```
Case ID: 12BusCase_networkdata.xlsx
radial_bus_location =
   Empty matrix: 0-by-1
```

B_diag =	
(1,1)	5.0000
(2,2)	5.0000
(3,3)	3.3333
(4,4)	4.0000
(5,5)	10.0000
(6,6)	3.3333
(7,7)	5.0000
(8,8)	3.8462
(9,9)	10.0000
(10,10)	2.5000
(11, 11)	3.3333
(12, 12)	5.0000
(13, 13)	5.0000
(14,14)	3.3333
(15, 15)	4.0000
(16, 16)	10.0000
(17, 17)	3.3333
(18, 18)	5.0000
(19, 19)	3.8462
(20,20)	10.0000
(21,21)	2.5000
(22,22)	3.3333
(23,23)	1.2500
(24,24)	1.2500

A_alt =	
(1,1)	1
(2,1)	1
(3,1)	1
(1,2)	-1
(4,2)	1
(5,2)	1
(6,2)	1
(7,2)	1
(4,3)	-1
(8,3)	1
(9 , 3)	1
(23,3)	1
(2,4)	-1

(25, 25)

1.2500

(5,4)	-1
(10,4)	1
(25,4)	1
(3,5)	-1
(6,5)	-1
(8,5)	-1
(10,5)	-1
(11,5)	1
(24,5)	1
(7 , 6)	-1
(9,6)	-1
(11,6)	-1
(12,7)	1
(13,7)	1
(14,7)	1
(12,8)	-1
(15,8)	1
(16,8)	1
(17,8)	1
(18,8)	1
(24,8)	-1
(15,9)	-1
(19,9)	1
(20,9)	1
(23,9)	-1
(13,10)	-1
(16,10)	-1
(21,10)	1
(25,10)	-1
(14,11)	-1
(17,11)	-1
(19,11)	-1
(21,11)	-1
(22,11)	1
(18, 12)	-1
(20,12)	-1
(22,12)	-1

AFACT MATRIX

Monitored GENERATOR

Line

	1	2	3	4	5	6 🖍
7	8	9	10	11	12	
1 to 2	0.0000	-0.4696	-0.3970	-0.3161	-0.3214	-0.4031 ∠
-0.3433	-0.3435	-0.3492	-0.3419	-0.3453	-0.3469	
1 to 4	0.0000	-0.3161	-0.3046	-0.4972	-0.2800	-0.3033 ∠
-0.3628	-0.3587	-0.3541	-0.3691	-0.3595	-0.3563	
1 to 5	0.0000	-0.2143	-0.2984	-0.1867	-0.3985	-0.2936 ∠
-0.2939	-0.2978	-0.2968	-0.2890	-0.2952	-0.2968	

-0.1773 🗹	-0.1009	0.0092	-0.3205	0.0581	0.0000	2 to 3
	-0.1455	-0.1391	-0.1247	-0.1533	-0.1342	-0.1319
0.1996≰	0.0828	-0.3622	0.1849	0.3070	0.0000	2 to 4
		-0.0286	-0.0545	-0.0098	-0.0302	-0.0389
-0.0249 🗹	-0.1843	0.0240	-0.0337	0.0988	0.0000	2 to 5
	-0.0655	-0.0650	-0.0611	-0.0640	-0.0688	-0.0650
-0.4004 🗸	-0.1190	0.0128	-0.2277	0.0665	0.0000	2 to 6
	-0.1171	-0.1126	-0.1017	-0.1220	-0.1103	-0.1076
0.1418 🗸	-0.1156	0.0189	0.2694	0.0582	0.0000	3 to 5
	0.0643	0.0587	0.0494	0.0736	0.0497	0.0518
-0.3575 ∠	0.0141	0.0027	0.3459	-0.0121	0.0000	3 to 6
	0.1296	0.1226	0.1084	0.1393	0.1150	0.1144
-0.0686 ∠	-0.1589	0.1086	-0.0715	-0.0027	0.0000	4 to 5
	-0.0444	-0.0416	-0.0322	-0.0455	-0.0440	-0.0390
-0.2420 🗹	0.1049	-0.0155	-0.1182	-0.0544	0.0000	5 to 6
	-0.0126	-0.0100	-0.0067	-0.0173	-0.0047	-0.0068
-0.0028 🗸	-0.0059	0.0041	-0.0031	-0.0002	0.0000	7 to 8
	-0.0104	0.0731	0.0756	-0.0064	-0.0741	0.3938
0.0074 🗸				0.0015	0.0000	7 to 10
	0.0748	0.1030	-0.1210	0.0730	0.0594	0.3777
-0.0046 🗸	-0.0013	0.0022	-0.0073	-0.0013	0.0000	7 to 11
	-0.0643	-0.1762	0.0454	-0.0666	0.0147	0.2285
-0.0139 🗹	0.0012	0.0037	-0.0236	-0.0045	0.0000	8 to 9
	-0.0980	-0.0200	0.0885	-0.2388	0.1316	0.0775
0.0205 🗸	0.0264	-0.0209	0.0272	0.0033	0.0000	8 to 10
	0.1703	0.0598	-0.3931	0.1589	0.2668	-0.0324
-0.0027 🗹	0.0026	-0.0006	-0.0052	-0.0011	0.0000	8 to 11
	-0.0574	-0.2249	-0.0049	-0.0623	0.0641	-0.0341
-0.0102 🗹	0.0016	0.0023	-0.0175	-0.0034	0.0000	8 to 12
	-0.3552	-0.0750	0.0590	-0.1798	0.1072	0.0436
0.0102 🗸		-0.0042		0.0030	0.0000	9 to 11
	0.0280	-0.2403	-0.0908	0.1577	-0.0527	-0.1139
0.0143 🗹	0.0000	-0.0045	0.0240	0.0045	0.0000	9 to 12
			-0.1032		-0.1146	-0.1067
-0.0071 🗹	-0.0047	0.0048	-0.0107	-0.0017	0.0000	10 to 11
	-0.0856	-0.1836	0.0946	-0.0864	-0.0187	-0.0175
-0.0041 🗹	-0.0016	0.0022	-0.0065	-0.0011	0.0000	11 to 12
	-0.1794	0.1749	0.0443	-0.0576	0.0074	0.0631
0.0384 🗹	0.0006	-0.0124	0.0642	0.0120	0.0000	3 to 9
	-0.3395	-0.3203	-0.2825	-0.3662	-0.2989	-0.2981
-0.0033 ∠	0.0378	-0.0197	-0.0159	-0.0055	0.0000	5 to 8
	-0.3298	-0.3332	-0.3262	-0.3155	-0.3562	-0.3392
-0.0351 ∠	-0.0384	0.0320	-0.0483	-0.0064	0.0000	4 to 10
	-0.3307	-0.3465	-0.3914	-0.3184	-0.3449	-0.3627

POWER TRANSFER DISTRIBUTION FACTOR (PTDF) MATRIX

Monitored Transaction

Line From(Sell) - To(Buy)

1 to 2 1 to 4 1 to 5 2 to 3 2 to 4 2 to 5 2 🗹

						7 to 10 7 to 1	
				9 to 11	9 to 12	10 to 11 11 to) L
12 3 t	to 9 5 t	to 8 4 t	0 10				
1 to 2	0.4696	0.3161	0.3214	-0.0726	-0.1535	-0.1482 ∠	
-0.0665	-0.0756	0.0060	0.0053	0.0817	0.0002	-0.0015 🗹	
0.0019		-0.0016					
0.0034	0.0017						
1 to 4	0.3161	0.4972	0.2800	-0.0115	0.1811	-0.0361 🗹	
-0.0128	-0.0246	-0.0013	-0.2172	0.0232	-0.0041	0.0063 🗹	
-0.0033	-0.0046	0.0105	0.0009	-0.0023	0.0055	0.0022 🗹	
-0.0096	-0.0032	0.0495	0.0786	-0.1281			
1 to 5	0.2143	0.1867	0.3985	0.0841	-0.0276	0.1843 ∠ -0.0049 ∠	
0.0794	0.1002	-0.0047	0.2119	-0.1049	0.0040	-0.0049 	
0.0013	-0.0010	-0.0088	-0.0026	-0.0010	-0.0016	-0.0000 	
	0.0016						
2 to 3	-0.0581	-0.0092	0.1009	0.3786	0.0489	0.1589 🗹	
	-0.2196						
	0.0191				-0.0142	-0.0078 	
	0.0064						
						0.2242 🗹	
0.1074	0.1021	-0.0147	-0.4450	-0.1168	-0.0087	0.0156 🗹	
	-0.0204					0.0090 🗹	
	-0.0098						
						0.2831 ✔	
	0.1506				0.0038		
0.0001					0.0010	0.0015 🗸	
	0.0005						
						0.1856	
	-0.1087				0.0027		
	0.0117				-0.0094	-0.0049 2	
	0.0045				0 0000	0.1500.	
						0.1738 🗸	
	0.3850						
	-0.0239				0.0149	0.00922	
	-0.0057				0 0147	-0.0262 	
	0.3317						
-0.0082		0.0066					
-0.0082		0.2066			0.0107	0.009/=	
4 to 5					_0 1112	0.1562 🗹	
	0.0874						
	0.0015						
	0.0013				0.0033	0.0011-	
5 to 6		0.0155		0.0637	-0.0389	-0.1593 ∠	
0.1876		0.1239		0.3469	-0.0021		
0.0032		0.0020		0.0078	-0.0073		
0.0033	0.0025		0.1096		0.0070	J. 00 10 <u>-</u>	
7 to 8					-0.0043	0.0057 🗸	
0.0027		-0.0003					
0.3207		-0.1496					

	0.0835				0.0070	0.0050./
7 to 10						-0.0058 🗸
-0.0060	0.0032	0.0030 0.1803			-0.0300	0.4986 ∠ -0.0017 ∠
0.2746	0.0283				-0.0300	-0.001/2
-0.2240 7 to 11					0 0034	0.0001 🗸
	-0.0059	-0.0022		0.0080		
	0.0813		0.1909			-0.0022 Ľ
0.4047		0.0593			0.1096	-0.0022 2
8 to 9					-0 0082	-0.0057 ∠
0.0094					-0.0541	
	0.3704				-0.2188	
	0.0780				0.2100	0.1400-
					0 0242	-0.0231 ∠
	0.0007					
	0.1079					
	-0.1105		-0.2404			*****
8 to 11	0.0011				-0.0006	-0.0038 ∠
0.0015	-0.0078	-0.0025	-0.0032		-0.0981	
	0.1263				0.1626	
0.2200		0.0571		0.0044		
8 to 12					-0.0057	-0.0049 🗹
0.0068			0.0008		-0.0636	
0.1185	0.2870	0.0483	0.1822	0.4624	-0.1048	0.1754 🗸
0.1339	0.2802	0.1623	-0.1057	-0.0566		
9 to 11	-0.0030	0.0042	-0.0018	-0.0137	0.0072	0.0012 🗸
-0.0073	0.0149	0.0064	-0.0060	-0.0084	-0.0612	-0.0231 🗹
0.1265	-0.2104	0.0381	0.1877	-0.0806	0.3980	0.1297 ✔
0.1495	-0.2683	-0.1410	0.0545	0.0866		
9 to 12	-0.0045	0.0045	-0.0000	-0.0195	0.0090	0.0045 🗸
-0.0098	0.0240	0.0097	-0.0045	-0.0143	0.0079	-0.0035 ∠
-0.0067			-0.0147		0.3373	0.7028⊭
-0.0032	0.3654		0.1147			
10 to 11		-0.0048				0.0030 🗸
0.0054	-0.0060	-0.0036	0.0094	0.0025	0.0012	-0.1120 🗸
	0.0678			0.0670	0.0972	-0.0008 Ľ
0.2782			0.0140			
11 to 12		-0.0022				0.0005 🗹
0.0030	-0.0049			0.0025		0.0189 🗸
-0.1118		-0.0368		0.1868	-0.2325	0.1218 🗸
-0.1307	0.3543	0.0511	-0.0090	-0.0421		,
3 to 9	-0.0120	0.0124	-0.0006			0.0114 🗸
-0.0264	0.0636	0.0258	-0.0130		0.0008	
0.0222	0.0672		0.0214	0.0406	-0.0458	-0.0267 ∠
0.0379		0.4304		0.2701		
5 to 8	0.0055	0.0197				-0.0433 🗸
-0.0022	-0.0537	-0.0126	-0.0574		0.0170	
	-0.0407		-0.0230		0.0177	0.0143 🗸
0.0070	-0.0034		0.3940		0 000=	0 0010 /
4 to 10						0.0319
0.0286	-0.0099	-0.0132	0.0704	-0.0033	-0.0179	0.0287 ∠

-0.0162 -0.0265 0.0465 0.0016 -0.0142 0.0281 0.0123

-0.0449 -0.0158 0.2701 0.3065 0.4234 0.0123

✓

LINE OUTAGE DISTRIBUTION FACTOR (LODF) MATRIX

Monitored Outage of one circuit

Line From - To

0.0073 0.0024			
0.0024	0 0063	0 0065	,
	0.0003	-0.0065	-0.0075 🗹
0.0365	0.0447		
0.4656	-0.0185	0.5474	-0.0503 ∠
-0.2965	0.0356	-0.0078	0.0126 🗹
0.0013	-0.0043	0.0091	0.0076
0.1297	-0.2221		
0.0000	0.1353	-0.0834	0.2570 🗹
			-0.0097
-0.0037	-0.0019	-0.0026	-0.0000 ~
-0.1662	0.1774		
0.1677	0.0000	0.1477	0.2217 🗸
0.1503	0.1171	0.0044	-0.0143 🗹
0.0068	0.0210	-0.0236	-0.0262 🗸
			0.3128 🗸
-0.0023		0.0311	0.0302 🗹
			0.0000 ✔
		0.0017	0.0050 🗸
		-0.0157	-0.0165 🗹
0.1922	-0.3399		0.2424 🗸
0.1836	-0.3941		
		0.0247	0.0310 ∠
		0.0278	0.0325 ∠
	0 1000		
-0.1665			
-0.1665 0.2642 0.0000	0.1107	-0.3363 0.0095	
	0.4656 -0.2965 0.0013 0.1297 0.0000 0.2892 -0.0037 -0.1662 0.1677 0.1503 0.0068 0.0550 -0.1376 -0.6074 -0.0023 0.1865 0.3064 0.2844 -0.0053 -0.1906 0.1979 0.1800 0.0032 -0.0145 0.1922 0.1836 -0.0127 -0.2728 -0.0235 -0.0157	0.4656 -0.0185 -0.2965 0.0356 0.0013 -0.0043 0.1297 -0.2221 0.0000 0.1353 0.2892 -0.1606 -0.0037 -0.0019 -0.1662 0.1774 0.1677 0.0000 0.1503 0.1171 0.0068 0.0210 0.0550 0.2322 -0.1376 -0.1789 -0.0023 -0.0213 0.1865 -0.5337 0.3064 0.2131 0.2844 -0.2440 -0.0053 -0.0061 -0.1906 0.1476 0.1979 0.4735 0.1800 0.4309 0.0032 -0.0127 -0.0145 0.1986 0.1922 -0.3399 0.1836 -0.3941 -0.0272 -0.0529 -0.0235 -0.5760 -0.0157 0.5691	0.4656 -0.0185 0.5474 -0.2965 0.0356 -0.0078 0.0013 -0.0043 0.0091 0.1297 -0.2221 -0.0834 0.2892 -0.1606 0.0074 -0.0037 -0.0019 -0.0026 -0.1662 0.1774 0.0000 0.1477 0.1503 0.1171 0.0044 0.0044 0.0068 0.0210 -0.0236 0.0550 0.2322 -0.0163 -0.0023 -0.0023 -0.0213 0.0311 0.1865 -0.5337 0.0311 0.2260 0.2844 -0.2440 0.0072 -0.0053 -0.0061 0.0017 -0.1906 0.1476 0.0050 0.1979 0.4735 0.1623 0.1800 0.4309 0.0050 0.0032 -0.0127 -0.0157 0.1836 -0.3941 0.0040 -0.0127 -0.0273 0.0247 -0.02728 -0.0529 -0.0529 -0.0235 -0.5760 -0.0446 -0.0157 0

0.0044	0.0024	-0.0348	-0.0034	0.0007	-0.0065	-0.0038 ∠
	0.0043		-0.1895			
5 to 6		0.0308			-0.1177	
		0.4177		0.0000	-0.0039	-0.0002 ∠
	0.0200		0.0074		-0.0121	-0.0160 🗹
0.0046	0.0039		0.1809	-0.0153		
7 to 8						0.0080 ∠
	0.0045		0.0138		0.0000	
	-0.1074		-0.2070		-0.1322	0.0134 🗸
	0.1294					
						-0.0081 🗸
-0.0112	0.0051		-0.0186			
	-0.0217			-0.0286	-0.0499	-0.0058 ∠
	0.0438	-0.1099	-0.0859			
7 to 11	0.0024		0.0022			0.0001 ∠
0.0062	-0.0097			0.0049		
	0.1291				0.1821	-0.0075 🗹
0.3070	-0.1732					,
8 to 9			-0.0021			
	-0.0404		0.0033		-0.1017	
	0.0000				-0.3635	-0.4737 ∠
		0.3778				,
8 to 10	-0.0062	0.0416	-0.0439	-0.0384	0.0732	-0.0323 ∠
-0.0323			-0.0646			
	0.1714		0.2912		0.1646	-0.0384 ∠
	-0.1712		-0.3967			
8 to 11		0.0012				-0.0052 L
0.0029	-0.0127				-0.1844	-0.0581 ∠
	0.2007				0.2702	-0.0164 ∠
0.3048		0.1002	-0.1014	0.0076		/
8 to 12	0.0064				-0.0173	
0.0128	-0.0310		0.0011		-0.1196	
	0.4558				-0.1741	0.5901 🗸
		0.2849			0 0010	0.0016.
9 to 11						0.0016
	0.0242			-0.0129		-0.0461
0.2124		0.1121	0.2639		0.0000	0.4365 🗹
0.2072	-0.4155		0.0899	0.1501	0 0071	0.00001
9 to 12	-0.0084	0.0089	-0.0000			0.0062 🗸
-0.0184	0.0389	0.0326	-0.0061	-0.0219		-0.0069 ∠
-0.0113	-0.5591			0.6525	0.5604	0.0000 ∠
-0.0045	0.5660		0.1892		0 0106	0.0041 🗸
10 to 11 0.0102	-0.0098	-0.0095 -0.0120	0.0129	0.0145		
	0.1076			0.0036		
					0.1613	-0.0027 2
0.0000 11 to 12		0.1330 -0.0043	0.0231		_0 0000	0.0007 🗸
0.0057				0.0086		0.0376×
-0.1878			-0.2356			0.4099 🗸
-0.1878 -0.1811			-0.2356 -0.0148		-0.3003	0.4099 E
					0 0736	0.0159 ∠
3 60 9	-0.0226	0.0246	-0.0010	-0.0841	0.0736	0.01392

```
0.0015
                                                           -0.0312 🗹
-0.0496
          0.1035
                   0.0871
                             -0.0177
                                       -0.0579
0.0373
          0.1068
                   -0.0484
                              0.0301
                                        0.0755
                                                -0.0761
                                                           -0.0897∠
                    0.0000
0.0525
          0.0297
                                        0.4684
                              0.4942
                                                             -0.0604 🗹
                                                    0.0427
5 to 8
           0.0104
                     0.0391
                              -0.0628
                                         0.0168
                    -0.0425
                                                            -0.0260 🗹
-0.0041
         -0.0874
                              -0.0784
                                        0.0630
                                                  0.0320
         -0.0647
                   -0.0884
-0.0101
                             -0.0324
                                       -0.0491
                                                  0.0294
                                                            0.0482 🗹
0.0097
        -0.0052
                   0.5258
                              0.0000
                                      0.5316
                             0.0638 0.0673 -0.1163
                                                              0.0445 🗹
4 to 10
        0.0121
                   -0.0637
                                                            0.0572 🗹
0.0537
        -0.0161
                  -0.0445
                              0.0961
                                       -0.0051
                                                -0.0336
-0.0272
       -0.0421
                   0.1368
                           0.0023 -0.0263
                                                 0.0467
                                                            0.0415 🗹
         -0.0245
                                       0.0000
-0.0622
                    0.4742
                             0.5058
```

```
Elapsed time is 0.106524 seconds.
```

>> PTDF_for_any_bus_to_bus

Enter the bus number where power is being injected: 1

Enter the bus number where power is being removed: 3

Warning: Self connecting nodes are not allowed, ignoring the diagonal of CM.

> In biograph (line 158)

In PTDF_for_any_bus_to_bus (line 37)

Distance from bus 1 to bus 3 is: 2

Path from bus 1 to bus 3 is:

1 2 3

POWER TRANSFER DISTRIBUTION FACTOR (PTDF) VECTOR

Monitored Transaction

Line From(Sell) - To(Buy)

0.0052

0.0175

-0.0167

1 to 3 1 to 2 0.3970 1 to 4 0.3046 1 to 5 0.2984 2 to 3 0.3205 2 to 4 -0.1849 0.0337 2 to 5 2 to 6 0.2277 3 to 5 -0.2694 -0.3459 3 to 6 4 to 5 0.0715 5 to 6 0.1182 7 to 8 0.0031 7 to 10 -0.0104 7 to 11 0.0073 8 to 9 0.0236 8 to 10 -0.0272

8 to 11

8 to 12

9 to 11

9	to	12	-0.0240
10	to	11	0.0107
11	to	12	0.0065
3	to	9	-0.0642
5	to	8	0.0159
4	to	10	0.0483
>>			