | $-0x_1 + 4.5x_{60} - 4x_3 + 1.5x_{109}$                     |
| $x_{47}$ | 8.85714285714  | $+2x_1 + 3.571429x_{60} - 12.857143x_3 + 11.285714x_{109}$  |
| $x_8$    | 3.42857142857  | $-3x_1 + 4.785714x_{60} + 0.571429x_3 - 3.357143x_{109}$    |
| $x_{49}$ | 8.57142857143  | $+1x_1 + 4.214286x_{60} - 12.571429x_3 + 10.357143x_{109}$  |
| $x_{50}$ | 7.57142857143  | $+1x_1 + 3.214286x_{60} - 10.571429x_3 + 9.357143x_{109}$   |
| $x_{51}$ | 3.85714285714  | $-0x_1 + 4.571429x_{60} - 2.857143x_3 + 0.285714x_{109}$    |

Forming the dual dictionary:

|           |                  |                |                    |            |                |                  |                |
|-----------|------------------|----------------|--------------------|------------|----------------|------------------|----------------|
| $y_1$     | 9                | $+0y_4$        | $-2y_{44}$         | $-74y_7$   | $-0y_2$        | $+56y_9$         | $-1y_{73}$     |
| $y_{60}$  | 0.571428571429   | $-0.071429y_4$ | $+0.071429y_{44}$  | $-1.5y_7$  | $+0.071429y_2$ | $-5.071429y_9$   | $-0.142857y_7$ |
| $y_3$     | 37.1428571429    | $-0.142857y_4$ | $+11.142857y_{44}$ | $-66y_7$   | $+0.142857y_2$ | $+21.857143y_9$  | $+2.714286y_7$ |
| $y_{109}$ | 39.2857142857    | $+1.214286y_4$ | $-12.214286y_{44}$ | $+37.5y_7$ | $-0.214286y_2$ | $+54.214286y_9$  | $-3.571429y_7$ |
| $z$       | $-42.1428571429$ | $-0.857143y_4$ | $-6.142857y_{44}$  | $-71y_7$   | $-0.142857y_2$ | $-125.857143y_9$ | $-0.714286y_7$ |

The Final Dual Dictionary is:

|           |       |         |             |          |         |           |            |          |             |             |             |             |             |          |
|-----------|-------|---------|-------------|----------|---------|-----------|------------|----------|-------------|-------------|-------------|-------------|-------------|----------|
| $y_1$     | 1     | $+1y_4$ | $-3y_{44}$  | $-53y_7$ | $-1y_2$ | $+127y_9$ | $+1y_{73}$ | $-47y_5$ | $+4y_{10}$  | $-46y_{12}$ | $-9y_{13}$  | $+15y_{27}$ | $+66y_{15}$ | $+68y_9$ |
| $y_{208}$ | 8     | $-1y_4$ | $+1y_{44}$  | $-21y_7$ | $+1y_2$ | $-71y_9$  | $-2y_{73}$ | $+40y_5$ | $-7y_{10}$  | $+39y_{12}$ | $+4y_{13}$  | $-16y_{27}$ | $-65y_{15}$ | $-66y_9$ |
| $y_3$     | 36    | $+0y_4$ | $+11y_{44}$ | $-63y_7$ | $-0y_2$ | $+32y_9$  | $+3y_{73}$ | $+59y_5$ | $+41y_{10}$ | $+58y_{12}$ | $+53y_{13}$ | $+18y_{27}$ | $+11y_{15}$ | $+10y_9$ |
| $y_{109}$ | 33    | $+2y_4$ | $-13y_{44}$ | $+54y_7$ | $-1y_2$ | $+110y_9$ | $-2y_{73}$ | $-94y_5$ | $-32y_{10}$ | $-93y_{12}$ | $-54y_{13}$ | $-2y_{27}$  | $+52y_{15}$ | $+54y_9$ |
| $z$       | $-41$ | $-1y_4$ | $-6y_{44}$  | $-74y_7$ | $-0y_2$ | $-136y_9$ | $-1y_{73}$ | $-30y_5$ | $-24y_{10}$ | $-30y_{12}$ | $-30y_{13}$ | $-11y_{27}$ | $-13y_{15}$ | $-13y_9$ |

Final primal dictionary obtained:

|          |                       |  |
|----------|-----------------------|--|
| $x_4$    | 1                     | $-1x_1 + 1x_{208} - 0x_3 - 2x_{109}$       |
| $x_{44}$ | 6                     | $+3x_1 - 1x_{208} - 11x_3 + 13x_{109}$     |
| $x_7$    | 74                    | $+53x_1 + 21x_{208} + 63x_3 - 54x_{109}$   |
| $x_2$    | $1.02279296144e - 14$ | $+1x_1 - 1x_{208} + 0x_3 + 1x_{109}$       |
| $x_9$    | 136                   | $-127x_1 + 71x_{208} - 32x_3 - 110x_{109}$ |
| $x_{73}$ | 1                     | $-1x_1 + 2x_{208} - 3x_3 + 2x_{109}$       |
| $x_5$    | 30                    | $+47x_1 - 40x_{208} - 59x_3 + 94x_{109}$   |
| $x_{10}$ | 24                    | $-4x_1 + 7x_{208} - 41x_3 + 32x_{109}$     |
| $x_{12}$ | 30                    | $+46x_1 - 39x_{208} - 58x_3 + 93x_{109}$   |
| $x_{13}$ | 30                    | $+9x_1 - 4x_{208} - 53x_3 + 54x_{109}$     |
| $x_{27}$ | 11                    | $-15x_1 + 16x_{208} - 18x_3 + 2x_{109}$    |
| $x_{15}$ | 13                    | $-66x_1 + 65x_{208} - 11x_3 - 52x_{109}$   |
| $x_9$    | 13                    | $-68x_1 + 66x_{208} - 10x_3 - 54x_{109}$   |
| $x_{17}$ | 24                    | $-5x_1 + 8x_{208} - 40x_3 + 31x_{109}$     |
| $x_{18}$ | 19                    | $-54x_1 + 54x_{208} - 23x_3 - 30x_{109}$   |
| $x_{19}$ | 13                    | $-66x_1 + 65x_{208} - 11x_3 - 52x_{109}$   |
| $x_{20}$ | 19                    | $-54x_1 + 54x_{208} - 23x_3 - 30x_{109}$   |
| $x_{21}$ | 6                     | $-28x_1 + 28x_{208} - 5x_3 - 22x_{109}$    |
| $x_{22}$ | 19                    | $-53x_1 + 53x_{208} - 23x_3 - 29x_{109}$   |
| $x_{23}$ | 18                    | $-16x_1 + 18x_{208} - 28x_3 + 10x_{109}$   |
| $x_{16}$ | 30                    | $-43x_1 + 45x_{208} - 45x_3 + 0x_{109}$    |
| $x_{25}$ | 24                    | $-1x_1 + 6x_{208} - 41x_3 + 34x_{109}$     |
| $x_{11}$ | 18                    | $+26x_1 - 21x_{208} - 35x_3 + 54x_{109}$   |
| $x_{24}$ | 30                    | $-41x_1 + 44x_{208} - 46x_3 + 2x_{109}$    |
| $x_{28}$ | 30                    | $-41x_1 + 44x_{208} - 46x_3 + 2x_{109}$    |
| $x_{26}$ | 18                    | $+25x_1 - 20x_{208} - 34x_3 + 53x_{109}$   |
| $x_{30}$ | 24                    | $-13x_1 + 17x_{208} - 39x_3 + 22x_{109}$   |
| $x_{31}$ | 6                     | $+5x_1 - 3x_{208} - 12x_3 + 15x_{109}$     |
| $x_{32}$ | 18                    | $-26x_1 + 28x_{208} - 28x_3 + 0x_{109}$    |
| $x_{33}$ | 17                    | $+25x_1 - 20x_{208} - 33x_3 + 52x_{109}$   |
| $x_{34}$ | 17                    | $+25x_1 - 20x_{208} - 33x_3 + 52x_{109}$   |
| $x_{35}$ | 24                    | $-12x_1 + 16x_{208} - 39x_3 + 23x_{109}$   |
| $x_{36}$ | 11                    | $+12x_1 - 9x_{208} - 22x_3 + 30x_{109}$    |
| $x_{37}$ | 17                    | $+25x_1 - 20x_{208} - 33x_3 + 52x_{109}$   |
| $x_{38}$ | 11                    | $+12x_1 - 9x_{208} - 22x_3 + 30x_{109}$    |
| $x_{39}$ | 24                    | $-13x_1 + 17x_{208} - 39x_3 + 22x_{109}$   |
| $x_{40}$ | 11                    | $+11x_1 - 8x_{208} - 22x_3 + 29x_{109}$    |
| $x_{41}$ | 30                    | $+0x_1 + 6x_{208} - 51x_3 + 44x_{109}$     |
| $x_{14}$ | 13                    | $-66x_1 + 65x_{208} - 11x_3 - 52x_{109}$   |
| $x_{42}$ | 13                    | $-64x_1 + 64x_{208} - 12x_3 - 50x_{109}$   |
| $x_{29}$ | 6                     | $+4x_1 - 2x_{208} - 12x_3 + 14x_{109}$     |
| $x_{43}$ | 3                     | $-10x_1 + 11x_{208} - 4x_3 - 6x_{109}$     |
| $x_{46}$ | 13                    | $-63x_1 + 63x_{208} - 13x_3 - 48x_{109}$   |
| $x_{47}$ | 16                    | $-48x_1 + 50x_{208} - 20x_3 - 28x_{109}$   |
| $x_8$    | 13                    | $-70x_1 + 67x_{208} - 9x_3 - 56x_{109}$    |
| $x_{49}$ | 17                    | $-58x_1 + 59x_{208} - 21x_3 - 36x_{109}$   |
| $x_{50}$ | 14                    | $-44x_1 + 45x_{208} - 17x_3 - 26x_{109}$   |
| $x_{51}$ | 13                    | $-64x_1 + 64x_{208} - 12x_3 - 50x_{109}$   |

Done.

Final Answer: 41

## 9 ilpTest9

Initial Dictionary

$$\begin{array}{c|cccc}
 x_1 & 1.2 & -3.1x_2 + 4.3x_3 - 0.5x_5 & & \\
 x_4 & 1 & -1x_2 + 1x_3 - 1x_5 & & \\
 x_6 & 2.5 & +1.3x_2 - 2.1x_3 + 1x_5 & & \\
 \hline
 z & 0 & -1.2x_2 - 2.3x_3 - 2.1x_5 & & 
 \end{array}$$

No initialization required → Proceed to Optimize.

Final dictionary after first LP relaxation solve:

$$\begin{array}{c|cccc}
 x_1 & 1.2 & -3.1x_2 + 4.3x_3 - 0.5x_5 & & \\
 x_4 & 1 & -1x_2 + 1x_3 - 1x_5 & & \\
 x_6 & 2.5 & +1.3x_2 - 2.1x_3 + 1x_5 & & \\
 \hline
 z & 0 & -1.2x_2 - 2.3x_3 - 2.1x_5 & & 
 \end{array}$$

After cutting plane is added

$$\begin{array}{c|cccc}
 x_1 & 1.2 & -3.1x_2 + 4.3x_3 - 0.5x_5 & & \\
 x_4 & 1 & -1x_2 + 1x_3 - 1x_5 & & \\
 x_6 & 2.5 & +1.3x_2 - 2.1x_3 + 1x_5 & & \\
 x_6 & -0.2 & +0.1x_2 + 0.7x_3 + 0.5x_5 & & \\
 x_7 & -0.5 & +0.7x_2 + 0.1x_3 & & \\
 \hline
 z & 0 & -1.2x_2 - 2.3x_3 - 2.1x_5 & & 
 \end{array}$$

Forming the dual dictionary:

$$\begin{array}{c|cccc}
 y_2 & 1.2 & +3.1y_1 + 1y_4 - 1.3y_6 - 0.1y_6 - 0.7y_7 & & \\
 y_3 & 2.3 & -4.3y_1 - 1y_4 + 2.1y_6 - 0.7y_6 - 0.1y_7 & & \\
 y_5 & 2.1 & +0.5y_1 + 1y_4 - 1y_6 - 0.5y_6 & & \\
 \hline
 z & -0 & -1.2y_1 - 1y_4 - 2.5y_6 + 0.2y_6 + 0.5y_7 & & 
 \end{array}$$

The Final Dual Dictionary is:

$$\begin{array}{c|cccc}
 y_7 & 3.70180722892 & -0.783133y_6 + 0.361446y_4 + 0.277108y_6 - 0.933735y_3 - 1.295181y_2 & & \\
 y_1 & 0.448795180723 & -0.144578y_6 - 0.240964y_4 + 0.481928y_6 - 0.210843y_3 + 0.030120y_2 & & \\
 y_5 & 2.32439759036 & -0.572289y_6 + 0.879518y_4 - 0.759036y_6 - 0.105422y_3 + 0.015060y_2 & & \\
 \hline
 z & 1.31234939759 & -0.018072y_6 - 0.530120y_4 - 2.939759y_6 - 0.213855y_3 - 0.683735y_2 & & 
 \end{array}$$

Final primal dictionary obtained:

|       |                 |  |
|-------|-----------------|--|
| $x_6$ | 0.0180722891566 | $+0.783133x_7 + 0.144578x_1 + 0.572289x_5$ |
| $x_4$ | 0.530120481928  | $-0.361446x_7 + 0.240964x_1 - 0.879518x_5$ |
| $x_6$ | 2.93975903614   | $-0.277108x_7 - 0.481928x_1 + 0.759036x_5$ |
| $x_3$ | 0.213855421687  | $+0.933735x_7 + 0.210843x_1 + 0.105422x_5$ |
| $x_2$ | 0.683734939759  | $+1.295181x_7 - 0.030120x_1 - 0.015060x_5$ |
| $z$   | -1.31234939759  | $-3.701807x_7 - 0.448795x_1 - 2.324398x_5$ |

After cutting plane is added

|          |                  |  |
|----------|------------------|--|
| $x_6$    | 0.0180722891566  | $+0.783133x_7 + 0.144578x_1 + 0.572289x_5$ |
| $x_4$    | 0.530120481928   | $-0.361446x_7 + 0.240964x_1 - 0.879518x_5$ |
| $x_6$    | 2.93975903614    | $-0.277108x_7 - 0.481928x_1 + 0.759036x_5$ |
| $x_3$    | 0.213855421687   | $+0.933735x_7 + 0.210843x_1 + 0.105422x_5$ |
| $x_2$    | 0.683734939759   | $+1.295181x_7 - 0.030120x_1 - 0.015060x_5$ |
| $x_8$    | -0.0180722891566 | $+0.216867x_7 + 0.855422x_1 + 0.427711x_5$ |
| $x_9$    | -0.530120481928  | $+0.361446x_7 + 0.759036x_1 + 0.879518x_5$ |
| $x_{10}$ | -0.939759036145  | $+0.277108x_7 + 0.481928x_1 + 0.240964x_5$ |
| $x_{11}$ | -0.213855421687  | $+0.066265x_7 + 0.789157x_1 + 0.894578x_5$ |
| $x_{12}$ | -0.683734939759  | $+0.704819x_7 + 0.030120x_1 + 0.015060x_5$ |
| $z$      | -1.31234939759   | $-3.701807x_7 - 0.448795x_1 - 2.324398x_5$ |

Forming the dual dictionary:

|       |                |  |
|-------|----------------|--|
| $y_7$ | 3.70180722892  | $-0.783133y_6 + 0.361446y_4 + 0.277108y_6 - 0.933735y_3 - 1.295181y_2 - 0.216867y_8 -$ |
| $y_1$ | 0.448795180723 | $-0.144578y_6 - 0.240964y_4 + 0.481928y_6 - 0.210843y_3 + 0.030120y_2 - 0.855422y_8 -$ |
| $y_5$ | 2.32439759036  | $-0.572289y_6 + 0.879518y_4 - 0.759036y_6 - 0.105422y_3 + 0.015060y_2 - 0.427711y_8 -$ |
| $z$   | 1.31234939759  | $-0.018072y_6 - 0.530120y_4 - 2.939759y_6 - 0.213855y_3 - 0.683735y_2 + 0.018072y_8 +$ |

The Final Dual Dictionary is:

|          |                |                                     |   |
|----------|----------------|-------------------------------------|---|
| $y_{12}$ | 5.00909090909  | $-1.018182y_6 + 0.727273y_4$        | $-1.181818y_3 - 1.909091y_2 + 0.836364y_1 + 0.4y_8 -$ |
| $y_{10}$ | 0.618181818182 | $-0.236364y_6 - 0.545455y_4 + 1y_6$ | $-0.363636y_3 + 0.181818y_2 - 2.127273y_1 - 1.8y_8 -$ |
| $y_5$    | 2.1            | $-0.5y_6 + 1y_4 - 1y_6$             | $-0y_3 + 0y_2 + 0.5y_1 - 0y_8$                        |
| $z$      | 5.31818181818  | $-0.936364y_6 - 0.545455y_4 - 2y_6$ | $-1.363636y_3 - 1.818182y_2 - 1.427273y_1 - 1.4y_8 -$ |



Final primal dictionary obtained:

|          |                |   |
|----------|----------------|---|
| $x_6$    | 0.936363636364 | $+1.018182x_{12} + 0.236364x_{10} + 0.5x_5$ |
| $x_4$    | 0.545454545455 | $-0.727273x_{12} + 0.545455x_{10} - 1x_5$   |
| $x_6$    | 2              | $-1x_{10} + 1x_5$                           |
| $x_3$    | 1.36363636364  | $+1.181818x_{12} + 0.363636x_{10} + 0x_5$   |
| $x_2$    | 1.81818181818  | $+1.909091x_{12} - 0.181818x_{10} - 0x_5$   |
| $x_1$    | 1.42727272727  | $-0.836364x_{12} + 2.127273x_{10} - 0.5x_5$ |
| $x_8$    | 1.4            | $-0.4x_{12} + 1.8x_{10} + 0x_5$             |
| $x_9$    | 0.881818181818 | $-0.109091x_{12} + 1.581818x_{10} + 0.5x_5$ |
| $x_{11}$ | 0.972727272727 | $-0.563636x_{12} + 1.672727x_{10} + 0.5x_5$ |
| $x_7$    | 0.909090909091 | $+1.454545x_{12} - 0.090909x_{10} - 0x_5$   |
| $z$      | -5.31818181818 | $-5.009091x_{12} - 0.618182x_{10} - 2.1x_5$ |

After cutting plane is added

|          |                 |   |
|----------|-----------------|---|
| $x_6$    | 0.936363636364  | $+1.018182x_{12} + 0.236364x_{10} + 0.5x_5$ |
| $x_4$    | 0.545454545455  | $-0.727273x_{12} + 0.545455x_{10} - 1x_5$   |
| $x_6$    | 2               | $-1x_{10} + 1x_5$                           |
| $x_3$    | 1.36363636364   | $+1.181818x_{12} + 0.363636x_{10} + 0x_5$   |
| $x_2$    | 1.81818181818   | $+1.909091x_{12} - 0.181818x_{10} - 0x_5$   |
| $x_1$    | 1.42727272727   | $-0.836364x_{12} + 2.127273x_{10} - 0.5x_5$ |
| $x_8$    | 1.4             | $-0.4x_{12} + 1.8x_{10} + 0x_5$             |
| $x_9$    | 0.881818181818  | $-0.109091x_{12} + 1.581818x_{10} + 0.5x_5$ |
| $x_{11}$ | 0.972727272727  | $-0.563636x_{12} + 1.672727x_{10} + 0.5x_5$ |
| $x_7$    | 0.909090909091  | $+1.454545x_{12} - 0.090909x_{10} - 0x_5$   |
| $x_{13}$ | -0.936363636364 | $+0.981818x_{12} + 0.763636x_{10} + 0.5x_5$ |
| $x_{14}$ | -0.545454545455 | $+0.727273x_{12} + 0.454545x_{10} + 1x_5$   |
| $x_{15}$ | -0.363636363636 | $+0.818182x_{12} + 0.636364x_{10} + 1x_5$   |
| $x_{16}$ | -0.818181818182 | $+0.090909x_{12} + 0.181818x_{10} + 0x_5$   |
| $x_{17}$ | -0.427272727273 | $+0.836364x_{12} + 0.872727x_{10} + 0.5x_5$ |
| $x_{18}$ | -0.4            | $+0.4x_{12} + 0.2x_{10} + 1x_5$             |
| $x_{19}$ | -0.881818181818 | $+0.109091x_{12} + 0.418182x_{10} + 0.5x_5$ |
| $x_{20}$ | -0.972727272727 | $+0.563636x_{12} + 0.327273x_{10} + 0.5x_5$ |
| $x_{21}$ | -0.909090909091 | $+0.545455x_{12} + 0.090909x_{10} + 0x_5$   |
| $z$      | -5.31818181818  | $-5.009091x_{12} - 0.618182x_{10} - 2.1x_5$ |

Forming the dual dictionary:

|          |                |  |   |
|----------|----------------|--|---|
| $y_{12}$ | 5.00909090909  | $-1.018182y_6 + 0.727273y_4$   | $-1.181818y_3 - 1.909091y_2 + 0.836364y_1 + 0.4y_8 -$ |
| $y_{10}$ | 0.618181818182 | $-0.236364y_6 - 0.545455y_4 + 1y_6$  | $-0.363636y_3 + 0.181818y_2 - 2.127273y_1 - 1.8y_8 -$ |
| $y_5$    | 2.1            | $-0.5y_6 + 1y_4 - 1y_6 - 0y_3$   | $+0y_2 + 0.5y_1 - 0y_8$                               |
| $z$      | 5.31818181818  | $-0.936364y_6 - 0.545455y_4 - 2y_6 - 1.363636y_3 - 1.818182y_2 - 1.427273y_1 - 1.4y_8 -$ |   |

The Final Dual Dictionary is:

|          |      |   |
|----------|------|---|
| $y_{21}$ | 7.3  | $-1.3y_6 + 1y_4 + 1y_5 - 2y_3 - 4y_2 + 3.3y_1 + 2.6y_8 + 2.3y_9 + 3.3y_{11} - 3y_7 + 1y_{10} + 0y_{14} + 0y_{15} -$     |
| $y_{16}$ | 11.3 | $-3.4y_6 + 2y_4 - 6y_5 - 1y_3 + 3y_2 - 10.6y_1 - 11.2y_8 - 12.6y_9 - 13.6y_{11} + 2y_7 - 6y_{10} - 8y_{14} - 9y_{15} -$ |
| $y_6$    | 2.1  | $-0.5y_6 + 1y_4 - 1y_5 - 0y_3 + 0.5y_1 - 0y_8 - 0.5y_9 - 0.5y_{11} + 0y_{10} - 1y_{14} - 1y_{15} -$                     |
| $z$      | 17   | $-3.9y_6 - 0y_4 - 2y_5 - 4y_3 - 3y_2 - 8.1y_1 - 8.2y_8 - 8.1y_9 - 8.1y_{11} - 2y_7 - 4y_{10} - 4y_{14} - 5y_{15} -$     |

Final primal dictionary obtained:

|          |                       |                                    |
|----------|-----------------------|------------------------------------|
| $x_6$    | 3.9                   | $+1.3x_{21} + 3.4x_{16} + 0.5x_6$  |
| $x_4$    | $3.77475828373e - 15$ | $-1x_{21} - 2x_{16} - 1x_6$        |
| $x_5$    | 2                     | $-1x_{21} + 6x_{16} + 1x_6$        |
| $x_3$    | 4                     | $+2x_{21} + 1x_{16} + 0x_6$        |
| $x_2$    | 3                     | $+4x_{21} - 3x_{16}$               |
| $x_1$    | 8.1                   | $-3.3x_{21} + 10.6x_{16} - 0.5x_6$ |
| $x_8$    | 8.2                   | $-2.6x_{21} + 11.2x_{16} + 0x_6$   |
| $x_9$    | 8.1                   | $-2.3x_{21} + 12.6x_{16} + 0.5x_6$ |
| $x_{11}$ | 8.1                   | $-3.3x_{21} + 13.6x_{16} + 0.5x_6$ |
| $x_7$    | 2                     | $+3x_{21} - 2x_{16}$               |
| $x_{10}$ | 4                     | $-1x_{21} + 6x_{16} - 0x_6$        |
| $x_{14}$ | 4                     | $-0x_{21} + 8x_{16} + 1x_6$        |
| $x_{15}$ | 5                     | $-0x_{21} + 9x_{16} + 1x_6$        |
| $x_{13}$ | 4.1                   | $+0.7x_{21} + 6.6x_{16} + 0.5x_6$  |
| $x_{17}$ | 4.9                   | $+0.3x_{21} + 7.4x_{16} + 0.5x_6$  |
| $x_{18}$ | 2.8                   | $-0.4x_{21} + 6.8x_{16} + 1x_6$    |
| $x_{19}$ | 1.9                   | $-0.7x_{21} + 5.4x_{16} + 0.5x_6$  |
| $x_{20}$ | 1.9                   | $+0.3x_{21} + 4.4x_{16} + 0.5x_6$  |
| $x_{12}$ | 1                     | $+2x_{21} - 1x_{16}$               |
| $z$      | -17                   | $-7.3x_{21} - 11.3x_{16} - 2.1x_6$ |

After cutting plane is added

|          |                       |              |               |           |
|----------|-----------------------|--------------|---------------|-----------|
| $x_6$    | 3.9                   | $+1.3x_{21}$ | $+3.4x_{16}$  | $+0.5x_6$ |
| $x_4$    | $3.77475828373e - 15$ | $-1x_{21}$   | $-2x_{16}$    | $-1x_6$   |
| $x_5$    | 2                     | $-1x_{21}$   | $+6x_{16}$    | $+1x_6$   |
| $x_3$    | 4                     | $+2x_{21}$   | $+1x_{16}$    | $+0x_6$   |
| $x_2$    | 3                     | $+4x_{21}$   | $-3x_{16}$    |           |
| $x_1$    | 8.1                   | $-3.3x_{21}$ | $+10.6x_{16}$ | $-0.5x_6$ |
| $x_8$    | 8.2                   | $-2.6x_{21}$ | $+11.2x_{16}$ | $+0x_6$   |
| $x_9$    | 8.1                   | $-2.3x_{21}$ | $+12.6x_{16}$ | $+0.5x_6$ |
| $x_{11}$ | 8.1                   | $-3.3x_{21}$ | $+13.6x_{16}$ | $+0.5x_6$ |
| $x_7$    | 2                     | $+3x_{21}$   | $-2x_{16}$    |           |
| $x_{10}$ | 4                     | $-1x_{21}$   | $+6x_{16}$    | $-0x_6$   |
| $x_{14}$ | 4                     | $-0x_{21}$   | $+8x_{16}$    | $+1x_6$   |
| $x_{15}$ | 5                     | $-0x_{21}$   | $+9x_{16}$    | $+1x_6$   |
| $x_{13}$ | 4.1                   | $+0.7x_{21}$ | $+6.6x_{16}$  | $+0.5x_6$ |
| $x_{17}$ | 4.9                   | $+0.3x_{21}$ | $+7.4x_{16}$  | $+0.5x_6$ |
| $x_{18}$ | 2.8                   | $-0.4x_{21}$ | $+6.8x_{16}$  | $+1x_6$   |
| $x_{19}$ | 1.9                   | $-0.7x_{21}$ | $+5.4x_{16}$  | $+0.5x_6$ |
| $x_{20}$ | 1.9                   | $+0.3x_{21}$ | $+4.4x_{16}$  | $+0.5x_6$ |
| $x_{12}$ | 1                     | $+2x_{21}$   | $-1x_{16}$    |           |
| $x_{22}$ | -0.9                  | $+0.7x_{21}$ | $+0.6x_{16}$  | $+0.5x_6$ |
| $x_{23}$ | -0.1                  | $+0.3x_{21}$ | $+0.4x_{16}$  | $+0.5x_6$ |
| $x_{24}$ | -0.2                  | $+0.6x_{21}$ | $+0.8x_{16}$  | $+1x_6$   |
| $x_{25}$ | -0.1                  | $+0.3x_{21}$ | $+0.4x_{16}$  | $+0.5x_6$ |
| $x_{26}$ | -0.1                  | $+0.3x_{21}$ | $+0.4x_{16}$  | $+0.5x_6$ |
| $x_{27}$ | -0.1                  | $+0.3x_{21}$ | $+0.4x_{16}$  | $+0.5x_6$ |
| $x_{28}$ | -0.9                  | $+0.7x_{21}$ | $+0.6x_{16}$  | $+0.5x_6$ |
| $x_{29}$ | -0.8                  | $+0.4x_{21}$ | $+0.2x_{16}$  | $+0x_6$   |
| $x_{30}$ | -0.9                  | $+0.7x_{21}$ | $+0.6x_{16}$  | $+0.5x_6$ |
| $x_{31}$ | -0.9                  | $+0.7x_{21}$ | $+0.6x_{16}$  | $+0.5x_6$ |
| $z$      | -17                   | $-7.3x_{21}$ | $-11.3x_{16}$ | $-2.1x_6$ |

Forming the dual dictionary:

|          |      |   |           |           |              |   |
|----------|------|---|-----------|-----------|--------------|---|
| $y_{21}$ | 7.3  | $-1.3y_6 + 1y_4 + 1y_5 - 2y_3 - 4y_2 + 3.3y_1$  | $+2.6y_8$ | $+2.3y_9$ | $+3.3y_{11}$ | $-3y_7 + 1y_{10} + 0y_{14} + 0y_{15} -$ |
| $y_{16}$ | 11.3 | $-3.4y_6 + 2y_4 - 6y_5 - 1y_3 + 3y_2 - 10.6y_1 - 11.2y_8 - 12.6y_9 - 13.6y_{11} + 2y_7 - 6y_{10} - 8y_{14} - 9y_{15} -$ |           |           |              |   |
| $y_6$    | 2.1  | $-0.5y_6 + 1y_4 - 1y_5 - 0y_3 + 0.5y_1 - 0y_8 - 0.5y_9 - 0.5y_{11} + 0y_{10} - 1y_{14} - 1y_{15} -$                     |           |           |              |   |
| $z$      | 17   | $-3.9y_6 - 0y_4 - 2y_5 - 4y_3 - 3y_2 - 8.1y_1 - 8.2y_8 - 8.1y_9 - 8.1y_{11} - 2y_7 - 4y_{10} - 4y_{14} - 5y_{15} -$     |           |           |              |   |

Unbounded Dictionary! The Final Dual Dictionary is:

|          |               |                 |                   |          |                 |                 |                   |      |
|----------|---------------|-----------------|-------------------|----------|-----------------|-----------------|-------------------|------|
| $y_4$    | 29.8583333333 | $-5.833333y_6$  | $-4.666667y_{21}$ | $+6y_5$  | $-10.416667y_3$ | $-15.416667y_2$ | $-1.083333y_{16}$ | $+0$ |
| $y_1$    | 2.91666666667 | $-0.666667y_6$  | $-0.333333y_{21}$ | $-0y_5$  | $-0.833333y_3$  | $-0.833333y_2$  | $-0.166667y_{16}$ | $-1$ |
| $y_{22}$ | 66.8333333333 | $-13.333333y_6$ | $-9.666667y_{21}$ | $+10y_5$ | $-21.666667y_3$ | $-31.666667y_2$ | $-2.333333y_{16}$ | $-1$ |
| $z$      | 53.525        | $-10.5y_6$      | $-6y_{21}$        | $+7y_5$  | $-16.75y_3$     | $-24.75y_2$     | $-0.75y_{16}$     | $-1$ |

Dual is unbounded. Primal is therefore infeasible.

Problem is ILP infeasible. Could not find an integer point.

Done.

Final Answer: Infeasible.

## 10 ilpTest10

Initial Dictionary

|       |      |                             |
|-------|------|-----------------------------|
| $x_4$ | 3.6  | $+7.7x_1 - 1.4x_2 + 1.3x_3$ |
| $x_5$ | 0.9  | $+7.2x_1 - 1.4x_2 + 0.6x_3$ |
| $x_6$ | 2.2  | $+4.5x_1 - 2.5x_2 + 3.5x_3$ |
| $x_7$ | -4.2 | $+5.6x_1 + 1.5x_2 - 2.9x_3$ |
| $x_8$ | 2.7  | $+2.6x_1 + 1.7x_2 - 1.1x_3$ |
| $x_9$ | 3.7  | $+0.1x_1 - 1.3x_2 - 3.3x_3$ |
| $z$   | 0    | $-0.6x_1 - 1.9x_2 - 0.3x_3$ |

$x_7$  leaves

Problem is feasible. Initialization phase yields a zero answer. Final dictionary after first LP relaxation solve:

|       |       |  |
|-------|-------|--|
| $x_4$ | 9.375 | $-3.4625x_2 + 5.2875x_3 + 1.375x_7$        |
| $x_5$ | 6.3   | $-3.328571x_2 + 4.328571x_3 + 1.285714x_7$ |
| $x_6$ | 5.575 | $-3.705357x_2 + 5.830357x_3 + 0.803571x_7$ |
| $x_1$ | 0.75  | $-0.267857x_2 + 0.517857x_3 + 0.178571x_7$ |
| $x_8$ | 4.65  | $+1.003571x_2 + 0.246429x_3 + 0.464286x_7$ |
| $x_9$ | 3.775 | $-1.326786x_2 - 3.248214x_3 + 0.017857x_7$ |
| $z$   | -0.45 | $-1.739286x_2 - 0.610714x_3 - 0.107143x_7$ |

After cutting plane is added

|          |        |                |                |                |
|----------|--------|----------------|----------------|----------------|
| $x_4$    | 9.375  | $-3.4625x_2$   | $+5.2875x_3$   | $+1.375x_7$    |
| $x_5$    | 6.3    | $-3.328571x_2$ | $+4.328571x_3$ | $+1.285714x_7$ |
| $x_6$    | 5.575  | $-3.705357x_2$ | $+5.830357x_3$ | $+0.803571x_7$ |
| $x_1$    | 0.75   | $-0.267857x_2$ | $+0.517857x_3$ | $+0.178571x_7$ |
| $x_8$    | 4.65   | $+1.003571x_2$ | $+0.246429x_3$ | $+0.464286x_7$ |
| $x_9$    | 3.775  | $-1.326786x_2$ | $-3.248214x_3$ | $+0.017857x_7$ |
| $x_9$    | -0.375 | $+0.4625x_2$   | $+0.7125x_3$   | $+0.625x_7$    |
| $x_{10}$ | -0.3   | $+0.328571x_2$ | $+0.671429x_3$ | $+0.714286x_7$ |
| $x_{11}$ | -0.575 | $+0.705357x_2$ | $+0.169643x_3$ | $+0.196429x_7$ |
| $x_{12}$ | -0.75  | $+0.267857x_2$ | $+0.482143x_3$ | $+0.821429x_7$ |
| $x_{13}$ | -0.65  | $+0.996429x_2$ | $+0.753571x_3$ | $+0.535714x_7$ |
| $x_{14}$ | -0.775 | $+0.326786x_2$ | $+0.248214x_3$ | $+0.982143x_7$ |
| $z$      | -0.45  | $-1.739286x_2$ | $-0.610714x_3$ | $-0.107143x_7$ |

Forming the dual dictionary:

|       |                |              |                |                |                |                |                |       |
|-------|----------------|--------------|----------------|----------------|----------------|----------------|----------------|-------|
| $y_2$ | 1.73928571429  | $+3.4625y_4$ | $+3.328571y_5$ | $+3.705357y_6$ | $+0.267857y_1$ | $-1.003571y_8$ | $+1.326786y_9$ | $-0.$ |
| $y_3$ | 0.610714285714 | $-5.2875y_4$ | $-4.328571y_5$ | $-5.830357y_6$ | $-0.517857y_1$ | $-0.246429y_8$ | $+3.248214y_9$ | $-0.$ |
| $y_7$ | 0.107142857143 | $-1.375y_4$  | $-1.285714y_5$ | $-0.803571y_6$ | $-0.178571y_1$ | $-0.464286y_8$ | $-0.017857y_9$ | $-0.$ |
| $z$   | 0.45           | $-9.375y_4$  | $-6.3y_5$      | $-5.575y_6$    | $-0.75y_1$     | $-4.65y_8$     | $-3.775y_9$    | $+0.$ |

The Final Dual Dictionary is:

|          |                |            |                 |                |                |                |                |       |
|----------|----------------|------------|-----------------|----------------|----------------|----------------|----------------|-------|
| $y_2$    | 1.35454545455  | $+8.4y_4$  | $+7.945455y_5$  | $+6.590909y_6$ | $+0.909091y_1$ | $+0.663636y_8$ | $+1.390909y_9$ | $+3.$ |
| $y_3$    | 0.518181818182 | $-4.1y_4$  | $-3.218182y_5$  | $-5.136364y_6$ | $-0.363636y_1$ | $+0.154545y_8$ | $+3.263636y_9$ | $+0.$ |
| $y_{11}$ | 0.545454545455 | $-7y_4$    | $-6.545455y_5$  | $-4.090909y_6$ | $-0.909091y_1$ | $-2.363636y_8$ | $-0.090909y_9$ | $-5.$ |
| $z$      | 0.763636363636 | $-13.4y_4$ | $-10.063636y_5$ | $-7.927273y_6$ | $-1.272727y_1$ | $-6.009091y_8$ | $-3.827273y_9$ | $-2.$ |

Final primal dictionary obtained:

|          |                   |                |                |                   |
|----------|-------------------|----------------|----------------|-------------------|
| $x_4$    | 13.4              | $-8.4x_2$      | $+4.1x_3$      | $+7x_{11}$        |
| $x_5$    | 10.0636363636     | $-7.945455x_2$ | $+3.218182x_3$ | $+6.545455x_{11}$ |
| $x_6$    | 7.92727272727     | $-6.590909x_2$ | $+5.136364x_3$ | $+4.090909x_{11}$ |
| $x_1$    | 1.27272727273     | $-0.909091x_2$ | $+0.363636x_3$ | $+0.909091x_{11}$ |
| $x_8$    | 6.00909090909     | $-0.663636x_2$ | $-0.154545x_3$ | $+2.363636x_{11}$ |
| $x_9$    | 3.82727272727     | $-1.390909x_2$ | $-3.263636x_3$ | $+0.090909x_{11}$ |
| $x_7$    | 2.92727272727     | $-3.590909x_2$ | $-0.863636x_3$ | $+5.090909x_{11}$ |
| $x_{10}$ | 1.79090909091     | $-2.236364x_2$ | $+0.054545x_3$ | $+3.636364x_{11}$ |
| $x_9$    | 1.45454545455     | $-1.781818x_2$ | $+0.172727x_3$ | $+3.181818x_{11}$ |
| $x_{12}$ | 1.65454545455     | $-2.681818x_2$ | $-0.227273x_3$ | $+4.181818x_{11}$ |
| $x_{13}$ | 0.918181818182    | $-0.927273x_2$ | $+0.290909x_3$ | $+2.727273x_{11}$ |
| $x_{14}$ | 2.1               | $-3.2x_2$      | $-0.6x_3$      | $+5x_{11}$        |
| $z$      | $-0.763636363636$ | $-1.354545x_2$ | $-0.518182x_3$ | $-0.545455x_{11}$ |

After cutting plane is added

|          |                   |                |                |                   |
|----------|-------------------|----------------|----------------|-------------------|
| $x_4$    | 13.4              | $-8.4x_2$      | $+4.1x_3$      | $+7x_{11}$        |
| $x_5$    | 10.0636363636     | $-7.945455x_2$ | $+3.218182x_3$ | $+6.545455x_{11}$ |
| $x_6$    | 7.92727272727     | $-6.590909x_2$ | $+5.136364x_3$ | $+4.090909x_{11}$ |
| $x_1$    | 1.27272727273     | $-0.909091x_2$ | $+0.363636x_3$ | $+0.909091x_{11}$ |
| $x_8$    | 6.00909090909     | $-0.663636x_2$ | $-0.154545x_3$ | $+2.363636x_{11}$ |
| $x_9$    | 3.82727272727     | $-1.390909x_2$ | $-3.263636x_3$ | $+0.090909x_{11}$ |
| $x_7$    | 2.92727272727     | $-3.590909x_2$ | $-0.863636x_3$ | $+5.090909x_{11}$ |
| $x_{10}$ | 1.79090909091     | $-2.236364x_2$ | $+0.054545x_3$ | $+3.636364x_{11}$ |
| $x_9$    | 1.45454545455     | $-1.781818x_2$ | $+0.172727x_3$ | $+3.181818x_{11}$ |
| $x_{12}$ | 1.65454545455     | $-2.681818x_2$ | $-0.227273x_3$ | $+4.181818x_{11}$ |
| $x_{13}$ | 0.918181818182    | $-0.927273x_2$ | $+0.290909x_3$ | $+2.727273x_{11}$ |
| $x_{14}$ | 2.1               | $-3.2x_2$      | $-0.6x_3$      | $+5x_{11}$        |
| $x_{15}$ | -0.4              | $+0.4x_2$      | $+0.9x_3$      | $+1x_{11}$        |
| $x_{16}$ | -0.0636363636364  | $+0.945455x_2$ | $+0.781818x_3$ | $+0.454545x_{11}$ |
| $x_{17}$ | -0.927272727273   | $+0.590909x_2$ | $+0.863636x_3$ | $+0.909091x_{11}$ |
| $x_{18}$ | -0.272727272727   | $+0.909091x_2$ | $+0.636364x_3$ | $+0.090909x_{11}$ |
| $x_{19}$ | -0.00909090909091 | $+0.663636x_2$ | $+0.154545x_3$ | $+0.636364x_{11}$ |
| $x_{20}$ | -0.827272727273   | $+0.390909x_2$ | $+0.263636x_3$ | $+0.909091x_{11}$ |
| $x_{21}$ | -0.927272727273   | $+0.590909x_2$ | $+0.863636x_3$ | $+0.909091x_{11}$ |
| $x_{22}$ | -0.790909090909   | $+0.236364x_2$ | $+0.945455x_3$ | $+0.363636x_{11}$ |
| $x_{23}$ | -0.454545454545   | $+0.781818x_2$ | $+0.827273x_3$ | $+0.818182x_{11}$ |
| $x_{24}$ | -0.654545454545   | $+0.681818x_2$ | $+0.227273x_3$ | $+0.818182x_{11}$ |
| $x_{25}$ | -0.918181818182   | $+0.927273x_2$ | $+0.709091x_3$ | $+0.272727x_{11}$ |
| $x_{26}$ | -0.1              | $+0.2x_2$      | $+0.6x_3$      | $+1x_{11}$        |
| $z$      | -0.763636363636   | $-1.354545x_2$ | $-0.518182x_3$ | $-0.545455x_{11}$ |

Forming the dual dictionary:

|          |                |            |                 |                |                |                |                |                   |
|----------|----------------|------------|-----------------|----------------|----------------|----------------|----------------|-------------------|
| $y_2$    | 1.35454545455  | $+8.4y_4$  | $+7.945455y_5$  | $+6.590909y_6$ | $+0.909091y_1$ | $+0.663636y_8$ | $+1.390909y_9$ | $+3.545455y_{11}$ |
| $y_3$    | 0.518181818182 | $-4.1y_4$  | $-3.218182y_5$  | $-5.136364y_6$ | $-0.363636y_1$ | $+0.154545y_8$ | $+3.263636y_9$ | $+0.545455y_{11}$ |
| $y_{11}$ | 0.545454545455 | $-7y_4$    | $-6.545455y_5$  | $-4.090909y_6$ | $-0.909091y_1$ | $-2.363636y_8$ | $-0.090909y_9$ | $-5.045455y_{11}$ |
| $z$      | 0.763636363636 | $-13.4y_4$ | $-10.063636y_5$ | $-7.927273y_6$ | $-1.272727y_1$ | $-6.009091y_8$ | $-3.827273y_9$ | $-2.945455y_{11}$ |

The Final Dual Dictionary is:

|          |                |                 |                 |                 |                   |                |                |                   |
|----------|----------------|-----------------|-----------------|-----------------|-------------------|----------------|----------------|-------------------|
| $y_2$    | 0.657142857143 | $+14.071429y_4$ | $+12.457143y_5$ | $+13.428571y_6$ | $+0.814286y_{15}$ | $+0.6y_8$      | $+2.771429y_9$ | $+0.571429y_{11}$ |
| $y_{25}$ | 0.571428571429 | $-3.285714y_4$  | $-2.095238y_5$  | $-6.269841y_6$  | $-0.968254y_{15}$ | $+1.333333y_8$ | $+3.714286y_9$ | $+0.571429y_{11}$ |
| $y_{20}$ | 0.428571428571 | $-6.714286y_4$  | $-6.571429y_5$  | $-2.619048y_6$  | $-0.809524y_{15}$ | $-3y_8$        | $-6.714286y_9$ | $+0.571429y_{11}$ |
| $z$      | 1.64285714286  | $-21.971429y_4$ | $-17.423810y_5$ | $-15.850794y_6$ | $-1.158730y_{15}$ | $-7.266667y_8$ | $-5.071429y_9$ | $-0.571429y_{11}$ |

Final primal dictionary obtained:

|          |                 |   |
|----------|-----------------|---|
| $x_4$    | 21.9714285714   | $-14.071429x_2 + 3.285714x_{25} + 6.714286x_{20}$ |
| $x_5$    | 17.4238095238   | $-12.457143x_2 + 2.095238x_{25} + 6.571429x_{20}$ |
| $x_6$    | 15.8507936508   | $-13.428571x_2 + 6.269841x_{25} + 2.619048x_{20}$ |
| $x_{15}$ | 1.15873015873   | $-0.814286x_2 + 0.968254x_{25} + 0.809524x_{20}$  |
| $x_8$    | 7.26666666667   | $-0.6x_2 - 1.333333x_{25} + 3x_{20}$              |
| $x_7$    | 5.07142857143   | $-2.771429x_2 - 3.714286x_{25} + 6.714286x_{20}$  |
| $x_1$    | 2.20634920635   | $-1.428571x_2 + 0.158730x_{25} + 0.952381x_{20}$  |
| $x_{10}$ | 4.03650793651   | $-2.514286x_2 - 1.587302x_{25} + 4.476190x_{20}$  |
| $x_9$    | 3.55238095238   | $-2.185714x_2 - 1.190476x_{25} + 3.857143x_{20}$  |
| $x_{12}$ | 3.92857142857   | $-2.628571x_2 - 2.285714x_{25} + 5.285714x_{20}$  |
| $x_{13}$ | 2.86825396825   | $-1.457143x_2 - 0.793651x_{25} + 3.238095x_{20}$  |
| $x_{14}$ | 4.46984126984   | $-2.714286x_2 - 3.253968x_{25} + 6.476190x_{20}$  |
| $x_9$    | 0.411111111111  | $+2.8x_2 - 5.222222x_{25} + 1.666667x_{20}$       |
| $x_{16}$ | 1.04126984127   | $-0.085714x_2 + 1.031746x_{25} + 0.190476x_{20}$  |
| $x_3$    | 1.06349206349   | $-1.285714x_2 + 1.587302x_{25} - 0.476190x_{20}$  |
| $x_{17}$ | 0.538095238095  | $-0.571429x_2 + 0.952381x_{25} + 0.714286x_{20}$  |
| $x_{19}$ | 0.538095238095  | $+0.428571x_2 - 0.047619x_{25} + 0.714286x_{20}$  |
| $x_{11}$ | 0.601587301587  | $-0.057143x_2 - 0.460317x_{25} + 1.238095x_{20}$  |
| $x_{21}$ | 0.538095238095  | $-0.571429x_2 + 0.952381x_{25} + 0.714286x_{20}$  |
| $x_{18}$ | 0.45873015873   | $+0.085714x_2 + 0.968254x_{25} - 0.190476x_{20}$  |
| $x_{23}$ | 0.91746031746   | $-0.328571x_2 + 0.936508x_{25} + 0.619048x_{20}$  |
| $x_{24}$ | 0.0793650793651 | $+0.342857x_2 - 0.015873x_{25} + 0.904762x_{20}$  |
| $x_{22}$ | 0.433333333333  | $-1x_2 + 1.333333x_{25} - 0x_{20}$                |
| $x_{26}$ | 1.13968253968   | $-0.628571x_2 + 0.492063x_{25} + 0.952381x_{20}$  |
| $z$      | -1.64285714286  | $-0.657143x_2 - 0.571429x_{25} - 0.428571x_{20}$  |



After cutting plane is added

|          |                  |   |
|----------|------------------|---|
| $x_4$    | 21.9714285714    | $-14.071429x_2 + 3.285714x_{25} + 6.714286x_{20}$ |
| $x_5$    | 17.4238095238    | $-12.457143x_2 + 2.095238x_{25} + 6.571429x_{20}$ |
| $x_6$    | 15.8507936508    | $-13.428571x_2 + 6.269841x_{25} + 2.619048x_{20}$ |
| $x_{15}$ | 1.15873015873    | $-0.814286x_2 + 0.968254x_{25} + 0.809524x_{20}$  |
| $x_8$    | 7.26666666667    | $-0.6x_2 - 1.333333x_{25} + 3x_{20}$              |
| $x_7$    | 5.07142857143    | $-2.771429x_2 - 3.714286x_{25} + 6.714286x_{20}$  |
| $x_1$    | 2.20634920635    | $-1.428571x_2 + 0.158730x_{25} + 0.952381x_{20}$  |
| $x_{10}$ | 4.03650793651    | $-2.514286x_2 - 1.587302x_{25} + 4.476190x_{20}$  |
| $x_9$    | 3.55238095238    | $-2.185714x_2 - 1.190476x_{25} + 3.857143x_{20}$  |
| $x_{12}$ | 3.92857142857    | $-2.628571x_2 - 2.285714x_{25} + 5.285714x_{20}$  |
| $x_{13}$ | 2.86825396825    | $-1.457143x_2 - 0.793651x_{25} + 3.238095x_{20}$  |
| $x_{14}$ | 4.46984126984    | $-2.714286x_2 - 3.253968x_{25} + 6.476190x_{20}$  |
| $x_9$    | 0.411111111111   | $+2.8x_2 - 5.222222x_{25} + 1.666667x_{20}$       |
| $x_{16}$ | 1.04126984127    | $-0.085714x_2 + 1.031746x_{25} + 0.190476x_{20}$  |
| $x_3$    | 1.06349206349    | $-1.285714x_2 + 1.587302x_{25} - 0.476190x_{20}$  |
| $x_{17}$ | 0.538095238095   | $-0.571429x_2 + 0.952381x_{25} + 0.714286x_{20}$  |
| $x_{19}$ | 0.538095238095   | $+0.428571x_2 - 0.047619x_{25} + 0.714286x_{20}$  |
| $x_{11}$ | 0.601587301587   | $-0.057143x_2 - 0.460317x_{25} + 1.238095x_{20}$  |
| $x_{21}$ | 0.538095238095   | $-0.571429x_2 + 0.952381x_{25} + 0.714286x_{20}$  |
| $x_{18}$ | 0.45873015873    | $+0.085714x_2 + 0.968254x_{25} - 0.190476x_{20}$  |
| $x_{23}$ | 0.91746031746    | $-0.328571x_2 + 0.936508x_{25} + 0.619048x_{20}$  |
| $x_{24}$ | 0.0793650793651  | $+0.342857x_2 - 0.015873x_{25} + 0.904762x_{20}$  |
| $x_{22}$ | 0.433333333333   | $-1x_2 + 1.333333x_{25} - 0x_{20}$                |
| $x_{26}$ | 1.13968253968    | $-0.628571x_2 + 0.492063x_{25} + 0.952381x_{20}$  |
| $x_{27}$ | -0.971428571429  | $+0.071429x_2 + 0.714286x_{25} + 0.285714x_{20}$  |
| $x_{28}$ | -0.42380952381   | $+0.457143x_2 + 0.904762x_{25} + 0.428571x_{20}$  |
| $x_{29}$ | -0.850793650794  | $+0.428571x_2 + 0.730159x_{25} + 0.380952x_{20}$  |
| $x_{30}$ | -0.15873015873   | $+0.814286x_2 + 0.031746x_{25} + 0.190476x_{20}$  |
| $x_{31}$ | -0.266666666667  | $+0.6x_2 + 0.333333x_{25} + 0x_{20}$              |
| $x_{32}$ | -0.0714285714286 | $+0.771429x_2 + 0.714286x_{25} + 0.285714x_{20}$  |
| $x_{33}$ | -0.206349206349  | $+0.428571x_2 + 0.841270x_{25} + 0.047619x_{20}$  |
| $x_{34}$ | -0.0365079365079 | $+0.514286x_2 + 0.587302x_{25} + 0.523810x_{20}$  |
| $x_{35}$ | -0.552380952381  | $+0.185714x_2 + 0.190476x_{25} + 0.142857x_{20}$  |
| $x_{36}$ | -0.928571428571  | $+0.628571x_2 + 0.285714x_{25} + 0.714286x_{20}$  |
| $x_{37}$ | -0.868253968254  | $+0.457143x_2 + 0.793651x_{25} + 0.761905x_{20}$  |
| $x_{38}$ | -0.469841269841  | $+0.714286x_2 + 0.253968x_{25} + 0.523810x_{20}$  |
| $x_{39}$ | -0.411111111111  | $+0.2x_2 + 0.222222x_{25} + 0.333333x_{20}$       |
| $x_{40}$ | -0.0412698412698 | $+0.085714x_2 + 0.968254x_{25} + 0.809524x_{20}$  |
| $x_{41}$ | -0.0634920634921 | $+0.285714x_2 + 0.412698x_{25} + 0.476190x_{20}$  |
| $x_{42}$ | -0.538095238095  | $+0.571429x_2 + 0.047619x_{25} + 0.285714x_{20}$  |
| $x_{43}$ | -0.538095238095  | $+0.571429x_2 + 0.047619x_{25} + 0.285714x_{20}$  |
| $x_{44}$ | -0.601587301587  | $+0.057143x_2 + 0.460317x_{25} + 0.761905x_{20}$  |
| $x_{45}$ | -0.538095238095  | $+0.571429x_2 + 0.047619x_{25} + 0.285714x_{20}$  |
| $x_{46}$ | -0.45873015873   | $+0.914286x_2 + 0.031746x_{25} + 0.190476x_{20}$  |
| $x_{47}$ | -0.91746031746   | $+0.328571x_2 + 0.063492x_{25} + 0.380952x_{20}$  |
| $x_{48}$ | -0.0793650793651 | $+0.657143x_2 + 0.015873x_{25} + 0.095238x_{20}$  |
| $x_{49}$ | -0.433333333333  | $+1x_2 + 0.666667x_{25} + 0x_{20}$                |
| $x_{50}$ | 0.139682539683   | $+0.628571x_2 + 0.507037x_{25} + 0.047619x_{20}$  |

Forming the dual dictionary:

|          |                |                  |                  |                  |                    |                 |          |
|----------|----------------|------------------|------------------|------------------|--------------------|-----------------|----------|
| $y_2$    | 0.657142857143 | +14.071429 $y_4$ | +12.457143 $y_5$ | +13.428571 $y_6$ | +0.814286 $y_{15}$ | +0.6 $y_8$      | +2.77142 |
| $y_{25}$ | 0.571428571429 | -3.285714 $y_4$  | -2.095238 $y_5$  | -6.269841 $y_6$  | -0.968254 $y_{15}$ | +1.333333 $y_8$ | +3.71428 |
| $y_{20}$ | 0.428571428571 | -6.714286 $y_4$  | -6.571429 $y_5$  | -2.619048 $y_6$  | -0.809524 $y_{15}$ | -3 $y_8$        | -6.71428 |
| $z$      | 1.64285714286  | -21.971429 $y_4$ | -17.423810 $y_5$ | -15.850794 $y_6$ | -1.158730 $y_{15}$ | -7.266667 $y_8$ | -5.07142 |

The Final Dual Dictionary is:

|          |                         |             |             |                  |                    |             |             |           |
|----------|-------------------------|-------------|-------------|------------------|--------------------|-------------|-------------|-----------|
| $y_{31}$ | -1.02140518266 $e - 14$ | +17 $y_4$   | +20 $y_5$   | -8.333333 $y_6$  | +0.333333 $y_{15}$ | +16 $y_8$   | +38 $y_7$   | +3.33333  |
| $y_{35}$ | 3                       | -47 $y_4$   | -46 $y_5$   | -18.333333 $y_6$ | -5.666667 $y_{15}$ | -21 $y_8$   | -47 $y_7$   | -6.66667  |
| $y_2$    | 0.1                     | +12.6 $y_4$ | +9 $y_5$    | +21.833333 $y_6$ | +1.666667 $y_{15}$ | -5.1 $y_8$  | -11.3 $y_7$ | +0.666667 |
| $z$      | 3.3                     | -43.4 $y_4$ | -37.5 $y_5$ | -28.2 $y_6$      | -4.2 $y_{15}$      | -14.6 $y_8$ | -20.9 $y_7$ | -5 $y_1$  |

Final primal dictionary obtained:

|          |                    |                    |                    |                 |
|----------|--------------------|--------------------|--------------------|-----------------|
| $x_4$    | 43.4               | $-17x_{31}$        | $+47x_{35}$        | $-12.6x_2$      |
| $x_5$    | 37.5               | $-20x_{31}$        | $+46x_{35}$        | $-9x_2$         |
| $x_6$    | 28.2               | $+8.333333x_{31}$  | $+18.333333x_{35}$ | $-21.833333x_2$ |
| $x_{15}$ | 4.2                | $-0.333333x_{31}$  | $+5.666667x_{35}$  | $-1.666667x_2$  |
| $x_8$    | 14.6               | $-16x_{31}$        | $+21x_{35}$        | $+5.1x_2$       |
| $x_7$    | 20.9               | $-38x_{31}$        | $+47x_{35}$        | $+11.3x_2$      |
| $x_1$    | 5                  | $-3.333333x_{31}$  | $+6.666667x_{35}$  | $-0.666667x_2$  |
| $x_{10}$ | 15.3               | $-22.666667x_{31}$ | $+31.333333x_{35}$ | $+5.266667x_2$  |
| $x_9$    | 13.4               | $-19x_{31}$        | $+27x_{35}$        | $+4.2x_2$       |
| $x_{12}$ | 16.9               | $-28x_{31}$        | $+37x_{35}$        | $+7.3x_2$       |
| $x_{13}$ | 11.3               | $-15.333333x_{31}$ | $+22.666667x_{35}$ | $+3.533333x_2$  |
| $x_{14}$ | 20                 | $-35.666667x_{31}$ | $+45.333333x_{35}$ | $+10.266667x_2$ |
| $x_{20}$ | 2.8                | $-4x_{31}$         | $+7x_{35}$         | $+1.1x_2$       |
| $x_{16}$ | 2.4                | $+2.333333x_{31}$  | $+1.333333x_{35}$  | $-1.733333x_2$  |
| $x_3$    | 1                  | $+6.666667x_{31}$  | $-3.333333x_{35}$  | $-4.666667x_2$  |
| $x_{17}$ | 3.3                | $-0x_{31}$         | $+5x_{35}$         | $-1.5x_2$       |
| $x_{19}$ | 2.5                | $-3x_{31}$         | $+5x_{35}$         | $+1.3x_2$       |
| $x_{11}$ | 3.7                | $-6.333333x_{31}$  | $+8.666667x_{35}$  | $+2.133333x_2$  |
| $x_{21}$ | 3.3                | $-0x_{31}$         | $+5x_{35}$         | $-1.5x_2$       |
| $x_{18}$ | 0.7                | $+3.666667x_{31}$  | $-1.333333x_{35}$  | $-1.866667x_2$  |
| $x_{23}$ | 3.4                | $+0.333333x_{31}$  | $+4.333333x_{35}$  | $-1.333333x_2$  |
| $x_{24}$ | 2.6                | $-3.666667x_{31}$  | $+6.333333x_{35}$  | $+1.366667x_2$  |
| $x_{22}$ | 1.5                | $+4x_{31}$         | $-0x_{35}$         | $-3.4x_2$       |
| $x_{26}$ | 4.2                | $-2.333333x_{31}$  | $+6.666667x_{35}$  | $-0.466667x_2$  |
| $x_{25}$ | 0.8                | $+3x_{31}$         | $-0x_{35}$         | $-1.8x_2$       |
| $x_{28}$ | 1.5                | $+1x_{31}$         | $+3x_{35}$         | $-0.7x_2$       |
| $x_{29}$ | 0.8                | $+0.666667x_{31}$  | $+2.666667x_{35}$  | $-0.466667x_2$  |
| $x_{30}$ | 0.4                | $-0.666667x_{31}$  | $+1.333333x_{35}$  | $+0.966667x_2$  |
| $x_9$    | 0.9                | $-22.333333x_{31}$ | $+11.666667x_{35}$ | $+14.033333x_2$ |
| $x_{32}$ | 1.3                | $+1x_{31}$         | $+2x_{35}$         | $-0.2x_2$       |
| $x_{33}$ | 0.6                | $+2.333333x_{31}$  | $+0.333333x_{35}$  | $-1.033333x_2$  |
| $x_{34}$ | 1.9                | $-0.333333x_{31}$  | $+3.666667x_{35}$  | $+0.033333x_2$  |
| $x_{27}$ | 0.4                | $+1x_{31}$         | $+2x_{35}$         | $-0.9x_2$       |
| $x_{36}$ | 1.3                | $-2x_{31}$         | $+5x_{35}$         | $+0.9x_2$       |
| $x_{37}$ | 1.9                | $-0.666667x_{31}$  | $+5.333333x_{35}$  | $-0.133333x_2$  |
| $x_{38}$ | 1.2                | $-1.333333x_{31}$  | $+3.666667x_{35}$  | $+0.833333x_2$  |
| $x_{39}$ | 0.7                | $-0.666667x_{31}$  | $+2.333333x_{35}$  | $+0.166667x_2$  |
| $x_{40}$ | 3                  | $-0.333333x_{31}$  | $+5.666667x_{35}$  | $-0.766667x_2$  |
| $x_{41}$ | 1.6                | $-0.666667x_{31}$  | $+3.333333x_{35}$  | $+0.066667x_2$  |
| $x_{42}$ | 0.3                | $-1x_{31}$         | $+2x_{35}$         | $+0.8x_2$       |
| $x_{43}$ | 0.3                | $-1x_{31}$         | $+2x_{35}$         | $+0.8x_2$       |
| $x_{44}$ | 1.9                | $-1.666667x_{31}$  | $+5.333333x_{35}$  | $+0.066667x_2$  |
| $x_{45}$ | 0.3                | $-1x_{31}$         | $+2x_{35}$         | $+0.8x_2$       |
| $x_{46}$ | 0.1                | $-0.666667x_{31}$  | $+1.333333x_{35}$  | $+1.066667x_2$  |
| $x_{47}$ | 0.2                | $-1.333333x_{31}$  | $+2.666667x_{35}$  | $+0.633333x_2$  |
| $x_{48}$ | 0.2                | $-0.333333x_{31}$  | $+0.666667x_{35}$  | $+0.733333x_2$  |
| $x_{49}$ | 0.0999999999999999 | $+2x_{31}$         | $-0x_{35}$         | $-0.2x_2$       |
| $x_{50}$ | 0.4                | $+1.333333x_{31}$  | $+0.333333x_{35}$  | $-0.233333x_2$  |

After cutting plane is added

|          |                    |                    |                    |                 |
|----------|--------------------|--------------------|--------------------|-----------------|
| $x_4$    | 43.4               | $-17x_{31}$        | $+47x_{35}$        | $-12.6x_2$      |
| $x_5$    | 37.5               | $-20x_{31}$        | $+46x_{35}$        | $-9x_2$         |
| $x_6$    | 28.2               | $+8.333333x_{31}$  | $+18.333333x_{35}$ | $-21.833333x_2$ |
| $x_{15}$ | 4.2                | $-0.333333x_{31}$  | $+5.666667x_{35}$  | $-1.666667x_2$  |
| $x_8$    | 14.6               | $-16x_{31}$        | $+21x_{35}$        | $+5.1x_2$       |
| $x_7$    | 20.9               | $-38x_{31}$        | $+47x_{35}$        | $+11.3x_2$      |
| $x_1$    | 5                  | $-3.333333x_{31}$  | $+6.666667x_{35}$  | $-0.666667x_2$  |
| $x_{10}$ | 15.3               | $-22.666667x_{31}$ | $+31.333333x_{35}$ | $+5.266667x_2$  |
| $x_9$    | 13.4               | $-19x_{31}$        | $+27x_{35}$        | $+4.2x_2$       |
| $x_{12}$ | 16.9               | $-28x_{31}$        | $+37x_{35}$        | $+7.3x_2$       |
| $x_{13}$ | 11.3               | $-15.333333x_{31}$ | $+22.666667x_{35}$ | $+3.533333x_2$  |
| $x_{14}$ | 20                 | $-35.666667x_{31}$ | $+45.333333x_{35}$ | $+10.266667x_2$ |
| $x_{20}$ | 2.8                | $-4x_{31}$         | $+7x_{35}$         | $+1.1x_2$       |
| $x_{16}$ | 2.4                | $+2.333333x_{31}$  | $+1.333333x_{35}$  | $-1.733333x_2$  |
| $x_3$    | 1                  | $+6.666667x_{31}$  | $-3.333333x_{35}$  | $-4.666667x_2$  |
| $x_{17}$ | 3.3                | $-0x_{31}$         | $+5x_{35}$         | $-1.5x_2$       |
| $x_{19}$ | 2.5                | $-3x_{31}$         | $+5x_{35}$         | $+1.3x_2$       |
| $x_{11}$ | 3.7                | $-6.333333x_{31}$  | $+8.666667x_{35}$  | $+2.133333x_2$  |
| $x_{21}$ | 3.3                | $-0x_{31}$         | $+5x_{35}$         | $-1.5x_2$       |
| $x_{18}$ | 0.7                | $+3.666667x_{31}$  | $-1.333333x_{35}$  | $-1.866667x_2$  |
| $x_{23}$ | 3.4                | $+0.333333x_{31}$  | $+4.333333x_{35}$  | $-1.333333x_2$  |
| $x_{24}$ | 2.6                | $-3.666667x_{31}$  | $+6.333333x_{35}$  | $+1.366667x_2$  |
| $x_{22}$ | 1.5                | $+4x_{31}$         | $-0x_{35}$         | $-3.4x_2$       |
| $x_{26}$ | 4.2                | $-2.333333x_{31}$  | $+6.666667x_{35}$  | $-0.466667x_2$  |
| $x_{25}$ | 0.8                | $+3x_{31}$         | $-0x_{35}$         | $-1.8x_2$       |
| $x_{28}$ | 1.5                | $+1x_{31}$         | $+3x_{35}$         | $-0.7x_2$       |
| $x_{29}$ | 0.8                | $+0.666667x_{31}$  | $+2.666667x_{35}$  | $-0.466667x_2$  |
| $x_{30}$ | 0.4                | $-0.666667x_{31}$  | $+1.333333x_{35}$  | $+0.966667x_2$  |
| $x_9$    | 0.9                | $-22.333333x_{31}$ | $+11.666667x_{35}$ | $+14.033333x_2$ |
| $x_{32}$ | 1.3                | $+1x_{31}$         | $+2x_{35}$         | $-0.2x_2$       |
| $x_{33}$ | 0.6                | $+2.333333x_{31}$  | $+0.333333x_{35}$  | $-1.033333x_2$  |
| $x_{34}$ | 1.9                | $-0.333333x_{31}$  | $+3.666667x_{35}$  | $+0.033333x_2$  |
| $x_{27}$ | 0.4                | $+1x_{31}$         | $+2x_{35}$         | $-0.9x_2$       |
| $x_{36}$ | 1.3                | $-2x_{31}$         | $+5x_{35}$         | $+0.9x_2$       |
| $x_{37}$ | 1.9                | $-0.666667x_{31}$  | $+5.333333x_{35}$  | $-0.133333x_2$  |
| $x_{38}$ | 1.2                | $-1.333333x_{31}$  | $+3.666667x_{35}$  | $+0.833333x_2$  |
| $x_{39}$ | 0.7                | $-0.666667x_{31}$  | $+2.333333x_{35}$  | $+0.166667x_2$  |
| $x_{40}$ | 3                  | $-0.333333x_{31}$  | $+5.666667x_{35}$  | $-0.766667x_2$  |
| $x_{41}$ | 1.6                | $-0.666667x_{31}$  | $+3.333333x_{35}$  | $+0.066667x_2$  |
| $x_{42}$ | 0.3                | $-1x_{31}$         | $+2x_{35}$         | $+0.8x_2$       |
| $x_{43}$ | 0.3                | $-1x_{31}$         | $+2x_{35}$         | $+0.8x_2$       |
| $x_{44}$ | 1.9                | $-1.666667x_{31}$  | $+5.333333x_{35}$  | $+0.066667x_2$  |
| $x_{45}$ | 0.3                | $-1x_{31}$         | $+2x_{35}$         | $+0.8x_2$       |
| $x_{46}$ | 0.1                | $-0.666667x_{31}$  | $+1.333333x_{35}$  | $+1.066667x_2$  |
| $x_{47}$ | 0.2                | $-1.333333x_{31}$  | $+2.666667x_{35}$  | $+0.633333x_2$  |
| $x_{48}$ | 0.2                | $-0.333333x_{31}$  | $+0.666667x_{35}$  | $+0.733333x_2$  |
| $x_{49}$ | 0.0999999999999999 | $+2x_{31}$         | $-0x_{35}$         | $-0.2x_2$       |
| $x_{50}$ | 0.4                | $+1.333333x_{31}$  | $+0.333333x_{35}$  | $-0.233333x_2$  |

Forming the dual dictionary:

|          |                        |            |            |                 |                   |            |            |             |
|----------|------------------------|------------|------------|-----------------|-------------------|------------|------------|-------------|
| $y_{31}$ | $-1.02140518266e - 14$ | $+17y_4$   | $+20y_5$   | $-8.333333y_6$  | $+0.333333y_{15}$ | $+16y_8$   | $+38y_7$   | $+3.333333$ |
| $y_{35}$ | $3$                    | $-47y_4$   | $-46y_5$   | $-18.333333y_6$ | $-5.666667y_{15}$ | $-21y_8$   | $-47y_7$   | $-6.666667$ |
| $y_2$    | $0.1$                  | $+12.6y_4$ | $+9y_5$    | $+21.833333y_6$ | $+1.666667y_{15}$ | $-5.1y_8$  | $-11.3y_7$ | $+0.666667$ |
| $z$      | $3.3$                  | $-43.4y_4$ | $-37.5y_5$ | $-28.2y_6$      | $-4.2y_{15}$      | $-14.6y_8$ | $-20.9y_7$ | $-5y_1$     |

The Final Dual Dictionary is:

|          |                    |                |                |                |                   |                |             |
|----------|--------------------|----------------|----------------|----------------|-------------------|----------------|-------------|
| $y_{81}$ | $2.74025289779$    | $+0.771075y_4$ | $+0.026344y_1$ | $-0.961538y_3$ | $-2.270021y_{15}$ | $-1.081665y_8$ | $+1.430980$ |
| $y_6$    | $0.00885142255005$ | $-0.862381y_4$ | $-0.077977y_1$ | $-0.153846y_3$ | $-0.100738y_{15}$ | $+0.041728y_8$ | $-0.715701$ |
| $y_{12}$ | $0.00263435194942$ | $-0.863804y_4$ | $-0.142255y_1$ | $+0.192308y_3$ | $-0.041886y_{15}$ | $-0.559009y_8$ | $-0.927292$ |
| $z$      | $3.82794520548$    | $-4.251233y_4$ | $-0.389041y_1$ | $-0.2y_3$      | $-1.332329y_{15}$ | $-6.653973y_8$ | $-1.216712$ |

Final primal dictionary obtained:

|          |                 |  |
|----------|-----------------|--|
| $x_4$    | 4.25123287671   | $-0.771075x_{81} + 0.862381x_6 + 0.863804x_{12}$ |
| $x_1$    | 0.38904109589   | $-0.026344x_{81} + 0.077977x_6 + 0.142255x_{12}$ |
| $x_3$    | 0.2             | $+0.961538x_{81} + 0.153846x_6 - 0.192308x_{12}$ |
| $x_{15}$ | 1.33232876712   | $+2.270021x_{81} + 0.100738x_6 + 0.041886x_{12}$ |
| $x_8$    | 6.65397260274   | $+1.081665x_{81} - 0.041728x_6 + 0.559009x_{12}$ |
| $x_5$    | 1.21671232877   | $-1.430980x_{81} + 0.715701x_6 + 0.927292x_{12}$ |
| $x_{47}$ | 0.0298630136986 | $+1.158325x_{81} - 0.008641x_6 + 0.045047x_{12}$ |
| $x_{10}$ | 0.580547945205  | $+0.366702x_{81} + 0.034563x_6 + 0.819810x_{12}$ |
| $x_9$    | 0.74602739726   | $+0.668335x_{81} + 0.041728x_6 + 0.690991x_{12}$ |
| $x_7$    | 0.189041095891  | $-0.987882x_{81} - 0.075869x_6 + 1.334563x_{12}$ |
| $x_{13}$ | 1.45561643836   | $+1.489463x_{81} + 0.031191x_6 + 0.556902x_{12}$ |
| $x_{14}$ | 0.0682191780822 | $-0.307165x_{81} - 0.050790x_6 + 1.258693x_{12}$ |
| $x_{20}$ | 0.687397260274  | $+1.565859x_{81} + 0.005058x_6 + 0.144362x_{12}$ |
| $x_{16}$ | 2.21890410959   | $+2.381981x_{81} + 0.069336x_6 - 0.062698x_{12}$ |
| $x_{31}$ | 1.23917808219   | $+1.488409x_{81} - 0.005690x_6 - 0.037408x_{12}$ |
| $x_{17}$ | 1.07945205479   | $+2.402529x_{81} + 0.088514x_6 + 0.026344x_{12}$ |
| $x_{19}$ | 1.77068493151   | $+1.573762x_{81} - 0.018335x_6 + 0.101686x_{12}$ |
| $x_{11}$ | 0.808219178082  | $+0.885142x_{81} - 0.020021x_6 + 0.220232x_{12}$ |
| $x_{21}$ | 1.07945205479   | $+2.402529x_{81} + 0.088514x_6 + 0.026344x_{12}$ |
| $x_{18}$ | 1.61917808219   | $+1.873024x_{81} + 0.055848x_6 - 0.114331x_{12}$ |
| $x_{23}$ | 1.82657534247   | $+2.535037x_{81} + 0.076291x_6 + 0.010801x_{12}$ |
| $x_{24}$ | 1.32054794521   | $+1.828240x_{81} - 0.011591x_6 + 0.127503x_{12}$ |
| $x_{22}$ | 0.131780821918  | $+1.537935x_{81} + 0.127713x_6 - 0.104847x_{12}$ |
| $x_{26}$ | 1.2002739726    | $+1.721812x_{81} + 0.063435x_6 + 0.102213x_{12}$ |
| $x_{25}$ | 1.16904109589   | $+2.127503x_{81} + 0.062592x_6 - 0.088514x_{12}$ |
| $x_{28}$ | 1.77890410959   | $+3.189673x_{81} + 0.038567x_6 - 0.024236x_{12}$ |
| $x_{29}$ | 1.06191780822   | $+2.706533x_{81} + 0.028662x_6 - 0.015279x_{12}$ |
| $x_{30}$ | 1.52410958904   | $+1.423340x_{81} - 0.033087x_6 + 0.013962x_{12}$ |
| $x_9$    | 0.660547945206  | $-4.864067x_{81} - 0.442360x_6 + 0.665964x_{12}$ |
| $x_{32}$ | 2.39506849315   | $+2.968915x_{81} + 0.012013x_6 - 0.032139x_{12}$ |
| $x_{33}$ | 1.60712328767   | $+2.420969x_{81} + 0.033930x_6 - 0.073235x_{12}$ |
| $x_{34}$ | 1.96684931507   | $+2.737619x_{81} + 0.016649x_6 + 0.016860x_{12}$ |
| $x_{35}$ | 0.11397260274   | $+0.870126x_{81} + 0.004426x_6 + 0.001317x_{12}$ |
| $x_{36}$ | 1.06575342466   | $+2.542677x_{81} - 0.006322x_6 + 0.069547x_{12}$ |
| $x_{37}$ | 1.43369863014   | $+3.475237x_{81} + 0.033298x_6 + 0.033720x_{12}$ |
| $x_{38}$ | 1.51589041096   | $+2.288198x_{81} - 0.013066x_6 + 0.043730x_{12}$ |
| $x_{39}$ | 0.449863013699  | $+1.254478x_{81} + 0.006744x_6 + 0.025817x_{12}$ |
| $x_{40}$ | 1.80657534247   | $+3.438883x_{81} + 0.060906x_6 + 0.030032x_{12}$ |
| $x_{41}$ | 1.27780821918   | $+1.994731x_{81} + 0.015595x_6 + 0.028451x_{12}$ |
| $x_{42}$ | 0.77698630137   | $+1.290832x_{81} - 0.020864x_6 + 0.029505x_{12}$ |
| $x_{43}$ | 0.77698630137   | $+1.290832x_{81} - 0.020864x_6 + 0.029505x_{12}$ |
| $x_{44}$ | 0.566575342466  | $+2.246575x_{81} + 0.030137x_6 + 0.068493x_{12}$ |
| $x_{45}$ | 0.77698630137   | $+1.290832x_{81} - 0.020864x_6 + 0.029505x_{12}$ |
| $x_{46}$ | 1.4101369863    | $+1.553214x_{81} - 0.037513x_6 + 0.012645x_{12}$ |
| $x_{56}$ | 0.402191780822  | $+0.909115x_{81} - 0.030980x_6 - 0.009220x_{12}$ |
| $x_{48}$ | 1.22712328767   | $+1.036354x_{81} - 0.027608x_6 + 0.003688x_{12}$ |
| $x_{49}$ | 2.20630136986   | $+2.717071x_{81} - 0.002529x_6 - 0.072181x_{12}$ |
| $x_{55}$ | 1.65616438356   | $+1.971549x_{81} + 0.004215x_6 - 0.046365x_{12}$ |

After cutting plane is added

|          |                 |  |
|----------|-----------------|--|
| $x_4$    | 4.25123287671   | $-0.771075x_{81} + 0.862381x_6 + 0.863804x_{12}$ |
| $x_1$    | 0.38904109589   | $-0.026344x_{81} + 0.077977x_6 + 0.142255x_{12}$ |
| $x_3$    | 0.2             | $+0.961538x_{81} + 0.153846x_6 - 0.192308x_{12}$ |
| $x_{15}$ | 1.33232876712   | $+2.270021x_{81} + 0.100738x_6 + 0.041886x_{12}$ |
| $x_8$    | 6.65397260274   | $+1.081665x_{81} - 0.041728x_6 + 0.559009x_{12}$ |
| $x_5$    | 1.21671232877   | $-1.430980x_{81} + 0.715701x_6 + 0.927292x_{12}$ |
| $x_{47}$ | 0.0298630136986 | $+1.158325x_{81} - 0.008641x_6 + 0.045047x_{12}$ |
| $x_{10}$ | 0.580547945205  | $+0.366702x_{81} + 0.034563x_6 + 0.819810x_{12}$ |
| $x_9$    | 0.74602739726   | $+0.668335x_{81} + 0.041728x_6 + 0.690991x_{12}$ |
| $x_7$    | 0.189041095891  | $-0.987882x_{81} - 0.075869x_6 + 1.334563x_{12}$ |
| $x_{13}$ | 1.45561643836   | $+1.489463x_{81} + 0.031191x_6 + 0.556902x_{12}$ |
| $x_{14}$ | 0.0682191780822 | $-0.307165x_{81} - 0.050790x_6 + 1.258693x_{12}$ |
| $x_{20}$ | 0.687397260274  | $+1.565859x_{81} + 0.005058x_6 + 0.144362x_{12}$ |
| $x_{16}$ | 2.21890410959   | $+2.381981x_{81} + 0.069336x_6 - 0.062698x_{12}$ |
| $x_{31}$ | 1.23917808219   | $+1.488409x_{81} - 0.005690x_6 - 0.037408x_{12}$ |
| $x_{17}$ | 1.07945205479   | $+2.402529x_{81} + 0.088514x_6 + 0.026344x_{12}$ |
| $x_{19}$ | 1.77068493151   | $+1.573762x_{81} - 0.018335x_6 + 0.101686x_{12}$ |
| $x_{11}$ | 0.808219178082  | $+0.885142x_{81} - 0.020021x_6 + 0.220232x_{12}$ |
| $x_{21}$ | 1.07945205479   | $+2.402529x_{81} + 0.088514x_6 + 0.026344x_{12}$ |
| $x_{18}$ | 1.61917808219   | $+1.873024x_{81} + 0.055848x_6 - 0.114331x_{12}$ |
| $x_{23}$ | 1.82657534247   | $+2.535037x_{81} + 0.076291x_6 + 0.010801x_{12}$ |
| $x_{24}$ | 1.32054794521   | $+1.828240x_{81} - 0.011591x_6 + 0.127503x_{12}$ |
| $x_{22}$ | 0.131780821918  | $+1.537935x_{81} + 0.127713x_6 - 0.104847x_{12}$ |
| $x_{26}$ | 1.2002739726    | $+1.721812x_{81} + 0.063435x_6 + 0.102213x_{12}$ |
| $x_{25}$ | 1.16904109589   | $+2.127503x_{81} + 0.062592x_6 - 0.088514x_{12}$ |
| $x_{28}$ | 1.77890410959   | $+3.189673x_{81} + 0.038567x_6 - 0.024236x_{12}$ |
| $x_{29}$ | 1.06191780822   | $+2.706533x_{81} + 0.028662x_6 - 0.015279x_{12}$ |
| $x_{30}$ | 1.52410958904   | $+1.423340x_{81} - 0.033087x_6 + 0.013962x_{12}$ |
| $x_9$    | 0.660547945206  | $-4.864067x_{81} - 0.442360x_6 + 0.665964x_{12}$ |
| $x_{32}$ | 2.39506849315   | $+2.968915x_{81} + 0.012013x_6 - 0.032139x_{12}$ |
| $x_{33}$ | 1.60712328767   | $+2.420969x_{81} + 0.033930x_6 - 0.073235x_{12}$ |
| $x_{34}$ | 1.96684931507   | $+2.737619x_{81} + 0.016649x_6 + 0.016860x_{12}$ |
| $x_{35}$ | 0.11397260274   | $+0.870126x_{81} + 0.004426x_6 + 0.001317x_{12}$ |
| $x_{36}$ | 1.06575342466   | $+2.542677x_{81} - 0.006322x_6 + 0.069547x_{12}$ |
| $x_{37}$ | 1.43369863014   | $+3.475237x_{81} + 0.033298x_6 + 0.033720x_{12}$ |
| $x_{38}$ | 1.51589041096   | $+2.288198x_{81} - 0.013066x_6 + 0.043730x_{12}$ |
| $x_{39}$ | 0.449863013699  | $+1.254478x_{81} + 0.006744x_6 + 0.025817x_{12}$ |
| $x_{40}$ | 1.80657534247   | $+3.438883x_{81} + 0.060906x_6 + 0.030032x_{12}$ |
| $x_{41}$ | 1.27780821918   | $+1.994731x_{81} + 0.015595x_6 + 0.028451x_{12}$ |
| $x_{42}$ | 0.77698630137   | $+1.290832x_{81} - 0.020864x_6 + 0.029505x_{12}$ |
| $x_{43}$ | 0.77698630137   | $+1.290832x_{81} - 0.020864x_6 + 0.029505x_{12}$ |
| $x_{44}$ | 0.566575342466  | $+2.246575x_{81} + 0.030137x_6 + 0.068493x_{12}$ |
| $x_{45}$ | 0.77698630137   | $+1.290832x_{81} - 0.020864x_6 + 0.029505x_{12}$ |
| $x_{46}$ | 1.4101369863    | $+1.553214x_{81} - 0.037513x_6 + 0.012645x_{12}$ |
| $x_{56}$ | 0.402191780822  | $+0.909115x_{81} - 0.030980x_6 - 0.009220x_{12}$ |
| $x_{48}$ | 1.22712328767   | $+1.036354x_{81} - 0.027608x_6 + 0.003688x_{12}$ |
| $x_{49}$ | 2.20630136986   | $+2.717071x_{81} - 0.002529x_6 - 0.072181x_{12}$ |
| $x_{57}$ | 1.65616438356   | $+1.971549x_{81} + 0.004215x_6 - 0.046365x_{12}$ |

Forming the dual dictionary:

|          |                  |                |                |                |                   |                |             |
|----------|------------------|----------------|----------------|----------------|-------------------|----------------|-------------|
| $y_{81}$ | 2.74025289779    | $+0.771075y_4$ | $+0.026344y_1$ | $-0.961538y_3$ | $-2.270021y_{15}$ | $-1.081665y_8$ | $+1.430980$ |
| $y_6$    | 0.00885142255005 | $-0.862381y_4$ | $-0.077977y_1$ | $-0.153846y_3$ | $-0.100738y_{15}$ | $+0.041728y_8$ | $-0.715701$ |
| $y_{12}$ | 0.00263435194942 | $-0.863804y_4$ | $-0.142255y_1$ | $+0.192308y_3$ | $-0.041886y_{15}$ | $-0.559009y_8$ | $-0.927292$ |
| $z$      | 3.82794520548    | $-4.251233y_4$ | $-0.389041y_1$ | $-0.2y_3$      | $-1.332329y_{15}$ | $-6.653973y_8$ | $-1.216712$ |

The Final Dual Dictionary is:

|           |     |              |            |              |                |            |            |               |               |              |       |
|-----------|-----|--------------|------------|--------------|----------------|------------|------------|---------------|---------------|--------------|-------|
| $y_{86}$  | 8   | $+26.25y_4$  | $+2.5y_1$  | $+23.75y_6$  | $-4.25y_{15}$  | $-2y_8$    | $+25y_5$   | $-3.5y_{47}$  | $+3y_{10}$    | $+1.75y_9$   | $+6$  |
| $y_3$     | 0.3 | $-1.3y_4$    | $+0y_1$    | $-3.5y_6$    | $-0.5y_{15}$   | $+1.1y_8$  | $-0.6y_5$  | $+0y_{47}$    | $+1.4y_{10}$  | $+1.1y_9$    | $+2$  |
| $y_{186}$ | 3   | $-38.5y_4$   | $-5y_1$    | $-22.5y_6$   | $-5.5y_{15}$   | $-13y_8$   | $-36y_5$   | $-2y_{47}$    | $-20y_{10}$   | $-17.5y_9$   | $-2$  |
| $z$       | 6   | $-41.925y_4$ | $-5.25y_1$ | $-22.075y_6$ | $-6.075y_{15}$ | $-18.9y_8$ | $-36.6y_5$ | $-1.65y_{47}$ | $-19.8y_{10}$ | $-17.475y_9$ | $-27$ |



Final primal dictionary obtained:

|           |        |                                       |
|-----------|--------|---------------------------------------|
| $x_4$     | 41.925 | $-26.25x_{86} + 1.3x_3 + 38.5x_{186}$ |
| $x_1$     | 5.25   | $-2.5x_{86} - 0x_3 + 5x_{186}$        |
| $x_6$     | 22.075 | $-23.75x_{86} + 3.5x_3 + 22.5x_{186}$ |
| $x_{15}$  | 6.075  | $+4.25x_{86} + 0.5x_3 + 5.5x_{186}$   |
| $x_8$     | 18.9   | $+2x_{86} - 1.1x_3 + 13x_{186}$       |
| $x_5$     | 36.6   | $-25x_{86} + 0.6x_3 + 36x_{186}$      |
| $x_{47}$  | 1.65   | $+3.5x_{86} - 0x_3 + 2x_{186}$        |
| $x_{10}$  | 19.8   | $-3x_{86} - 1.4x_3 + 20x_{186}$       |
| $x_9$     | 17.475 | $-1.75x_{86} - 1.1x_3 + 17.5x_{186}$  |
| $x_7$     | 27.45  | $-6.5x_{86} - 2.9x_3 + 28x_{186}$     |
| $x_{13}$  | 15.55  | $+1.5x_{86} - 0.8x_3 + 15x_{186}$     |
| $x_{14}$  | 26.675 | $-4.75x_{86} - 2.6x_3 + 27.5x_{186}$  |
| $x_{20}$  | 5.1    | $+4x_{86} - 0.1x_3 + 5x_{186}$        |
| $x_{16}$  | 4.025  | $+5.75x_{86} + 0.6x_3 + 2.5x_{186}$   |
| $x_{31}$  | 1.325  | $+4.75x_{86} + 0.2x_3 + 0.5x_{186}$   |
| $x_{17}$  | 5.3    | $+5x_{86} + 0.5x_3 + 5x_{186}$        |
| $x_{19}$  | 4.725  | $+4.75x_{86} - 0.1x_3 + 3.5x_{186}$   |
| $x_{11}$  | 5.875  | $+2.25x_{86} - 0.4x_3 + 5.5x_{186}$   |
| $x_{21}$  | 5.3    | $+5x_{86} + 0.5x_3 + 5x_{186}$        |
| $x_{18}$  | 1.625  | $+4.75x_{86} + 0.6x_3 + 0.5x_{186}$   |
| $x_{23}$  | 5.525  | $+5.75x_{86} + 0.5x_3 + 4.5x_{186}$   |
| $x_{24}$  | 5.175  | $+5.25x_{86} - 0.1x_3 + 4.5x_{186}$   |
| $x_{22}$  | 1.7    | $+2x_{86} + 0.8x_3 + 2x_{186}$        |
| $x_{26}$  | 6.075  | $+3.25x_{86} + 0.2x_3 + 5.5x_{186}$   |
| $x_{25}$  | 2.075  | $+5.25x_{86} + 0.6x_3 + 1.5x_{186}$   |
| $x_{28}$  | 4.325  | $+8.75x_{86} + 0.5x_3 + 3.5x_{186}$   |
| $x_{29}$  | 3.25   | $+7.5x_{86} + 0.4x_3 + 3x_{186}$      |
| $x_{30}$  | 2.1    | $+5x_{86} - 0x_3 + 1x_{186}$          |
| $x_{109}$ | 1.075  | $+1.25x_{86} - 0x_3 + 1.5x_{186}$     |
| $x_{32}$  | 4.025  | $+8.75x_{86} + 0.4x_3 + 2.5x_{186}$   |
| $x_{33}$  | 2.425  | $+6.75x_{86} + 0.5x_3 + 1.5x_{186}$   |
| $x_{34}$  | 4.625  | $+7.75x_{86} + 0.3x_3 + 3.5x_{186}$   |
| $x_{35}$  | 0.85   | $+2.5x_{86} + 0.1x_3 + 1x_{186}$      |
| $x_{36}$  | 4.25   | $+7.5x_{86} + 0.1x_3 + 4x_{186}$      |
| $x_{37}$  | 5.35   | $+9.5x_{86} + 0.4x_3 + 5x_{186}$      |
| $x_{38}$  | 3.8    | $+7x_{86} + 0.1x_3 + 3x_{186}$        |
| $x_{39}$  | 2.05   | $+3.5x_{86} + 0.1x_3 + 2x_{186}$      |
| $x_{40}$  | 6.225  | $+8.75x_{86} + 0.5x_3 + 5.5x_{186}$   |
| $x_{41}$  | 3.65   | $+5.5x_{86} + 0.2x_3 + 3x_{186}$      |
| $x_{42}$  | 1.875  | $+4.25x_{86} - 0x_3 + 1.5x_{186}$     |
| $x_{43}$  | 1.875  | $+4.25x_{86} - 0x_3 + 1.5x_{186}$     |
| $x_{44}$  | 4.325  | $+5.75x_{86} + 0.2x_3 + 4.5x_{186}$   |
| $x_{45}$  | 1.875  | $+4.25x_{86} - 0x_3 + 1.5x_{186}$     |
| $x_{46}$  | 1.95   | $+5.5x_{86} - 0x_3 + 1x_{186}$        |
| $x_{56}$  | 0.15   | $+3.5x_{86} + 0x_3 + 0x_{186}$        |
| $x_{48}$  | 1.425  | $+3.75x_{86} - 0x_3 + 0.5x_{186}$     |
| $x_{49}$  | 2.45   | $+8.5x_{86} + 0.4x_3 + 1x_{186}$      |
| $x_{55}$  | 2.1    | $+6x_{86} + 0.3x_3 + 1x_{186}$        |

After cutting plane is added

|           |        |                                       |
|-----------|--------|---------------------------------------|
| $x_4$     | 41.925 | $-26.25x_{86} + 1.3x_3 + 38.5x_{186}$ |
| $x_1$     | 5.25   | $-2.5x_{86} - 0x_3 + 5x_{186}$        |
| $x_6$     | 22.075 | $-23.75x_{86} + 3.5x_3 + 22.5x_{186}$ |
| $x_{15}$  | 6.075  | $+4.25x_{86} + 0.5x_3 + 5.5x_{186}$   |
| $x_8$     | 18.9   | $+2x_{86} - 1.1x_3 + 13x_{186}$       |
| $x_5$     | 36.6   | $-25x_{86} + 0.6x_3 + 36x_{186}$      |
| $x_{47}$  | 1.65   | $+3.5x_{86} - 0x_3 + 2x_{186}$        |
| $x_{10}$  | 19.8   | $-3x_{86} - 1.4x_3 + 20x_{186}$       |
| $x_9$     | 17.475 | $-1.75x_{86} - 1.1x_3 + 17.5x_{186}$  |
| $x_7$     | 27.45  | $-6.5x_{86} - 2.9x_3 + 28x_{186}$     |
| $x_{13}$  | 15.55  | $+1.5x_{86} - 0.8x_3 + 15x_{186}$     |
| $x_{14}$  | 26.675 | $-4.75x_{86} - 2.6x_3 + 27.5x_{186}$  |
| $x_{20}$  | 5.1    | $+4x_{86} - 0.1x_3 + 5x_{186}$        |
| $x_{16}$  | 4.025  | $+5.75x_{86} + 0.6x_3 + 2.5x_{186}$   |
| $x_{31}$  | 1.325  | $+4.75x_{86} + 0.2x_3 + 0.5x_{186}$   |
| $x_{17}$  | 5.3    | $+5x_{86} + 0.5x_3 + 5x_{186}$        |
| $x_{19}$  | 4.725  | $+4.75x_{86} - 0.1x_3 + 3.5x_{186}$   |
| $x_{11}$  | 5.875  | $+2.25x_{86} - 0.4x_3 + 5.5x_{186}$   |
| $x_{21}$  | 5.3    | $+5x_{86} + 0.5x_3 + 5x_{186}$        |
| $x_{18}$  | 1.625  | $+4.75x_{86} + 0.6x_3 + 0.5x_{186}$   |
| $x_{23}$  | 5.525  | $+5.75x_{86} + 0.5x_3 + 4.5x_{186}$   |
| $x_{24}$  | 5.175  | $+5.25x_{86} - 0.1x_3 + 4.5x_{186}$   |
| $x_{22}$  | 1.7    | $+2x_{86} + 0.8x_3 + 2x_{186}$        |
| $x_{26}$  | 6.075  | $+3.25x_{86} + 0.2x_3 + 5.5x_{186}$   |
| $x_{25}$  | 2.075  | $+5.25x_{86} + 0.6x_3 + 1.5x_{186}$   |
| $x_{28}$  | 4.325  | $+8.75x_{86} + 0.5x_3 + 3.5x_{186}$   |
| $x_{29}$  | 3.25   | $+7.5x_{86} + 0.4x_3 + 3x_{186}$      |
| $x_{30}$  | 2.1    | $+5x_{86} - 0x_3 + 1x_{186}$          |
| $x_{109}$ | 1.075  | $+1.25x_{86} - 0x_3 + 1.5x_{186}$     |
| $x_{32}$  | 4.025  | $+8.75x_{86} + 0.4x_3 + 2.5x_{186}$   |
| $x_{33}$  | 2.425  | $+6.75x_{86} + 0.5x_3 + 1.5x_{186}$   |
| $x_{34}$  | 4.625  | $+7.75x_{86} + 0.3x_3 + 3.5x_{186}$   |
| $x_{35}$  | 0.85   | $+2.5x_{86} + 0.1x_3 + 1x_{186}$      |
| $x_{36}$  | 4.25   | $+7.5x_{86} + 0.1x_3 + 4x_{186}$      |
| $x_{37}$  | 5.35   | $+9.5x_{86} + 0.4x_3 + 5x_{186}$      |
| $x_{38}$  | 3.8    | $+7x_{86} + 0.1x_3 + 3x_{186}$        |
| $x_{39}$  | 2.05   | $+3.5x_{86} + 0.1x_3 + 2x_{186}$      |
| $x_{40}$  | 6.225  | $+8.75x_{86} + 0.5x_3 + 5.5x_{186}$   |
| $x_{41}$  | 3.65   | $+5.5x_{86} + 0.2x_3 + 3x_{186}$      |
| $x_{42}$  | 1.875  | $+4.25x_{86} - 0x_3 + 1.5x_{186}$     |
| $x_{43}$  | 1.875  | $+4.25x_{86} - 0x_3 + 1.5x_{186}$     |
| $x_{44}$  | 4.325  | $+5.75x_{86} + 0.2x_3 + 4.5x_{186}$   |
| $x_{45}$  | 1.875  | $+4.25x_{86} - 0x_3 + 1.5x_{186}$     |
| $x_{46}$  | 1.95   | $+5.5x_{86} - 0x_3 + 1x_{186}$        |
| $x_{56}$  | 0.15   | $+3.5x_{86} + 0x_3 + 0x_{186}$        |
| $x_{48}$  | 1.425  | $+3.75x_{86} - 0x_3 + 0.5x_{186}$     |
| $x_{49}$  | 2.45   | $+8.5x_{86} + 0.4x_3 + 1x_{186}$      |
| $x_{50}$  | 2.1    | $+6x_{86} + 0.3x_3 + 1x_{186}$        |

Forming the dual dictionary:

|           |     |              |            |              |                |            |            |               |               |              |       |
|-----------|-----|--------------|------------|--------------|----------------|------------|------------|---------------|---------------|--------------|-------|
| $y_{86}$  | 8   | $+26.25y_4$  | $+2.5y_1$  | $+23.75y_6$  | $-4.25y_{15}$  | $-2y_8$    | $+25y_5$   | $-3.5y_{47}$  | $+3y_{10}$    | $+1.75y_9$   | $+6$  |
| $y_3$     | 0.3 | $-1.3y_4$    | $+0y_1$    | $-3.5y_6$    | $-0.5y_{15}$   | $+1.1y_8$  | $-0.6y_5$  | $+0y_{47}$    | $+1.4y_{10}$  | $+1.1y_9$    | $+2$  |
| $y_{186}$ | 3   | $-38.5y_4$   | $-5y_1$    | $-22.5y_6$   | $-5.5y_{15}$   | $-13y_8$   | $-36y_5$   | $-2y_{47}$    | $-20y_{10}$   | $-17.5y_9$   | $-2$  |
| $z$       | 6   | $-41.925y_4$ | $-5.25y_1$ | $-22.075y_6$ | $-6.075y_{15}$ | $-18.9y_8$ | $-36.6y_5$ | $-1.65y_{47}$ | $-19.8y_{10}$ | $-17.475y_9$ | $-27$ |

Unbounded Dictionary! The Final Dual Dictionary is:

|           |               |           |                |               |               |             |             |               |                |       |
|-----------|---------------|-----------|----------------|---------------|---------------|-------------|-------------|---------------|----------------|-------|
| $y_{193}$ | 96.9999999999 | $-130y_1$ | $-29y_{191}$   | $-14y_{187}$  | $-157y_{15}$  | $-355y_8$   | $-987y_4$   | $-61y_{47}$   | $-534y_{10}$   | $-4$  |
| $y_3$     | 20.1          | $-33y_1$  | $-6.7y_{191}$  | $-4y_{187}$   | $-36.8y_{15}$ | $-84.7y_8$  | $-255.4y_4$ | $-13.2y_{47}$ | $-130.6y_{10}$ | $-11$ |
| $y_9$     | 5.9999999999  | $-10y_1$  | $-2y_{191}$    | $-1y_{187}$   | $-11y_{15}$   | $-26y_8$    | $-77y_4$    | $-4y_{47}$    | $-40y_{10}$    | $-3$  |
| $z$       | 55.3999999999 | $-67y_1$  | $-13.4y_{191}$ | $-5.9y_{187}$ | $-83.1y_{15}$ | $-190.5y_8$ | $-508.3y_4$ | $-32.2y_{47}$ | $-275.9y_{10}$ | $-24$ |

Dual is unbounded. Primal is therefore infeasible.

Problem is ILP infeasible. Could not find an integer point.

Done.

Final Answer: Infeasible