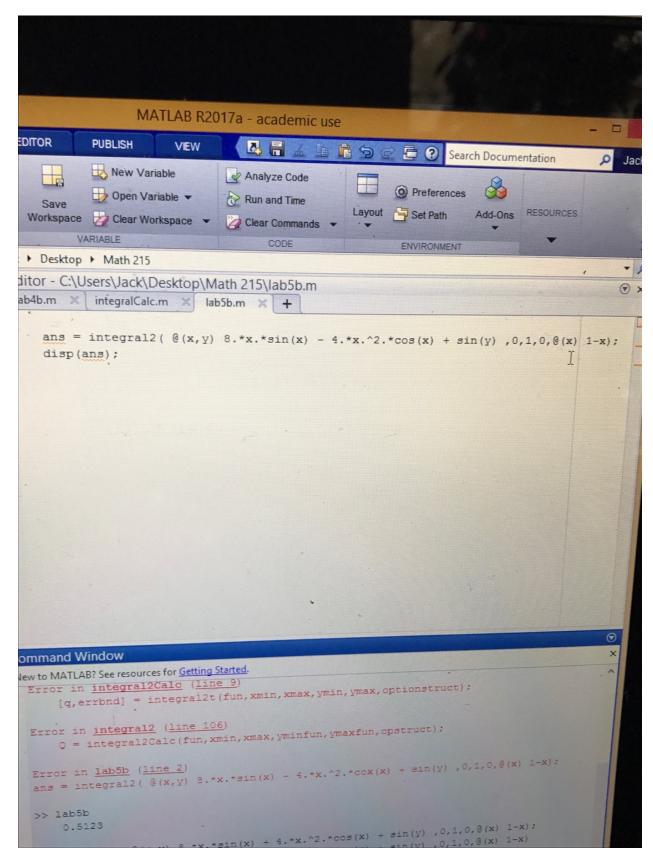
Jack Gregory, Brett Levenson, Andy Poulos, Rishabh Shah, John Stefan December 5, 2017 Lab5

Exercise One

Exercise one via line integrals



Exercise one via Green's Theorem

Exercise Two

```
>> F = [x, y, z];
>> % curve of intersection lies above circle with radius 3 centered at orgin
>> % paramatizing the plane
>> z = 5 - x
z =
5 - x
>> syms t
>> x = 3\cos(t);
x = 3\cos(t);
Error: Unexpected MATLAB expression.
Did you mean:
>> x = 3*cos(t);
>> y = 3*sin(t);
>> z = 5 - 3*cos(t);
>> % integrate
>> F = [x, y, z]
F =
[ 3*\cos(t), 3*\sin(t), 5 - 3*\cos(t) ]
>> syms dr
>> dr = diff(F)
dr =
[-3*sin(t), 3*cos(t), 3*sin(t)]
>> integral(dot(F, dr), 0, 2*pi)
Error using integral (line 82)
First input argument must be a function handle.
>> dot(F, dr)
ans =
9*sin(conj(t))*cos(t) - 9*cos(conj(t))*sin(t) - 3*sin(t)*(3*cos(conj(t)) - 5)
>> integral(ans, 0, 2*pi)
Error using <a href="integral">integral</a> (line 82)
First input argument must be a function handle.
```

Exercise two part one

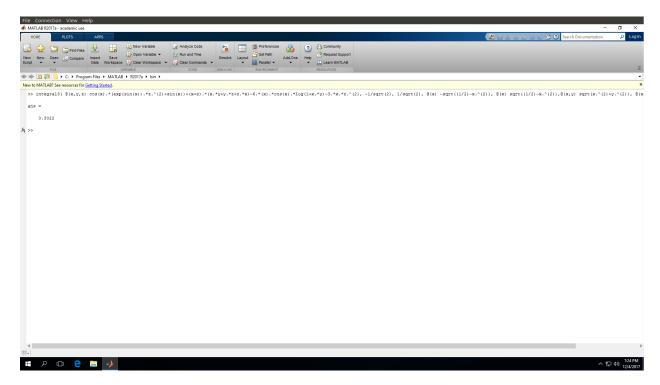
```
Command Window
New to MATLAB? See resources for Getting Started.
  >> integral(@(t) 9.*sin(t).*cos(t) - 9.*cos(t).*sin(t) - 3.*sin(t).*(3*cos(t) - 5), 0, 2*pi)
    -1.4294e-15
  >> % Therefore the line integral is zero
  >> % Applying Stock's theorm
  >> curl(F)
  Error using sym/curl (line 43)
  Argument contains less than three variables. Use vector of three variables as second argument.
  >> F = [x, y, z]
  F =
  [ 3*\cos(t), 3*\sin(t), 5 - 3*\cos(t) ]
  >> x = x; y = y; z = z;
  >> F = [x, y, z]
  F =
  [ 3*\cos(t), 3*\sin(t), 5 - 3*\cos(t) ]
  >> X
  x =
  3*cos(t)
  >> x = x
  x =
  3*cos(t)
  >> delete x y z
  Warning: File 'x' not found.
Warning: File 'y' not found.
Warning: File 'z' not found.
  >> clear x y z
  >> F = [x, y, z]
  Undefined function or variable 'x'.
  >> syms x y z
  >> F = [x, y, z]
```

Exercise two part two

```
>> F = [x, y, z]
F =
[ x, y, z]
>> curl(F, [x, y, z])
ans =
0
0
0
0
>> dot(ans, ds) % Dot product with curl of 0 will be zero
Undefined function or variable 'ds'.
>> % Therefore integral over surface S using the curl will also result in 0
>> % The first integral is easier by hand because we don; t need to compute the curl of F
>> % which would require taking the cross product.
>> % However, the second one is easier numerically because the terms result in zero
>> % so it is easier for the computer to approximate it
```

Exercise two part three

Exercise Three



Exercise three