

Sharon A Glendale
Assignment 3
Z23285379

Insertion Sort

n	Theoretical RT = $\Theta(n^2)$	Simulated RT (ms)	Hidden Constant
1000	1×10^5	411	4.11×10^{-4}
2000	4×10^5	1730	4.33×10^{-4}
3000	9×10^5	3746	4.16×10^{-4}
4000	16×10^5	6718	4.2×10^{-4}
5000	25×10^5	10374	4.15×10^{-4}
6000	36×10^5	15130	4.2×10^{-4}
7000	49×10^5	20361	4.16×10^{-4}
8000	64×10^5	26652	4.16×10^{-4}
9000	81×10^5	34084	4.21×10^{-4}
10000	1×10^7	42119	4.21×10^{-4}
11000	12.1×10^7	50747	4.19×10^{-5}
12000	14.4×10^7	60868	4.23×10^{-5}
13000	16.9×10^7	74153	4.39×10^{-5}
14000	19.6×10^7	86803	4.43×10^{-5}
15000	22.5×10^7	97052	4.31×10^{-5}
16000	25.6×10^7	108977	4.26×10^{-5}
17000	28.9×10^7	127369	4.41×10^{-5}
18000	32.4×10^7	135876	4.2×10^{-5}
19000	36.1×10^7	154822	4.29×10^{-5}
20000	40×10^7	171850	4.3×10^{-5}

$$\begin{aligned}
 C_1 &= \frac{411}{10^5} = 4.11 \times 10^{-4} & C_6 &= \frac{15130}{36 \times 10^5} = 4.2 \times 10^{-4} & C_{11} &= \frac{50747}{12.1 \times 10^7} = 4.19 \times 10^{-5} & C_{16} &= \frac{108977}{25.6 \times 10^7} = 4.26 \times 10^{-5} \\
 C_2 &= \frac{1730}{4 \times 10^5} = 4.33 \times 10^{-4} & C_7 &= \frac{20361}{49 \times 10^5} = 4.16 \times 10^{-4} & C_{12} &= \frac{60868}{14.4 \times 10^7} = 4.23 \times 10^{-5} & C_{17} &= \frac{127369}{28.9 \times 10^7} = 4.41 \times 10^{-5} \\
 C_3 &= \frac{3746}{9 \times 10^5} = 4.16 \times 10^{-4} & C_8 &= \frac{26652}{64 \times 10^5} = 4.16 \times 10^{-4} & C_{13} &= \frac{74153}{16.9 \times 10^7} = 4.39 \times 10^{-5} & C_{18} &= \frac{135876}{32.4 \times 10^7} = 4.2 \times 10^{-5} \\
 C_4 &= \frac{6718}{16 \times 10^5} = 4.2 \times 10^{-4} & C_9 &= \frac{34084}{81 \times 10^5} = 4.21 \times 10^{-4} & C_{14} &= \frac{86803}{19.6 \times 10^7} = 4.43 \times 10^{-5} & C_{19} &= \frac{154822}{36.1 \times 10^7} = 4.29 \times 10^{-5} \\
 C_5 &= \frac{10374}{25 \times 10^5} = 4.15 \times 10^{-4} & C_{10} &= \frac{42119}{10^7} = 4.21 \times 10^{-4} & C_{15} &= \frac{97052}{22.5 \times 10^7} = 4.31 \times 10^{-5} & C_{20} &= \frac{171850}{40 \times 10^7} = 4.3 \times 10^{-5}
 \end{aligned}$$

$$C_{\max} = C_9 \text{ or } C_{10}$$

Heap Sort

n	Theoretical RT = Onlgn	Simulated RT (ms)	Hidden Constant
1000	99657.8	58	
2000	109657.8 21931400	113	
3000	15500 34652100	174	
4000	19657.8 47862800	247	
5000	22877 61438500	54	
6000	13550.7 75364200	413	
7000	17731 89411760	506	
8000	19657.8 103725600	608	
9000	13135.7 118221300	727	
10000	13287.7 132877000	849	
11000	13425.0 147677200	905	
12000	13550.7 162608400	997	
13000	13666.0 177660600	1123	
14000	13773.1 192823400	1234	
15000	13872.6 208089000	1448	
16000	13965.7 2234512000	1479	
17000	14053.2 2389044001	1606	
18000	14135.7 254442600	1828	
19000	14213.7 270060300	1883	
20000	14287.7 285754000	2021	

$$C_1 = \frac{58}{99657.8} = 0.00058 \quad C_6 = \frac{413}{75364200} = 0.0054844 \quad C_{11} = \frac{905}{147677200} = 0.0612852 \quad C_{16} = \frac{1479}{2234512000} = 0.00068189$$

$$C_2 = \frac{113}{21931400} = 5.125 E^{-6} \quad C_7 = \frac{506}{89411760} = 0.05659 \quad C_{12} = \frac{997}{162608400} = 0.0061313 \quad C_{17} = \frac{1606}{2389044001} = 0.000722$$

$$C_3 = \frac{174}{34652100} = 5.021 E^{-6} \quad C_8 = \frac{608}{103725600} = 0.0058616 \quad C_{13} = \frac{1123}{177660600} = 0.006322 \quad C_{18} = \frac{1828}{254442600} = 0.00718$$

$$C_4 = \frac{247}{47862800} = 5.1609 E^{-6} \quad C_9 = \frac{727}{118221300} = 0.006149 \quad C_{14} = \frac{1234}{192823400} = 0.006399 \quad C_{19} = \frac{1883}{270060300} = 0.0069752$$

$$C_5 = \frac{54}{61438500} = 8.7892 E^{-7} \quad C_{10} = \frac{849}{132877000} = 0.006389 \quad C_{15} = \frac{1448}{208089000} = 0.006956 \quad C_{20} = \frac{2021}{285754000} = 0.007057$$

$$C_{\max} = C_{20}$$

	1000	2000	3000	4000	5000	6000	7000	8000	9000	10000	11000	12000
Insert_Sort	411	1730	3746	6718	10374	15130	20361	26652	34084	42119	50747	60868
Heap_Sort	58	113	174	247	54	413	506	608	727	849	905	997

