GADTs Meet Their Match:

Pattern-Matching Warnings That Account for GADTs, Guards, and Laziness

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Guard Syntax

DNF Syntax

Clause Tree Syntax

$$\mathcal{T}[r] ::= \text{Rhs} \mid \text{Many } \overline{r}$$
 $t_G \in \text{Gdt} ::= \mathcal{T}[t_G] \mid \text{Guard } g \ t_G$
 $t_A \in \text{Ant} ::= \mathcal{T}[t_A] \mid \text{MayDiverge } t_A \mid \text{Inaccessible } t_A$

Checking Guard Trees

$$\mathcal{U}(\nabla, \mathsf{Rhs}) = \times \\ \mathcal{U}(\nabla, \mathsf{Many} \, \bar{t}) = \mathcal{U}(...\mathcal{U}(\mathcal{U}(\nabla, t_1), t_2)..., t_n) \\ \mathcal{U}(\nabla, \mathsf{Guard} \, (!x) \, t) = \mathcal{U}(\nabla \oplus (x \not\approx \bot), t) \\ \mathcal{U}(\nabla, \mathsf{Guard} \, (!x) \, t) = \mathcal{U}(\nabla \oplus (x \not\approx \bot), t) \\ \mathcal{U}(\nabla, \mathsf{Guard} \, (!x \, z \, p) \, t) = \mathcal{U}(\nabla \oplus (x \not\approx \bot), t) \\ \mathcal{U}(\nabla, \mathsf{Guard} \, (K \, \overline{a} \, \overline{\gamma} \, \overline{y} : \overline{\tau} \leftarrow x) \, t) = (\nabla \oplus (x \not\approx K) \oplus (x \not\approx \bot)) \vee \mathcal{U}(\nabla \oplus (K \, \overline{y} : \overline{\tau} \leftarrow x) \oplus \overline{\gamma}, gs) \\ \hline \mathcal{A}_{\Gamma}(\nabla, \mathsf{Guard} \, (K \, \overline{a} \, \overline{\gamma} \, \overline{y} : \overline{\tau} \leftarrow x) \, t) = (\nabla \oplus (x \not\approx K) \oplus (x \not\approx \bot)) \vee \mathcal{U}(\nabla \oplus (K \, \overline{y} : \overline{\tau} \leftarrow x) \oplus \overline{\gamma}, gs) \\ \hline \mathcal{A}_{\Gamma}(\nabla, \mathsf{Rhs}) = \begin{cases} \mathsf{Inaccessible} \, \mathsf{Rhs}, & \mathcal{V}(\Gamma, \nabla) \Rightarrow \varnothing \\ \mathsf{Rhs}, & \mathsf{otherwise} \end{cases} \\ \mathcal{A}_{\Gamma}(\nabla, \mathsf{Many} \, \overline{t}) = \mathsf{Many} \, (\mathcal{A}_{\Gamma}(\nabla_0', t_1), \dots, \mathcal{A}_{\Gamma}(\nabla_{n-1}', t_n)) \, \mathsf{where} \, \begin{cases} \nabla_0' = \nabla \\ \nabla_0' = \nabla \\ \nabla_{n+1}' = \mathcal{U}(\nabla_n', t_{n+1}) \end{pmatrix} \\ \mathcal{A}_{\Gamma}(\nabla, \mathsf{Guard} \, (!x) \, t) = \mathcal{D}(\nabla, \mathcal{A}_{\Gamma}(\nabla \oplus (x \not\approx \bot), t)) \\ \mathcal{A}_{\Gamma}(\nabla, \mathsf{Guard} \, (!x \, z = e) \, t) = \mathcal{A}_{\Gamma}(\nabla \oplus (x \not\approx e), t) \\ \mathcal{A}_{\Gamma}(\nabla, \mathsf{Guard} \, (K \, \overline{a} \, \overline{\gamma} \, \overline{y} : \overline{\tau} \leftarrow x) \, t) = \mathcal{D}(\nabla, \mathcal{A}_{\Gamma}(\nabla \oplus (K \, \overline{y} : \overline{\tau} \leftarrow x) \oplus \overline{\gamma}, t)) \end{cases}$$

$$\mathcal{D}(\nabla, \mathsf{Ant}) = \mathsf{Ant}$$

$$\mathcal{D}(\nabla, t) = \begin{cases} t, & \mathcal{V}(\Gamma, \nabla \oplus (x \not\approx \bot)) \Rightarrow \varnothing \\ \mathsf{MayDiverge} \, t & \mathsf{otherwise} \end{cases}$$

Putting it all together

- (0) Input: Context with match vars Γ and desugared Gdt t
- (1) Report *n* value vectors of $\mathcal{V}(\Gamma, \mathcal{U}(\checkmark, t)) \Rightarrow V$ as uncovered
- (2) Report the collected redundant and not-redundant-but-inaccessible clauses in $\mathcal{A}_{\Gamma}(\sqrt{t})$ (TODO: Write a function that collects the RHSs, maybe add numbers to Rhs to distinguish).

$$\boxed{\mathcal{V}(\Gamma, \nabla) \Rightarrow \mathcal{P}(V)}$$

This is provideEvidence

$$\frac{\mathcal{V}(\Gamma, \times) \Rightarrow \varnothing}{\mathcal{V}(\Gamma, \nabla_1) \Rightarrow V_1 \quad \mathcal{V}(\Gamma, \nabla_2) \Rightarrow V_2} \quad \frac{\mathcal{V}(\Gamma, \nabla_1) \Rightarrow V_1 \quad \mathcal{V}(\Gamma, \nabla_2) \Rightarrow V_2}{\mathcal{V}(\Gamma, \nabla_1 \vee \nabla_2) \Rightarrow V_1 \cup V_2} \quad \frac{\mathcal{V}(\Gamma, \Delta) \Rightarrow \{v \mid \mathcal{V}(\Gamma, \Delta) \Rightarrow v\}}{\mathcal{V}(\Gamma, \Delta) \Rightarrow \{v \mid \mathcal{V}(\Gamma, \Delta) \Rightarrow v\}}$$

$$\mathcal{V}(\Gamma, \Delta) \Rightarrow V$$

$$\frac{\mathcal{V}(\Gamma, \Delta) \Rightarrow V}{\mathcal{V}(\emptyset, \Delta) \Rightarrow ()} \qquad \frac{\mathcal{V}((x_1 : \sigma_1, ..., x_n : \sigma_n, \Gamma), (K (x_1 : \sigma_1) ... (x_n : \sigma_n) \leftarrow y, \Delta)) \Rightarrow (a_1, ..., a_n, v_2, ..., v_m)}{\mathcal{V}(y : \tau, \Gamma, \Delta) \Rightarrow (K x_1 ... x_n, v_2, ..., v_m)}$$

no more fuel

$$\overline{V(x_1:\tau_1,...,x_n:\tau_n,\Delta) \Rightarrow (_,...,_)} \\
\overline{\mathcal{T}(\Delta)}$$

Test a Δ for satisfiability

This figure is completely out of date, don't waste your time Test if Oracle state Delta is unsatisfiable

$$\frac{ \biguplus_{\text{SAT}} \Gamma \vdash \Delta}{ \biguplus_{\text{SAT}} \Gamma \vdash f vs \Gamma \vdash \Delta}$$

$$\frac{\biguplus_{\text{SAT}} \Gamma \vdash \Delta}{ \biguplus_{\text{SAT}} \Gamma \vdash \Delta}$$

Test a list of SAT roots for inhabitants

$$\begin{array}{c|c}
 & \swarrow_{\text{SAT}} \Gamma \vdash \overline{x} \triangleright \Delta \\
 & \swarrow_{\text{SAT}} \Gamma \vdash x_i \triangleright \Delta \\
 & \swarrow_{\text{SAT}} \Gamma \vdash \overline{x} \triangleright \Delta
\end{array}$$

Test a single SAT root for inhabitants

Add a single equality to Δ

$$\nvdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta \delta$$

Term stuff: Bottom, negative info, positive info + generativity, positive info + univalence

$$\frac{x \not\approx sth \in \Delta}{\not\vdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx \bot} \qquad \frac{x \approx K \ \overline{y} \in \Delta}{\not\vdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx \bot}$$

$$\frac{x \not\approx K \in \Delta}{\not\vdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K \ \overline{y}} \qquad \frac{x \approx K_i \ \overline{y} \in \Delta \quad i \neq j \quad K_i \text{ and } K_j \text{ generative}}{\not\vdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K \ \overline{y}}$$

$$\frac{x \approx K \ \overline{\tau} \ \overline{y} \in \Delta \quad \not\vdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K_j \ \overline{z}}{\not\vdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K \ \overline{\sigma} \ \overline{z}}$$

$$\frac{x \approx K \ \overline{\tau} \ \overline{y} \in \Delta \quad \not\vdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta y_i \approx z_i}{\not\vdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K \ \overline{\sigma} \ \overline{z}}$$

Type stuff: Hand over to unspecified type oracle

 au_1 and au_2 incompatible to Givens in Δ according to type oracle

$$\nvdash_{SAT} \Gamma \vdash \oplus \Delta \tau_1 \sim \tau_2$$

Mixed: Instantiate K and see if that leads to a contradiction TODO: Proper instantiation

$$\frac{\cancel{\nvdash}_{SAT} \ \Gamma \vdash y \triangleright \Delta \cup y \not\approx \bot}{\cancel{\nvdash}_{SAT} \ \Gamma \vdash \oplus \Delta x \approx K \ \overline{y}}$$