

Name :

ID #

**Problem # 1 (6 points)**

Charge entering the positive terminal of an element is  $Q = 8(1 - e^{-t})$  mC, if the power delivered to the element is  $P = 8e^{-t}$  W, determine:

a) The voltage across the element at any time  $t$ .

$$i(t) = \frac{dQ}{dt} = 8e^{-t} \text{ mA}$$

$$P(t) = i(t) v(t)$$

$$8e^{-t} = 8e^{-t} \times 10^{-3} \text{ A} \cdot v(t)$$

$$v(t) = 1000 \text{ V}$$

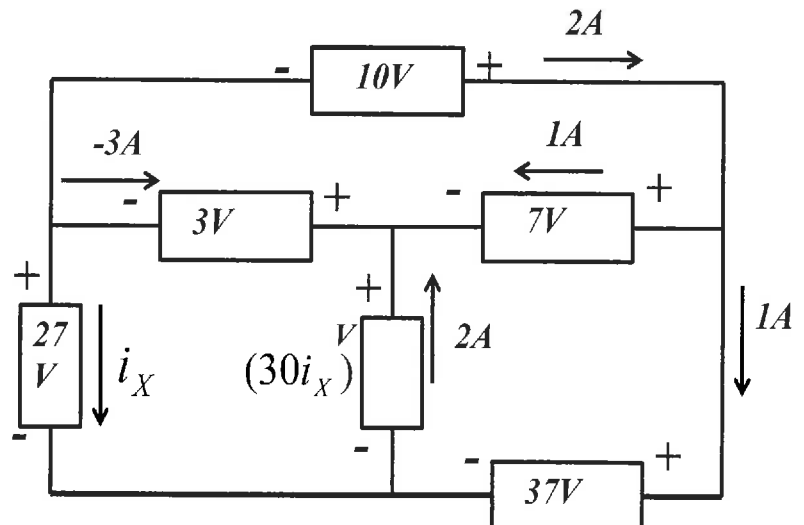
b) Energy delivered in one seconds (between 0 and 1sec).

$$W = \int_0^1 P(t) dt = \int_0^1 8e^{-t} dt = -8e^{-t} \Big|_0^1$$

$$W = -8e^{-1} + 8 = 5.057 \text{ J}$$

**Problem # 2 (6 points)**

Find current  $i_x$  in this circuit using the balance of consumed and supplied power.



$$27I_x - 60I_x + 37 + 7 + 9 - 20 = 0$$

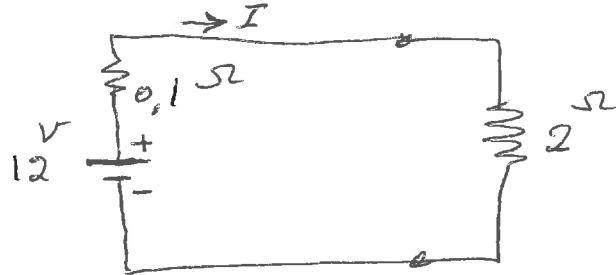
$$-33I_x + 33 = 0$$

$$I_x = 1 \text{ A}$$

**Problem # 3 (8 points)**

The internal resistance of a 12 volts battery is  $0.1\Omega$ . If battery is connected to a  $2\Omega$  resistive load, answer the following questions:

a) Draw the electric circuit associated with this application that includes the battery as a voltage source, and the resistors.



b) Calculate the power delivered to the  $2\Omega$  resistive load.

$$I = \frac{12 \text{ V}}{2 + 0,1} = \frac{12}{2,1} = 5,714 \text{ A}$$

$$P_{2\Omega} = 2^{\Omega} \cdot (5,714)^2 = 65,3 \text{ W}$$

c) Power dissipated in the internal resistance of the battery.

$$P_{0,1\Omega} = 0,1^{\Omega} \cdot I^2 = 0,1 \times (5,714)^2 = 3,265 \text{ W}$$

d) Power supplied by the battery

$$P_{\text{Battery}} = V \cdot I = 12 \times 5,714^{\text{A}} = 68,57 \text{ W}$$