

Problem #1

$$\begin{aligned}
 5 \angle 90^\circ \left[7 - j5 + \frac{10}{5 + j5} \right] &= 5 \angle 90^\circ \left[7 - j5 + \frac{2(1-j)}{(1+j)(1-j)} \right] \\
 &= 5 \angle 90^\circ [7 - j5 + (1-j)] = 5 \angle 90^\circ [8 - j6] \\
 &= 5 \angle 90^\circ \times 10 \angle -36.87^\circ = 50 \angle 53.13^\circ
 \end{aligned}$$

Problem #2

$$Z_{eq} = 1/Y_{eq}$$

$$Y_{eq} = j\omega C + \frac{1}{100 + j\omega} = j\omega C + \frac{100 - j\omega}{10000 + \omega^2}$$

$$Y_{eq} = \frac{j\omega C (10^4 + \omega^2) - j\omega + 100}{10^4 + \omega^2}$$

For Z_{eq} or Y_{eq} to be real the imaginary part must be zero.

$$\therefore \omega (10^4 + \omega^2) - \omega = 0$$

$$10^4 + \omega^2 = \frac{1}{C} = \frac{10^6}{50} = 2 \times 10^4$$

$$\omega^2 = 10^4$$

$$\omega = 100, \quad f = \frac{100}{2\pi} = 15.9 \text{ Hz}$$

Problem #3

$$v_s(t) = 10 \sin(\omega t + 30^\circ) = 10 \cos(\omega t - 60^\circ)$$

$$V_s = 10 \angle -60^\circ$$

With inductor removed, the open circuit voltage

is:

$$V_{oc} = V_{Th} = \frac{V_s \times 1 \Omega}{2 - j2} = V_s \frac{2 + j2}{8} = \frac{1}{4} V_s (1 + j)$$

$$V_{Th} = \frac{10 \angle -60^\circ}{4} \cdot \sqrt{2} \angle 45^\circ = 3.536 \angle -15^\circ$$

To find Z_{Th} , apply V_t and find I_t when V_s is short circuit:

$$I_x \rightarrow -I_t, \quad V_t = 2 I_x + I_t \times (1 \Omega \parallel (1 - j2))$$

$$V_t = -2 I_t + I_t \frac{1 - j2}{2 - j2}$$

$$Z_{Th} = \frac{V_t}{I_t} = -2 + \frac{(1 - j2)(2 + j2)}{8}$$

$$= -2 + \frac{1 + j1 - j2 + 2}{4}$$

$$= -2 + 0.75 - 0.25j$$

$$= -1.25 - j0.25 = -0.25(5 + j)$$

$$= 0.25 \angle 18^\circ \times \sqrt{26} \angle 11.31^\circ$$

$$1.275 \angle -168.7^\circ = 1.275 \angle 191.31^\circ = 1.275 \angle -168.69^\circ$$

