

## Computer Networks - HW4

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Ans 1- Given: Transmission time of packets = 5ms  
Propagation delay (one way) = 200ms  
No packet losses

Solution:-

$$\eta_{sw} = \frac{T}{S} \quad \left( \begin{array}{l} \text{Given} \\ \text{Assuming no packet losses} \end{array} \right)$$

Where  $T$  = packet transmission time

$S$  = total time from start of transmission to return of acknowledgement.

$$\begin{aligned} \therefore \eta_{sw} &= \frac{5 \times 10^{-3} \text{ sec}}{(5 \times 10^{-3} + 2 \times 200 \times 10^{-3}) \text{ sec}} \\ &= \frac{5}{5 + 400} \\ &= \frac{5}{405} = \frac{1}{81} = 0.0123 = 1.23\% \end{aligned}$$

Therefore, efficiency of Stop and Wait (SAW) = 1.23%.

$$\eta_{GBN} = \min \left\{ 1, \frac{WT}{S} \right\}$$

Where  $T$  = packet transmission time

$S$  = total time from start of transmission to return of acknowledgement.

$W$  = window size.

$$\begin{aligned} \therefore \eta_{GBN} &= \min \left\{ 1, \frac{5 \times 5 \times 10^{-3} \text{ sec}}{(5 \times 10^{-3} + 2 \times 200 \times 10^{-3}) \text{ sec}} \right\} \\ &= \min \left\{ 1, \frac{25}{405} \right\} = \frac{5}{81} = 0.0617 = 6.17\% \end{aligned}$$

Therefore, efficiency of Go-Back-N protocol with window size of 5 packets is 6.17%.

Ans 2a) Given:  $N$  stations share 56 kbps pure ALOHA channel.  
Each station outputs a 1000 bit frame on average every 100 sec.

To find: Maximum value of  $N$ .

Solution:- Maximum efficiency of Pure ALOHA = 18.4%.

$$\text{Hence, achievable rate} = 56 \times 10^3 \times 0.184 \text{ bps} \\ = 56 \times 184 \text{ bps}$$

Now, in 100 sec,  $N$  stations transmit 1000 bit frames  
Hence,  $(1000N/100)$  bits are transferred per second.

$$\therefore 56 \times 184 = 1000N/100$$

$$\Rightarrow N = \frac{56 \times 184}{10} = 56 \times 18.4 = 1030.4$$

$$\Rightarrow N = 1030$$

b) Given: Slotted ALOHA where users generate 50 requests/sec.  
Time is slotted in units of 40 ms.

Solution:

i) Probability of success in  $k$  attempts =  $e^{-G}(1-e^{-G})^{k-1}$

For success in 1<sup>st</sup> attempt,  $k=1$

$$\therefore P_1 = e^{-G}$$

Now,  $G$  = number of requests in 40 ms =  $\frac{50}{1000} \times 40 = 2$   
i.e. 2 requests per unit time

$$\text{Hence, } P_1 = e^{-2} = 0.135$$

Therefore, chance of success in 1<sup>st</sup> attempt = 0.135



ii) Probability of  $k$  collisions and then a success

$$\begin{aligned} P_{k+1} &= e^{-G}(1-e^{-G})^k \\ &= e^{-2}(1-e^{-2})^k \\ &= 0.135 \times 0.865^k \end{aligned}$$

iii) Expected number of transmission attempts needed when there are a large number of requests is given by

$$E = e^G = e^2 = 7.389$$

Ans 3-

a) i) Signal propagation speed in twin length cable  
 $= 0.82c$  { where  $c$  = speed of light in vacuum }  
 $= 0.82 \times 3 \times 10^8 \text{ m/s}$   
 $= 2.46 \times 10^8 \text{ m/s}$

$$\text{Signal propagation time} = \frac{\text{Distance}}{\text{Signal Propagation Speed}}$$

$$= \frac{2 \times 1000 \text{ m}}{2.46 \times 10^8 \text{ m/s}}$$

$$= \frac{2000}{246 \times 10^6} \text{ sec} = \frac{1}{123} \text{ ms} = 0.00813 \text{ ms} = 8.13 \mu\text{s}$$

$$\begin{aligned} \text{Length of contention slot} &= 2 \times \text{signal propagation time} \\ &= 2 \times 8.13 \mu\text{s} \\ &= 16.26 \mu\text{s} \end{aligned}$$

ii) Signal propagation speed in fibre optic cable =  $0.65c$

$$= 0.65 \times 3 \times 10^8 \text{ m/s}$$

$$= 1.95 \times 10^8 \text{ m/s}$$

$$\begin{aligned}
 \text{Signal propagation time} &= \frac{\text{Distance}}{\text{Signal Propagation Speed}} \\
 &= \frac{40 \times 10^3 \text{ m}}{1.95 \times 10^8 \text{ m/s}} \\
 &= \frac{4 \times 10^{-4} \text{ sec}}{1.95} = \frac{40 \text{ ms}}{195} = 205.13 \mu\text{s} \\
 &= \frac{40 \text{ ms}}{195}
 \end{aligned}$$

$$\begin{aligned}
 \text{Length of contention slot} &= 2 \times \text{signal propagation time} \\
 &= 2 \times 205.13 \mu\text{s} \\
 &= 410.26 \mu\text{s}
 \end{aligned}$$

b) Given: Two stations contend for the channel using binary exponential backoff algorithm.

To find:  $\Rightarrow$  Probability that contention ends on round  $k$ .

$\Rightarrow$  Mean number of rounds per contention period.

Solution:

The probability of collision in the  $i^{\text{th}}$  round for 2 stations contending for the channel using exponential backoff algorithm is given by  $\frac{1}{2^{i-1}}$

Therefore, probability that the contention ends in round  $k$  = probability that first  $(k-1)$  attempts fail, followed by success in the  $k^{\text{th}}$  round.

$$P_k = \underbrace{\left( \prod_{i=1}^{k-1} \frac{1}{2^{i-1}} \right)}_{\text{Probability of failure in } (k-1) \text{ rounds}} \times \underbrace{\left( 1 - \frac{1}{2^{k-1}} \right)}_{\text{Probability of success in } k^{\text{th}} \text{ round,}}$$



$$P_k = (1 \times 2^{-1} \times 2^{-2} \times \dots \times 2^{-(k-2)}) (1 - 2^{-(k-1)})$$

$$P_k = \left[ \frac{(-1) + (-2) + \dots + (-(k-2))}{2} \right] (1 - 2^{-(k-1)})$$

$$P_k = \left[ \frac{-(k-2)(k-1)/2}{2} \right] (1 - 2^{-(k-1)})$$

Therefore, probability that the contention ends in round  $k$  is

$$P_k = \left[ \frac{-(k-2)(k-1)/2}{2} \right] (1 - 2^{-(k-1)}) = \left[ \frac{2^{(k-1)} - 1}{2} \right] \times 2^{-\left[ \frac{(k-2)(k-1)}{2} + (k-1) \right]}$$

$$\therefore P_k = \frac{(2^{(k-1)} - 1)}{2^{k(k-1)/2}}$$

$$\text{Mean number of rounds per contention period} = \sum_{k=1}^{\infty} k p_k$$

where  $k$  = round number

$p_k$  = probability that contention ends in  $k^{\text{th}}$  round

$$\text{Therefore, maximum number of rounds/contention slot} = \sum_{k=1}^{\infty} k \left[ \frac{2^{(k-1)} - 1}{2^{k(k-1)/2}} \right]$$

Ans 4- Difference between LAN switches and Routers.

LAN switches

Router

- |  |   |
|--|---|
| i> It is a layer 2 device  | i> It is a layer 3 device   |
| ii> Works on MAC addresses   | ii> Works on IP addresses   |
| iii> Used for connecting various hosts inside a LAN network.                                   | iii> Used for connecting various LAN networks together.   |
| iv> Layer 2 switching is hardware based and switches use ASICs to maintain MAC address tables. | iv> Layer 3 routing is both software and hardware based and uses protocols for routing packets. |
| v> Switches operating on layer 2 are faster since they are hardware based.                     | v> Routers operating on layer 3 are slower since they are software based.                       |

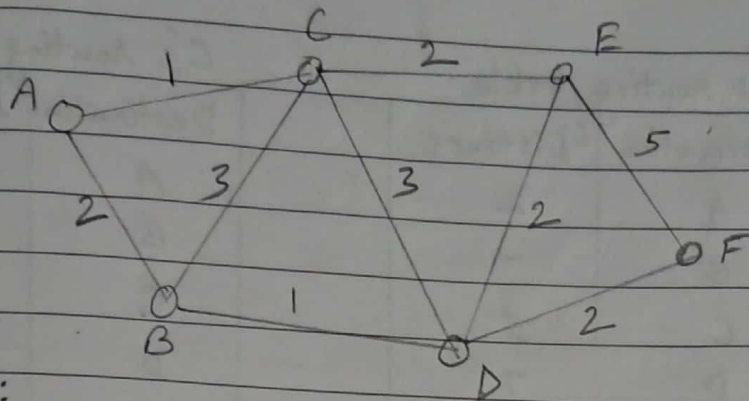


Table 1:

Step	Black nodes	$D(A), nh(A)$	$D(B), nh(B)$	$D(C), nh(C)$	$D(D), nh(D)$	$D(E), nh(E)$
0	{F}	$\infty, -$	$\infty, -$	$\infty, -$	2, F	5, F
1	{F, D}	$\infty, -$	3, D	5, D	2, F	4, D
2	{F, D, B}	5, B	3, D	5, D	2, F	4, D
3	{F, D, B, E}	5, B	3, D	5, D	2, F	4, D
4	{F, D, B, E, C}	5, B	3, D	5, D	2, F	4, D
5	{F, D, B, E, C, A}	5, B	3, D	5, D	2, F	4, D

Table 2 (Routing Table):

Destination	Next Hop	Cost
A	D	5
B	D	3
C	D	5
D	D	2
E	D	4

Ans 6-

B's routing table

Destination	Distance
A	2
B	-
C	5
D	7
F	1
G	4

C's routing table

Destination	Distance
A	4
B	5
C	-
D	2
F	2
G	3

A's Routing Table:

Destination	Distance	Next Hop
B	2	B
C	4	C
D	6	C
F	3	B
G	6	B