GADTs Meet Their Match:

Pattern-Matching Warnings That Account for GADTs, Guards, and Laziness

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Guard Syntax

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K \in \text{Con} \\ x, y, a, b \in \text{Var} \\ \tau, \sigma \in \text{Type} \\ e \in \text{Expr} ::= x : \tau \\ \mid K \overline{a} \overline{\gamma} \overline{e} : \overline{\tau}  n \in \mathbb{N} \\ \gamma \in \text{TyCt} ::= \tau_1 \sim \tau_2 \mid \dots \\ g \in \text{Grd} ::= \text{let } x : \tau = e \\ \mid K \overline{a} \overline{\gamma} \overline{y} : \overline{\tau} \leftarrow x
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Constraint Formula Syntax

$$\begin{array}{lll} \Gamma & ::= & \varnothing \mid \Gamma, x : \tau \mid \Gamma, a & \text{Context} \\ \delta & ::= & \checkmark \mid \times \mid K \ \overline{a} \ \overline{\gamma} \ \overline{y} : \overline{\tau} \leftarrow x \mid x \not\approx K \mid x \approx \bot \mid x \not\approx \bot \mid x \approx e \end{array} \\ \begin{array}{ll} \text{Constraint Literals} \\ \Delta & ::= & \delta \mid \Delta \land \Delta \mid \Delta \lor \Delta \end{array}$$

Clause Tree Syntax

 $t_G, u_G \in \text{Gdt}$::= Rhs | $t_G; u_G$ | Guard $g t_G$ $t_A, u_A \in \text{Ant}$::= AccessibleRhs | InaccessibleRhs | $t_A; u_A$ | MayDiverge t_A

Checking Guard Trees

Putting it all together

- (0) Input: Context with match vars Γ and desugared Gdt t
- (1) Report *n* value vectors of $\mathcal{V}(\Gamma, \mathcal{U}(\checkmark, t)) \Rightarrow V$ as uncovered
- (2) Report the collected redundant and not-redundant-but-inaccessible clauses in $\mathcal{A}_{\Gamma}(\sqrt{t})$ (TODO: Write a function that collects the RHSs, maybe add numbers to Rhs to distinguish).

$$\boxed{\mathcal{V}(\Gamma, \Delta) \Rightarrow \mathcal{P}(V)}$$

This is provideEvidence

$$\frac{\mathcal{V}(\Gamma, \times) \Rightarrow \varnothing}{\mathcal{V}(\Gamma, \Delta_1) \Rightarrow V_1 \quad \mathcal{V}(\Gamma, \Delta_2) \Rightarrow V_2} \quad \frac{\mathcal{V}(\Gamma, \Delta_1) \Rightarrow V_1 \quad \mathcal{V}(\Gamma, \Delta_2) \Rightarrow V_2}{\mathcal{V}(\Gamma, \Delta_1 \vee \Delta_2) \Rightarrow V_1 \cup V_2} \quad \frac{\mathcal{V}(\Gamma, \Delta) \Rightarrow \{v \mid \mathcal{V}(\Gamma, \Delta) \Rightarrow v\}}{\mathcal{V}(\Gamma, \Delta) \Rightarrow \{v \mid \mathcal{V}(\Gamma, \Delta) \Rightarrow v\}}$$

$$\mathcal{V}(\Gamma, \Delta) \Rightarrow V$$

$$\frac{\mathcal{V}(\Gamma, \Delta) \Rightarrow V}{\mathcal{V}(\emptyset, \Delta) \Rightarrow ()} \qquad \frac{\mathcal{V}((x_1 : \sigma_1, ..., x_n : \sigma_n, \Gamma), (K (x_1 : \sigma_1) ... (x_n : \sigma_n) \leftarrow y, \Delta)) \Rightarrow (a_1, ..., a_n, v_2, ..., v_m)}{\mathcal{V}(y : \tau, \Gamma, \Delta) \Rightarrow (K x_1 ... x_n, v_2, ..., v_m)}$$

no more fuel

$$\overline{V(x_1:\tau_1,...,x_n:\tau_n,\Delta) \Rightarrow (_,...,_)} \\
\overline{\mathcal{T}(\Delta)}$$

Test a Δ for satisfiability

This figure is completely out of date, don't waste your time Test if Oracle state Delta is unsatisfiable

$$\frac{ \cancel{\vdash}_{SAT} \Gamma \vdash \Delta}{ \cancel{\vdash}_{SAT} \Gamma \vdash fvs\Gamma \triangleright \Delta}$$

$$\frac{\cancel{\vdash}_{SAT} \Gamma \vdash \Delta}{ \cancel{\vdash}_{SAT} \Gamma \vdash \Delta}$$

Test a list of SAT roots for inhabitants

$$| \mathcal{V}_{SAT} \Gamma \vdash \overline{x} \triangleright \Delta |$$

$$\mathcal{V}_{SAT} \Gamma \vdash x_i \triangleright \Delta |$$

$$\mathcal{V}_{SAT} \Gamma \vdash \overline{x} \triangleright \Delta |$$

Test a single SAT root for inhabitants

Add a single equality to Δ

$$\nvdash_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta \delta$$

Term stuff: Bottom, negative info, positive info + generativity, positive info + univalence

$$\frac{x \not\approx sth \in \Delta}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta x \approx \bot} \qquad \frac{x \approx K \ \overline{y} \in \Delta}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta x \approx \bot}$$

$$\frac{x \not\approx K \in \Delta}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta x \approx K \ \overline{y}} \qquad \frac{x \approx K_i \ \overline{y} \in \Delta \quad i \neq j \quad K_i \text{ and } K_j \text{ generative}}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta x \approx K \ \overline{y}}$$

$$\frac{x \approx K \ \overline{\tau} \ \overline{y} \in \Delta \quad \bigvee_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta x \approx K_j \ \overline{z}}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta x \approx K \ \overline{\sigma} \ \overline{z}} \qquad \frac{x \approx K \ \overline{\tau} \ \overline{y} \in \Delta \quad \bigvee_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta y_i \approx z_i}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \wedge \Delta x \approx K \ \overline{\sigma} \ \overline{z}}$$

Type stuff: Hand over to unspecified type oracle

 τ_1 and τ_2 incompatible to Givens in Δ according to type oracle

$$\not\vdash_{SAT} \Gamma \vdash \wedge \Delta \tau_1 \sim \tau_2$$

Mixed: Instantiate K and see if that leads to a contradiction TODO: Proper instantiation

$$\frac{\cancel{\nvdash}_{SAT} \ \Gamma \vdash y \triangleright \Delta \cup y \not\approx \bot}{\cancel{\nvdash}_{SAT} \ \Gamma \vdash \wedge \Delta x \approx K \ \overline{y}}$$