

GADTs Meet Their Match:

Pattern-Matching Warnings That Account for GADTs, Guards, and Laziness

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Guard Syntax

| | | | | | |
|--------------------|------|--------------|--|-------|---|
| $K \in$ | Con | $\gamma \in$ | TyCt | $::=$ | $\tau_1 \sim \tau_2 \mid \dots$ |
| $x, y, a, b \in$ | Var | $g \in$ | Grd | $::=$ | $\text{let } x : \tau = e$ |
| $\tau, \sigma \in$ | Type | | | | $\mid K \bar{a} \bar{\gamma} \bar{y} : \bar{\tau} \leftarrow x$ |
| $e \in$ | Expr | $::=$ | $x : \tau$ | | $\mid !x$ |
| | | | $\mid K \bar{a} \bar{\gamma} \bar{e} : \bar{\tau}$ | | |
| | | | $\mid \dots$ | | |

DNF Syntax

| | | | |
|----------|-------|---|----------|
| Γ | $::=$ | $\emptyset \mid \Gamma, x : \tau \mid \Gamma, a$ | Context |
| δ | $::=$ | $\gamma \mid K \bar{x} : \bar{\tau} \leftarrow \bar{y} \mid x \neq K \mid x \approx \perp \mid x \neq \perp \mid x \approx e$ | Literals |
| Δ | $::=$ | $\checkmark \mid \Delta \wedge \delta$ | Clause |
| ∇ | $::=$ | $\times \mid \Delta \mid \nabla_1 \vee \nabla_2$ | Formula |
| | | $\times \oplus \delta = \times$ | |
| | | $\Delta \oplus \delta = \Delta \wedge \delta$ | |
| | | $\nabla_1 \vee \nabla_2 \oplus \delta = (\nabla_1 \oplus \delta) \vee (\nabla_2 \oplus \delta)$ | |

Clause Tree Syntax

| | | |
|----------------------|-------|--|
| $\mathcal{T}[r]$ | $::=$ | Rhs \mid Many \bar{r} |
| $t_G \in \text{Gdt}$ | $::=$ | $\mathcal{T}[t_G] \mid$ Guard $g \ t_G$ |
| $t_A \in \text{Ant}$ | $::=$ | $\mathcal{T}[t_A] \mid$ MayDiverge $t_A \mid$ Inaccessible t_A |

Checking Guard Trees

$$\mathcal{U}(\nabla, \text{Gdt}) = \nabla$$

| | | |
|---|-----|--|
| $\mathcal{U}(\nabla, \text{Rhs})$ | $=$ | \times |
| $\mathcal{U}(\nabla, \text{Many } \bar{t})$ | $=$ | $\mathcal{U}(\dots \mathcal{U}(\mathcal{U}(\nabla, t_1), t_2) \dots, t_n)$ |
| $\mathcal{U}(\nabla, \text{Guard } (!x) \ t)$ | $=$ | $\mathcal{U}(\nabla \oplus (x \neq \perp), t)$ |
| $\mathcal{U}(\nabla, \text{Guard } (\text{let } x = e) \ t)$ | $=$ | $\mathcal{U}(\nabla \oplus (x \approx e), t)$ |
| $\mathcal{U}(\nabla, \text{Guard } (K \bar{a} \bar{\gamma} \bar{y} : \bar{\tau} \leftarrow x) \ t)$ | $=$ | $(\nabla \oplus (x \neq K) \oplus (x \neq \perp)) \cup \mathcal{U}(\nabla \oplus (K \bar{y} : \bar{\tau} \leftarrow x) \oplus \bar{\gamma}, gs)$ |

$$\mathcal{A}_\Gamma(\nabla, \text{Gdt}) = \text{Ant}$$

| | | |
|--|-----|--|
| $\mathcal{A}_\Gamma(\nabla, \text{Rhs})$ | $=$ | $\begin{cases} \text{Inaccessible Rhs,} & \mathcal{V}(\Gamma, \nabla) = \emptyset \\ \text{Rhs,} & \text{otherwise} \end{cases}$ |
| $\mathcal{A}_\Gamma(\nabla, \text{Many } \bar{t})$ | $=$ | Many $(\mathcal{A}_\Gamma(\nabla'_0, t_1), \dots, \mathcal{A}_\Gamma(\nabla'_{n-1}, t_n))$ where $\begin{cases} \nabla'_0 & = \nabla \\ \nabla'_{n+1} & = \mathcal{U}(\nabla'_n, t_{n+1}) \end{cases}$ |
| $\mathcal{A}_\Gamma(\nabla, \text{Guard } (!x) \ t)$ | $=$ | $\mathcal{D}(\nabla, \mathcal{A}_\Gamma(\nabla \oplus (x \neq \perp), t))$ |
| $\mathcal{A}_\Gamma(\nabla, \text{Guard } (\text{let } x = e) \ t)$ | $=$ | $\mathcal{A}_\Gamma(\nabla \oplus (x \approx e), t)$ |
| $\mathcal{A}_\Gamma(\nabla, \text{Guard } (K \bar{a} \bar{\gamma} \bar{y} : \bar{\tau} \leftarrow x) \ t)$ | $=$ | $\mathcal{D}(\nabla, \mathcal{A}_\Gamma(\nabla \oplus (K \bar{y} : \bar{\tau} \leftarrow x) \oplus \bar{\gamma}, t))$ |

$$\mathcal{D}(\nabla, \text{Ant}) = \text{Ant}$$

$$\mathcal{D}(\nabla, t) = \begin{cases} t, & \mathcal{V}(\Gamma, \nabla \oplus (x \approx \perp)) = \emptyset \\ \text{MayDiverge } t & \text{otherwise} \end{cases}$$

$$\mathcal{V}(\Gamma, \nabla) = \text{values}$$

TBD: Oracle implementation. This is provideEvidence

Putting it all together

- (0) Input: Context with match vars Γ and desugared Gdt t
- (1) Report n value vectors of $\mathcal{V}(\Gamma, \mathcal{U}(\checkmark, t))$ as uncovered
- (2) Report the collected redundant and not-redundant-but-inaccessible clauses in $\mathcal{A}_\Gamma(\checkmark, t)$ (TODO: Write a function that collects the RHSs, maybe add numbers to Rhs to distinguish).

This figure is completely out of date, don't waste your time

Test if Oracle state Delta is unsatisfiable

$$\frac{\boxed{\not\vdash_{\text{SAT}} \Gamma \vdash \Delta} \quad \not\vdash_{\text{SAT}} \Gamma \vdash f\text{us}\Gamma \triangleright \Delta}{\not\vdash_{\text{SAT}} \Gamma \vdash \Delta}$$

Test a list of SAT roots for inhabitants

$$\frac{\boxed{\not\vdash_{\text{SAT}} \Gamma \vdash \bar{x} \triangleright \Delta} \quad \not\vdash_{\text{SAT}} \Gamma \vdash x_i \triangleright \Delta}{\not\vdash_{\text{SAT}} \Gamma \vdash \bar{x} \triangleright \Delta}$$

Test a single SAT root for inhabitants

$$\frac{\boxed{\not\vdash_{\text{SAT}} \Gamma \vdash x \triangleright \Delta} \quad \not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta x \approx \perp \quad \{\bar{K}\} \text{ COMPLETE set} \quad \overline{\forall \bar{y} : \bar{\tau}. \not\vdash_{\text{SAT}} \Gamma, \bar{y} : \bar{\tau} \vdash \oplus \Delta x \approx K \bar{y}}}{\not\vdash_{\text{SAT}} \Gamma \vdash x \triangleright \Delta}$$

Add a single equality to Δ

$$\boxed{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta \delta}$$

Term stuff: Bottom, negative info, positive info + generativity, positive info + univalence

$$\frac{x \not\approx sth \in \Delta}{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta x \approx \perp} \quad \frac{x \approx K \bar{y} \in \Delta}{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta x \approx \perp}$$

$$\frac{x \not\approx K \in \Delta}{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta x \approx K \bar{y}} \quad \frac{x \approx K_i \bar{y} \in \Delta \quad i \neq j \quad K_i \text{ and } K_j \text{ generative}}{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta x \approx K_j \bar{z}}$$

$$\frac{x \approx K \bar{\tau} \bar{y} \in \Delta \quad \not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta \tau_i \sim \sigma_i}{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta x \approx K \bar{\sigma} \bar{z}} \quad \frac{x \approx K \bar{\tau} \bar{y} \in \Delta \quad \not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta y_i \approx z_i}{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta x \approx K \bar{\sigma} \bar{z}}$$

Type stuff: Hand over to unspecified type oracle

$$\frac{\tau_1 \text{ and } \tau_2 \text{ incompatible to Givens in } \Delta \text{ according to type oracle}}{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta \tau_1 \sim \tau_2}$$

Mixed: Instantiate K and see if that leads to a contradiction TODO: Proper instantiation

$$\frac{\overline{\not\vdash_{\text{SAT}} \Gamma \vdash y \triangleright \Delta \cup y \not\approx \perp}}{\not\vdash_{\text{SAT}} \Gamma \vdash \oplus \Delta x \approx K \bar{y}}$$