

# Testing **PLC** Software with **Symbolic Execution**

Sergey Grebenshchikov, TUM

Here: IEC 61131-3 ST

# Testing **PLC** Software with **Symbolic Execution**

Sergey Grebenshchikov, TUM

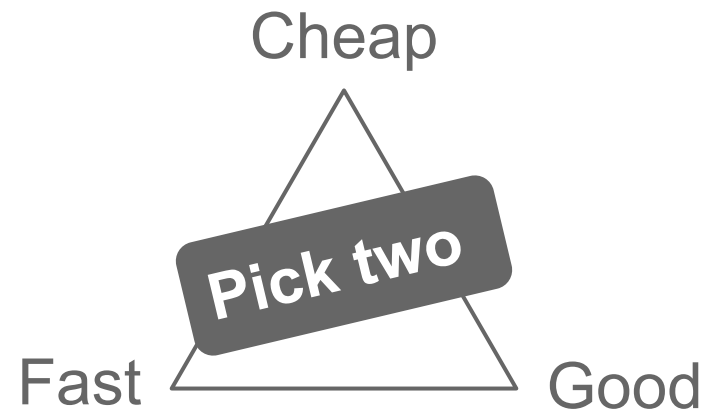
# Motivation

**Testing Software Is Easy.**

**Testing Software Well Is Hard.**

**Real-Time**

**Testing Software **Well** Is Harder.**







Highly applicable

Computation scales well

Quality scales badly

Low assurance

Limited by avail. theory

Comput. scales badly

Quality scales well

High assurance

Manual tests

Verification

Highly applicable

Computation scales well

Quality scales badly

Low assurance

Limited by avail. theory

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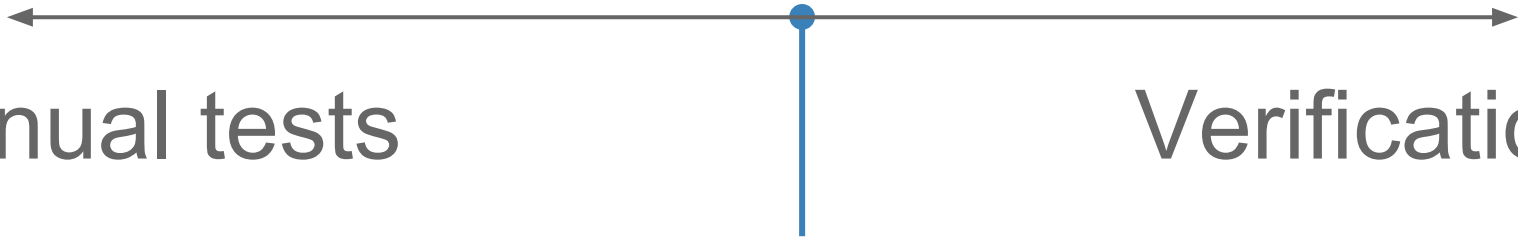
Quality scales well

High assurance

Manual tests

Verification

Model-based testing  
sweet spot



What if there is **no model**?

**Legacy code**

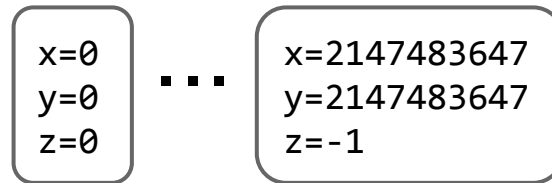
**Partial models**

**What if there is no model?**

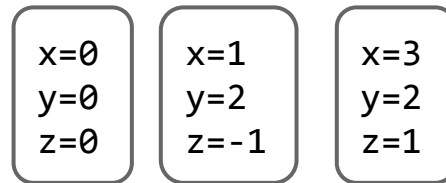
**Supplement MBT with symbolic execution!**

# Symbolic execution recap.

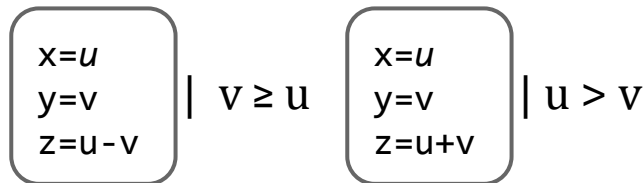
```
f(int x, int y) {  
    int z = 0;  
    assume(x,y>=0)  
    if(x>y) {  
        z = x+y;  
    } else {  
        z = x-y;  
    }  
    assert(...)  
}
```



Explicit-state model checking



Manual testing



Symbolic execution

# Problem statement

**Adapt SymEx methods to PLC software.**  
**Focus today: Error handling.**

# Problem statement

**Adapt SymEx methods to PLC software.**  
**Focus today: Error handling.**

There are **challenges!**

FUNCTION\_BLOCK Example

VAR

Step1 : TON;

Step2 : TON;

END\_VAR

VAR\_GLOBAL

SensorA : BOOL;

SensorB : REAL;

B : BOOL;

Run : BOOL

Error : BOOL;

Example : Example;

END\_VAR

IF Run THEN

Step1(IN := (

PT := t#

IF (Step1.Q OR

Error := TRUE;

END\_IF

B := SensorB > 0.55;

IF SensorA THEN

Step2(IN := B;

PT := t#50ms);

END\_IF

END\_IF

END\_FUNCTION\_BLOCK

**Challenges**

END\_PROGRAM

// Specification:

// When in *Run* mode, SensorB

// must reach > 0.55 (B = TRUE)

// within at most 100ms.

// If this is not the case,

// an *Error* must be signaled

// within 50ms



FUNCTION\_BLOCK Example

VAR

Step1 : TON;

Step2 : TON;

END\_VAR

IF Run THEN

Step1(IN := (NOT SensorA);

PT := t#100ms);

IF (Step1.Q OR Step2.Q) THEN

Error := TRUE;

END\_IF

B := SensorB > 0.55;

IF SensorA THEN

Step2(IN := B;

PT := t#50ms);

END\_IF

END\_IF

END\_FUNCTION\_BLOCK

VAR\_GLOBAL

SensorA : BOOL;

SensorB : REAL;

B: BOOL;

Run : BOOL

Error : BOOL;

Example : Example;

END\_VAR

BEGIN\_PROGRAM

RUN := TRUE;

Ex();

END\_PROGRAM

// Specification:

// When in *Run* mode, SensorB

// must reach > 0.55 (B = TRUE)

// within at most 100ms.

// If this is not the case,

// an *Error* must be signaled

// within 50ms

FUNCTION\_BLOCK Example

VAR

Step1 : TON;

Step2 : TON;

END\_VAR

**Time-dependent  
data and control  
flow**

IF Run THEN

Step1(IN := (NOT SensorA);

PT := t#100ms);

IF (Step1.Q OR Step2.Q) THEN

Error := TRUE;

END\_IF

B := SensorB > 0.55;

IF SensorA THEN

Step2(IN := B;

PT := t#50ms);

END\_IF

END\_IF

END\_FUNCTION\_BLOCK

VAR\_GLOBAL

SensorA : BOOL;

SensorB : REAL;

B : BOOL;

Run : BOOL

Error : BOOL;

Example : Example;

END\_VAR

**Sensor data**

BEGIN\_PROGRAM

RUN := TRUE;

Ex();

END\_PROGRAM

// Specification:

// When in *Run* mode, *SensorA*

// must be *TRUE*.

// When *SensorA* is *TRUE*,

// *Error* is not the case,

// an *Error* must be signaled

// within 50ms

**Informal specifications**

## **Time dependency**

Symbolic timestamps, Last-modified constraints

## **Temporal symbolic monitoring**

Timed sequence diagrams (and MTL)  
over symbolic traces

# Requirements and solution

**By example**

Specification

Analysis

Insight

**R<sub>1</sub>: Simple specification language that makes sense to domain experts.**



```
graph LR; A[Specification] --> B[Analysis]; B --> C[Insight]
```

Specification

Analysis

Insight

FUNCTION\_BLOCK Example

VAR

Step1 : TON;

Step2 : TON;

END\_VAR

IF Run THEN

Step1(IN := (NOT SensorA);

PT := t#100ms);

IF (Step1.Q OR Step2.Q) THEN

Error := TRUE;

END\_IF

B := SensorB > 0.55;

IF SensorA THEN

Step2(IN := B;

PT := t#50ms);

END\_IF

END\_IF

END\_FUNCTION\_BLOCK

VAR\_GLOBAL

SensorA : BOOL;

SensorB : REAL;

B: BOOL;

Run : BOOL

Error : BOOL;

Example : Example;

END\_VAR

BEGIN\_PROGRAM

RUN := TRUE;

Ex();

END\_PROGRAM

**// Specification:**

**// When in *Run* mode, SensorB**

**// must reach > 0.55 (B = TRUE)**

**// after at most 100ms.**

**// If this is not the case,**

**// an *Error* must be signaled**

**// within 50ms**

```

time ::= int ms
timespec ::=  $\geq$  time |  $\leq$  time
tsd ::=  may { tsd }
        |  must { tsd }
        |  within(timespec) { tsd }
        |  delay(timespec) { tsd }
        |  constraint(constr) { tsd }
        |  message(global-var)
        |  tsd; tsd
        |  {}

```

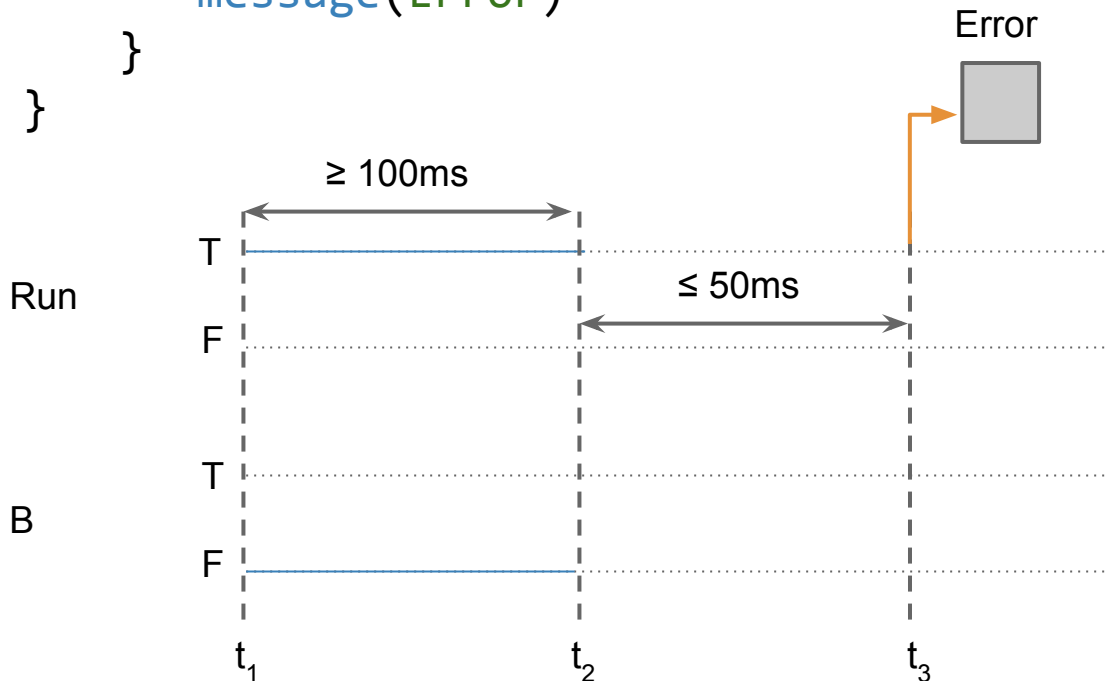
*constr* ::= Boolean+LA formulae over program variables  
*global-var* ::= Global variables

```

may {
    delay(>=0ms){
        constraint(Run & !B) {
            delay(>=100ms){}
        }
    }
}
must {
    within(<=50ms){
        message(Error)
    }
}

```

// When in *Run* mode, SensorB  
 // must reach  $> 0.55$  ( $B = \text{TRUE}$ )  
 // after at most 100ms.  
 // If this is not the case,  
 // an *Error* must be signaled  
 // within 50ms





# Scenario based specification

Scenario Builder

Coverage Analysis

Path Analysis

Scenario name

Save

Scenario1

Open Delete

F3

Open Delete

F2

Open Delete

F4

Open Delete

Scenario1  
(alt)

Open Delete

Default  
Example

Open Delete

F5

Open Delete

F1

Open Delete

F1.dev

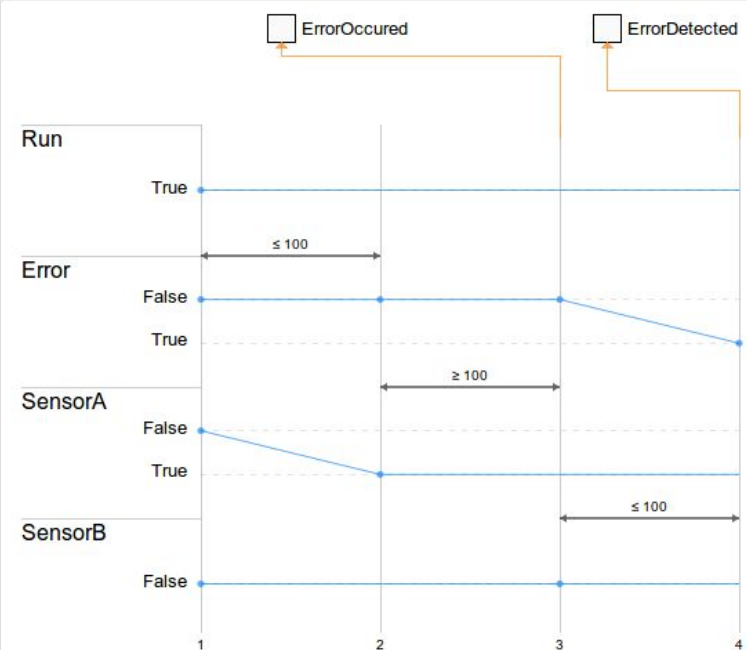
Open Delete

F1.dev.1

Open Delete

```
1 ((constraint (Run True)
2       (Error False)
3       (SensorA False)
4       (SensorB False))
5   (later (<=100)
6     (constraint (SensorA True)
7       (Error False)))
8   (later (>=100)
9     (constraint (SensorB False)
10      (Error False)))
11  (send ErrorOccurred)
12  (later (<=100) (constraint (Error True))
13    (send ErrorDetected))
14 )
15
```

Your input parsed just fine :)



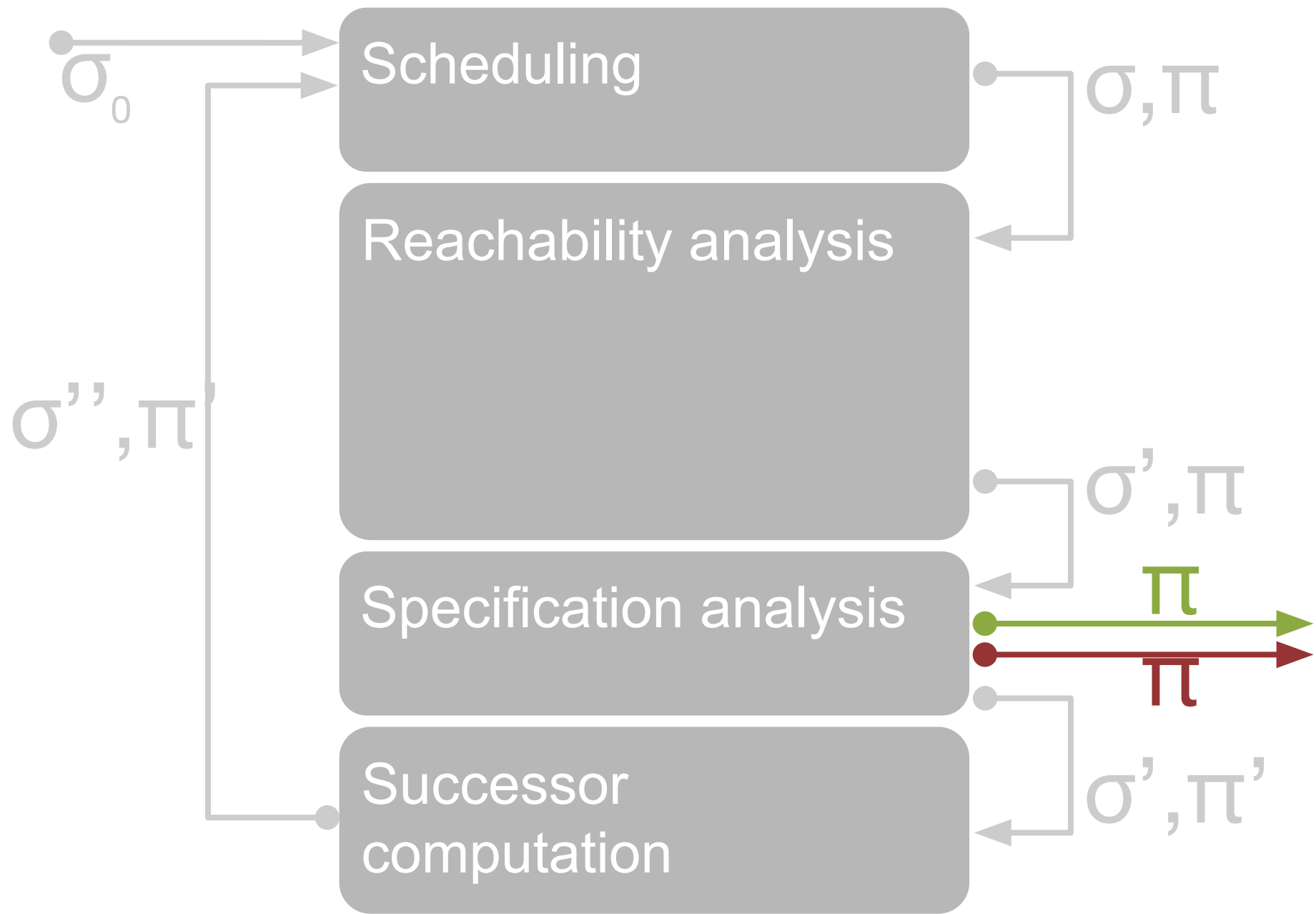
$R_2$ : **Automatic** search for **test cases** that the software passes/fails w.r.t the **given specification**.



Specification

Analysis

Insight



```

A: IF Run THEN
B:   Step1(IN := (NOT SensorA);
C:     PT := t#100ms);
D:   IF (Step1.Q OR Step2.Q) THEN
E:     Error := TRUE;
F:   END_IF
G:   B := SensorB > 0.55;
H:   IF SensorA THEN
I:     Step2(IN :=B;
J:       PT := t#50ms);
K:   END_IF
K: END_IF

```

```

may {
    delay(>=0ms){
        constraint(Run & !B) {
            delay(>=100ms){}
        }
    }
}
must {
    within(<=50ms){
        message(Error)
    }
}

```

$$\left( G: B := \text{SensorB} > 0.55; \right)$$

$$\left( \begin{array}{l} \text{constraint}(\text{Run} \ \& \ !B) \{ \\ \quad \text{delay}(\geq 100\text{ms})\{\} \\ \} \end{array} \right)$$

$$\left( \begin{array}{l} t: t_1 \\ \text{Run}: v\text{Run}_\theta, tv\text{Run}_\theta \\ B: vB_\theta, tvB_\theta \\ \text{SensorB}: v\text{SB}_\theta, tv\text{SB}_\theta \end{array} \right)$$

$$\left( C \right)$$

## Reachability analysis

Memory state  
transition

Temporal  
transition

Constraint generation

SMT query

$$\left( G: B := \text{SensorB} > 0.55; \right)$$

$$\left( \begin{array}{l} \text{constraint}(\text{Run} \ \& \ !B) \{ \\ \quad \text{delay}(>=100\text{ms})\{\} \\ \} \end{array} \right)$$

$$\left( \begin{array}{l} t: t_1 \\ \text{Run}: v\text{Run}_\theta, tv\text{Run}_\theta \\ B: vB_\theta, tvB_\theta \\ \text{SensorB}: v\text{SB}_\theta, tv\text{SB}_\theta \end{array} \right)$$

$$\left( \begin{array}{l} C \\ vB_1 = v\text{SB}_\theta > 0.55 \\ tvB_1 = \text{ite}(vB_1 = vB_\theta, tvB_\theta, t_1) \\ t_1 >= t_\theta \ \& \ t_1 <= t_\theta + t_{\text{cycle}} \end{array} \right)$$

## Reachability analysis

Memory state  
transition

Temporal  
transition

Constraint generation

SMT query

$$\left( G: B := \text{SensorB} > 0.55; \right)$$

$$\left( \begin{array}{l} \text{constraint}(\text{Run} \ \& \ !B) \{ \\ \quad \text{delay}(>=100\text{ms})\{\} \\ \} \end{array} \right)$$

$$\left( \begin{array}{l} t: t_2 \\ \text{Run}: v\text{Run}_\theta, tv\text{Run}_\theta \\ B: vB_1, tvB_1 \\ \text{SensorB}: v\text{SB}_\theta, tv\text{SB}_\theta \end{array} \right)$$

$$\left( \begin{array}{l} C \\ vB_1 = v\text{SB}_\theta > 0.55 \\ tvB_1 = \text{ite}(vB_1 = vB_\theta, tvB_\theta, t_1) \\ t_1 \geq t_\theta \ \& \ t_1 \leq t_\theta + t_{\text{cycle}} \end{array} \right)$$

## Reachability analysis

Memory state  
transition

Temporal  
transition

Constraint generation

SMT query

$$\left( G: B := \text{SensorB} > 0.55; \right)$$

$$\left( \begin{array}{l} \text{constraint}(\text{Run} \ \& \ !B) \{ \\ \quad \text{delay}(\geq 100\text{ms})\{\} \\ \} \end{array} \right)$$

$$\left( \begin{array}{l} t: t_2 \\ \text{Run}: v\text{Run}_\theta, tv\text{Run}_\theta \\ B: vB_1, tvB_1 \\ \text{SensorB}: v\text{SB}_\theta, tv\text{SB}_\theta \end{array} \right)$$

$$\left( C' \right)$$

## Reachability analysis

Memory state  
transition

Temporal  
transition

Constraint generation

SMT query



$$\left( G: B := \text{SensorB} > 0.55; \right)$$

$$\left( \text{constraint}(\text{Run} \ \& \ !B) \{ \right. \\ \left. \text{delay}(\geq 100\text{ms})\{ \} \right. \\ \left. \} \right)$$

$$\left( \begin{array}{l} t: t_2 \\ \text{Run}: v\text{Run}_0, tv\text{Run}_0 \\ B: vB_1, tvB_1 \\ \text{SensorB}: v\text{SB}_0, tv\text{SB}_0 \end{array} \right)$$

$$\left( C' \ \& \ v\text{Run}_0 \ \& \ !vB_1 \right)$$

## Reachability analysis

Memory state  
transition

Temporal  
transition

Constraint generation

SMT query

$$\left[ \begin{array}{l} G: B := \text{SensorB} > 0.55; \end{array} \right]$$

$$\left[ \begin{array}{l} \text{constraint}(\text{Run} \ \& \ !B) \{ \\ \quad \text{delay}(>=100\text{ms})\{\} \\ \} \end{array} \right]$$

$$\left[ \begin{array}{l} t: t_2 \\ \text{Run}: v\text{Run}_\theta, tv\text{Run}_\theta \\ B: vB_1, tvB_1 \\ \text{SensorB}: v\text{SB}_\theta, tv\text{SB}_\theta \end{array} \right]$$

$$\left[ \begin{array}{l} C'' \end{array} \right]$$

## Reachability analysis

Memory state  
transition

Temporal  
transition

Constraint generation

SMT query

SMT query to Z3:  
 **$\text{SAT}(C'')$** ?

```

A: IF Run THEN
B:   Step1(IN := (NOT SensorA);
C:     PT := t#100ms);
D:   IF (Step1.Q OR Step2.Q) THEN
E:     Error := TRUE;
F:   END_IF
G:   B := SensorB > 0.55;
H:   IF SensorA THEN
I:     Step2(IN :=B;
J:       PT := t#50ms);
K:   END_IF
K: END_IF

```

```

may {
    delay(>=0ms){
        constraint(Run & !B) {
            delay(>=100ms){}
        }
    }
}
must {
    within(<=50ms){
        message(Error)
    }
}

```

$$\left( \begin{array}{l} H: \text{ IF SensorA THEN } \dots \end{array} \right) \quad \left( \begin{array}{l} \text{constraint}(\text{Run} \ \& \ !B) \{ \\ \quad \text{delay}(\geq 100\text{ms})\{\} \\ \} \end{array} \right)$$

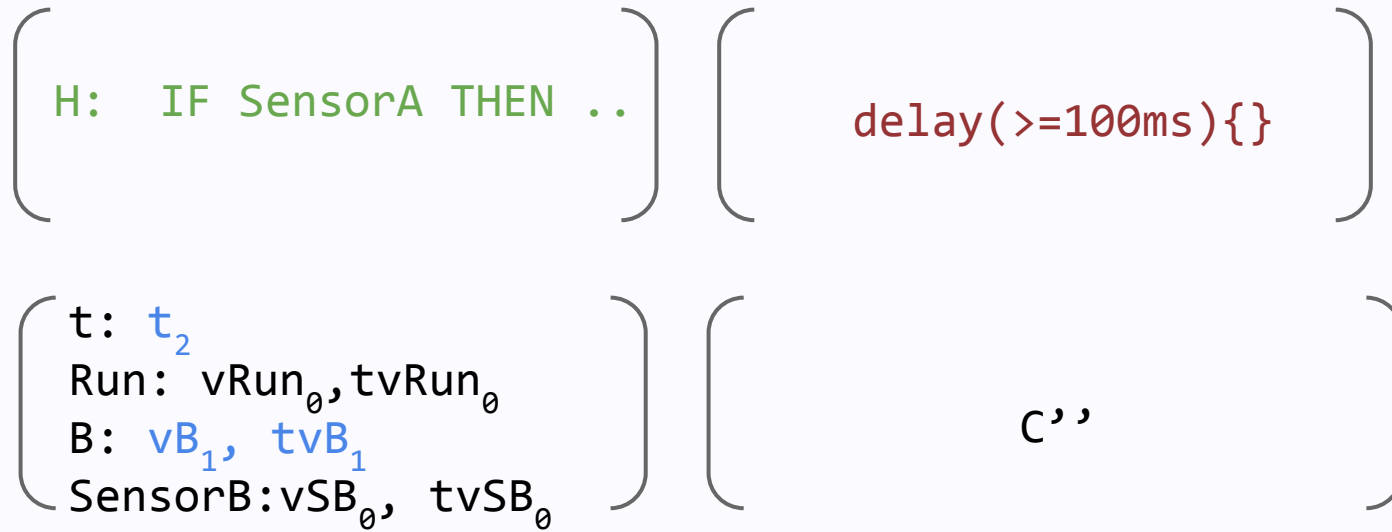
$$\left( \begin{array}{l} t: t_2 \\ \text{Run}: v\text{Run}_\theta, tv\text{Run}_\theta \\ B: vB_1, tvB_1 \\ \text{SensorB}: v\text{SB}_\theta, tv\text{SB}_\theta \end{array} \right) \quad \left( \begin{array}{c} C'' \end{array} \right)$$

Successor computation

Control flow  
automaton

x

Specification  
automaton



Successor computation

Control flow  
automaton

x

Specification  
automaton

**R<sub>3</sub>: Analysis results and test cases are **clearly presented** and their meaning **quantified**.**



```
graph LR; A[Specification] --> B[Analysis]; B --> C[Insight];
```

Specification

Analysis

Insight

# Coverage analysis

Scenario Builder

Coverage Analysis

Path Analysis

Unit

TON.PouMain 100

Main.PouMain 100

Example.PouMain 90

Code coverage

```
IF(Run) THEN 3
  Step1(IN := NOT SensorA, PT := t#100ms) 3
  IF(Step1.Q OR Step2.Q) THEN 3
    Error := TRUE 3
  END_IF 3
  B := SensorB > 0.55 3
  IF (SensorA) THEN 3
    Step2(IN := B; PT := t#50ms) 1
  END_IF 3
END_IF 3
```

Specification coverage

```
may 1 {
  delay(>=0ms) 1 {
    constraint(Run & !B) 1 {
      delay(>=100ms) { 292 }
    }
  }
}
must 1 {
  within(<=50ms) 35 {
    message(Error)
  }
}
```

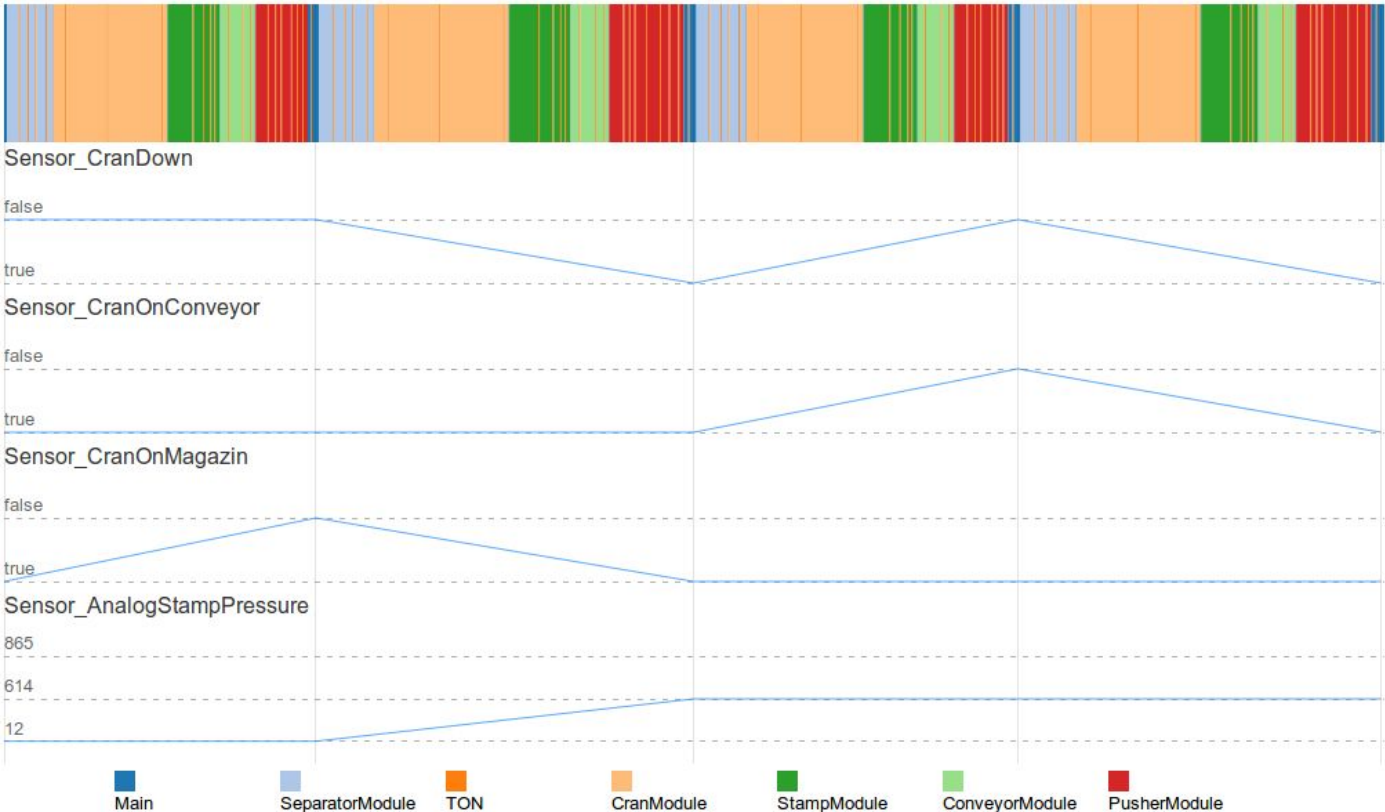
# Path visualisation

Path

0

1

- Sensor\_CranPosition
- Sensor\_CranPositionStamp
- Sensor\_CranSucked
- Sensor\_CranUp
- Sensor\_MagazinCapacitiv...
- Sensor\_MagazinEmergenc...
- Sensor\_MagazinOpticalSe...
- Sensor\_MagazinSwitchMa...
- Sensor\_SliderMovedOut
- Sensor\_SliderNotMovedOut
- Sensor\_SorterCapacitiveS...
- Sensor\_SorterCapacitiveS...
- Sensor\_SorterEmergencyS...
- Sensor\_SorterLightbarrier...





**R<sub>4</sub>: An extensible library that can be  
used in other tools and customized.**



Specification

Analysis

Insight

Integrate in  
reports

Visualisation

Import

JSON

plcOpenXML

Work with  
CODESYS

Use as presented  
here

C# API

TSD Frontend

ST Frontend

Specification

Heuristic

Add languages,  
algorithms

Analysis

Encoding

Low-level  
optimizations

PLC Core

SMT (MSR Z3)

# Summary

**SymEx** is a **success story** in desktop software, **not yet adopted for PLC.**

**SymEx is a valuable companion  
technique to MBT.**

**We adapted SymEx to the  
requirements of real-time PLC  
software.**

**We built the first ever SymEx engine  
for the IEC 61131-3.**

**You can use it as a library in your own tools today.**



+ Symbolic execution



Manual tests

Verification

Model-based  
testing



# Backup Slides

