# Studying Permutation-based Combinatorial Optimization Problems and Proposing Efficient Estimation of Distribution Algorithms

### Josu Ceberio

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### Personal Information

#### Josu Ceberio

- Computer Science, University of the Basque Country (UPV/EHU).
- Master in Computational Engineering and Intelligent Systems, University of the Basque Country (UPV/EHU).

- PhD Student at the Intelligent Systems Group (ISG), University of the Basque Country (UPV/EHU)
- ► Supervised by Alexander Mendiburu and Jose A. Lozano.
- ▶ Predoctoral grant of the Basque Government. 3<sup>rd</sup> year.

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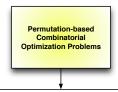
- PhD Student at the Intelligent Systems Group (ISG), University of the Basque Country (UPV/EHU)
- ► Supervised by Alexander Mendiburu and Jose A. Lozano.
- ightharpoonup Predoctoral grant of the Basque Government.  $3^{rd}$  year.
- ► ISG research interests: Bioinformatics, High Performance Computing, Machine Learning and **Optimization**.

"Propose state-of-the-art solutions to permutation problems by means of estimation of distribution algorithms"

### The foundations

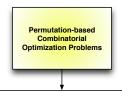
Permutation-based Combinatorial Optimization Problems

### The foundations



Problems whose solutions are naturally codified as permutations.

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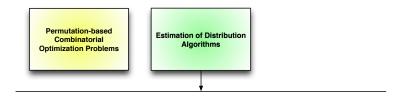


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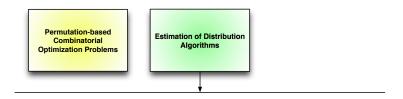
Permutation Flowshop Scheduling Problem

### The foundations



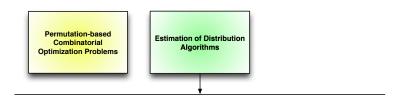
▶ Existing EDAs-based approaches do not propose efficient solutions.

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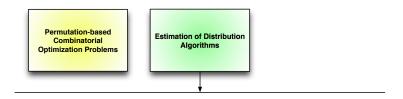
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- Designed for integer or real encoding problems.

#### The foundations



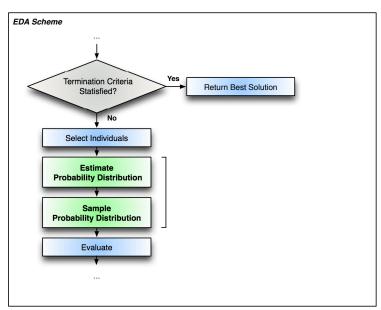
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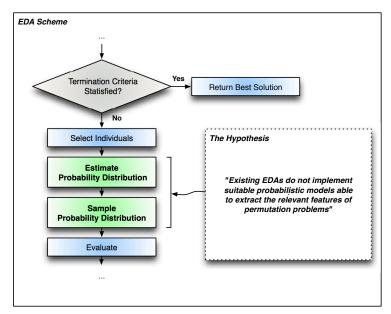


- ▶ Existing EDAs-based approaches do not propose efficient solutions.
- Designed for integer or real encoding problems.
  - ▶ An infinite non-numerable subset of  $\mathbb{R}^n$ .

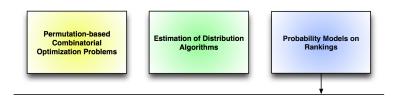
### The Hypothesis



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#### The contribution



▶ Estimate an explicit probability distribution on  $S_n$ .

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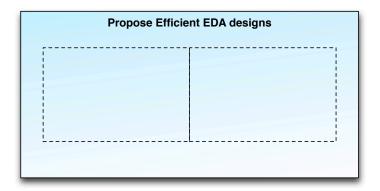
Permutation-based
Combinatorial
Optimization Problems

Estimation of Distribution
Algorithms

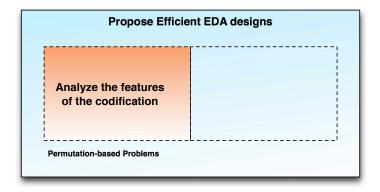
Probability Models on
Rankings

- ▶ Estimate an explicit probability distribution on  $S_n$ .
- ► Thurstone order statistics → Plackett-Luce
- ► Induced by paired comparisons → Bradley-Terry
- ▶ Distance-based ranking models. → Mallows
- ▶ Multistage ranking models. → Generalized Mallows

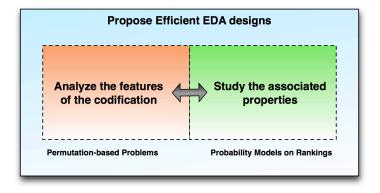
The Challenge



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1. Review existing EDAs for Permutation-based Problems

#### Publications:

J. Ceberio, E. Irurozki, A. Mendiburu, J.A. Lozano. A Review on Estimation of Distribution Algorithms in Permutation-based Combinatorial Optimization Problems. Progress in Artificial Intelligence. April 2012, Volume 1, Issue 1, pp 103-117. Cited by 10 papers.

1. Review existing EDAs for Permutation-based Problems

 Study probability models on rankings and introduce a model in EDAs

#### Publications:

J. Ceberio, A. Mendiburu, J.A. Lozano. Introducing The Mallows Model on Estimation of Distribution Algorithms. In Proceedings of 2011 International Conference on Neural Information Processing (ICONIP-2011), Shanghai, China, November 2011.

1. Review existing EDAs for Permutation-based Problems

2. Study probability models on rankings and introduce a model in FDAs

 Propose an EDA based approach that outperforms the state-of-theart results of a problem

#### Publications:

J. Ceberio, E. Irurozki, A. Mendiburu, J.A. Lozano. A Distance-based Ranking Model Estimation of Distribution Algorithm for the Flowshop Scheduling Problem.

IEEE Transactions on Evolutionary Computation. 2013. In Press.

1. Review existing EDAs for Permutation-based Problems

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4. Study permutation problems and determine the relevant features for applying EDAs.

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- ▶ J. Ceberio, A. Mendiburu, J.A. Lozano. The Plackett-Luce Ranking Model on Permutation-based Optimization Problems. 2013 IEEE Congress on Evolutionary Computation (CEC-2013), Cancun, Mexico, June 2013.
- ▶ J. Ceberio, A. Mendiburu, J.A. Lozano. Understanding Instance Complexity in the Linear Ordering Problem. The International Conference on Intelligent Data Engineering and Automated Learning (IDEAL-2013), Hefei, China, October 2013.

1. Review existing EDAs for Permutation-based Problems 2. Study probability models on rankings and introduce a model in **EDAs** 3. Propose an EDA based approach that outperforms the state-of-theart results of a problem 4. Study permutation problems and determine the relevant features for applying EDAs.

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### Ongoing Work:

- Structural analysis of the Linear Ordering Problem.
- Incorporate information about the problem in the search process.

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