Introduction to Machine Learning K-means and Clustering Problems

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1. You are given five data samples:

i	1	2	3	4	5
x_{i1}	0	1	0	2	2
x_{i2}	0	0	1	2	3

- (a) Draw the five points.
- (b) Starting with K = 2 cluster centers at (0,0) and (1,0), what are the cluster assignments and new cluster centers after one iteration of K-means?
- 2. K-means for outlier detection. Write a function for outlier detection:

```
def outlier_detect(Xtr,Xts,nc,t):
    ...
    return outlier
```

The function should:

- Perform K-means clustering on the training data Xtr;
- Given the matrix of test data Xts, it sets an output outlier[i]=1 if the sample Xts[i,:] is greater than some distance t from all cluster centers.

Try to avoid for loops. You may assume you have the following functions:

- 3. Initialization. Write a few lines of python code to initialize K-means by selecting K random samples of the training data as the cluster centers. Make sure you do not pick the same sample twice.
- 4. Clustering as pre-processing. Suppose we want to cluster data and then fit a linear model in each cluster. You are given training data Xtr,ytr and test data Xts,yts for a regression problem. Write code to do the following:
 - Perform K-means clustering on the training data Xtr with a given number nc clusters;

- In each cluster in the training data, fit a linear model.
- Compute the predicted outputs yhat_ts and mean squared error of the model on the test data.

You may assume you have the following functions:

```
km = KMeans(n_cluster=nc)  # Creates a K—Means object
km.fit(X)  # Fits the k—means clusters
km.predict(X)  # Finds the index of the closest cluster

reg = LinearRegression()  # Creates a linear regression object
reg.fit(X,y)  # Fits the linear model
yhat = reg.predict(X)  # Predicts the output
```

Note: You may need a list of regression objects.