

(1) DPV Problem 6.3. Your algorithm should run in time at most  $O(n^2)$  (although a better running time is also possible).

6.3. Yuckdonald's is considering opening a series of restaurants along Quaint Valley Highway (QVH). The  $n$  possible locations are along a straight line, and the distances of these locations from the start of QVH are, in miles and in increasing order,  $m_1, m_2, \dots, m_n$ . The constraints are as follows:

- At each location, Yuckdonald's may open at most one restaurant. The expected profit from opening a restaurant at location  $i$  is  $p_i$ , where  $p_i > 0$  and  $i = 1, 2, \dots, n$ .
- Any two restaurants should be at least  $k$  miles apart, where  $k$  is a positive integer.

$i$  = # of possible locations (sorted based on distance)

$j$  = List of distances from QVH ( $m(j)$  is the distance between QVH and the  $i$  location)

$p$  = list of expected profits ( $p(i)$  is the profit from the restaurant at  $i$  location)

$k$  = min distances between pair of restaurants

$dp(\#i)$  = list of max profits based on each location

$$dp(i) = \max[dp(i-1), p(i) + dp(j)]$$

Where the max profit is  $dp(n)$

Runs in  $O(n \log n)$  sorting and binary search