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Touristic guide for city guidance with minimum-maximum optimization multi-criteria model: Budget VS Number of cities

*Abstract* – This articles consists in developing a description of the implementation of a modelling and optimization process on the development of a software tool for trip guidance among cities with the goal to maximize the quantity of visited places and minimizing the budget spent on the trip. With the use of a mathematical model, verifying with a computational methods tool (GAMS) and generating appropriate metaheuristics (SPEA 2), this paper illustrates the basis for implementing a project of such magnitude and what it would take to make it a reality.

*Key Terms –* Multi-objective optimization, evolutionary algorithms, mathematical modelling, touristic guidance, transport.

# INTRODUCTION

T

RAVELLING represents one of the most enriching experiences for the contemporaneous human because it allows him to leaving his sedentary nature and discover new places, flavors and people. In spite of this, not everyone has the same preferences or restrictions at the moment of planning a new journey, in other words, parameters as the number of available days for travelling, cities for visiting, budget, among others, are too specific for each traveler. This means that there exist numerous ways to execute a journey, for which it is desirable that every planned journey is the best among the available alternatives.

Talking about the state of the art for this particular problem, there are some applications can be classified among the following types:

* Plan routes with the least cost distance between points: In this regard, applications like Rome2Rio and Google Maps can be taken into account. Among various functionalities Google Maps offers, the most famous ones consist on showing detailed information about geographical regions and sites worldwide with the “best” route (the one with lowest costs of transportation) that allows you to go from one place to another [1]. In the case of Rome2Rio, it offers the possibility to query for any route between cities cities, landmarks, attractions or addresses across the globe in a multi-modal manner. [2]
* Plan activities to do in a particular city: For this category, the best solution available is “Google Trips”, which is a mobile application that gathers your travel information from Gmail and organizes daily itineraries for your time being in the specified city (the app can work without the use of internet) [3]. Also, other solutions like “Sygic Travel” just receive the place you are going to and the number of days as an input in order to perform your itinerary during the whole trip. [4].

As it can be seen, the specific problem that is being treated inside this article is not formally solved by any of the existing tools, that either generate routes with the lowest transportation costs for going from one city to another, or create a daily itinerary with all the activities that the person can do during the whole trip.

# PROBLEM DEFINITION

From the point of view of the traveler, the best journey is that which minimizes costs. Here, a good journey is defined by the quantity of visited places and the quality of these. In other words, the problem to attack is to minimize the cost of travelling maximizing the amount and quality of the visited places. Under this premise, the variables taken into consideration re the next ones:

**Places to visit:** Each traveler has a list of the places he would like to potentially visit in his next journey.

**Places’ score:** Each place must have a score which must be comparable to other places´, in order to decide which of them is better.

**Time:** A traveler has a limited time window to accomplish his journey.

**Living cost (daily):** The traveler must afford his own living in each place he visits. For this, the cost of average living per place is going to be used.

**Transport costs:** Moving from one place to another implies some costs. For now, only terrestrial means will be considered in such parameter.

**Maximum number of days per place:** This, with the goal of giving every traveler enough time (the one he/she considers necessary) to know each place he visits, meaning, the planned number of days in each place must not surpass this number. This parameter also allows us to avoid the model to only consider one city (with the best score and lowest living costs) by forcing the change after a certain quantity of days.

**Minimum number of days:** This number decide how much of a “nomad” can a traveler be, given a minimum threshold of days that can result in constant displacements. IN the opposite way, if it has a high value, the movement between places will be harshly reduced. This can e useful for travelers that don´t mind moving frequently or minimizing their displacements (e.g. Travelers with children, motor liabilities or the elderly).

# OBJECTIVES STABLISHMENT

1. Identify the best travelling plan given a set of places (cities) and the other proposed restrictions.

2. Identify and implement a metaheuristic that allows the program to find good solutions to the problem given a certain execution time threshold.

# MODEL FORMULATION AND PLANNING

## Model conceptualization

**Parameters**:

* mind; Minimum number of days.
* maxd: Maximum number of days.
* s: Starting point.
* d: Number of days.
* CT: Transport costs matrix for going from one city to another. Currently only terrestrial means are taken into account.
* CV: Average living costs array for every city.
* n: Number of cities.
* : Priority for maximizing the number of days.
* : Priority for minimizing the Budget spent.
* S: Scores matrix for city i with an interest point l.
* R: Quantity of reviews matrix for city i with an interest point l.

**Decision variable:**

In day *i*, the traveler stays in city *j*.

**Target function**: W estate a multi-objective model using the method of pondered summation of weights between the two proposed functions: quantity of days and spent Budget (divided in transport and living costs).

(1)

Where:

Formula () assigns a score to a destiny l proportional to his aggregated rating (average) and the number of persons that have rated the destination. The formula “normalizes” scores dividing them by 5 and seeks to penalize those destinations with a huge amount of reviews by calculating the squared root of such values. Due to the fact that there can be places without a huge popularity that should be considered in the travelling plan, this penalty is taken into consideration.

In equation (1), we decided to normalized both functions F1 (quantity of places) and F2 (costs function) with the use of two factors:

1. F1: Multiply by the minimum of the scores calculated in “Puntaje” times the number of days, plus 1
2. F2: Divide by the summation of the maximum cost of transport with the maximum average living cost, times d.

**Restrictions**:

1. The costs structure for going from one place to another must be represented in real numbers. Their value will always be greater or equal than zero.
2. The structure of costs for average living by day is represented with real numbers with values greater or equal than zero.
3. The scores structure is represented with real numbers ranging from 1 to 5.

Where l is the predefined number of points of interest per city. l

1. The structure of quantity of reviews is represented with real numbers bigger tan or equal to zero.

Where l is the predefined number of points of interest per city. l

1. The summation of the priorities must be equal to 1.
2. The priorities are rational numbers between 0 and1:
3. The person cannot surpass his minimum and maximum threshold of days per city during the journey:
4. The person cannot go to two cities on the same day:

*9)*  The first day (i=0) the person must go to someplace:

## Data Adquisition

Cost of living per city was extracted from Numbeo and transport costs were extracted from Rome2Rio. Specifically, data was retrieved manually but both sources expose API’s for automatization of this process, which we left for a further iteration as Rome2Rio API requires their approval.

An important consideration is that transport between any cities a and b is the cheapest found in the Rome2Rio ’query’ from city a to city b. As this cost might not be the same on both directions, a to b might have a different cost than b to a.

# MODEL TRADUCTION

To solve this complex problem, we translated the previous mathematical model into the evolutionary algorithm SPEA 2 (a metaheuristic) in order to achieve quickly almost-optimal solutions. Additionally, the following design decisions were taken into account:

## Chromosome: <Allele on day 1> - <Allele on day 2>- …. <Allele on day d>

*Allele: < Id of the city visited >*

## Euclidian distance with the two target functions:

## Since SPEA 2 already calculates the whole Pareto Front, the use of parameters P1 and P2 are no longer necessary.

## Truncation operator in environmental selection consists on removing the least-fit items on until

## Variation recombination was applied with double cut crossover (with allele cut points chosen randomly) and uniform crossover. Mutation operator consisted on changing an allele’s city to another random city, with a probability of 10%, iterating through every allele of the chromosome.

## As P, and A are sets, they don’t have duplicate chromosomes.

## Termination was only limited to a maximum number of generations. This is left variable as it heavily impacts execution time.

# VERIFICATION AND VALIDATION

For the verification process, we used the language GAMS with the development environment “gamside” that allowed the proper translation of the mathematic model in order to solve the problem with mathematical methods that, despite not being optimal in time, i sable to find answers for the basic scenarios of the previously stated model through the use of a mixed integer non-linear problem solver (MINLP) like BONMIN or COUENNE.

In order to validate the metaheuristic stated in section V, multiple input files were created for our verification program in GAMS that would represent a series of scenarios with their respective parameters theoretically calculated without the help of any external source. For each one of such scenarios, a test was done with the code in both GAMS and Java. The results of these tests are:

1. *Base Scenario 1 (Basic functioning)*
   1. P2=0
   2. Mind=1 and Maxd=1
   3. d=4
   4. n=4
   5. The rest is random

EXPECTED: Travel to each city in one day.

GAMS:

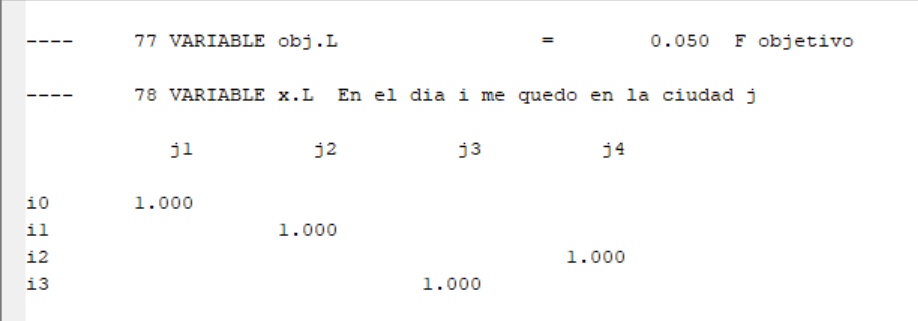


Fig 1. Resultado del escenario base 1 en GAMS

SPEA 2 (Java):

1. *Base Scenario 2 (Number of days):* 
   1. n=2
   2. mind=3
   3. maxd=5
   4. d=8
   5. s=1
   6. Puntaje(1)=10
   7. Puntaje(2)=1
   8. p1=1
   9. p2=0
   10. The rest is random

EXPECTED: 5 days in the first city, and 3 in the other one.

GAMS:

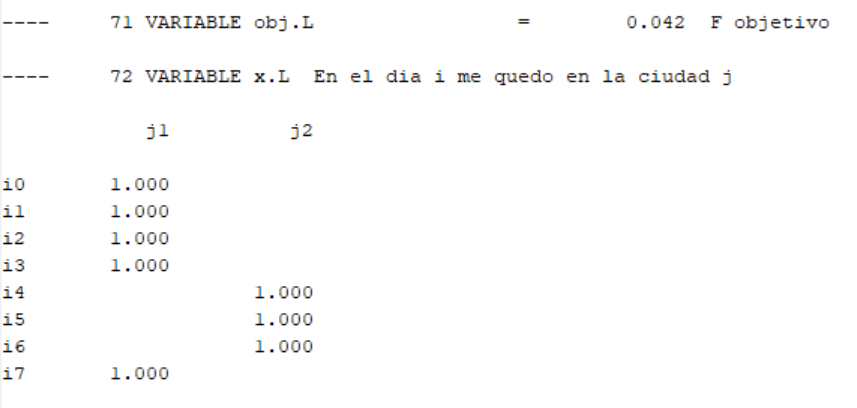


Fig 2. Resultado del escenario base 2 en GAMS

SPEA 2 (Java):

1. *Base Scenario 3 (Average living cost):*
   1. n=2
   2. mind=3
   3. maxd=5
   4. d=8
   5. s=1
   6. The values in the transport costs matrix are the same.
   7. p1=0
   8. p2=1
   9. The rest is random.

EXPECTED: 5 days in the first city, 3 in the other one.

GAMS:

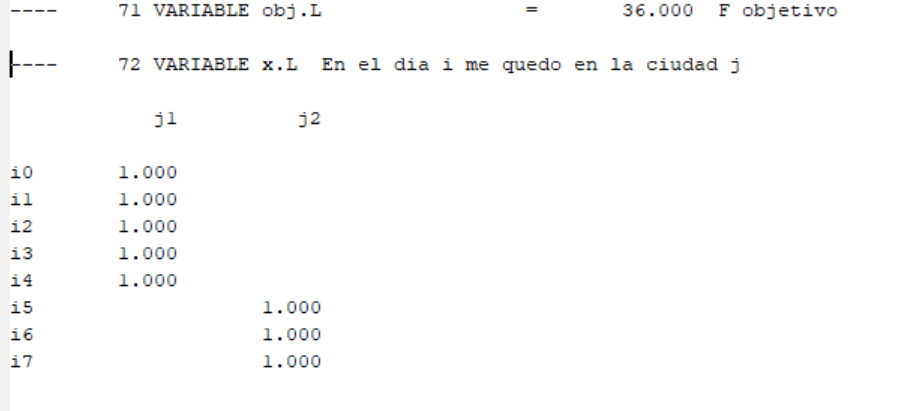


Fig 3. Resultado del escenario base 3

1. *Base Scenario 4 (Transport costs):* 
   1. n=3
   2. mind=|
   3. maxd=1
   4. d=3
   5. s=1
   6. p2=1
   7. p1=0



Fig 4. Tabla de costos del escenario base 4.

* 1. Average living cost is the same for every city.
  2. The rest is random

EXPECTED: Goes from city 1 to 2, and then from 2 to 3.

GAMS:

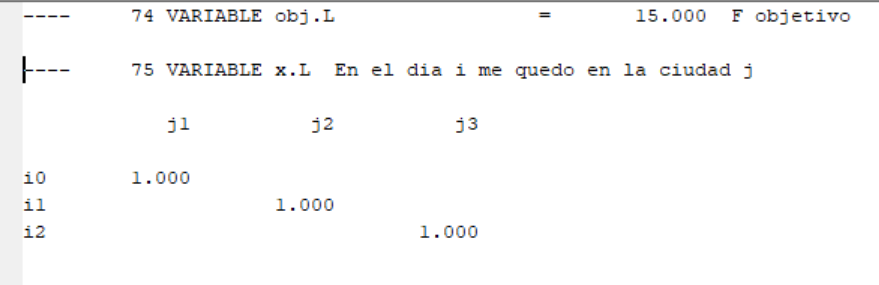


Fig 5. Resultado obtenido del escenario base 4 en GAMS

1. *Intermediate Scenario:*
   1. n=10
   2. 5 cities have high living cost and low scores (From city 1 to 5)
   3. 5 cities have low living cost and high scores (From city 6 to 10).
   4. Transport costs are the same.
   5. d=15
   6. maxd=3
   7. mind=1
   8. p1=0.5
   9. p2=0.5
   10. s: One of the cheap cities (from 6 to 10).
   11. The rest is random

EXPECTED: Go to the cheapest cities.

GAMS:

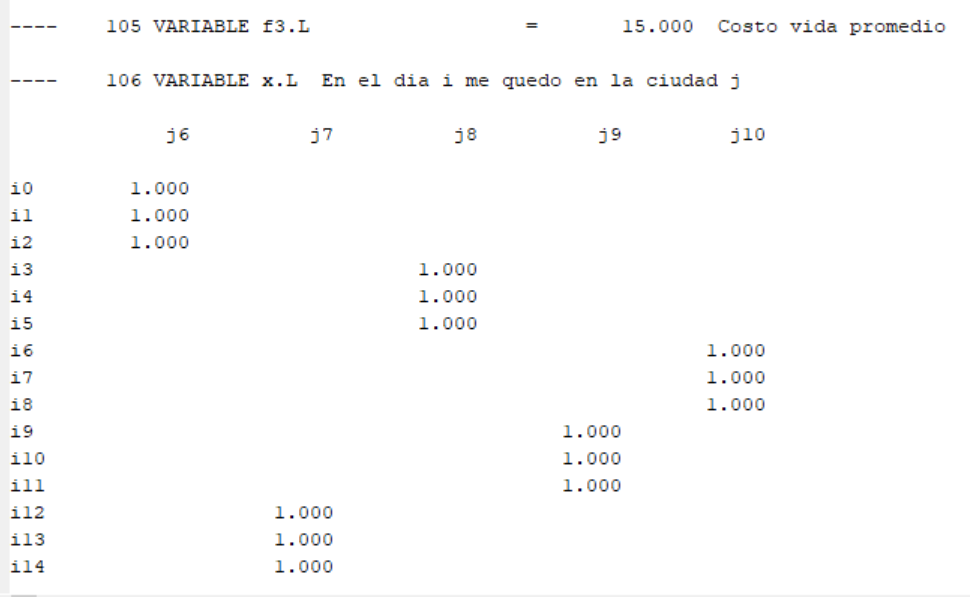


Fig 6. Resultado obtenido del escenario intermedio en GAMS

SPEA 2 (Java):

1. *Real life Scenario:* 
   1. n=16. The researched cities from Spain are in order:
      1. valencia
      2. barcelona
      3. sevilla
      4. granada
      5. málaga
      6. córdoba
      7. cádiz
      8. almería
      9. toledo
      10. salamanca
      11. madrid
      12. zaragoza
      13. pamplona
      14. bilbao
      15. segovia
      16. santander
   2. Transport costs are researched in “Rome2Rio”.
   3. Average living costs are researched in “Numbeo”.
   4. Scores and quantity of reviews are researched in Google.
   5. d=50
   6. maxd=5
   7. mind=2
   8. The rest is random

EXPECTED: Unknown

GAMS: Unknown

SPEA 2 (Java):

# RESULTS ANALYSIS

# CONCLUSIONS AND FUTURE WORK

TABLE I

Units for Magnetic Properties

|  |  |  |
| --- | --- | --- |
| Symbol | Quantity | Conversion from Gaussian and  CGS EMU to SI a |
| Φ | magnetic flux | 1 Mx → 10−8 Wb = 10−8 V·s |
| *B* | magnetic flux density,  magnetic induction | 1 G → 10−4 T = 10−4 Wb/m2 |
| *H* | magnetic field strength | 1 Oe → 103/(4π) A/m |
| *m* | magnetic moment | 1 erg/G = 1 emu  → 10−3 A·m2 = 10−3 J/T |
| *M* | magnetization | 1 erg/(G·cm3) = 1 emu/cm3  → 103 A/m |
| 4π*M* | magnetization | 1 G → 103/(4π) A/m |
| σ | specific magnetization | 1 erg/(G·g) = 1 emu/g → 1 A·m2/kg |
| *j* | magnetic dipole  moment | 1 erg/G = 1 emu  → 4π × 10−10 Wb·m |
| *J* | magnetic polarization | 1 erg/(G·cm3) = 1 emu/cm3  → 4π × 10−4 T |
| χ*,* κ | susceptibility | 1 → 4π |
| χρ | mass susceptibility | 1 cm3/g → 4π × 10−3 m3/kg |
| μ | permeability | 1 → 4π × 10−7 H/m  = 4π × 10−7 Wb/(A·m) |
| μr | relative permeability | μ → μr |
| *w, W* | energy density | 1 erg/cm3 → 10−1 J/m3 |
| *N, D* | demagnetizing factor | 1 → 1/(4π) |

Vertical lines are optional in tables. Statements that serve as captions for the entire table do not need footnote letters.

aGaussian units are the same as cg emu for magnetostatics; Mx = maxwell, G = gauss, Oe = oersted; Wb = weber, V = volt, s = second, T = tesla, m = meter, A = ampere, J = joule, kg = kilogram, H = henry.

BIBLIOGRAPHY

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Costo de vida promedio: <https://www.numbeo.com/cost-of-living/>

Puntajes y cantidad de reviews: <https://www.google.com.co/destination/map/topsights?q=Bogot%C3%A1&sa=X&site=search&output=search&dest_mid=%2Fm%2F01dzyc&dest_mid=%2Fm%2F01dzyc&tcfs>

*Basic format for books:*

1. J. K. Author, “Title of chapter in the book,” in *Title of His Published Book, x*th ed. City of Publisher, Country if not
2. USA: Abbrev. of Publisher, year, ch. *x*, sec. *x*, pp. *xxx–xxx.*

*Examples:*

1. G. O. Young, “Synthetic structure of industrial plastics,” in *Plastics,* 2nd ed., vol. 3, J. Peters, Ed. New York: McGraw-Hill, 1964, pp. 15–64.
2. W.-K. Chen, *Linear Networks and Systems.* Belmont, CA: Wadsworth, 1993, pp. 123–135.

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1. J. K. Author, “Name of paper,” *Abbrev. Title of Periodical*, vol. *x,* no. *x,* pp*. xxx-xxx,* Abbrev. Month, year.

*Examples:*

1. J. U. Duncombe, “Infrared navigation—Part I: An assessment   
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2. E. P. Wigner, “Theory of traveling-wave optical laser,” *Phys. Rev*.,   
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1. J. K. Author, “Title of report,” Abbrev. Name of Co., City of Co., Abbrev. State, Rep. *xxx*, year.

*Examples:*

1. E. E. Reber, R. L. Michell, and C. J. Carter, “Oxygen absorption in the earth’s atmosphere,” Aerospace Corp., Los Angeles, CA, Tech. Rep. TR-0200 (4230-46)-3, Nov. 1988.
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*Basic format for handbooks:*

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*Examples:*

1. *Transmission Systems for Communications*, 3rd ed., Western Electric Co., Winston-Salem, NC, 1985, pp. 44–60.
2. *Motorola Semiconductor Data Manual*, Motorola Semiconductor Products Inc., Phoenix, AZ, 1989.

*Basic format for books (when available online):*

1. Author. (year, month day). *Title.* (edition) [Type of medium]. *volume (issue).* Available: site/path/file

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1. J. Jones. (1991, May 10). *Networks.* (2nd ed.) [Online]. Available: [http://www.atm.com](http://www.atm.com/)

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1. Author. (year, month). Title. *Journal.* [Type of medium]. *volume (issue),* pages. Available: site/path/file

*Example:*

1. R. J. Vidmar. (1992, Aug.). On the use of atmospheric plasmas as electromagnetic reflectors. *IEEE Trans. Plasma Sci.* [Online]. *21(3),* pp. 876–880. Available:<http://www.halcyon.com/pub/journals/21ps03-vidmar>

*Basic format for papers presented at conferences (when available online):*

1. Author. (year, month). Title. Presented at Conference title. [Type of Medium]. Available: site/path/file

*Example:*

1. PROCESS Corp., MA. Intranets: Internet technologies deployed behind the firewall for corporate productivity. Presented at   
   INET96 Annual Meeting. [Online]. Available: <http://home.process.com/Intranets/wp2.htp>

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*Example:*

1. S. L. Tall een. (1996 , Apr . ). The In t r an et Archi -tecture: M a nagi ng i n f o rm at i on i n t h e ne w paradigm. Amdahl Corp., CA. [Online]. Available:<http://www.amdahl.com/doc/products/bsg/intra/infra/html>

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[Online]. Available: NEXIS Library: LEXPAT File: DESIGN

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1. G. Brandli and M. Dick, “Alternating current fed power supply,”   
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*Examples:*

1. J. O. Williams, “Narrow-band analyzer,” Ph.D. dissertation, Dept. Elect. Eng., Harvard Univ., Cambridge, MA, 1993.
2. N. Kawasaki, “Parametric study of thermal and chemical nonequilibrium nozzle flow,” M.S. thesis, Dept. Electron. Eng., Osaka Univ., Osaka, Japan, 1993.

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2. J. K. Author, “Title of paper,” unpublished.
3. J. K. Author, “Title of paper,” to be published.

*Examples:*

1. A. Harrison, private communication, May 1995.
2. B. Smith, “An approach to graphs of linear forms,” unpublished.
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1. *Title of Standard*, Standard number, date.

*Examples:*

1. IEEE Criteria for Class IE Electric Systems, IEEE Standard 308, 1969.
2. Letter Symbols for Quantities, ANSI Standard Y10.5-1968.

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Mr. Author’s awards and honors include the Frew Fellowship (Australian Academy of Science), the I. I. Rabi Prize (APS), the European Frequency and Time Forum Award, the Carl Zeiss Research Award, the William F. Meggers Award and the Adolph Lomb Medal (OSA).

1. Costos de transporte: Se mandó la propuesta para solicitar acceso al API de Rome2Río que contiene costos de desplazamiento entre ciudades sobre diferentes medios de transporte. Sin embargo, la solicitud no ha sido respondida por lo que es necesario extraer los datos manualmente . [↑](#footnote-ref-1)