

High Level Parallel Programming

Programming with the STL

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The Standard Library

- Provides a collection of useful C++ classes and functions
 - ➤ Is itself implemented in C++
 - Part of the ISO C++ standard
 - Defines interface, semantics and contracts the implementation has to abide by (e.g. runtime complexity)
 - Implementation is not part of the standard
 - Multiple vendors provide their own implementations
 - Best known
 - libstdc++ (used by gcc)
 - libc++ (used by llvm)

The Standard Library

- > All features are declared within the std namespace
- Functionality is divided into sub-libraries each consisting of multiple headers
- > Includes parts of the C standard library
 - For backward compatibility
 - Headers begin with "c" (e.g., cstring)
 - Never use them unless you absolutely know what you are doing!

Features Overview

Most important library features

- Utilities
 - Memory management (new, delete, unique_ptr, shared_ptr)
 - Error handling (exceptions, assert)
 - Time (clocks, durations, timestamps, etc.)
 - Optionals, Variants, Tuples, etc.

Strings

- String class
- String views
- C-style string handling

Containers

Array, vector, lists, maps, sets

Features Overview

- Algorithms
 - (Stable) sort, search, max, min, ...
- > Iterators
- Numerics
 - Common mathematic functions (sqrt, pow, mod, log, etc.)
 - Complex numbers
 - Random number generation
- > I/O
 - Input-/Output streams
 - File streams
 - String streams

Features Overview

> Threads

- Thread class
- (shared) mutexes
- Futures

> Much more

- Localization
- Regex
- Atomics
- Filesystem support
- **.**...

Optionals

- std::optional is a class encapsulating a value that might or might not exist
 - Defined in the header <optional>
 - Some functions might fail or return without a valid result (e.g. looking up a non-existing file)
 - ➤ It's unfavorable to encode such failures with a value of the function domain (e.g., an empty string when file could not be read)
 - > It helps to express such results
 - At any point in time, an optional either has a value, or it doesn't
 - If the computation succeeded, it returns an optional containing a value

Optionals

- If it failed, it returns an optional without a value
- ➤ The template parameter T denotes, of which type the optional may contain a value
 - For example, optional<int> might contain an int
- Guarantees to not dynamically allocate any memory when being assigned a value
- Is an object, despite supporting the dereference operators * and ->
- ➤ Internally implemented as an object with a member of type T and a boolean

Optionals: Creations

```
std::optional<std::string> might_fail(int arg) {
  if (arg == 0) {
    return std::optional<std::string>("zero");
  } else if (arg == 1) {
    return "one"; // equivalent to the case above
  } else if (arg < 7) {
    // std::make_optional takes constructor arguments of type T
    return std::make_optional<std::string>("less than 7");
  } else {
    return std::nullopt; // alternatively: return {}
}
```

Optionals are created through its constructor or with std::make_optional

Optionals: Creations

```
might_fail(3).value(); // "less than 7"
might_fail(8).value();
// throws std::bad_optional_access

*might_fail(3); // "less than 7"
might_fail(6)->size(); // 11
might_fail(7)->empty(); // undefined behavior
```

The value of an optional can be read with value() (throws exception when empty) or dereferenced with * or -> (undefined behavior when empty)

Optionals: Checking and Accessing

```
might_fail(3).has_value(); // true
might_fail(8).has_value(); // false

// Or even simpler:
std::optional<std::string> opt5 = might_fail(5)
if (opt5) { //contextual conversion to bool
   opt5->size(); // 11
}
```

There are multiple ways to check whether an optional has a value

Pairs

- std::pair<T, U> is a template class that stores exactly one object of type T and one of type U
 - Defined in the header <utility>
 - Constructor takes object of T and U
 - Pairs can also be constructed with std::make_pair()
 - Objects can be accessed with first and second
 - Can be compared for equality and inequality
 - Can be compared lexicographically with <, <=, >, and >=

```
std::pair<int, double> p1(123, 4.56);
p1.first; // == 123
p1.second; // == 4.56

auto p2 = std::make_pair(456, 1.23);
// p2 has type std::pair<double, int>
p1 < p2; // true</pre>
```

Tuple

- std::tuple is a template class with n type template parameters that stores exactly one object of each of the n types.
 - Defined in the header <tuple>
 - Constructor takes all objects
 - Tuples can also be constructed with std::make_tuple()
 - > The ith object can be accessed with std::get<i>()
 - Just like pairs, tuples define all relational comparison operators

```
std::pair<int, double, char> t1(123, 4.56, 'x');
std::get<1>(t1); // == 4.56

auto t2 = std::make_tuple(456, 1.23, 'y');
// t2 has type std::tuple<int, double, char>
t1 < t2; // true</pre>
```

The STL Basic Model

manipulate data, but don't know about containers

Algorithms

Iterators

Algorithms and containers interact through iterators Each container has its own iterator types

store data, but don't know about algorithms

Containers

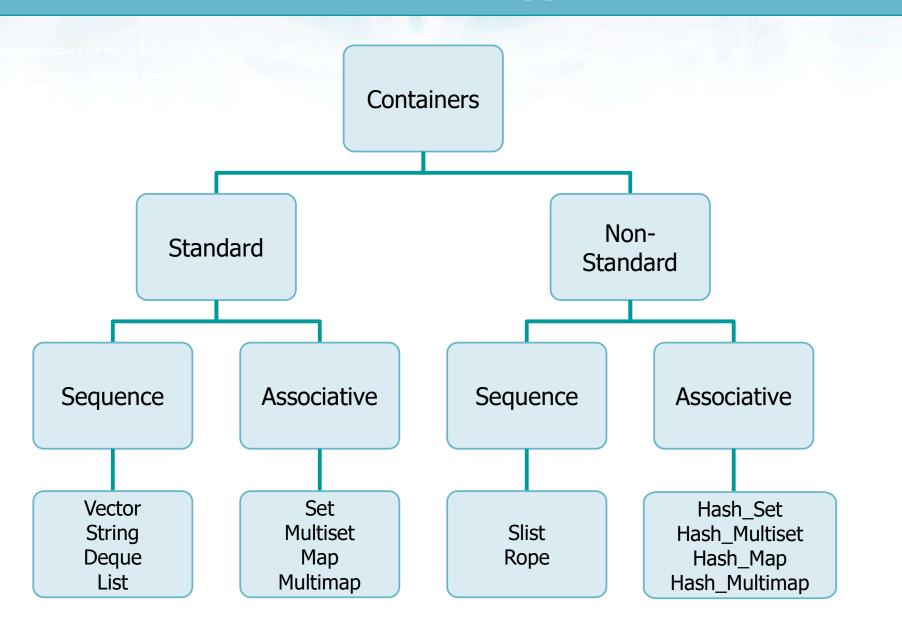
Containers

- A container is an object that stores a collection of other objects
 - Manage the storage space for their elements
 - Generic
 - The type(s) of elements stored are template parameter(s)
 - Provide member functions for accessing elements directly, or through iterators
 - (Most) member functions shared between containers

Containers

- Make guarantees about the complexity of their operations
 - Sequence containers (e.g. std::array, std::vector, std::list): Optimized for sequential access
 - Associative containers (e.g. std::set, std::map):
 Sorted, optimized for search (O(logn))
 - Unordered associative containers (e.g. std::unordered_set, std::unordered_map): Hashed, optimized for search
 - Amortized: O(1)
 - Worst case: O(n))
- Use containers whenever possible
 - When in doubt, use std::vector!

Types of Containers



Containers: std::vector

- Vectors are arrays that can dynamically grow
 - Defined in the header <vector>
 - > Elements are still stored contiguously
 - Elements can be inserted and removed at any position
 - Pre-allocates memory for a certain amount of elements
 - Allocates new, larger chunk of memory and moves elements when memory is exhausted
 - Memory for a given amount of elements can be reserved with reserve

Containers: std::vector

- > Time complexity
 - Random access
 - O(1)
 - Insertion and removal at the end
 - Typically: O(1)
 - Worst case: O(n) due to possible reallocation
 - Insertion and removal at any other position
 - O(n)
- Access to the underlying C-style data array with data member function

Containers: std::vector

- Vectors are constructed just like arrays
- Access elements via C-style array notation, via at(), or through a raw pointer
- Update elements via C-style array notation, via at(), or through a raw pointer
 - > Note
 - It is not possible to insert new elements this way
 - You can only update existing ones

```
std::vector<int> fib = {1,1,2,3};

fib.at(0) // == 1;
fib[1] // == 1;
int* fib_ptr = fib.data();
fib_ptr[2] // == 3;

fib[3] = 43;
fib.at(2) = 42;
fib.data()[1] = 41; // fib is now 1, 41, 42, 43
```

Containers: std::unordered_map

- Maps are associative containers consisting of keyvalue pairs
 - Defined in the header <unordered_map>
 - > Keys are required to be unique
 - > At least two template parameters
 - Key and T (type of the values)
 - > Is internally a hash table
 - Amortized O(1) complexity for random access, search, insertion, and removal

Containers: std::unordered_map

- No way to access keys or values in order (use std::map for that!)
- Accepts custom hash- and comparison functions through third and fourth template parameter
- Use std::unordered_map if you need a hash table, but don't need ordering

Containers: std::unordered_map

- Maps can be constructed pairwise
- Lookup the value to a key with C-style array notation, or with at()
- A pair can also be searched for with find
 - > To check if a key exists, use count

```
std::unordered_map<std::string,double> name_to_grade
{{"maier", 1.3}, {"huber", 2.7}, {"schmidt", 5.0}};

name_to_grade["huber"]; // == 2.7
name_to_grade.at("schmidt"); // == 5.0

auto search = name_to_grade.find("schmidt");
if (search != name_to_grade.end()) {
    // Returns an iterator pointing to a pair!
    search->first; // == "schmidt"
    search->second; // == 5.0
}
name_to_grade.count("schmidt"); // == 1
name_to_grade.count("blafasel"); // == 0
```

Containers: std::map

- In contrast to unordered maps, the keys of std::map are sorted
 - Defined in the header <map>
 - Interface largely the same to std::unordered_map
 - Optionally accepts a custom comparison function as template parameter
 - ➤ Is internally a tree (usually AVL- or R/B-Tree)
 - O(log n) complexity for random access, search, insertion, and removal

Containers: std::map

- std:map also allows to search for ranges
 - upper_bound(key) returns an iterator pointing to the first greater element than key
 - lower_bound(key) returns an iterator pointing to the first element **not lower** than key

```
std::map<int, int> x_to_y = {{1, 1}, {3, 9}, {7, 49}};

// gt3 points to {7, 49}
auto gt3 = x_to_y.upper_bound(3);

// geq3 points to {3, 9}
auto geq3 = x_to_y.lower_bound(3);
```

Containers: Thread Safety

- Containers give some thread safety guarantees:
 - Two different containers: All member functions can be called concurrently by different threads (i.e. different containers don't share state)
 - ➤ The same container: All const member functions can be called concurrently. at(), [] (expect in associative containers), data(), front()/back(), begin()/end(), find() also count as const
 - ➤ Iterator operations that only read (e.g. incrementing or dereferencing an iterator) can be run concurrently with reads of other iterators and const member functions
 - Different elements of the same container can be modified concurrently

Containers: Thread Safety

Be careful

As long as the standard does not explicitly require a member function to be sequential, the standard library implementation is allowed to parallelize it internally (see e.g. std::transform vs. std::for_each)

Rule of thumb

- Simultaneous reads on the same container are always okay
- Simultaneous read/writes on different containers are also okay
- Everything else requires synchronization

Iterators

- Iterators are objects that can be thought of as pointer abstractions
 - > Problem
 - Different element access methods for each container
 - > Therefore
 - Container types not easily exchangeable in code
 - > Solution
 - Iterators abstract over element access and provide pointer-like interface

Iterators

- Allow for easy exchange of underlying container type
- The standard library defines multiple iterator types as containers have varying capabilities (random access, traversable in both directions, etc.)

Be careful

When writing to a container, all existing iterators are invalidated and can no longer be used (some exceptions apply)

Iterators: An Example

```
std::vector<std::string> vec = {"one", "two", "three", "four"};
std::vector<std::string>::iterator it = vec.begin();
auto end = vec.end();
std::cout << *it; // prints "one"</pre>
std::cout << it->size(); // prints 3
std::cout << *end; // undefined behavior</pre>
++it; // Prefer to use pre-increment
std::cout << *it; // prints "two"</pre>
// prints "three, four, "
while (it != end) {
   std::cout << *it << ",";
   it++;
// available also in the range expression (C++11 and +)
for (auto elem : vec) {
     std::cout << elem << ","; // prints "one, two, three, four,"</pre>
```

Iterators: An Example

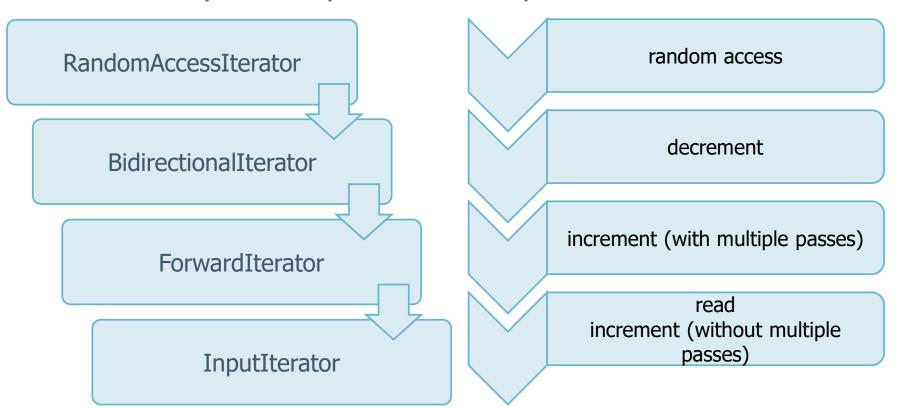
```
std::vector<std::string> vec = {"one", "two", "three", "four"};
std::vector<std::string>::iterator it = vec.begin();
auto end = vec.end();
std::cout <<
std::cout <<
                 Such a loop requires the range expression (here:
                 vec) to have a begin() and end() member.
std::cout <
                 vec.begin() is assigned to an internal iterator which
                  is dereferenced, assigned to the range declaration
++it; // Pre
std::cout <
                  (here: auto elem), and then incremented until it
                 equals vec.end().
// prints "t
while (it != ena) {
   std::cout << *it ·
   it++;
// available also in the range expression (C++11 and +)
for (auto elem : vec) {
     std::cout << elem << ","; // prints "one, two, three, four,"</pre>
```

Iterators: An Advanced Example

```
std::vector<std::string> vec = {"one", "two", "three", "four"};
for (it = vec.begin(); it != vec.end(); ++it) {
  // (*it).size
   if (it->size == 3) {
       it = vec.insert(it, "foo");
       // it now points to the newly inserted element
       ++it;
//vec == {"foo", "one", "foo", "two", "three", "four"}
for (it = vec.begin(); it != vec.end(); ++it) {
   if (it->size == 3) {
       it = vec.erase(it);
       // erase returns a new, valid iterator
       // pointing at the next element
//vec == {"three", "four"}
```

Iterators Hierarchy

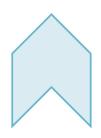
- Iterators are instantiation of classes
 - > It exist a hierarchy of Iterators
 - They differ by the kind of operations allowed



Iterators Hierarchy

- Iterators are instantiation of classes
 - > It exist a hierarchy of Iterators
 - They differ by the kind of operations allowed

OutputIterator



write increment (without multiple passes)

Iterators: Input and Output

- Input- and OutputIterator are the most basic iterators
- They have the following features
 - > Equality comparison
 - Checks if two iterators point to the same position
 - Dereferencable with the * and -> operators
 - Incrementable, to point at the next element in sequence
 - > A dereferenced **InputIterator** can only by read
 - ➤ A dereferenced **OutputIterator** can only be written to

Iterators: Input and Output

- As the most restrictive iterators, they have a few limitations
 - Single-pass only
 - They cannot be decremented
 - Only allow equality comparison, <, >=, etc. not supported
 - Can only be incremented by one (i.e., it + 2 does not work)
- Used in single-pass algorithms such as find() (InputIterator) or copy() (Copying from an InputIterator to an OutputIterator)

Iterators: Forward and Bidirectional

- ForwardIterator combines InputIterator and OutputIterator
 - All the features and restrictions shared between input- and output iterator apply
 - > Dereferenced iterator can be read and written to
- BidirectionalIterator generalizes ForwardIterator
 - Additionally allows decrementing (walking backwards)
 - Therefore supports multi-pass algorithms traversing the container multiple times
 - > All other restrictions of ForwardIterator still apply

Iterators: Random

- RandomAccessIterator generalizes BidirectionalIterator
 - Additionally allows random access with operator[]
 - Supports relational operators, such as < or >=
 - ➤ Can be incremented or decremented by any amount (i.e. it + 2 does work)

Function Objects

- Regular functions are not objects in C++
 - Cannot be passed as parameters (unless a function pointer is allowed
 - Cannot have state
- C++ additionally defines the FunctionObject named requirement
- For a type T to be a FunctionObject
 - > T has to be an object
 - operator()(args) has to be defined for T for a suitable argument list args which can be empty
 - Often referred to as functors

Function Objects

- There are several valid function objects defined in C++
 - Pointers to functions
 - Lambda expressions
 - > Stateful function objects in form of classes
- Functions and function references are not function objects
 - Can still be used in the same way due to implicit function-to-pointer conversion

Function Pointers

- While functions are not objects, they do have an address
 - Location in memory where the actual assembly code resides
 - > Allows declaration of function pointers
- Function pointers to non-member functions
 - Declaration
 - return-type (*identifier)(args)
 - Allows passing functions as parameters
 - E.g., passing a custom compare function to std::sort
 - E.g., passing a callback to a method
- Can be invoked in the same way as a function

Function Pointers

```
int callFunc(int (*func)(int, int), int arg1, int arg2) {
 return (*func)(arg1, arg2);
double callFunc(double (*func)(double), double argument) {
 return func(argument); // Automatically dereferenced
int add(int arg1, int arg2) { return arg1 + arg2; }
double add4(double argument) { return argument + 4; }
int main() {
  auto i = callFunc(add, 2, 4); // i = 6
  auto j = callFunc(&add4, 4); // j = 8, "&" can be omitted
```

Lambda Expressions

- Function pointers can be unwieldy
 - > Function pointers cannot easily capture environment
 - Must pass all variables that affect function by parameter
 - Cannot have "local" functions within other functions
- C++ defines lambda expressions as a more flexible alternative
 - Lambda expressions construct a closure
 - Closures store a function together with an environment
 - Lambda expressions can capture variables from the scope where they are defined

Lambda Expressions

Lambda expression syntax

```
[ captures ] ( params ) -> ret { body }
```

- > captures specifies the parts of the environment that should be stored
- params is a comma-separated list of function parameters
- ret specifies the return type and can be omitted, in which case the return type is deduced from return statements inside the body

Lambda Expressions

- The list of captures can be empty
 - Results in stateless lambda expression
 - Stateless lambda expressions are implicitly convertible to function pointers
- Lambda expressions have unique unnamed class type
 - Must use auto when assigning lambda expressions to variables
 - Declaration of a lambda variable (e.g. as member) is not possible

Lambda Expression

```
int callFunc(int (*func)(int, int), int arg1, int arg2) {
     return func(arg1, arg2);
int main() {
  auto lambda = [](int arg1, int arg2) {
          return arg1 + arg2;
  };
  int i = callFunc(lambda, 2, 4); // i = 6
  int j = lambda(5, 6); // j = 11
```

Lambda Expression: Uniqueness constraint

```
// ERROR: Compilation will fail due to ambiguous return type
auto getFunction(bool first) {
  if (first) {
    return []() {
      return 42;
  } else {
    return []() {
      return 42;
                             All lambda
    };
                           expressions have
                             unique types
```

Lambda Expressions: Captures

- Lambda captures specify what constitutes the state of a lambda expression
 - Can refer to automatic variables in the surrounding scopes (up to the enclosing function)
 - Can refer to the "this" pointer in the surrounding scope (if present)
- Captures can either capture by-copy or by-reference
 - Capture by-copy creates a copy of the captured variable in the lambda state
 - Capture by-reference creates a reference to the captured variable in the lambda state
 - Captures can be used in the lambda expression body like regular variables or references

Lambda Expressions: Captures

- Lambda captures are provided as a commaseparated list of captures
 - By-copy
 - identifier or identifier initializer
 - > By-reference
 - & identifier or & identifier initializer
 - identifier must refer to automatic variables in the surrounding scopes
 - identifier can be used as an identifier in the lambda body
 - > Each variable may be captured only once

Lambda Expressions: Captures

- First capture can optionally be a capture-default
 - By-copy
 - =
 - By-reference
 - **&**
- Allows any variable in the surrounding scopes to be used in the lambda body
- Specifies the capture type for all variables without explicit captures
- If present, only diverging capture types can be specified afterwards

Lambda Expression: Captures

```
int main() {
  int i = 0;
  int j = 42;
  auto lambda1 = [i](){}; // i by-copy
  auto lambda2 = [&i](){};  // i by-reference
  auto lambda3 = [&j, i](){}; // j by-reference, i by-copy
  auto lambda4 = [=, \&i](){}; // j by-copy, i by-reference
  // ERROR: non-diverging capture types
  auto lambda5 = [\&, \&i]()\{\};
  // ERROR: non-diverging capture types
  auto lambda6 = [=, i](){};
```

Lambda Expression: Captures

```
int main() {
  int i = 42;
  auto lambda1 = [i]() { return i + 42; };
  auto lambda2 = [&i]() { return i + 42; };

i = 0;
  int a = lambda1(); // a = 84
  int b = lambda2(); // b = 42
}
```

Be careful, the capture is done at definition, thus if you capture by-copy the value is persistent, otherwise (by-reference) the reference is persistent

Lambda Expression: Captures

```
#include <memory>
int main() {
   auto ptr = std::make_unique<int>(4);
   auto f2 = [inner = ptr.get()]() { return *inner;};
   int a = f2(); //4
   ptr.reset();
   int b = f2(); // undefined behavior
}
```

Lifetime issues due to capturing...

Stateful Function Objects

- Situation so far
 - > Functions are generally stateless
 - State must be kept in surrounding object, e.g., class instances
 - Lambda expressions allow limited state-keeping
- Function objects can be implemented in a regular class
 - Allows the function object to keep arbitrary state
 - Difference to lambda expressions
 - State can be changed during lifetime

Stateful Function Objects: std::function

- std::function is a general-purpose wrapper for all callable targets
 - Defined in the <functional> header
 - > Able to store, copy and invoke the wrapped target
 - Potentially incurs dynamic memory allocations
 - Often adds unnecessary overhead
 - Should be avoided where possible

Stateful Function Objects: std::function

```
#include <functional>
std::function<int()> getFunction(bool first) {
 int a = 14;
 if (first)
    return [=]() { return a; };
 else
    return [=]() { return 2 * a; };
int main() {
 return getFunction(false)() + getFunction(true)(); // 42
```

The Algorithms Library

- The algorithms library is part of the C++ standard library
 - Defines operations on ranges of elements [first, last)
 - Bundles functions for sorting, searching, manipulating, etc.
 - Ranges can be specified using pointers or any appropriate iterator type
 - Spread in 4 headers
 - <algorithm>
 - <numeric>
 - <memory>
 - <cstdlib>
- We will focus on <algorithm> as it bundles the most relevant parts

std::sort

- Sorts all elements in a range [first, last) in ascending order
 - void sort(RandomIt first, RandomIt last);
 - Iterators must be RandomAccessIterators
 - Elements must be swappable (std::swap or userdefined swap)
 - Elements must be move-assignable and moveconstructible
 - Does not guarantee order of equal elements
 - Needs O(n * log(N)) comparisons

std::sort

```
// using custom comparison
#include <algorithm>
#include <vector>
int main() {
   std::vector<unsigned> v =
                     {3, 4, 1, 2};
   std::sort(v.begin(),
            v.end(),
            [] (unsigned lhs,
                unsigned rhs) {
                return lhs > rhs;
            }); // 4, 3, 2, 1
```

std::sort

```
// using default comparison
// operator
#include <algorithm>
#include <vector>

    Sorting algorithms can be modified

int
      through custom comparison functions

    Supplied as function objects

          (Compare named requirement)

    Must establish a strict weak ordering

                 on the elements
                    • Syntax:
      bool cmp(const Type1 &a, const Type2
                      &b);

    Return true if and only if a and be

                 must be swaped
```

```
// using custom comparison
#include <algorithm>
#include <vector>
int main() {
   std::vector<unsigned> v =
                     {3, 4, 1, 2};
   std::sort(v.begin(),
            v.end(),
            [] (const unsigned &lhs,
            const unsigned &rhs) {
                return lhs > rhs;
            }); // 4, 3, 2, 1
```

Further Sorting

- Sometimes std::sort may not be the optimal choice
 - Does not necessarily keep order of equal-ranked elements
 - Sorts the entire range (unnecessary e.g. for top-k queries)
- Keep the order of equal-ranked elements
 - > std::stable_sort
- Partially sort a range
 - > std::partial_sort
- Check if a range is sorted
 - > std::is_sorted
 - > std::is_sorted_until

Searching

- The algorithms library offers a variety of searching operations
 - Different set of operations for sorted and unsorted ranges
 - Searching on sorted ranges is faster in general
 - Sorting will pay off for repeated lookups
- Arguments against sorting
 - > Externally prescribed order that may not be modified
 - > Frequent updates or insertions
- General semantics
 - Search operations return iterators pointing to the result
 - Unsuccessful operations are usually indicated by returning the end iterator of a range [first, last)

Searching

- Find the first element satisfying some criteria
 - > std::find
 - > std::find if
 - > std::find_if_not
- Search for a range of elements in another range of elements
 - > std::search
- Count matching elements
 - > std::count
 - > std::count_if
- Many more useful operations (see reference documentation)

std::find, std::find_if

```
#include <algorithm>
#include <vector>
int main() {
   std::vector<int> v = \{2, 6, 1, 7, 3, 7\};
   auto res1 = std::find(vec.begin(), vec.end(), 7);
   int a = std::distance(vec.begin(), res1);
   // a = 3 is the index distance between Iterator begin() and res1
   auto res2 = std::find(vec.begin(), vec.end(), 9);
   if(res2 == vec.end()
       std::cout << "Not found!";</pre>
   auto res1 = std::find if(vec.begin(),
                             vec.end(),
                             [](int val) { return (val % 2) == 1; }
   int a = std::distance(vec.begin(), res1); // 2
```

Searching: sorted ranges

- On sorted ranges, binary search operations are offered
 - Complexity O(log(N)) when range is given as RandomAccessIterator
 - Can employ custom comparison function (see above)
 - When called with ForwardIterators complexity is linear in number of iterator increments
- Search for one occurrence of a certain element
 - > std::binary_search
- Search for range boundaries
 - std::lower_bound
 - std::upper_bound
- Search for all occurrences of a certain element
 - > std::equal_range
- Certain Containers already implement (some of) them!

Permutations

- The algorithms library offers operations to permute a given range
 - > Can iterate over permutations in lexicographical order
 - > Requires at least BidirectionalIterators
 - Values must be swappable
 - Order is determined using operator< by default</p>
 - ➤ A custom comparison function can be supplied (see above)
- Initialize a dense range of elements
 - > std::iota
- Iterate over permutations in lexicographical order
 - > std::next_permutation
 - > std::prev_permutation

Additional Functionalities

- The algorithms library offers many more operations
 - > std::min & std::max over a range instead of two elements
 - std::merge & std::in_place_merge for merging of sorted ranges
 - Multiple set operations (intersection, union, difference, ...)
 - Heap functionality
 - Sampling of elements using std::sample
 - Swapping elements using std::swap
 - Range modifications
 - std::copy To copy elements to new location
 - std::rotate To rotate range
 - std::shuffle To randomly reorder elements
- For even more operations see the reference documentation