

Lab 6: The e/m Ratio for Electrons

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1 Linearization

We start with our force balance equation:

$$\begin{aligned}
 evB_{\perp} &= \frac{mv^2}{r} \\
 B_H - B_E &= \frac{mv^2}{evr} \\
 \text{From conservation of energy: } v &= \sqrt{\frac{2eV}{m}} \\
 \therefore B_H &= \frac{m \left(\frac{2eV}{m} \right)}{er \sqrt{\frac{2eV}{m}}} + B_E \\
 B_H &= \frac{2V}{r \sqrt{2eV/m}} + B_E \\
 B_H &= \sqrt{\frac{m}{e}} \frac{\sqrt{2V}}{r} + B_E \\
 \therefore \frac{8\mu_0 NI}{\sqrt{125}R} &= \sqrt{\frac{m}{e}} \frac{\sqrt{2V}}{r} + B_E
 \end{aligned}$$

Then, for $y = mx + b$:

$y = B_H$, $m = \sqrt{m/e}$, $x = \sqrt{2V}/r$, and $b = B_E$

2 Background Magnetic Field

There are two main sources of magnetic field within the laboratory actually. There is also Earth's magnetic field as well, the cool thing that makes a compass work.

3 Earth's Magnetic Field

When using LINEST, we find our $B_E \approx 2.34 \times 10^{-5}$ T. When comparing our B_E to the Earth's magnetic field in Edmonton according to NOAA (56.4×10^{-6}), we can see that the NOAA value is slightly larger. More specifically, $\frac{56.4 \times 10^{-6}}{2.34 \times 10^{-5}} \approx 2.4$ times larger.

When calculating our Helmholtz magnetic field strength with $I = 3.13$ A:

$$B_H = \frac{8}{\sqrt{125}R} \mu_0 NI = \frac{8}{(0.33)\sqrt{125}} (1.25663706212 \times 10^{-6})(72)(3.13) \approx 6.14 \times 10^{-4} \text{ T}$$

When dividing the two, we end up getting: $\frac{6.14 \times 10^{-4}}{56.4 \times 10^{-6}} \approx 10.9$, and so, our Helmholtz magnetic field strength is approximately 10.9 times larger than the Earth's magnetic field strength.

4 Helmholtz Orientation

The Helmholtz coils are oriented exactly 18 degrees to help negate the effect of Earth's magnetic fields. This helps us to conduct our experiment in a controlled manner without any external forces (or fields) impacting our results.

5 Magnetic Field Direction

When viewing our experiment from a top-down view, our magnetic field direction would be going OUT of the page, or in real life, it would be going towards the roof of the building. We know this because of the right-hand rule. Our forefinger goes to the direction a positive charge would be going, so down. Then, our thumb, when directly perpendicular to the forefinger, goes towards the force, which is to the right of the page. Finally as a result, our palm is facing into the page. However, we need to remember that this is the case of a positive charge, so the electron would be opposite, and so would be coming OUT of the page., and so our final answer is out of the page.

6 Table

Table 1: Raw experimental data along with the data used to plot our values (the last two columns). Note that the values were calculated using SI values of our measured data.

Current (A)	Diameter (cm)	Voltage (V)	$(B_H \pm 0.02) \times 10^{-4} \text{ T}$	$\sqrt{2V}/r$
1.43	11.5	25	2.81	123 ± 1
2.01	10.3	25	3.94	137 ± 2
2.26	9.00	25	4.43	157 ± 2
2.62	7.80	25	5.14	181 ± 2
3.13	6.50	25	6.14	218 ± 3
1.96	11.5	30	3.85	135 ± 1
2.18	10.3	30	4.28	150 ± 1
2.45	9.00	30	4.81	172 ± 2
2.78	7.80	30	5.45	199 ± 2
3.22	6.50	30	6.32	238 ± 3
2.14	11.5	35	4.20	146 ± 1
2.36	10.3	35	4.63	162 ± 1
2.62	9.00	35	5.14	186 ± 2
2.98	7.80	35	5.85	215 ± 2
3.47	6.50	35	6.81	257 ± 3

7 Graph

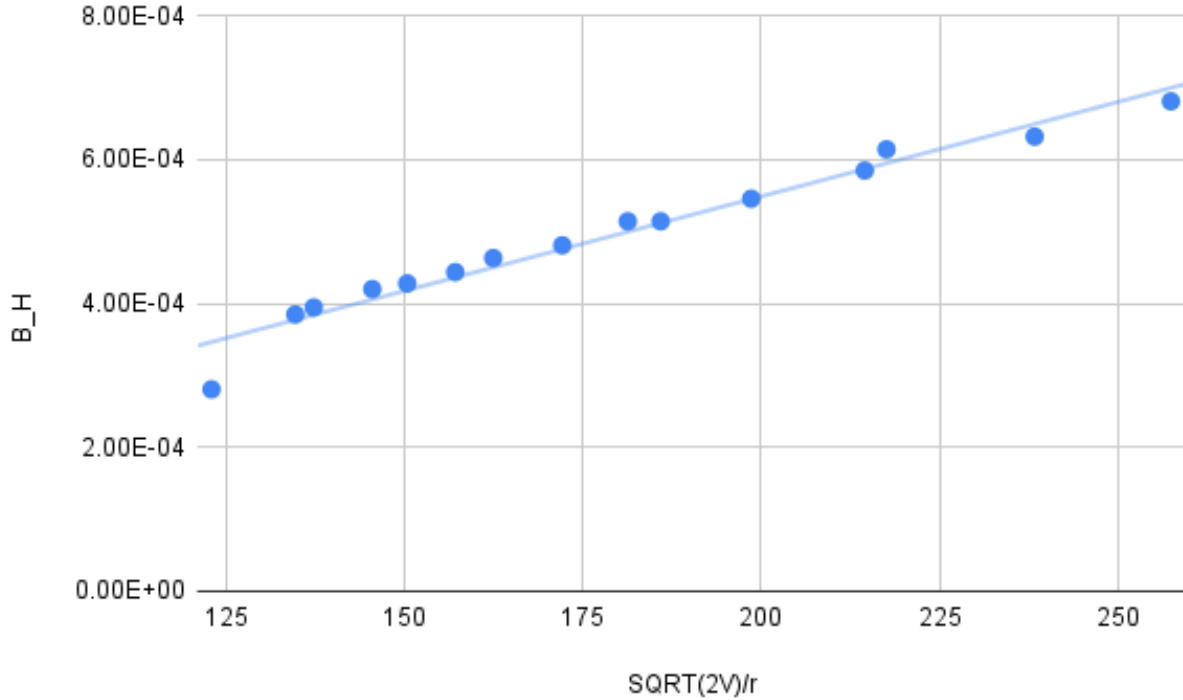


Figure 1: Graph of $B_H = \sqrt{\frac{m}{e}} \sqrt{2V}/r + B_E$, with slope $\sqrt{m/e} = (2.6 \pm 0.1) \times 10^{-6}$ kg/C and intercept $B_E = (3 \pm 3) \times 10^{-8}$ T. We used this to find our e/m ratio.

8 E/M

So we know our slope is $\sqrt{m/e} = (2.6 \pm 0.1) \times 10^{-6}$, so to find our e/m ratio, we first square our value and then take the inverse. Our resulting value is:

$$\frac{e}{m} = \left(\sqrt{\frac{m}{e}} \right)^{-2} \approx (1.45 \pm 0.3) \times 10^{11} \text{ C/kg}$$

9 Comparison

The currently accepted value for the e/m ratio is $\frac{1.602176634 \times 10^{-19}}{9.1093837015 \times 10^{-31}} \approx 1.76 \times 10^{11} \text{ J/kg}$. Although, we can easily see that compared to our measured value, the accepted e/m ratio is between zero and one error interval away. i.e;

$$0 \leq \left(\frac{e}{m} \right)_{\text{experimental}} - \left(\frac{e}{m} \right)_{\text{accepted}} \leq \delta \left[\left(\frac{e}{m} \right)_{\text{experimental}} - \left(\frac{e}{m} \right)_{\text{accepted}} \right]$$

$$0 \leq 0.3 \times 10^{11} \leq 0.3 \times 10^{11}$$

And so we can conclude that there is good agreement between the numbers.

References

- [1] Department of Physics. *PHYS 126 Lab Manual*. University of Alberta, 2025.
- [2] TA assisted with the lab, and provided guidance on the data collection and analysis.
- [3] Lab partner Morgann Reinhart assisted with the data collection and analysis.