

$$f(x)=\begin{cases}\exp x& if\,x<0\\x^2& if\,0\leq x<2\\x^3+x^2+1& if\,2\leq x<6\end{cases}$$

$$(1) \quad \begin{array}{l} f: \\ R^d \rightarrow \\ R \end{array} \quad \begin{array}{l} \phi: \\ [0,\infty) \rightarrow \\ R \end{array}$$

$$f(x)=\phi(\|x\|), x\in \mathbb{R}^d$$

$$\phi(\|x\|), x\in R^d, \\ \|\cdot\|$$

$$x_1,\ldots,x_N\in R^d\\ \phi: R^d\rightarrow R\\ \lambda_1,\ldots,\lambda_N\\ \sum_{i=1}^N\lambda_i p(x_i)=0,$$

$$p_m\sum_{i=1}^N\sum_{j=1}^N\lambda_i\lambda_j\phi(\|x_i-x_j\|)>0.$$

$$\|\cdot\|$$

$$d_0$$

$$R^d$$

$$\phi_{l,k}(r)=(1-r)^n_+p(r)k\geq 1,$$

$$(3) \quad \begin{array}{l} r=\\ \|\cdot\|\\ (1-r)_+=\\ \max\{0,(1-r)\}\\ l=\lfloor \frac{d}{2}\rfloor+\\ k+1\\ ??\\ p(r)\\ \phi_{l,k}\\ 2k\\ q=\\ ??\\ ??\\ \frac{r}{\sigma}\\ [0,\sigma]\\ ??\\ \xi=1.5 \end{array}$$

$$\begin{array}{ll} \phi(r)=(1-r)^2_+ & C^0 \\ \phi(r)=(1-r)^4_+(4r+1) & C^2 \\ \phi(r)=(1-r)^6_+(35r^2+18r+3) & C^4 \\ \phi(r)=(1-r)^8_+(32r^3+25r^2+8r+1) & C^6 \end{array}$$

$$x_1,\ldots,x_N\in R^d\\ u(x_1),\ldots,u(x_N)$$

$$s(x)=\sum_{j=1}^N\lambda_j\phi(\|x-x_j\|)+p(x),$$

$$(4) \quad \begin{array}{l} \|\cdot\|\\ \lambda_j\in R\\ j=1,\ldots,N\\ p\in \Pi^d_{m-1}\\ d-m-1\\ 1\\ A\in \mathbb{R}^{N\times N} \end{array}$$