Solving Data-flow Problems in Syntax Trees

Sebastian Graf September 9, 2017

Karlsruhe Institute of Technology

Introduction

- My master's thesis¹: Call Arity vs. Demand Analysis
 - Result: Usage Analysis generalising Call Arity
 - Precision of Call Arity without co-call graphs
- Requirements led to complex analysis order
- Specification of data-flow problem decoupled from its solution

https://pp.ipd.kit.edu/uploads/publikationen/graf17masterarbeit.pdf

Strictness Analysis

- Provides lower bounds on evaluation cardinality
- Is this variable evaluated at least once?
 - *Strictness*: Str $:= S \mid L$
 - Strict (Yes!)
 - Lazy (Not sure)
- Enables call-by-value, unboxing

```
main = do
let x = \ldots -S
let y = \ldots -S
let z = \ldots -L
print (x + if odd y then y else z)
```

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  let !y = ... -- S
  let z = ... -- L
  print (x + if odd y then y else z)
```

GHC's Demand Analyser

- Performs strictness analysis (among other things)
- Fuels Worker/Wrapper transformation
- Backward analysis
 - Which strictness does an expression place on its free variables?
 - Which strictness does a function place on its arguments?
- *Strictness type*: $StrType = \langle FVs \rightarrow Str, Str^* \rangle$

Strictness Signatures

- Looks at the right-hand side of const before the let body!
- Unleashes strictness type of const's RHS at call sites

```
let const a b = a -- const :: \langle [], [S, L] \rangle in const y \qquad \qquad -- S \qquad \qquad \text{(error "G") } -- L
```

- Whole expression is strict in z
- Only digests f for manifest arity 1, can't look under lambda
- f is called with 2 arguments

```
let f x = -- f :: \langle [z \mapsto L], [S] \rangle

if odd x

then \y \to y*z

else \y \to y+z

in f 1 2
```

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```
let f x = -- f :: \langle [z \mapsto L], [S] \rangle

if odd x

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in seq (f 1) 42
```

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```

- Solution: Analyse RHS when incoming arity is known
- Formally: Finite approximation of strictness transformer
 - $\bullet \;\; \mathsf{StrTrans} = \mathbb{N} \to \mathsf{StrType}$
- Exploit laziness to memoise results?

```
let f x = -- f<sub>1</sub> :: \langle [z \mapsto L], [S] \rangle

if odd x

then y \rightarrow y*z

else y \rightarrow y+z

in f 1 2
```

- Solution: Analyse RHS when incoming arity is known
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 - $\bullet \;\; \mathsf{StrTrans} = \mathbb{N} \to \mathsf{StrType}$
- Exploit laziness to memoise results?

```
let f x = -- f<sub>2</sub> :: \langle [z \mapsto S], [S, S] \rangle

if odd x

then y \rightarrow y*z

else y \rightarrow y+z

in f 1 2
```

Recursion

- Exploit laziness to memoise approximations?
- X Recursion leads to termination problems
- Rediscovered fixed-point iteration, detached from the syntax tree
- Leads to data-flow framework, solved by worklist algorithm

```
let fac n =
    if n == 0
        then 1
        else n * fac (n-1)
in fac 12
```

- Allocate nodes to break recursion
 - One top-level node
 - One node per pair of (let binding, incoming arity)
- Initialise worklist to top-level node
- ullet Initialise nodes with ot

```
let f 0 = const 0

f 1 = id

f n = f (n 'mod' 2)

in f x y
```

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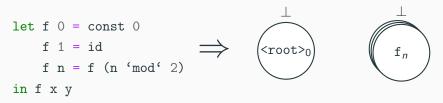
in f x y

f_n
```

- Allocate nodes to break recursion
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Worklist: {<root>0}

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Worklist: {<root>0}

```
let f 0 = const 0

f 1 = id

f n = f (n 'mod' 2)

in f x y
```

Worklist: $\{<root>_0\}$

```
let f 0 = const 0

f 1 = id

f n = f (n 'mod' 2)

in f x y
```

```
let f 0 = const 0

f 1 = id

f n = f (n 'mod' 2)

in f x y
```

```
let f = const 0
f = id
f = f (n 'mod' 2)
in f = x y
```

```
let f 0 = const 0

f 1 = id

f n = f (n 'mod' 2)

in f x y

\downarrow \qquad \qquad \downarrow = \langle [], [S, S] \rangle
```

```
let f 0 = const 0

f 1 = id

f n = f (n 'mod' 2)

in f x y

([],[S,L])
```

Worklist: $\{f_2, < root >_0\}$

Worklist: $\{f_2\}$

Worklist: $\{f_2\}$

```
 \begin{array}{c} \langle [x \mapsto S, y \mapsto L], [] \rangle & \langle [], [S, L] \rangle \\ \text{let f 0 = const 0} \\ \text{f 1 = id} \\ \text{f n = f (n 'mod' 2)} \end{array} \\ \text{in f x y}
```

Implementation

- Hide iteration strategy behind TransferFunction monad
- Data-flow nodes k, denoting lattice v
- Single 'impure' primitive depend0n

```
data TransferFunction k v a
instance Monad (TransferFunction k v)

dependOn
    :: Ord k
    => k
```

-> TransferFunction k v (Maybe v)

Implementation

 DataFlowFramework assigns TransferFunction and ChangeDetector to nodes

Implementation

- runFramework solves data-flow problems
- Specification as DataFlowFramework
- Implements iteration strategy
 - Can use worklist algorithm, starting from a specified root set

runFramework

- :: Ord k
- => DataFlowFramework k v
- -> Set k
- -> Map k v

Applied to Strictness Analysis

- Denote expressions by their strictness transformer
- Model points of strictness transformer separately
- Instantiate as
 DataFlowFramework (ExprNode, Arity) StrType
- ExprNode: Totally ordered, allocated as needed
 - Dictates priority in worklist
 - Performance depends on suitable priorities

Comparison to hoopl

- hoop1 (Ramsey et al. 2010) works on CFGs
 - Our data-flow graph is much less restrictive
 - Edges implicit in DSL
- Designed for imperative languages
- 'Operational' rather than 'denotational'
 - Analysis along control-flow rather than data-flow
- Makes (join-semi)lattice explicit
 - TODO
- Also includes a solution for transformations

Discussion

- ✓ Decouple analysis logic from iteration logic by a graph-based approach
- X Coupling not as painful as it would be in imperative programs
- ✓ Still obscures intent, even obstructs ideas
- √ 'Hacks' such as caching of analysis results as in Peyton Jones et al. (2006, §9.2) between iterations for free
- Unclear how performance is affected
- X Can only shine if shared concerns are actually extracted from a number of analyses

Conclusion

- Pitched an interesting idea that came out of my thesis
- Separate specification of the data-flow problem from computing its solution
- Graph-based abstraction, single solver
- Future Work:
 - 1. Monotone maps with partially-ordered keys²
 - 2. Polish API, make a package
 - 3. Testdrive and measure it in GHC

²https://github.com/sgraf812/pomaps/

Bibliography



Ramsey, Norman, João Dias, and Simon Peyton Jones (2010). "Hoopl: A Modular, Reusable Library for Dataflow Analysis and Transformation". In: *Proceedings of the Third ACM Haskell Symposium on Haskell*. Haskell '10. Baltimore, Maryland, USA: ACM, pp. 121–134. ISBN: 978-1-4503-0252-4. DOI: 10.1145/1863523.1863539. URL:

http://doi.acm.org/10.1145/1863523.1863539.

Backup

Example

```
let f 0 = const 0

f 1 = id

f n = f (n 'mod' 2)

in f x y

(\text{root})_0
```

Example

```
let f 0 = const 0

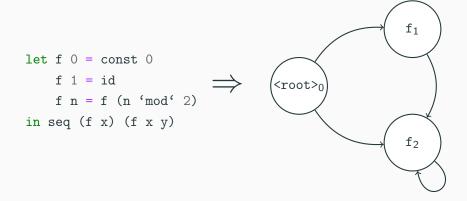
f 1 = id

f n = f (n 'mod' 2)

in seq (f x) (f x y)

(root>_0)
```

Example



Implementation: Behind the Curtain

• TransferFunction is a State monad around WorklistState

Threading annotated expressions

- Annotated CoreExprs are the reason why we do this!
- Thread it through all nodes:
 DataFlowFramework (ExprNode, Arity) (StrType, CoreExpr)
- Complicates change detection
 - Expressions follow AST structure
 - Possibly change when strictness type did not
 - ChangeDetector has to check set of changed dependencies
- Str ::= *S* | *L* not enough for annotating functions
 - Str ::= $S^n \mid L$ with arity $n \in \mathbb{N}$
 - 'f was called at least once, with at least n arguments'
- ... Or do it as the Demand Analyser does: Assume manifest arity for annotation
 - Be careful not to inline unsaturated wrappers!