

Shivani_gowda_ps2

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```
[1]: %load_ext autoreload
      %autoreload 2
      %matplotlib inline
```

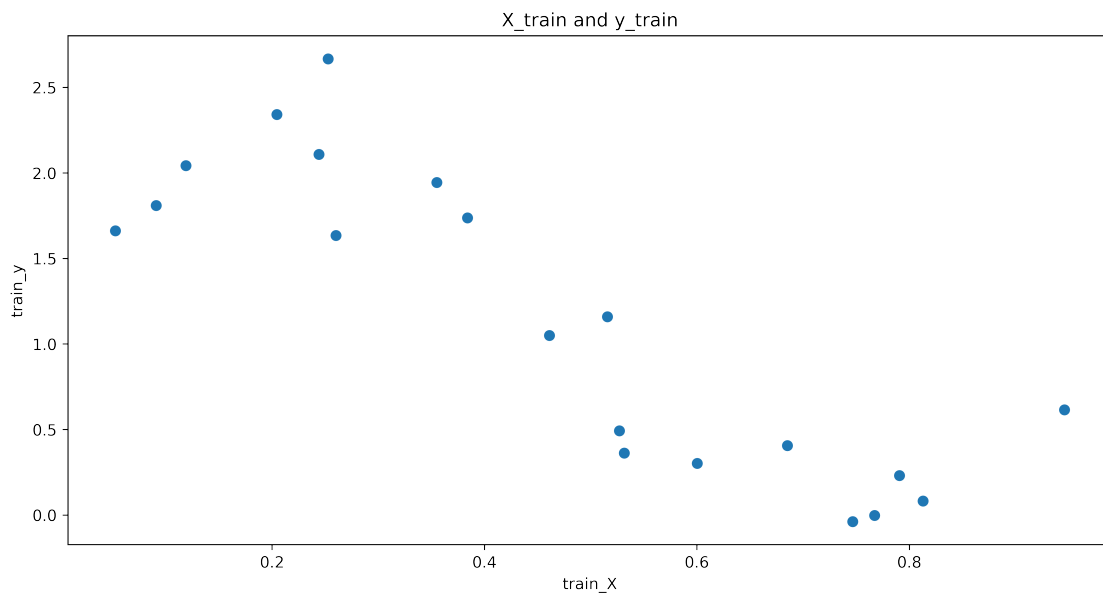
```
[5]: import sys
      from pathlib import Path
      import matplotlib.pyplot as plt

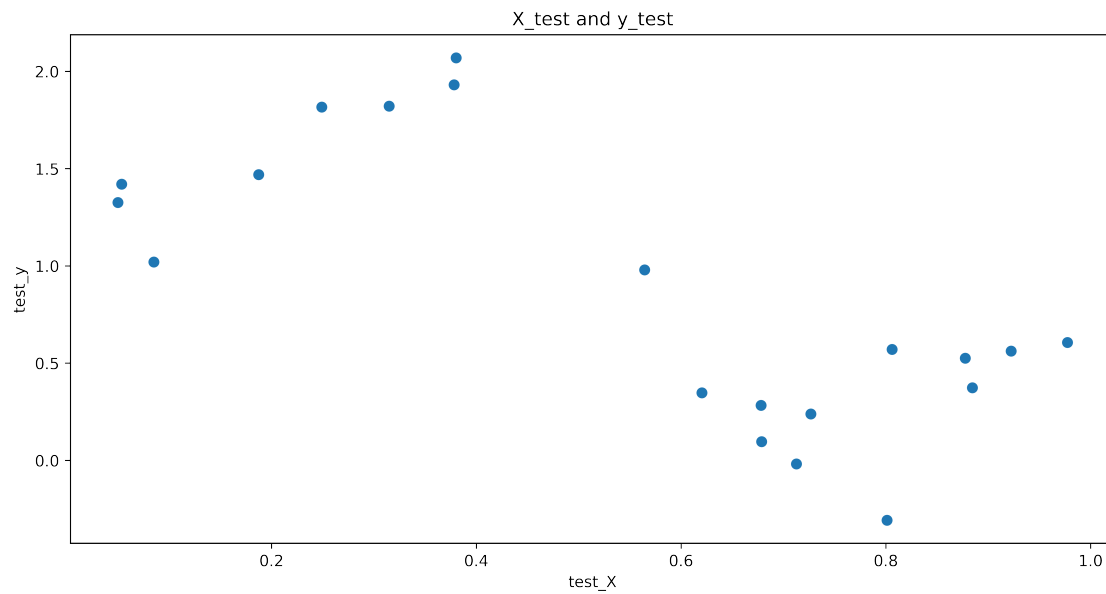
      plt.rcParams["figure.figsize"] = (12, 6)
      plt.rcParams['figure.dpi'] = 600
      if 'source' not in sys.path:
          sys.path.append('source')
```

```
[8]: import regression
      from regression import main
```

```
[19]: main()
```

Visualizing data...





Investigating linear regression...

```
[[1.      0.515773]
 [1.      0.790645]
 [1.      0.685289]
 [1.      0.946009]
 [1.      0.53169 ]
 [1.      0.118853]
 [1.      0.600345]
 [1.      0.090962]
 [1.      0.355033]
 [1.      0.204493]
 [1.      0.812833]
 [1.      0.252854]
 [1.      0.527025]
 [1.      0.260206]
 [1.      0.244096]
 [1.      0.383914]
 [1.      0.767244]
 [1.      0.461121]
 [1.      0.746685]
 [1.      0.052486]]
```

```
coef: [6.578865 7.953225 7.426445 8.730045 6.65845  4.594265 7.001725 4.45481
 5.775165 5.022465 8.064165 5.26427  6.635125 5.30103  5.22048  5.91957
```

7.83622 6.305605 7.733425 4.26243]

cost function: 314.5730363712805

number of iterations: 616

sgd solution: [2.44078184 -2.81863861]

Time for sgd solution: 0.09516255598282441

table for varying alpha size

number of iterations: 64620

number of iterations: 7330

number of iterations: 616

number of iterations: 152

	alpha	iterations	coef
0	0.0001	64620	[2.44509281 -2.81382739]
1	0.0010	7330	[2.44555307 -2.81594059]
2	0.0100	616	[2.44078184 -2.81863861]
3	0.1000	152	[2.38405089 -2.87906028]

closed_form solution: [2.44640709 -2.81635359]

Time for closed_form solution: 0.00021810800535604358

Results with eta = None

number of iterations: 2320

sgd solution after predicting tmax: [2.44652801 -2.81718713]

Investigating polynomial regression...

Polynomial feature: [[1. 0.515773 0.26602179]

[1. 0.790645 0.62511952]

[1. 0.685289 0.46962101]

[1. 0.946009 0.89493303]

[1. 0.53169 0.28269426]

[1. 0.118853 0.01412604]

[1. 0.600345 0.36041412]

[1. 0.090962 0.00827409]

[1. 0.355033 0.12604843]

[1. 0.204493 0.04181739]

[1. 0.812833 0.66069749]

[1. 0.252854 0.06393515]

[1. 0.527025 0.27775535]

```

[1.      0.260206  0.06770716]
[1.      0.244096  0.05958286]
[1.      0.383914  0.14738996]
[1.      0.767244  0.58866336]
[1.      0.461121  0.21263258]
[1.      0.746685  0.55753849]
[1.      0.052486  0.00275478]]

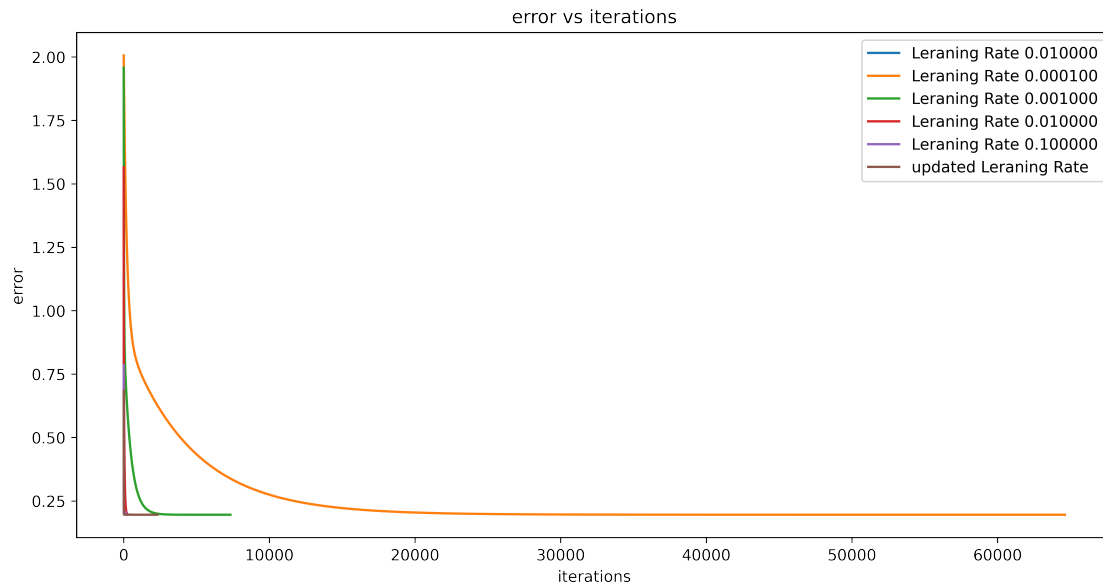
```

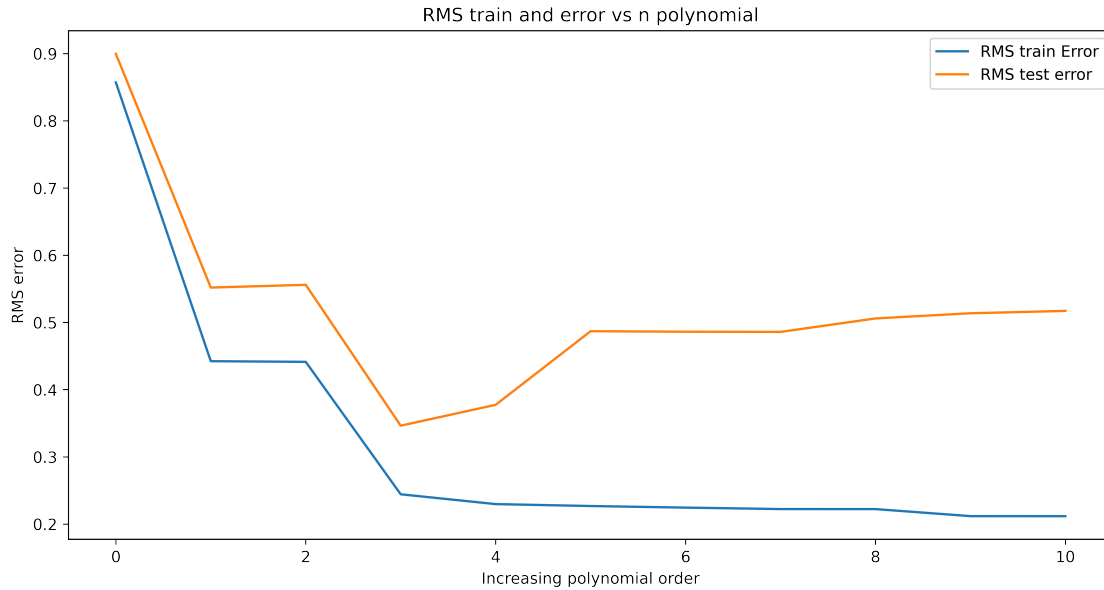
```
RMS_error = [7.79451604]
```

```

Investigating regularized regression...
RMS train minimum error: %f [0.211693]
RMS test minimum error: %f [0.34635263]

```





3rd order is giving the lowest RMS error
Done!

0.1 Visualization:

0.1.1 1.

The scatter plot X-train vs y-train and x-test and y-test has many rises and dips, hence cannot be easily fitted into a linear solution. And hence using a polynomial function would give more accuracy.

0.2 Linear Regression:

0.2.1 4(c).

The coefficients are almost the same except for the small change in decimals but for the one with learning rate 0.1, there is comparatively more change observed. After computing closed form solution I have observed that both extremely high and low rates are yielding coefficients that are slightly different than closed forms. As the learning rate increases, the time taken for convergence is small.

0.2.2 5(b).

I have obtained almost same coefficients for both the SGD and closed-form solution, except for some minor changes in the least significant decimals. ### 5(c). The runtime for SGD is 0.1300 seconds and for closed solution it is 0.0002 seconds and hence it can be concluded that SGD takes more time while compared to closed form solution.

0.2.3 6.

With the proposed learning rate the algorithm is taking more time to converge but the coefficients values are almost the same as previous.

0.2.4 9.

from the graph, RMS train and error vs n polynomial, it can be observed that, degree 3 fits the best. Because, at degree 3, we can observe that RMS test error is minimum and later it starts increasing. Overfitting can be observed in the above graph because, the training error after degree 3 decreases and remains constant, but the RMS test error increases. This shows the overfitting of the model to train data.