## **GADTs Meet Their Match:**

Pattern-Matching Warnings That Account for GADTs, Guards, and Laziness

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## $K \in \text{Con}$ $x, y, a, b \in \text{Var}$ $\tau, \sigma \in \text{Type}$

Pattern Syntax

$$e \in \operatorname{Expr} ::= x : \tau$$
 $\mid K \overline{a} \overline{\gamma} \overline{e} : \overline{\tau}$ 
 $\mid ...$ 
 $\gamma \in \operatorname{TyCt} ::= \tau_1 \sim \tau_2 \mid ...$ 
 $g \in \operatorname{Grd} ::= \operatorname{let} x : \tau = e;$ 

!x;

 $K \overline{a} \overline{y} \overline{y : \tau} \leftarrow x;$ 

## **Oracle Syntax**

$$\begin{array}{lll} \Gamma & ::= & \varnothing \mid \Gamma, x : \tau \mid \Gamma, a & \text{Context} \\ \Theta & ::= & \times \mid \Gamma \vdash \Delta \mid \Theta_1 \lor \Theta_2 & \text{"Deltas"} \\ \Delta & ::= & \checkmark \mid \Delta \land \delta & \text{Delta} \\ \delta & ::= & \gamma \mid x_1 \approx x_2 \mid x \approx K \ \overline{y} \mid x \not\approx K \mid x \approx \bot \mid x \not\approx \bot \mid x \approx e \end{array}$$

## **Adding Constraints**

## **Binding Free Variables**

#### Pattern-match Result

$$r ::= \langle \Theta_u, \Theta_d, \Theta_c \rangle$$

$$\begin{split} \langle \Theta_u, \Theta_d, \Theta_c \rangle \cup_U \Theta &= \langle \Theta_u \vee \Theta, \Theta_d, \Theta_c \rangle \\ \langle \Theta_u, \Theta_d, \Theta_c \rangle \cup_D \Theta &= \langle \Theta_u, \Theta_d \vee \Theta, \Theta_c \rangle \end{split}$$

### Pattern-match checking

#### **TODO LIST**

GADTs Meet Their Match: 1:3

# Pattern-match Result ClauseResult $c \in Coverage$ ∷= Redundant RhsInaccessible RhsReachable ClauseResult $:= \langle \overline{\Delta}, Coverage \rangle$ $= \langle \times, Redundant \rangle$ empty $\begin{array}{ccc} & & & & & \\ \hline r \cup_C \overline{\Delta} \\ \hline \langle \overline{\Delta_u}, \rangle & \cup_C & \overline{\Delta_c} & = & \langle \overline{\Delta_u}, \mathsf{Covered} \rangle \text{ if any } \Delta_c \text{ inhabited} \\ r & \cup_C & = & r \\ \hline \end{array}$ $r \cup_U \overline{\Delta}$ Pattern-match checking $pmc \overline{\Delta} \overline{Grd} = r$ $\operatorname{pmc} \overline{\Delta} \epsilon$ = empty $\cup_C \overline{\Delta}$ $= \operatorname{pmc} \overline{\Delta \oplus x : \tau \oplus x \approx e} \, \overline{g}$ $pmc \ \overline{\Delta} \ (let \ x : \tau = e; \ \overline{g})$ = pmc $\overline{\Delta \oplus x \not\approx \perp} \overline{g}$ $\mathsf{pmc} \; \overline{\Delta} \; (!x; \; \overline{g})$ $\operatorname{pmc} \overline{\Delta} \; (K \; \overline{a} \; \overline{\gamma} \; \overline{x : \tau} \leftarrow y; \; \overline{g}) \;\; = \;\; \operatorname{pmc} \overline{\Delta \; \oplus \; \overline{x} \; \oplus \; \overline{x} : \tau} \; \oplus \; x \approx K \; \overline{a} \; \overline{\gamma} \; \overline{x : \tau} \; \overline{g}$ $\cup_D \overline{\Delta \oplus x \approx \bot}$ $\cup_{U} \overline{\Delta} \oplus x \not\approx K$

#### REFERENCES

Lennart Augustsson. 1985. Compiling pattern matching. In Proceedings of the 1985 Conference on Functional Programming and Computer Architecture.

Edwin Brady. 2013a. Idris, a general-purpose dependently typed programming language: Design and implementation. *Journal of Functional Programming* 23 (9 2013), 552–593. Issue 05. https://doi.org/10.1017/S095679681300018X

Edwin Brady. 2013b. Programming and Reasoning with Algebraic Effects and Dependent Types. In *Proceedings of the 18th ACM SIGPLAN International Conference on Functional Programming (ICFP '13)*. ACM, New York, NY, USA, 133–144. https://doi.org/10.1145/2500365.2500581

James Cheney and Ralf Hinze. 2003. First-class phantom types. Technical Report. Cornell University.

Koen Claessen, Moa Johansson, Dan Rosén, and Nicholas Smallbone. 2013. Automating Inductive Proofs Using Theory Exploration.. In *CADE (Lecture Notes in Computer Science)*, Maria Paola Bonacina (Ed.), Vol. 7898. Springer, 392–406.

Thierry Coquand. 1992. Pattern matching with dependent types. In *Proceedings of the Workshop on Types for Proofs and Programs*.

#### Test if Oracle state Delta is unsatisfiable

$$\frac{\not\vdash_{SAT} \Gamma \vdash \Delta}{\not\vdash_{SAT} \Gamma \vdash f vs\Gamma \triangleright \Delta}$$

$$\frac{\not\vdash_{SAT} \Gamma \vdash \Delta}{\not\vdash_{SAT} \Gamma \vdash \Delta}$$

#### Test a list of SAT roots for inhabitants

$$\begin{array}{c|c}
 & \swarrow_{\text{SAT}} \Gamma \vdash \overline{x} \triangleright \Delta \\
 & \swarrow_{\text{SAT}} \Gamma \vdash x_i \triangleright \Delta \\
 & \swarrow_{\text{SAT}} \Gamma \vdash \overline{x} \triangleright \Delta
\end{array}$$

#### Test a single SAT root for inhabitants

## Add a single equality to $\Delta$

$$\nvdash_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta \delta$$

Term stuff: Bottom, negative info, positive info + generativity, positive info + univalence

$$\frac{x \not\approx sth \in \Delta}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx \bot} \qquad \frac{x \approx K \, \overline{y} \in \Delta}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx \bot}$$

$$\frac{x \not\approx K \in \Delta}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K \, \overline{y}} \qquad \frac{x \approx K_i \, \overline{y} \in \Delta \quad i \neq j \quad K_i \text{ and } K_j \text{ generative}}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K \, \overline{y}}$$

$$\frac{x \approx K \, \overline{\tau} \, \overline{y} \in \Delta \quad \bigvee_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta \tau_i \sim \sigma_i}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K \, \overline{\sigma} \, \overline{z}} \qquad \frac{x \approx K \, \overline{\tau} \, \overline{y} \in \Delta \quad \bigvee_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta y_i \approx z_i}{\bigvee_{\mathsf{SAT}} \Gamma \vdash \oplus \Delta x \approx K \, \overline{\sigma} \, \overline{z}}$$

Type stuff: Hand over to unspecified type oracle

 $au_1$  and  $au_2$  incompatible to Givens in  $\Delta$  according to type oracle

$$\not\vdash_{SAT} \Gamma \vdash \oplus \Delta \tau_1 \sim \tau_2$$

Mixed: Instantiate K and see if that leads to a contradiction TODO: Proper instantiation

$$\frac{\cancel{\nvdash}_{SAT} \ \Gamma \vdash y \triangleright \Delta \cup y \not\approx \bot}{\cancel{\nvdash}_{SAT} \ \Gamma \vdash \oplus \Delta x \approx K \ \overline{y}}$$

Joshua Dunfield. 2007a. Refined Typechecking with Stardust. In *Proceedings of the 2007 Workshop on Programming Languages Meets Program Verification (PLPV '07)*. ACM, New York, NY, USA, 21–32. https://doi.org/10.1145/1292597.1292602

- Joshua Dunfield. 2007b. A Unified System of Type Refinements. Ph.D. Dissertation. Carnegie Mellon University. CMU-CS-07-129.
- Richard A. Eisenberg and Stephanie Weirich. 2012. Dependently Typed Programming with Singletons. In *Proceedings of the 2012 Haskell Symposium (Haskell '12)*. ACM, New York, NY, USA, 117–130. https://doi.org/10.1145/2364506.2364522
- M Erwig and SL Peyton Jones. 2000. Pattern guards and transformational patterns. In *Proceedings of the 2000 Haskell Symposium*. ACM.
- Jacques Garrigue and Jacques Le Normand. 2011. Adding GADTs to OCaml: the direct approach. In Workshop on ML.
- Jean-Yves Girard, Paul Taylor, and Yves Lafont. 1989. Proofs and Types. Cambridge University Press, New York, NY, USA.
- Georgios Karachalias, Tom Schrijvers, Dimitrios Vytiniotis, and Simon Peyton Jones. 2015. *GADTs meet their match (extended version)*. Technical Report. KU Leuven. http://people.cs.kuleuven.be/~george.karachalias/papers/gadtpm\_ext.pdf
- Neelakantan R. Krishnaswami. 2009. Focusing on Pattern Matching. In *Proceedings of the 36th Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '09)*. ACM, New York, NY, USA, 366–378. https://doi.org/10.1145/1480881.1480927
- Alain Laville. 1991. Comparison of Priority Rules in Pattern Matching and Term Rewriting. J. Symb. Comput. 11, 4 (May 1991), 321–347. https://doi.org/10.1016/S0747-7171(08)80109-5
- Fabrice Le Fessant and Luc Maranget. 2001. Optimizing Pattern-Matching. In *Proceedings of the 2001 International Conference on Functional Programming*.
- Luc Maranget. 1992. Compiling Lazy Pattern Matching. In Proceedings of the 1992 ACM Conference on LISP and Functional Programming (LFP '92). ACM, New York, NY, USA, 21–31. https://doi.org/10.1145/141471.141499
- Luc Maranget. 2007. Warnings for pattern matching. Journal of Functional Programming 17 (2007), 387-421. Issue 3.
- Luc Maranget. 2008. Compiling pattern matching to good decision trees. In Proceedings of the ACM Workshop on ML.
- Luc Maranget and Projet Para. 1994. Two Techniques for Compiling Lazy Pattern Matching. Technical Report.
- The Coq development team. 2004. *The Coq proof assistant reference manual*. LogiCal Project. http://coq.inria.fr Version 8.0. C. McBride and J. McKinna. 2004. The view from the left. *Journal of Functional Programming* 14, 1 (2004), 69–111.
- Neil Mitchell and Colin Runciman. 2008. Not All Patterns, but Enough: An Automatic Verifier for Partial but Sufficient Pattern Matching. In *Proceedings of the First ACM SIGPLAN Symposium on Haskell (Haskell '08)*. ACM, New York, NY, USA, 49–60. https://doi.org/10.1145/1411286.1411293
- Ulf Norell. 2007. Towards a practical programming language based on dependent type theory. Ph.D. Dissertation. Department of Computer Science and Engineering, Chalmers University of Technology, SE-412 96 Göteborg, Sweden.
- Ulf Norell. 2008. Dependently typed programming in Agda. In In Lecture Notes from the Summer School in Advanced Functional Programming.
- Simon Peyton Jones, Dimitrios Vytiniotis, Stephanie Weirich, and Geoffrey Washburn. 2006. Simple Unification-based Type Inference for GADTs. In *Proceedings of the Eleventh ACM SIGPLAN International Conference on Functional Programming (ICFP '06)*. ACM, New York, NY, USA, 50–61. https://doi.org/10.1145/1159803.1159811
- Norman Ramsey, João Dias, and Simon Peyton Jones. 2010. Hoopl: A Modular, Reusable Library for Dataflow Analysis and Transformation. In *Proceedings of the Third ACM Haskell Symposium on Haskell (Haskell '10)*. ACM, New York, NY, USA, 121–134. https://doi.org/10.1145/1863523.1863539
- Patrick M. Rondon, Ming Kawaguci, and Ranjit Jhala. 2008. Liquid Types. In *Proceedings of the 2008 ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI '08)*. ACM, New York, NY, USA, 159–169. https://doi.org/10.1145/1375581.1375602
- Tom Schrijvers, Simon Peyton Jones, Manuel Chakravarty, and Martin Sulzmann. 2008. Type Checking with Open Type Functions. In *Proceedings of the 13th ACM SIGPLAN International Conference on Functional Programming (ICFP '08)*. ACM, New York, NY, USA, 51–62. https://doi.org/10.1145/1411204.1411215
- Tom Schrijvers, Simon Peyton Jones, Martin Sulzmann, and Dimitrios Vytiniotis. 2009. Complete and Decidable Type Inference for GADTs. In *Proceedings of the 14th ACM SIGPLAN International Conference on Functional Programming (ICFP '09)*. ACM, New York, NY, USA, 341–352. https://doi.org/10.1145/1596550.1596599
- R. C. Sekar, R. Ramesh, and I. V. Ramakrishnan. 1995. Adaptive Pattern Matching. SIAM J. Comput. 24, 6 (Dec. 1995), 1207–1234. https://doi.org/10.1137/S0097539793246252
- Peter Sestoft. 1996. ML pattern match compilation and partial evaluation. In *Partial Evaluation*, Olivier Danvy, Robert Glück, and Peter Thiemann (Eds.). Lecture Notes in Computer Science, Vol. 1110. Springer Berlin Heidelberg, 446–464. https://doi.org/10.1007/3-540-61580-6\_22
- Tim Sheard. 2004. Languages of the Future. In In OOPSLA '04: Companion to the 19th annual ACM SIGPLAN conference on Object-oriented programming systems, languages, and applications. ACM Press, 116–119.
- W Sonnex, S Drossopoulou, and S Eisenbach. 2012. Zeno: An Automated Prover for Properties of Recursive Data Structures. Springer-Verlag Berlin, 407–421. https://doi.org/10.1007/978-3-642-28756-5\_28
- Martin Sulzmann, Manuel M. T. Chakravarty, Simon Peyton Jones, and Kevin Donnelly. 2007. System F with Type Equality Coercions. In *Proceedings of the 2007 ACM SIGPLAN International Workshop on Types in Languages Design and*

- Implementation (TLDI '07). ACM, New York, NY, USA, 53-66. https://doi.org/10.1145/1190315.1190324
- Peter Thiemann. 1993. Avoiding Repeated Tests in Pattern Matching. In 3rd International Workshop on Static Analysis, Gilberto Filé (Ed.). Padova, Italia, 141–152.
- Niki Vazou, Eric L. Seidel, Ranjit Jhala, Dimitrios Vytiniotis, and Simon Peyton-Jones. 2014. Refinement Types for Haskell. In *Proceedings of the 19th ACM SIGPLAN International Conference on Functional Programming (ICFP '14)*. ACM, New York, NY, USA, 269–282. https://doi.org/10.1145/2628136.2628161
- Dimitrios Vytiniotis, Simon Peyton jones, Tom Schrijvers, and Martin Sulzmann. 2011. Outsidein(x) Modular Type Inference with Local Assumptions. J. Funct. Program. 21, 4-5 (Sept. 2011), 333–412. https://doi.org/10.1017/S0956796811000098
- Philip Wadler. 1987a. Efficient compilation of pattern matching. In *The implementation of functional programming languages*, SL Peyton Jones (Ed.). Prentice Hall, 78–103.
- P. Wadler. 1987b. Views: A Way for Pattern Matching to Cohabit with Data Abstraction. In *Proceedings of the 14th ACM SIGACT-SIGPLAN Symposium on Principles of Programming Languages (POPL '87)*. ACM, New York, NY, USA, 307–313. https://doi.org/10.1145/41625.41653
- Hongwei Xi. 1998a. Dead Code Elimination Through Dependent Types. In *Proceedings of the First International Workshop on Practical Aspects of Declarative Languages (PADL '99)*. Springer-Verlag, London, UK, 228–242.
- Hongwei Xi. 1998b. Dependent Types in Practical Programming. Ph.D. Dissertation. Carnegie Mellon University.
- Hongwei Xi. 2003. Dependently typed pattern matching. Journal of Universal Computer Science 9 (2003), 851-872.
- Hongwei Xi, Chiyan Chen, and Gang Chen. 2003. Guarded Recursive Datatype Constructors. In Proceedings of the 30th ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '03). ACM, New York, NY, USA, 224–235. https://doi.org/10.1145/604131.604150
- Dana N. Xu. 2006. Extended Static Checking for Haskell. In Proceedings of the 2006 ACM SIGPLAN Workshop on Haskell (Haskell '06). ACM, New York, NY, USA, 48–59. https://doi.org/10.1145/1159842.1159849
- Dana N. Xu, Simon Peyton Jones, and Koen Claessen. 2009. Static Contract Checking for Haskell. In *Proceedings of the 36th Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '09)*. ACM, New York, NY, USA, 41–52. https://doi.org/10.1145/1480881.1480889
- Brent A. Yorgey, Stephanie Weirich, Julien Cretin, Simon Peyton Jones, Dimitrios Vytiniotis, and José Pedro Magalhães. 2012. Giving Haskell a Promotion. In *Proceedings of the 8th ACM SIGPLAN Workshop on Types in Language Design and Implementation (TLDI '12)*. ACM, New York, NY, USA, 53–66. https://doi.org/10.1145/2103786.2103795