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11/8/2022

Seasonality Analysis on the CPI index in the country of Canada from 2000 to 2009 per month.

This seasonality analysis regarding the CPI index in the country of Canada from 2000 to 2009 was a project assigned in Elementary Economic Forecasting, an undergraduate course instructed at the University of Connecticut. The objective of this project was to understand and display the seasonal patterns of the data being analyzed. There are 120 documented observations in this analysis; with each one representing the months from January 2000 to December 2009. The code for this project was written in R.

Here is the code below:

```
library(readr)
library(seastests)
```

```
#Time Series of Consumer Price Index
CPI_1 <- read_csv("CPI.csv")
View(CPI_1)
```

```
CPI<-ts(data=CPI_1, start=c(2000,1), frequency=12)
```

```
print(CPI)
```

	CPI
1	211.933
2	212.705

3	212.495
4	212.709
5	213.022
6	214.790
7	214.726
8	215.445
9	215.861
10	216.509
11	217.234
12	217.347
13	217.488
14	217.281
15	217.353

16	217.403
17	217.290
18	217.199
19	217.605
20	217.923
21	218.275
22	219.035
23	219.590
24	220.472
25	221.187
26	221.898
27	223.046
28	224.093

29	224.806
30	224.806
31	225.395
32	226.106
33	226.597
34	226.750
35	227.169
36	227.223
37	227.842
38	228.329
39	228.807
40	229.187
41	228.713

42	228.524
43	228.590
44	229.918
45	231.015
46	231.638
47	231.249
48	231.221
49	231.679
50	232.937
51	232.282
52	231.797
53	231.893
54	232.445

55	232.900
56	233.456
57	233.544
58	233.669
59	234.100
60	234.719
61	235.288
62	235.547
63	236.028
64	236.468
65	236.918
66	237.231
67	237.498

68	237.460
69	237.477
70	237.430
71	236.983
72	236.252
73	234.718
74	235.236
75	236.005
76	236.156
77	236.974
78	237.684
79	238.053
80	238.028

81	237.506
82	237.781
83	238.016
84	237.817
85	237.833
86	237.469
87	238.038
88	238.827
89	239.464
90	240.167
91	240.150
92	240.602
93	241.051

94	241.691
95	242.029
96	242.772
97	243.780
98	243.961
99	243.749
100	244.051
101	243.962
102	244.182
103	244.390
104	245.297
105	246.418
106	246.587

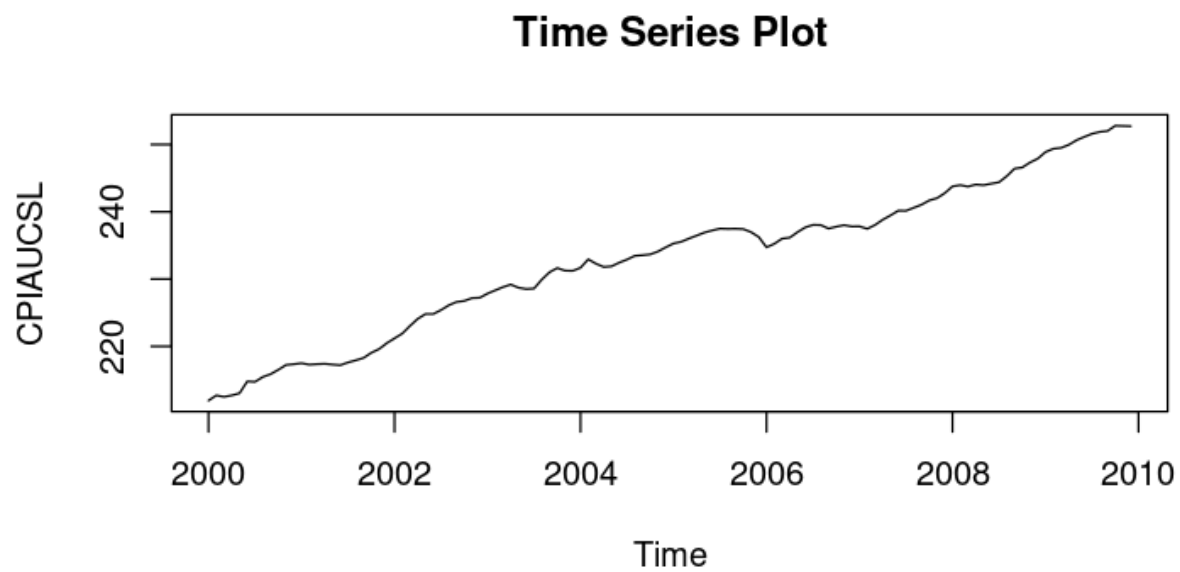
107	247.332
108	247.901
109	248.884
110	249.369
111	249.498
112	249.956
113	250.646
114	251.134
115	251.597
116	251.879
117	252.010
118	252.794
119	252.760

120	252.723
-----	---------

View(CPI)

```
#Time series plot
plot(CPI,main ="Time Series Plot")
```

View(ts)



```
time <- seq(1, 120, by=1)
View(time)
```

#Linear Model

```
CPIAUSCL<-data.frame(time, CPI)
linear.mod <- lm(CPI~time, data=CPIAUSCL)
print(summary(linear.mod))
```

```
Call:
lm(formula = CPI ~ time, data = CPIAUSCL)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-3.5292	-1.7505	-0.2766	1.6960	3.2218

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	2.140e+02	3.419e-01	626.12	<2e-16 ***
time	3.134e-01	4.904e-03	63.91	<2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.861 on 118 degrees of freedom

Multiple R-squared: 0.9719, Adjusted R-squared: 0.9717

F-statistic: 4085 on 1 and 118 DF, p-value: < 2.2e-16

$Y = 2.140e+02 + 3.134e-01(\text{time})$

#Quadratic Model

`time2 <- time^2`

`quad.mod <- lm(formula = CPI ~ time2, data = CPIAUSCL)`

`print(summary(quad.mod))`

Call:

`lm(formula = CPI ~ time2, data = CPIAUSCL)`

Residuals:

	Min	1Q	Median	3Q	Max
	-9.436	-1.932	-0.523	3.514	5.583

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	2.214e+02	5.163e-01	428.77	<2e-16 ***
time2	2.395e-03	7.934e-05	30.18	<2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3.76 on 118 degrees of freedom

Multiple R-squared: 0.8853, Adjusted R-squared: 0.8844

F-statistic: 911.1 on 1 and 118 DF, p-value: < 2.2e-16

$Y = 2.214e+02 + 2.395e-03(\text{time})$

#Exponential Model

```
time.e <- log(time)
exp.model <- lm(formula = CPI ~ time.e, data = CPIAUSCL)
print(summary(exp.model))
```

Call:

```
lm(formula = CPI ~ time.e, data = CPIAUSCL)
```

Residuals:

Min	1Q	Median	3Q	Max
-6.414	-2.768	-1.314	2.002	20.106

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	191.8274	1.7363	110.48	<2e-16 ***
time.e	10.7936	0.4421	24.41	<2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.515 on 118 degrees of freedom

Multiple R-squared: 0.8347, Adjusted R-squared: 0.8333

F-statistic: 596 on 1 and 118 DF, p-value: < 2.2e-16

$Y = 191.8274 + 10.7936 (\text{time.e})$

#Linear-log-quadratic trend estimation with seasonal dummies

```
mond <- seasonaldummy(CPI)
logls.seas <- data.frame(cbind(CPI, time, mond))
linear.seas.mod <- lm(CPI ~ mond + time, data = logls.seas)
print(summary(linear.seas.mod))
```

Call:

```
lm(formula = CPI ~ mond + time, data = logls.seas)
```

Residuals:

Min	1Q	Median	3Q	Max
-3.3933	-1.7956	-0.4292	1.6890	3.3416

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	214.188575	0.702953	304.698	<2e-16 ***
mondJan	-0.338813	0.871893	-0.389	0.698
mondFeb	-0.241784	0.871573	-0.277	0.782
mondMar	-0.297856	0.871283	-0.342	0.733

mondApr	-0.276227	0.871024	-0.317	0.752
mondMay	-0.285099	0.870796	-0.327	0.744
mondJun	-0.150670	0.870598	-0.173	0.863
mondJul	-0.189442	0.870430	-0.218	0.828
mondAug	0.018586	0.870292	0.021	0.983
mondSep	0.069615	0.870186	0.080	0.936
mondOct	0.169643	0.870109	0.195	0.846
mondNov	0.114472	0.870064	0.132	0.896
time	0.312972	0.005153	60.740	<2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.945 on 107 degrees of freedom

Multiple R-squared: 0.9722, Adjusted R-squared: 0.969

F-statistic: 311.5 on 12 and 107 DF, p-value: < 2.2e-16

$Y = 214.188575 - 0.338813(\text{mondJan}) - .241784(\text{mondFeb}) - .297856(\text{mondMar})$
 $- .276227(\text{mondApr}) - .285099(\text{mondMay}) - .150670(\text{mondJun}) - .189442(\text{mondJul}) +$
 $.018586(\text{mondAug}) + .069615(\text{mondSep}) + .169643(\text{mondOct}) + .114472(\text{mondNov})$
 $+ .312972(\text{time})$

```
mond <- seasonaldummy(CPI)
```

```
time2 <- time^2
```

```
logqls.seas <- data.frame(cbind(CPI,time,time2, mond))
```

```
quad.seas.mod <- lm(formula = CPI ~ time + time2 + mond, data = logqls.seas)
```

```
print(summary(quad.seas.mod))
```

Call:

```
lm(formula = CPI ~ time + time2 + mond, data = logqls.seas)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-3.7197	-1.4446	0.0825	1.5978	2.7369

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	2.128e+02	7.657e-01	277.880	< 2e-16 ***
time	3.837e-01	1.953e-02	19.653	< 2e-16 ***
time2	-5.849e-04	1.563e-04	-3.743	0.000296 ***

mondJan	-3.388e-01	8.233e-01	-0.412	0.681511
mondFeb	-2.476e-01	8.230e-01	-0.301	0.764084
mondMar	-3.084e-01	8.227e-01	-0.375	0.708533
mondApr	-2.903e-01	8.225e-01	-0.353	0.724854
mondMay	-3.015e-01	8.223e-01	-0.367	0.714619
mondJun	-1.682e-01	8.221e-01	-0.205	0.838259
mondJul	-2.070e-01	8.219e-01	-0.252	0.801657
mondAug	2.210e-03	8.218e-01	0.003	0.997859
mondSep	5.558e-02	8.217e-01	0.068	0.946201
mondOct	1.591e-01	8.216e-01	0.194	0.846811
mondNov	1.086e-01	8.216e-01	0.132	0.895065

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.837 on 106 degrees of freedom

Multiple R-squared: 0.9754, Adjusted R-squared: 0.9724

F-statistic: 323.6 on 13 and 106 DF, p-value: < 2.2e-16

$Y = 2.128e+02 - 3.388e-01(\text{mondJan}) - 2.476e-01(\text{mondFeb}) - 3.084e-01(\text{mondMar}) - 2.903e-01(\text{mondApr}) - 3.015e-01(\text{mondMay}) - 1.682e-01(\text{mondJun}) - 2.070e-01(\text{mondJul}) + 2.210e-03(\text{mondAug}) + 5.558e-02(\text{mondSep}) + 1.591e-01(\text{mondOct}) + 1.086e-01(\text{mondNov}) + 3.837e-01(\text{time}) - 5.849e-04(\text{time}^2)$

time.e <- log(time)

exp.model <- lm(formula = CPI ~ time.e, data = CPIAUSCL)

print(summary(exp.model))

logels.seas <- data.frame(cbind(CPI,time,time.e, mond))

exp.seas.mod <- lm(formula = CPI ~ time + time.e + mond, data = logels.seas)

print(summary(exp.seas.mod))

Call:

lm(formula = CPI ~ time + time.e + mond, data = logels.seas)

Residuals:

	Min	1Q	Median	3Q	Max
	-3.5997	-1.3549	0.1793	1.4193	2.5213

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	2.095e+02	1.129e+00	185.516	< 2e-16	***
time	2.668e-01	1.033e-02	25.828	< 2e-16	***
time.e	1.934e+00	3.861e-01	5.009	2.2e-06	***
mondJan	3.429e-02	7.912e-01	0.043	0.966	
mondFeb	7.143e-04	7.889e-01	0.001	0.999	
mondMar	-1.287e-01	7.879e-01	-0.163	0.871	

mondApr	-1.562e-01	7.873e-01	-0.198	0.843
mondMay	-2.003e-01	7.869e-01	-0.255	0.800
mondJun	-9.207e-02	7.866e-01	-0.117	0.907
mondJul	-1.504e-01	7.864e-01	-0.191	0.849
mondAug	4.302e-02	7.863e-01	0.055	0.956
mondSep	8.348e-02	7.862e-01	0.106	0.916
mondOct	1.762e-01	7.861e-01	0.224	0.823
mondNov	1.166e-01	7.861e-01	0.148	0.882

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.758 on 106 degrees of freedom

Multiple R-squared: 0.9775, Adjusted R-squared: 0.9747

F-statistic: 354.2 on 13 and 106 DF, p-value: < 2.2e-16

$$Y = 2.095e+02 + 3.429e-02(\text{mondJan}) + 7.143e-04(\text{mondFeb}) - 1.287e-01(\text{mondMar}) \\ - 1.562e-01(\text{mondApr}) - 2.003e-01(\text{mondMay}) - 9.207e-02(\text{mondJun}) \\ - 1.504e-01(\text{mondJul}) + 4.302e-02(\text{mondAug}) + 8.348e-02(\text{mondSep}) + \\ 1.762e-01(\text{mondOct}) + 1.166e-01(\text{mondNov}) + 2.668e-01(\text{time}) + \\ 1.934e+00(\text{time.e})$$

While the Exponential Model has the lowest residual median out of all three models in terms of residuals, it has the highest range of residuals out of all three models. This means that this model does not accurately predict all the CPIS accurately for each observation as well as the Linear Model. The Linear Model has the lowest residual range out of all the models. This means that the predicted CPI for each observation in the Linear Model is the least off from the actual outcome. In terms of the plots, the Linear Model seems to be the most aligned with the actual results. Given that the Linear Model also yielded the highest R², the predicted outcomes of the Linear Model and the actual results from the dataset have the strongest correlation with each other out of all three models.

#TimeFrame

```
time_new <- seq(1, 120, by=1)
View(time_new)
```

```
CPIAUSCL<-data.frame(time_new, CPI)
print(CPIAUSCL)
```


	CPI
1	211.933
2	212.705
3	212.495
4	212.709
5	213.022
6	214.790
7	214.726
8	215.445
9	215.861
10	216.509
11	217.234
12	217.347

13	217.488
14	217.281
15	217.353
16	217.403
17	217.290
18	217.199
19	217.605
20	217.923
21	218.275
22	219.035
23	219.590
24	220.472
25	221.187

26	221.898
27	223.046
28	224.093
29	224.806
30	224.806
31	225.395
32	226.106
33	226.597
34	226.750
35	227.169
36	227.223
37	227.842
38	228.329

39	228.807
40	229.187
41	228.713
42	228.524
43	228.590
44	229.918
45	231.015
46	231.638
47	231.249
48	231.221
49	231.679
50	232.937
51	232.282

52	231.797
53	231.893
54	232.445
55	232.900
56	233.456
57	233.544
58	233.669
59	234.100
60	234.719
61	235.288
62	235.547
63	236.028
64	236.468

65	236.918
66	237.231
67	237.498
68	237.460
69	237.477
70	237.430
71	236.983
72	236.252
73	234.718
74	235.236
75	236.005
76	236.156
77	236.974

78	237.684
79	238.053
80	238.028
81	237.506
82	237.781
83	238.016
84	237.817
85	237.833
86	237.469
87	238.038
88	238.827
89	239.464
90	240.167

91	240.150
92	240.602
93	241.051
94	241.691
95	242.029
96	242.772
97	243.780
98	243.961
99	243.749
100	244.051
101	243.962
102	244.182
103	244.390

104	245.297
105	246.418
106	246.587
107	247.332
108	247.901
109	248.884
110	249.369
111	249.498
112	249.956
113	250.646
114	251.134
115	251.597
116	251.879

117	252.010
118	252.794
119	252.760
120	252.723

```
linear.mod <- lm(CPI~time_new, data=CPIAUSCL)
print(summary(linear.mod))
```

Call:

```
lm(formula = CPI ~ time_new, data = CPIAUSCL)
```

Residuals:

```
      Min       1Q   Median       3Q      Max
-3.5292 -1.7505 -0.2766  1.6960  3.2218
```

Coefficients:

```
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 2.140e+02   3.419e-01  626.12   <2e-16 ***
time_new     3.134e-01   4.904e-03   63.91   <2e-16 ***
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 1.861 on 118 degrees of freedom

Multiple R-squared: 0.9719, Adjusted R-squared: 0.9717

F-statistic: 4085 on 1 and 118 DF, p-value: < 2.2e-16

#Linear Graph

```
CPA_10.act <- CPIAUSCL$CPI
```

```
CPA_10.pred <- predict(linear.mod, CPIAUSCL)
```

```
CPA_10.resid <- CPA_10.act - CPA_10.pred
```

```
CPA_10.resid.plot <- CPA_10.resid + 200
```

```
CPA_10.pred.seas <- predict(linear.seas.mod, CPIAUSCL)
```

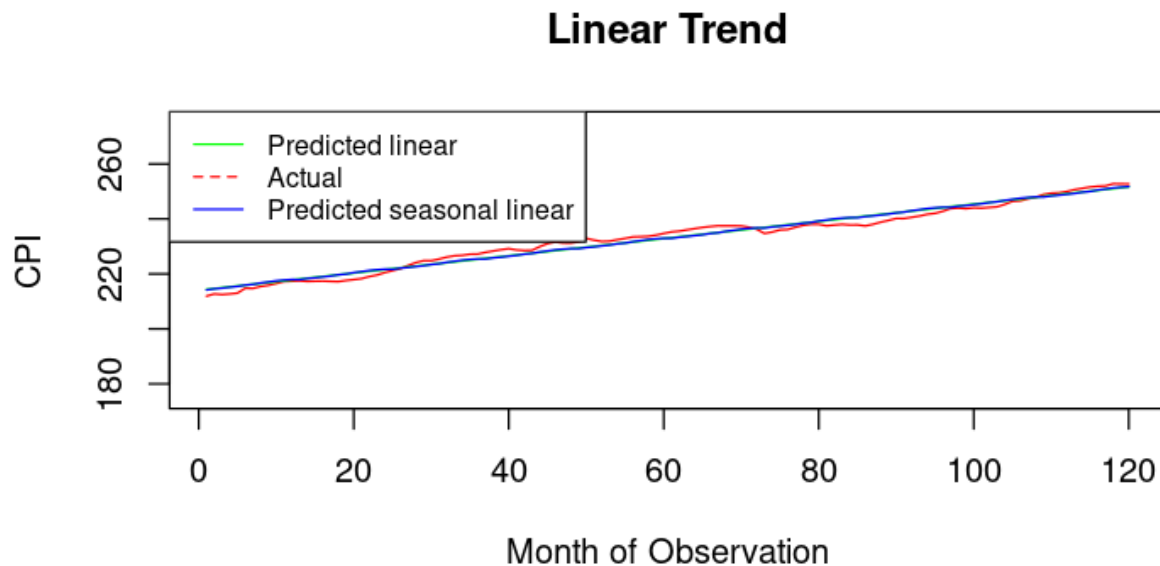
```
CPA_10.resid.seas <- CPA_10.act - CPA_10.pred.seas
```

```
CPA_10.pred.seas.plot <- CPA_10.resid.seas + 200
```

```

plot(CPA_10.act, type="l", axes=TRUE, main ="Linear Trend", ylim=c(175,275), xlab="Month of
Observation", ylab="CPI", col="red")
lines(CPA_10.pred, col="green")
lines(CPA_10.pred.seas, col="blue")
legend("topleft", legend=c("Predicted linear", "Actual", 'Predicted seasonal linear'),
      col=c("green",'red' ,"blue"), lty=1:2, cex=0.8)

```



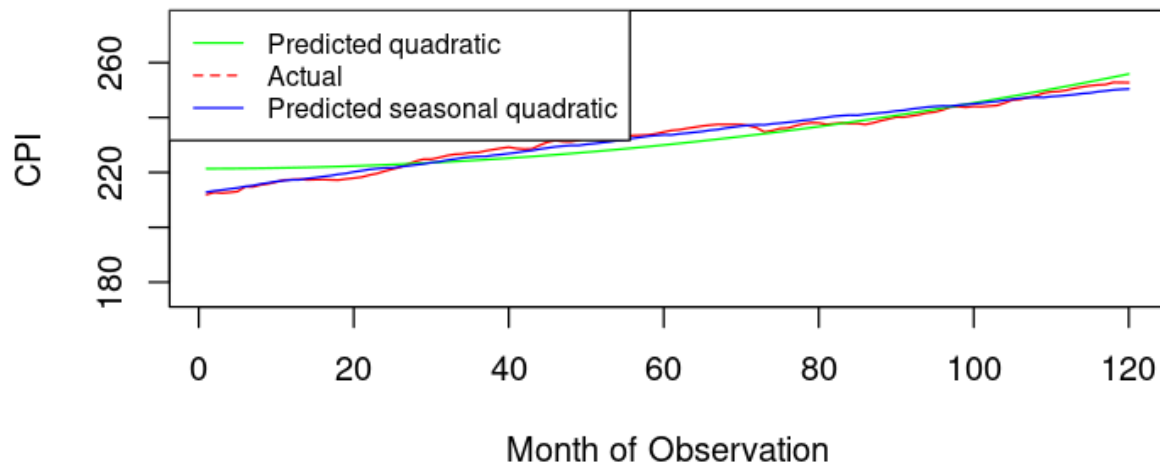
#Quadratic Graph

```

time2 <- time^2
quad.mod <- lm(formula = CPI ~ time2, data = CPIAUSCL)
print(summary(quad.mod))
CPIAUSCL.act <- CPIAUSCL$CPI
CPIAUSCL.pred <- predict(quad.mod,CPIAUSCL)
CPIAUSCL.resid <- CPIAUSCL.act- CPIAUSCL.pred
CPIAUSCL.resid.plot <- CPIAUSCL.resid + 200
CPIAUSCL.pred.seas <- predict(quad.seas.mod, CPIAUSCL)
CPIAUSCL.resid.seas <- CPIAUSCL.act - CPIAUSCL.pred.seas
CPIAUSCL.pred.seas.plot <- CPIAUSCL.resid.seas + 200
plot( CPIAUSCL.act, type="l", axes=TRUE, main ="Quadratic Trend", ylim=c(175,275),
xlab="Month of Observation", ylab="CPI", col="red")
lines( CPIAUSCL.pred, col="green")
lines(CPIAUSCL.pred.seas, col="blue")
legend("topleft", legend=c("Predicted quadratic", "Actual", 'Predicted seasonal quadratic'),
      col=c("green",'red' ,"blue"), lty=1:2, cex=0.8)

```

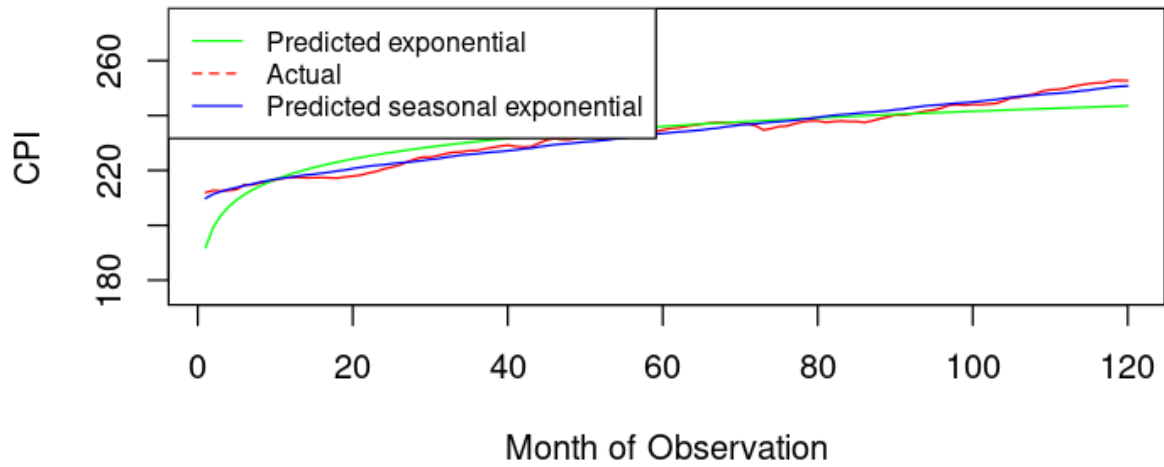
Quadratic Trend



#Exponential Graph

```
CPIAUSCL_1.act <- CPIAUSCL$CPI
CPIAUSCL_1.pred <- predict(exp.model, CPIAUSCL)
CPIAUSCL_1.resid <- CPIAUSCL_1.act - CPIAUSCL_1.pred
CPIAUSCL_1.resid.plot <- CPIAUSCL_1.resid + 200
CPIAUSCL_1.pred.seas <- predict(exp.seas.mod, CPIAUSCL)
CPIAUSCL_1.resid.seas <- CPIAUSCL_1.act - CPIAUSCL_1.pred.seas
CPIAUSCL_1.pred.seas.plot <- CPIAUSCL_1.resid.seas + 200
plot( CPIAUSCL_1.act, type="l", axes=TRUE, main ="Exponential Trend", ylim=c(175,275),
xlab="Month of Observation", ylab="CPI", col="red")
lines( CPIAUSCL_1.pred, col="green")
lines( CPIAUSCL_1.pred.seas, col="blue")
legend("topleft", legend=c("Predicted exponential", "Actual", 'Predicted seasonal exponential'),
col=c("green",'red' ,"blue"), lty=1:2, cex=0.8)
```

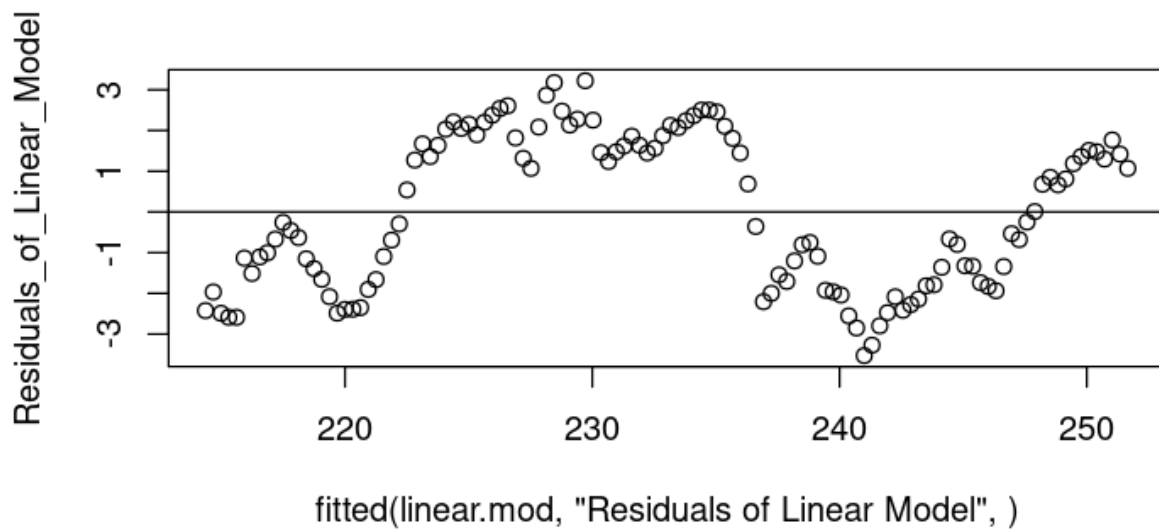
Exponential Trend



#Linear Residuals

```
Residuals_of_Linear_Model <- resid(linear.mod)
plot(fitted(linear.mod, "Residuals of Linear Model"), Residuals_of_Linear_Model)
```

abline(0,0)

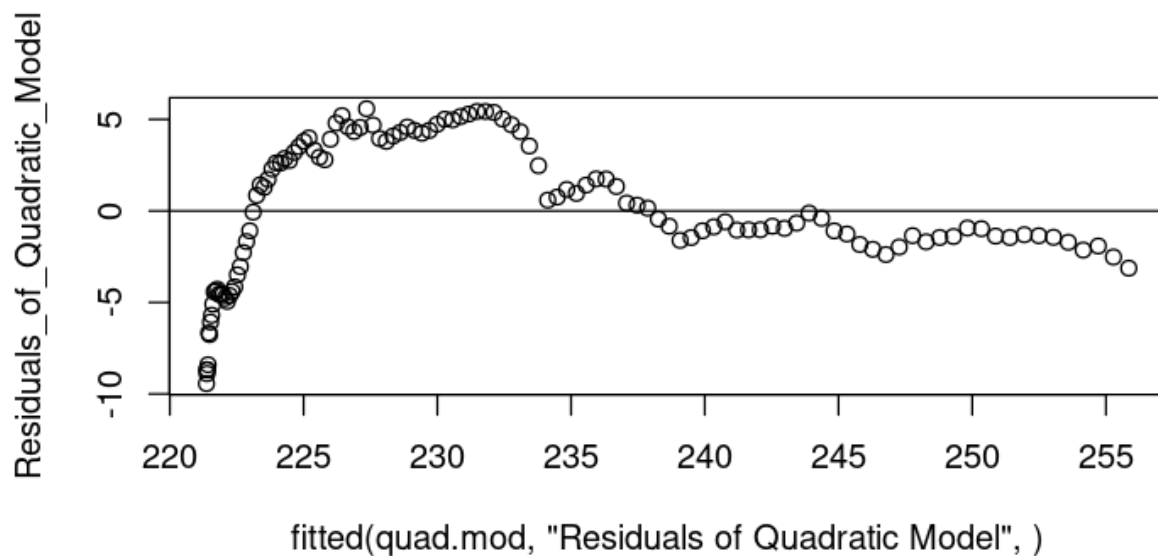


As one can observe this residual plot, one may notice some sharp spikes in the fitted model, which form a nonlinear pattern. However, the observations are spread out in a "C" shaped pattern; indicating heteroskedasticity and bias. The black dots represent the respective observations while the dotted horizontal line represents the regression model.

#Quadratic Residuals

```
Residuals_of_Quadratic_Model <- CPIAUSCL$resid
plot(fitted(quad.mod, "Residuals of Quadratic Model"), Residuals_of_Quadratic_Model)
```

```
abline(0,0)
```

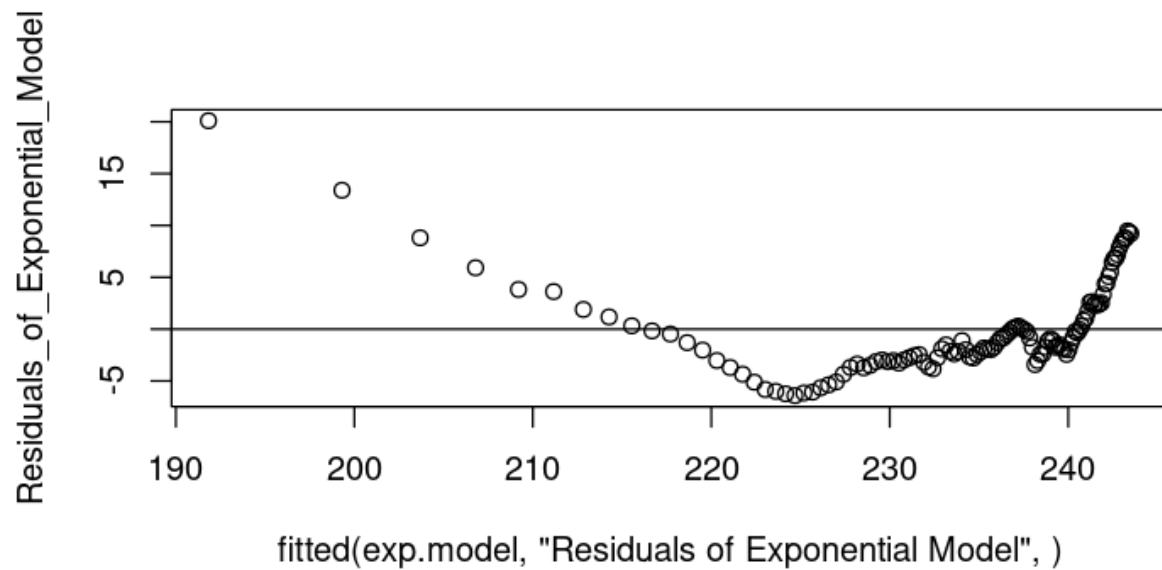


As one can observe this residual plot, one may notice some sharp spikes in the fitted model, which form a nonlinear pattern. However, the observations are spread out in a "C" shaped pattern; indicating heteroskedasticity and bias. The black dots represent the respective observations while the dotted horizontal line represents the regression model.

#Exponential Residuals

```
Residuals_of_Exponential_Model <- resid(exp.model)
plot(fitted(exp.model, "Residuals of Exponential Model"), Residuals_of_Exponential_Model)
```

```
abline(0,0)
```



As one can observe, there is a double yet subtle hump along the lowest line in the residual plot. In addition, their residuals are quite spread out in no particular pattern which indicates constant variance and homoscedasticity. The black dots are the respective residuals while the dotted horizontal line represents the regression model.

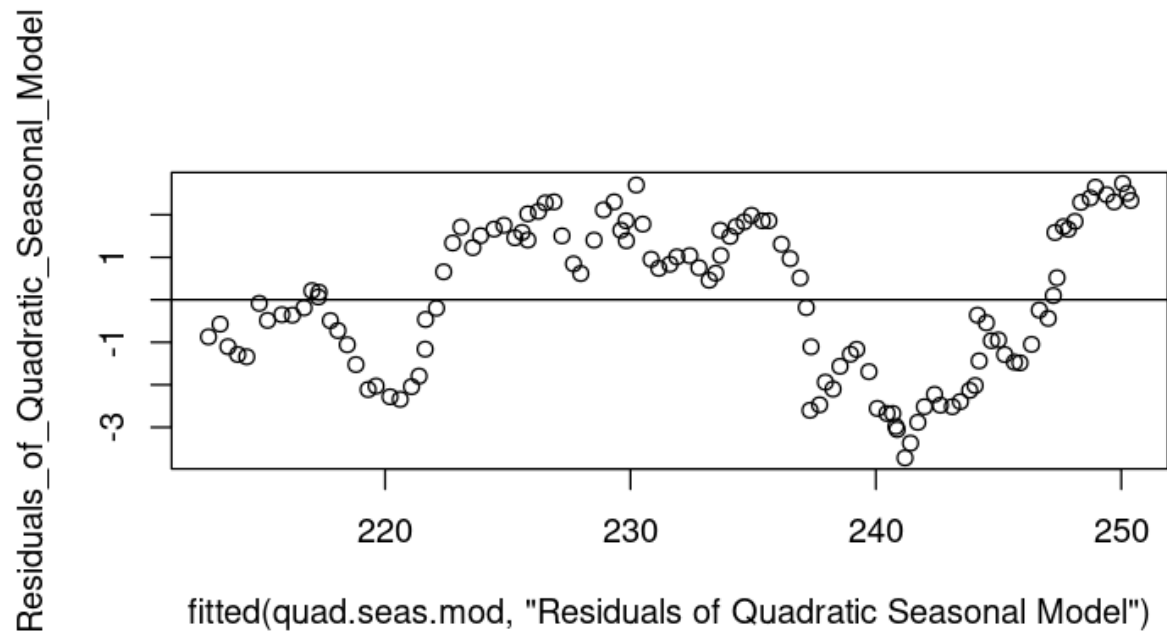
```
#Seasonal Quadratic Residuals
```

```
Residuals_of_Quadratic_Seasonal_Model <- resid(quad.seas.mod)
```

```
typeof(Residuals_of_Quadratic_Seasonal_Model)
```

```
plot(fitted(quad.seas.mod, "Residuals of Quadratic Seasonal Model"),  
     Residuals_of_Quadratic_Seasonal_Model)
```

```
abline(0,0)
```

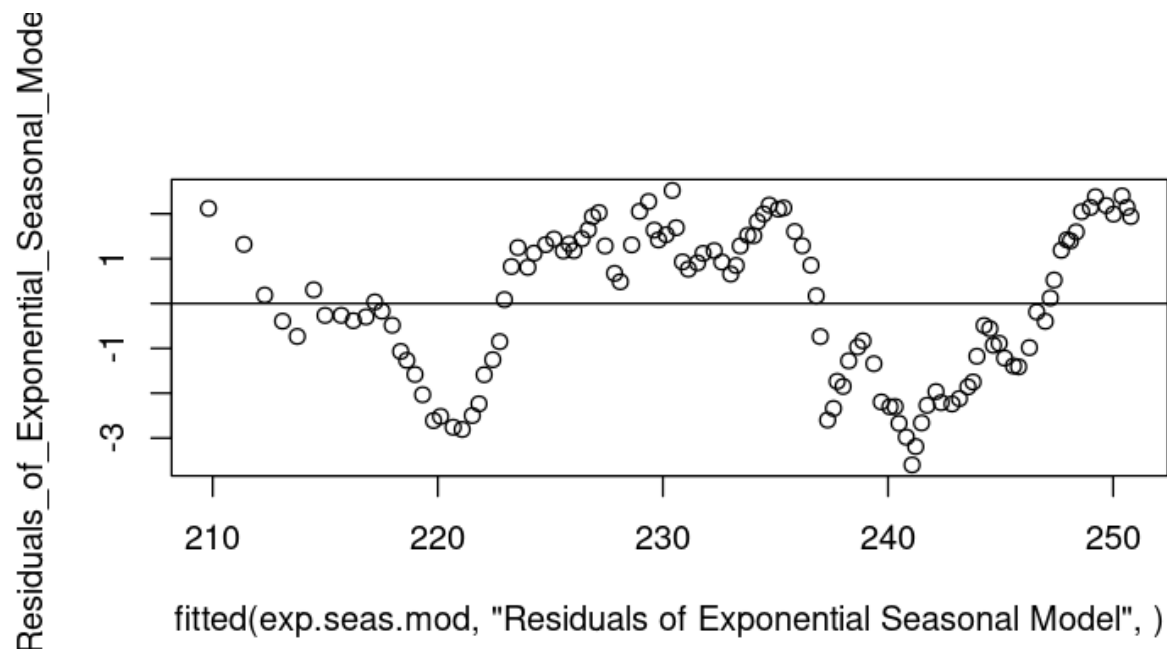


As one can observe, there is a double yet subtle hump along the lowest line in the residual plot. In addition, their residuals are quite spread out in no particular pattern which indicates constant variance and homoscedasticity. The black dots are the respective residuals while the dotted horizontal line represents the regression model.

#Seasonal Exponential Residuals

```
Residuals_of_Exponential_Seasonal_Model <- resid(exp.seas.mod)
```

```
plot(fitted(exp.seas.mod, "Residuals of Exponential Seasonal Model"),
     Residuals_of_Exponential_Seasonal_Model)
abline(0,0)
```

As one can observe, there is a double yet subtle hump along the lowest line in the residual plot. In addition, their residuals are quite spread out in no particular pattern which indicates constant variance and homoscedasticity. The black dots are the respective residuals while the dotted horizontal line represents the regression model.

#Seasonal Linear Residuals

```
Residuals_of_Linear_Seasonal_Model <- resid(linear.seas.mod)
plot(fitted(linear.seas.mod, "Residuals of Linear Seasonal Model", ),
Residuals_of_Linear_Seasonal_Model)
abline(0,0)
```

#AIC vs BIC

```
AIC <- AIC(linear.mod,quad.mod,exp.model,quad.seas.mod,linear.seas.mod,exp.seas.mod)
BIC <- BIC(linear.mod,quad.mod,exp.model,quad.seas.mod,linear.seas.mod,exp.seas.mod)
mod.selection <- data.frame(cbind(AIC,BIC[,2]))
names(mod.selection)[3] <- "BIC"
print(mod.selection)
```

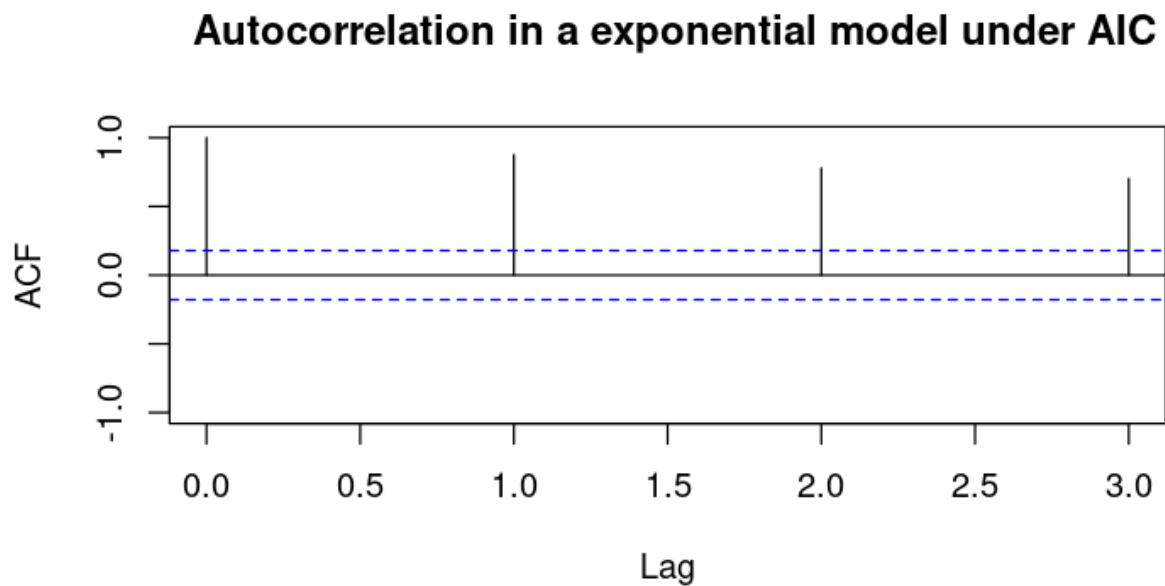
	df	AIC	BIC
linear.mod	3	493.5627	501.9251
quad.mod	3	662.4199	670.7823
exp.model	3	706.2842	714.6467
quad.seas.mod	15	501.6160	543.4284

```
linear.seas.mod 14 514.5087 553.5336  
exp.seas.mod    15 491.0178 532.8301
```

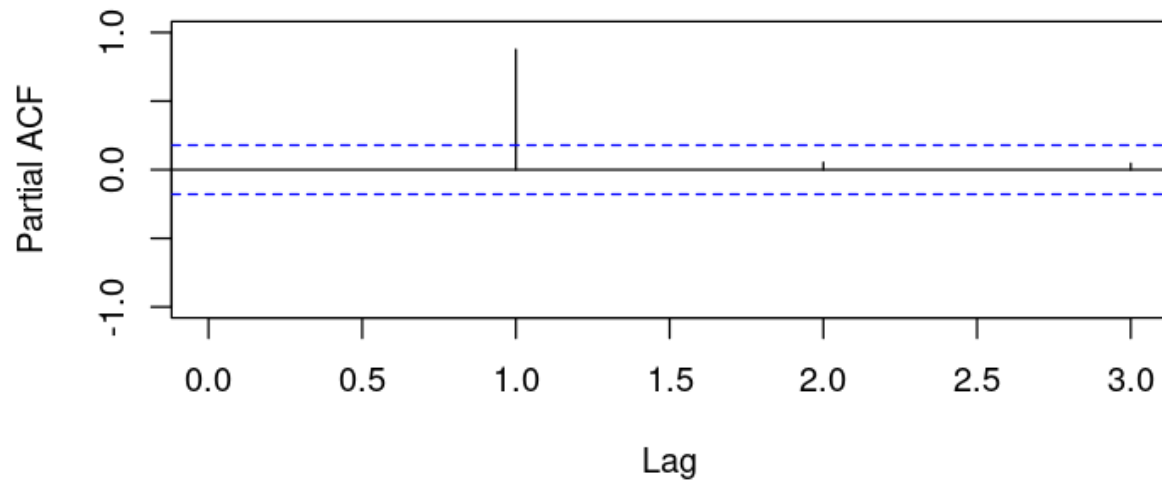
#Exponential auto and partial correlation plots

```
plot(acf(residual_exp, plot = F), xlim = c(0,3), ylim = c(-1, 1), main = " Autocorrelation in a  
exponential model under AIC")
```

```
plot(acf(residual_exp, plot = F, type = "p"), xlim = c(0,3),ylim = c(-1,1), main = "Partial  
Autocorrelation in a exponential model under AIC")
```



Partial Autocorrelation in a exponential model under AIC

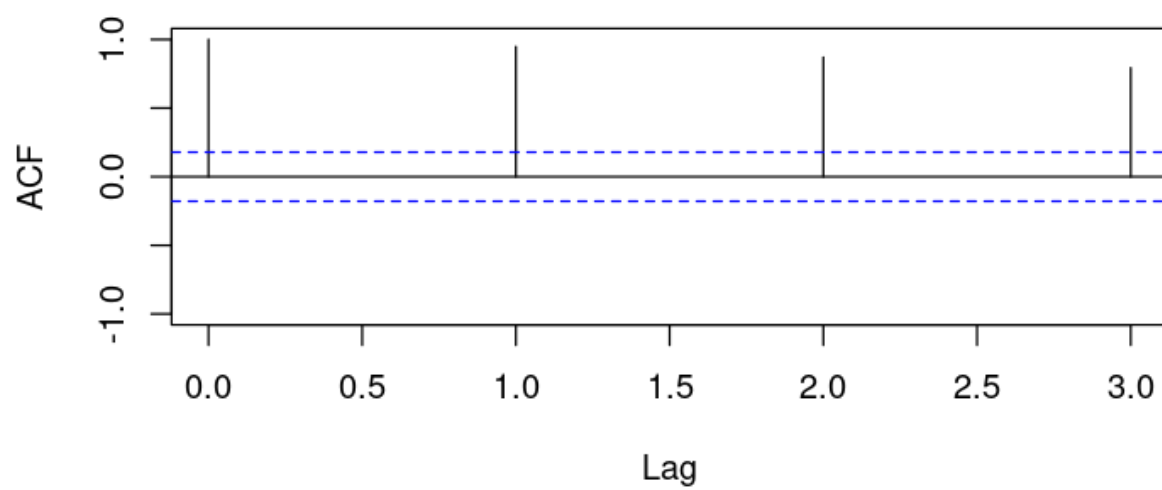


As one can observe, there is statistical significance in the partial and autocorrelation plots, indicating that the lags directly beforehand influenced the CPI values.

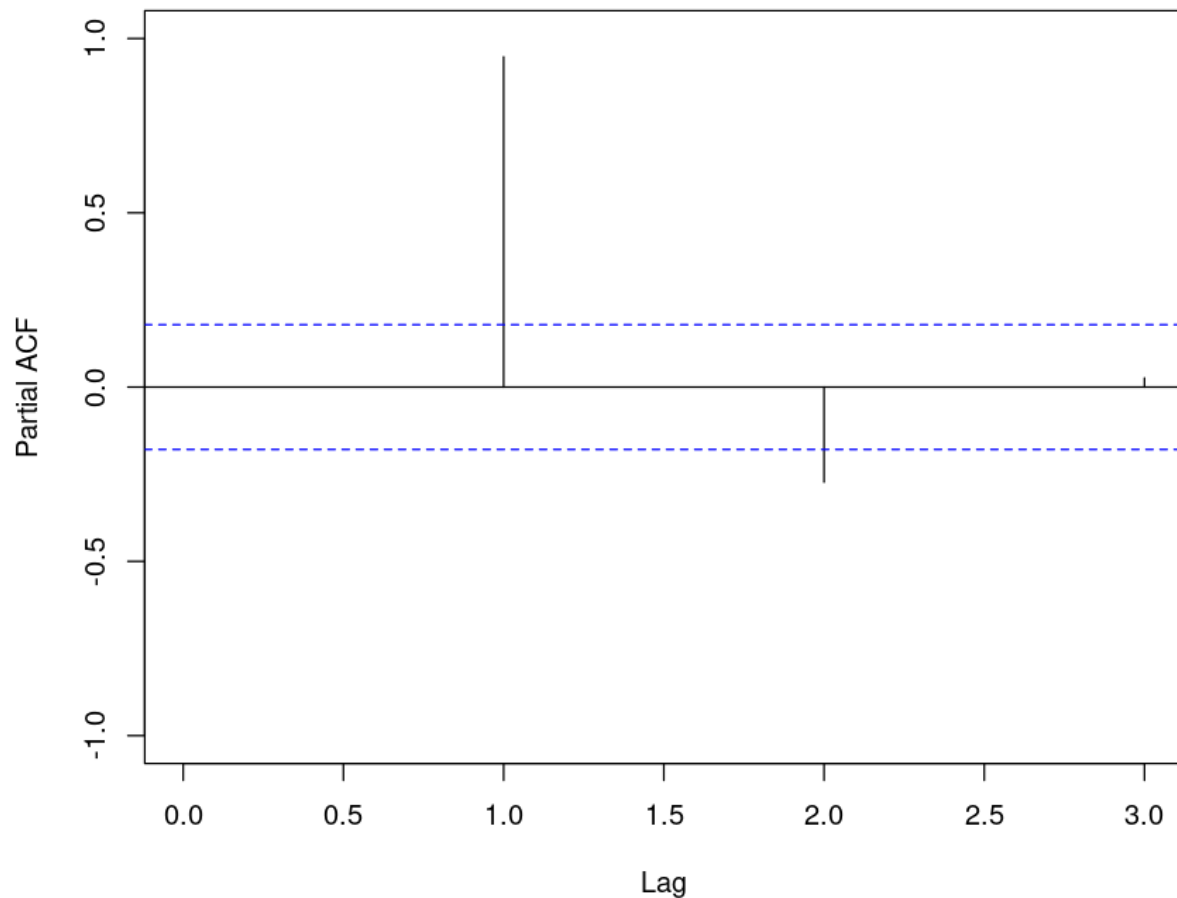
The plots below graphically summarize the strength of a relationship with an observation in a time series with observations at prior time steps. The autocorrelation with lag zero always equals 1, because this represents the autocorrelation between each term and itself. Each spike that rises above or falls below the shaded blue shapes is considered to be statistically significant. This means the spike has a value that is significantly different from zero. If a spike is significantly different from zero, that is evidence of autocorrelation. A spike that's close to zero is evidence against autocorrelation. Meanwhile, the lags within partial autocorrelation plots depend on the lag directly beforehand. Since the AIC was lower in value than the BIC, the AIC will be used for the correlation plots.

```
plot(acf(residual_exp_seas, plot = F), xlim = c(0,3), ylim = c(-1, 1), main = " Autocorrelation in a  
exponential seasonal model under AIC")  
plot(acf(residual_exp_seas, plot = F, type = "p"), xlim = c(0,3),ylim = c(-1,1), main = "Partial  
Autocorrelation in a exponential seasonal model under AIC")
```

Autocorrelation in a exponential seasonal model under AIC



Partial Autocorrelation in a exponential seasonal model under AIC



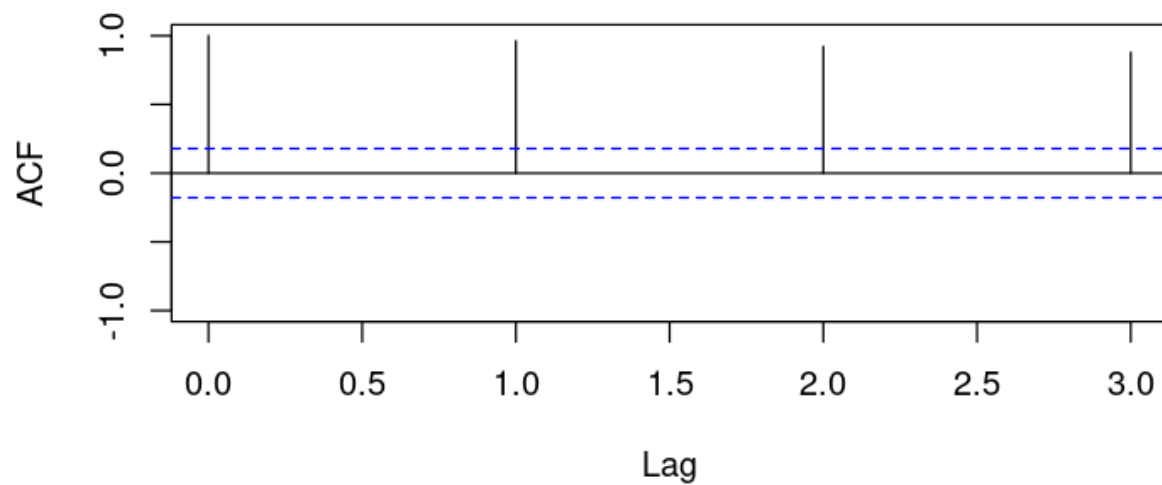
The plots above graphically summarize the strength of a relationship with an observation in a time series with observations at prior time steps. The autocorrelation with lag zero always equals 1, because this represents the autocorrelation between each term and itself. Each spike that rises above or falls below the shaded blue shapes is considered to be statistically significant. This means the spike has a value that is significantly different from zero. If a spike is significantly different from zero, that is evidence of autocorrelation. A spike that's close to zero is evidence against autocorrelation. Meanwhile, the lags within partial autocorrelation plots depend on the lag directly beforehand. Since the AIC was lower in value than the BIC, the AIC will be used for the correlation plots.

As one can observe, there is statistical significance in the partial and autocorrelation plots, indicating that the lags directly beforehand influenced the CPI values.

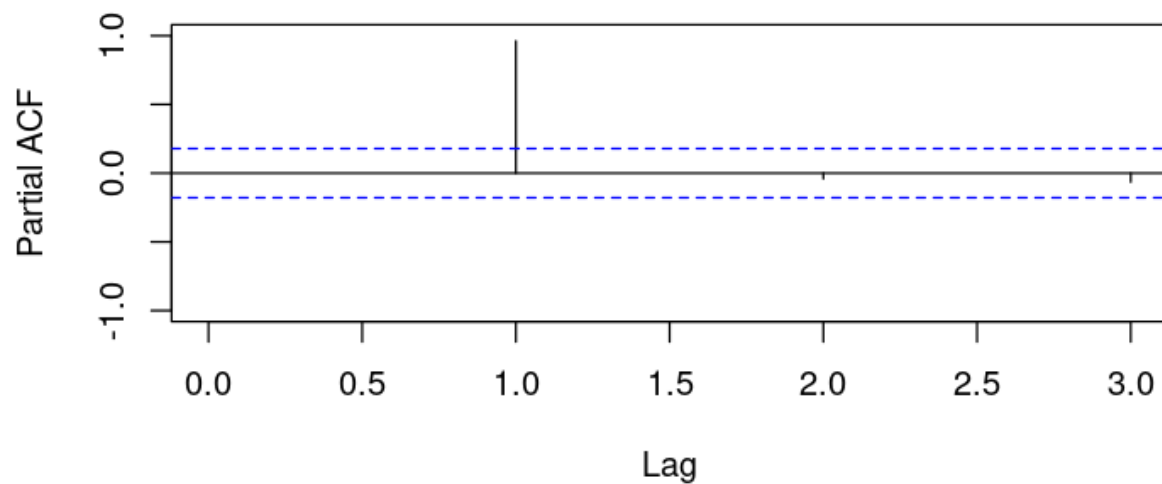
#Quadratic auto and partial correlation plots

```
plot(acf(residual_quad, plot = F), xlim = c(0,3), ylim = c(-1, 1), main = " Autocorrelation in a  
quadratic model under AIC")  
plot(acf(residual_quad, plot = F, type = "p"), xlim = c(0,3),ylim = c(-1,1), main = "Partial  
Autocorrelation in a quadratic model under AIC")
```

Autocorrelation in a quadratic model under AIC



Partial Autocorrelation in a quadratic model under AIC

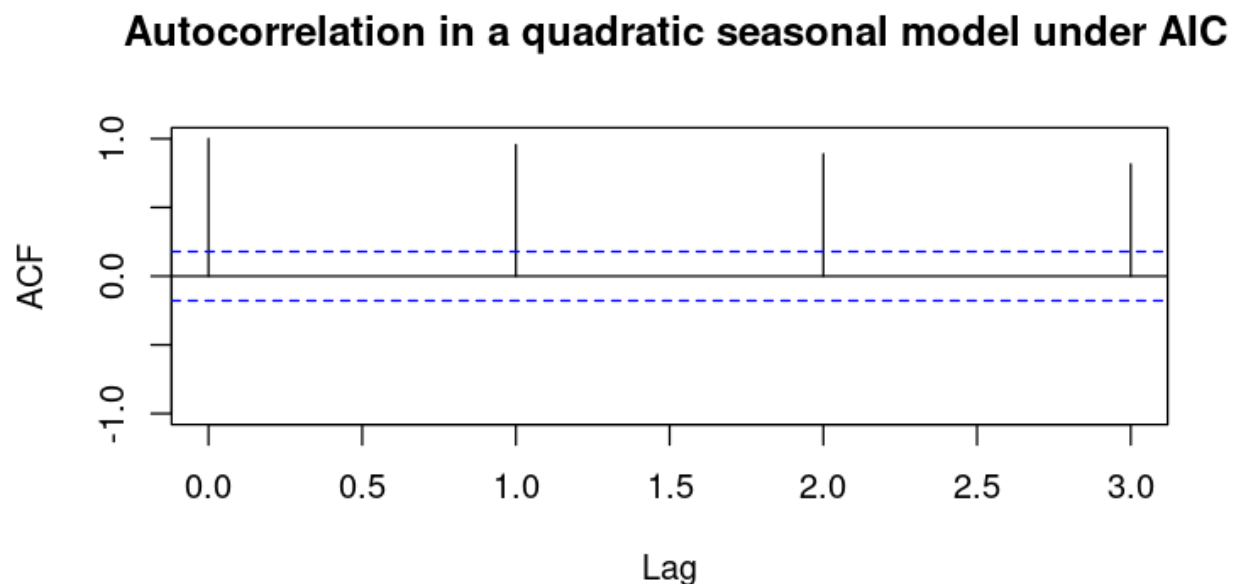


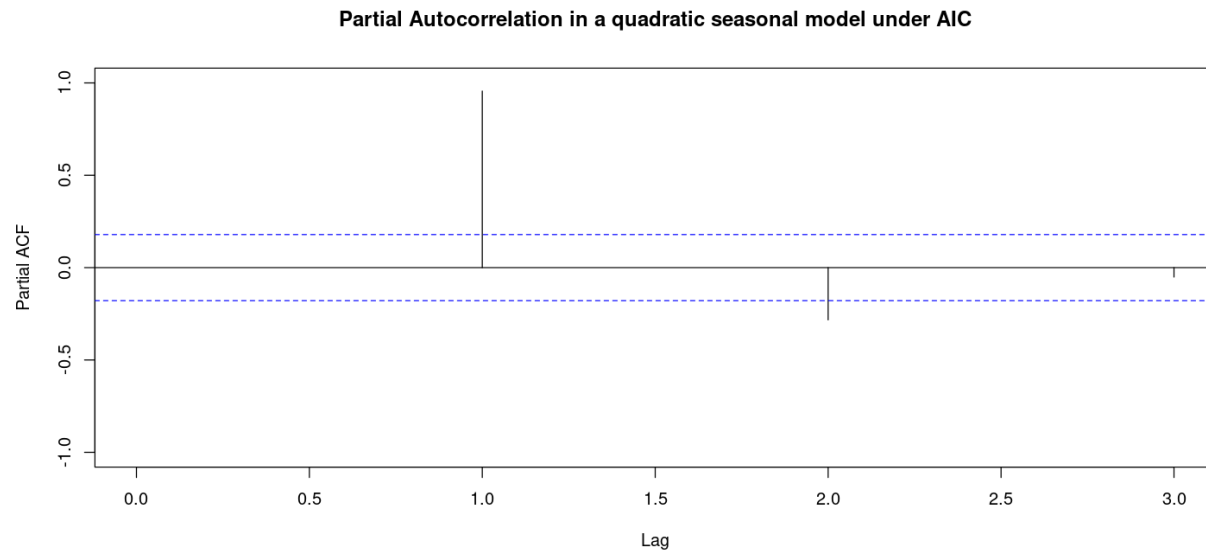
The plots above graphically summarize the strength of a relationship with an observation in a time series with observations at prior time steps. The autocorrelation with lag zero always equals 1, because this represents the autocorrelation between each term and itself. Each spike that rises above or falls below the shaded blue shapes is considered to be statistically significant. This means the spike has a value that is significantly different from zero. If a spike is significantly different from zero, that is evidence of autocorrelation. A spike that's close to zero is evidence against autocorrelation. Meanwhile, the lags within partial autocorrelation plots depend on the lag directly beforehand. Since the AIC was lower in value than the BIC, the AIC will be used for the correlation plots.

As one can observe, there is statistical significance in the partial and autocorrelation plots, indicating that the lags directly beforehand influenced the CPI values.

```
plot(acf(Residuals_of_Quadratic_Seasonal_Model, plot = F), xlim = c(0,3), ylim = c(-1, 1), main = " Autocorrelation in a quadratic seasonal model under AIC")
```

```
plot(acf(Residuals_of_Quadratic_Seasonal_Model, plot = F, type = "p"), xlim = c(0,3),ylim = c(-1,1), main = "Partial Autocorrelation in a quadratic seasonal model under AIC")
```





The plots above graphically summarize the strength of a relationship with an observation in a time series with observations at prior time steps. The autocorrelation with lag zero always equals 1, because this represents the autocorrelation between each term and itself. Each spike that rises above or falls below the shaded blue shapes is considered to be statistically significant. This means the spike has a value that is significantly different from zero. If a spike is significantly different from zero, that is evidence of autocorrelation. A spike that's close to zero is evidence against autocorrelation. Meanwhile, the lags within partial autocorrelation plots depend on the lag directly beforehand. Since the AIC was lower in value than the BIC, the AIC will be used for the correlation plots.

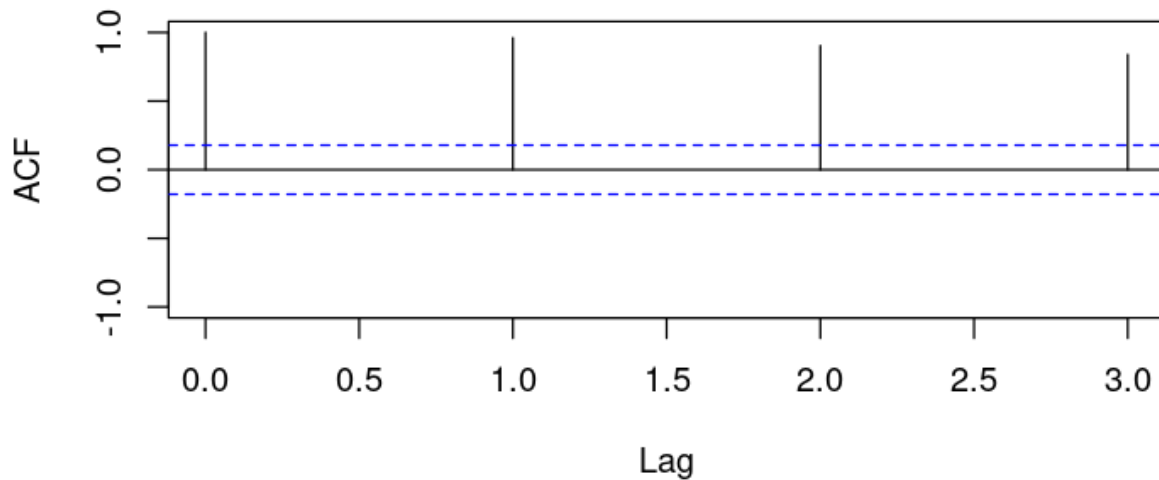
As one can observe, there is statistical significance in the partial and autocorrelation plots, indicating that the lags directly beforehand influenced the CPI values.

#Linear auto and partial correlation plots

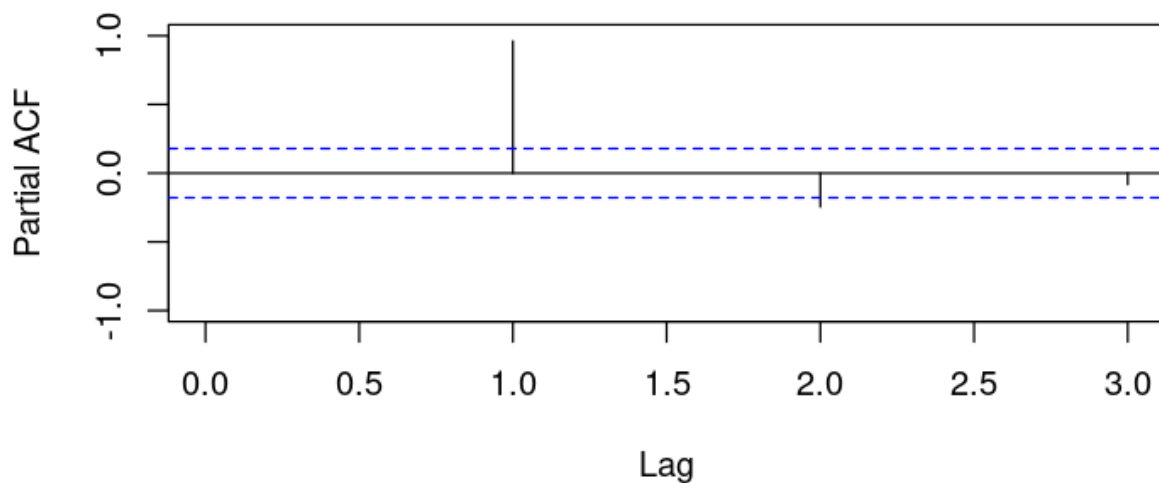
```
plot(acf(residual_linear, plot = F), xlim = c(0,3), ylim = c(-1, 1), main = " Autocorrelation in a linear model under AIC")
```

```
plot(acf(residual_linear, plot = F, type = "p"), xlim = c(0,3),ylim = c(-1,1), main = "Partial Autocorrelation in a linear model under AIC")
```


Autocorrelation in a linear model under AIC



Partial Autocorrelation in a linear model under AIC



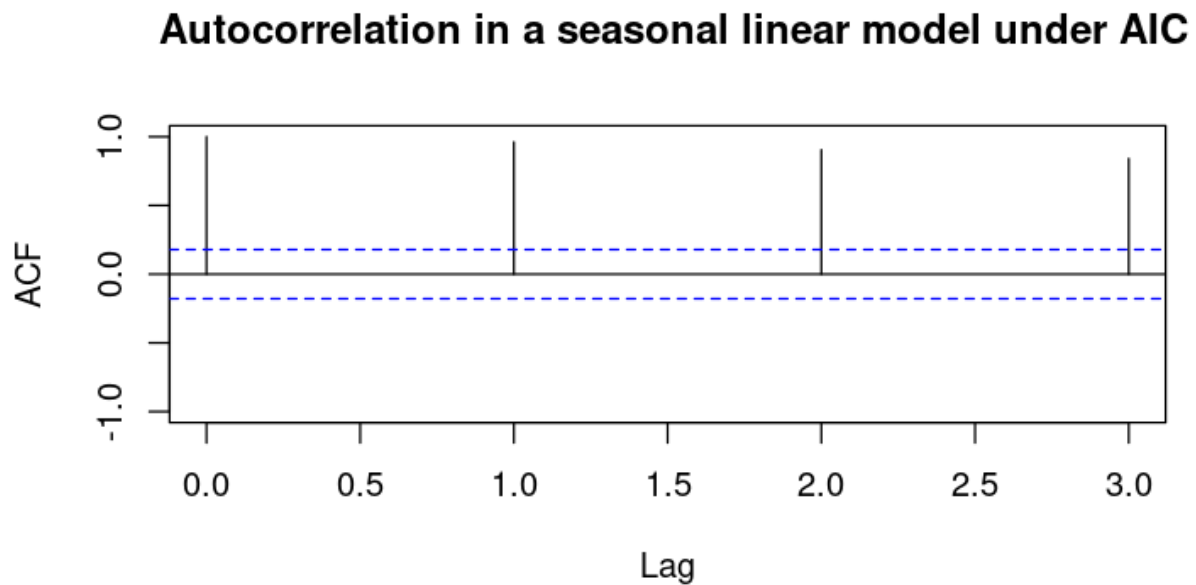
The plots above graphically summarize the strength of a relationship with an observation in a time series with observations at prior time steps. The autocorrelation with lag zero always equals 1, because this represents the autocorrelation between each term and itself. Each spike that rises above or falls below the shaded blue shapes is considered to be statistically significant. This means the spike has a value that is significantly different from zero. If a spike is significantly different from zero, that is evidence of autocorrelation. A spike that's close to zero is evidence against autocorrelation. Meanwhile, the lags within partial autocorrelation plots depend

on the lag directly beforehand. Since the AIC was lower in value than the BIC, the AIC will be used for the correlation plots.

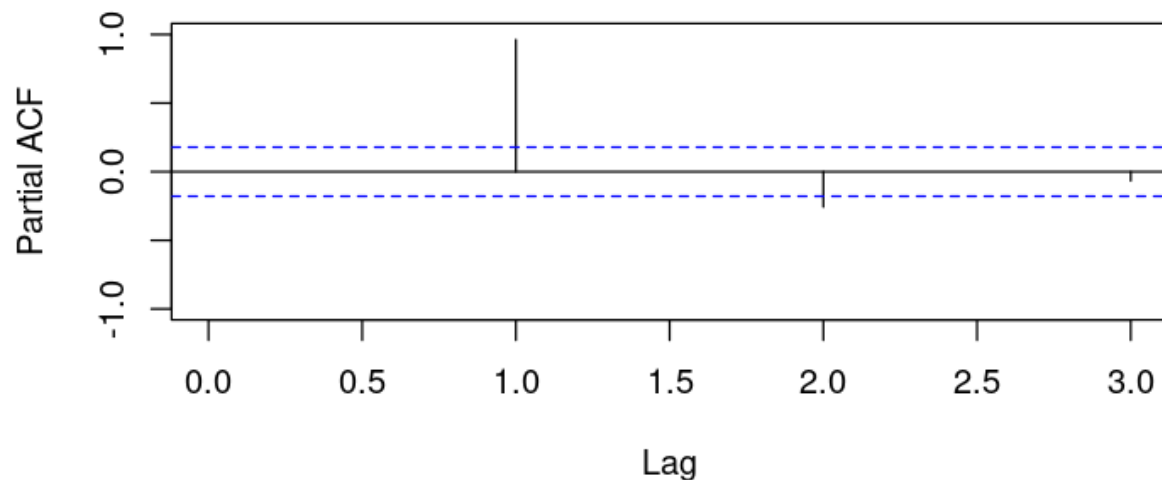
As one can observe, there is statistical significance in the partial and autocorrelation plots, indicating that the lags directly beforehand influenced the CPI values.

```
plot(acf(residual_Lin_seas, plot = F), xlim = c(0,3), ylim = c(-1, 1), main = " Autocorrelation in a seasonal linear model under AIC")
```

```
plot(acf(residual_Lin_seas, plot = F, type = "p"), xlim = c(0,3),ylim = c(-1,1), main = "Partial Autocorrelation in a linear seasonal model under AIC")
```



Partial Autocorrelation in a linear seasonal model under AIC



The plots above graphically summarize the strength of a relationship with an observation in a time series with observations at prior time steps. The autocorrelation with lag zero always equals 1, because this represents the autocorrelation between each term and itself. Each spike that rises above or falls below the shaded blue shapes is considered to be statistically significant. This means the spike has a value that is significantly different from zero. If a spike is significantly different from zero, that is evidence of autocorrelation. A spike that's close to zero is evidence against autocorrelation. Meanwhile, the lags within partial autocorrelation plots depend on the lag directly beforehand. Since the AIC was lower in value than the BIC, the AIC will be used for the correlation plots.

As one can observe, there is statistical significance in the partial and autocorrelation plots, indicating that the lags directly beforehand influenced the CPI values.

#Seasonality Test

```
fried(CPI, freq = 12, diff = T, residuals = F, autoarima = T)
```

```
Test used: Friedman rank
```

```
Test statistic: 4.2
```

```
P-value: 0.9636688
```

Given that the p value of the Friedman test, an algorithm that determines whether a time series contains seasonality or trends, was 0.9636688; the null hypothesis has been rejected. However, since the alpha threshold of .05 is utilized in this algorithm, it is statistically significant that CPI

values within the country of Canada from the years 2000 to 2009 did not have any indication of seasonality or trends within its values. As such, the alternative hypothesis being that the CPI index in Canada from 2000 to 2009 was seasonally adjusted is supported by the Friedman test.