

**B.E COMPUTER SCIENCE AND ENGINEERING 3rd YEAR 1st SEMESTER
EXAMINATION 2021**

Formal Languages and Automata Theory

Full Marks: 100

The question paper is divided in **Part A & Part B**. All questions from both parts are to be answered.

Duration: **5 hours** including time for downloading the question paper and uploading the answer script

Start Time & Date: 11:00 AM on 25 Jan 2021

Part A

Full Marks: 70

1(a) Design a Turing Machine (TM) to determine whether an even length binary string is a palindrome.

(b) Define Recursively Enumerable languages and Recursive languages. Are all Recursively Enumerable languages Recursive? Under what condition a Recursively Enumerable language can be Recursive?

10+4

Or

State the Halting Problem for Turing Machines. Prove that the Halting Problem is undecidable.

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2(a) Let **w** be the yield of a Parse tree formed by a grammar in Chomsky Normal Form. Also assume that the length of the longest path in the Parse tree is **n**. Then prove that $|w| \leq 2^{n-1}$.

(b) State the Pumping lemma for Context Free Languages (CFLs)

(c) Using the Pumping lemma, prove that

$$L = \{0^{n \cdot m} \mid n \text{ and } m \text{ are prime numbers}\}$$

is not a CFL.

4+2+4.5

3(a) Give the state diagram of a Push Down Automaton (PDA) to accept $\{0^{2n}1^{3n} \mid n > 0\}$

(b) Eliminate ϵ -productions from the following Context Free Grammar:

$$\begin{aligned} S &\rightarrow aXbY \\ X &\rightarrow aX \mid \epsilon \\ Y &\rightarrow bY \mid \epsilon \end{aligned}$$

(c) Give a Context Free Grammar (CFG) that generates

$$L = \{w \in \{0,1\}^* \mid w \text{ contains at least three 1's}\}$$

5+3+2.5

4(a) Prove that Regular languages are closed under Reversal.

(b) Given $E = 01^* + 10^*$, find E^R where R denotes Reversal of a Regular Expression.

4+3

5. Prove that if a Deterministic finite Automaton (DFA) has **n** states then there is a string of length in $[n, 2n-1]$, which is in $L(A)$, and the language $L(A)$ is infinite.

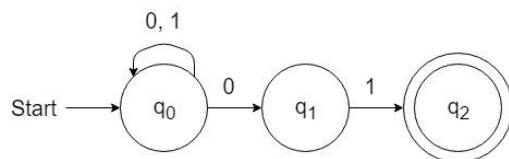
10.5

6(a) Construct a minimum state Deterministic Finite Automaton (DFA) for the following:

	0	1
A	B	C
B	A	D
*C	E	F
*D	E	F
*E	E	F
F	F	F

Asterisk marked states in the above State- transition-table are accept/final states

- (b) Give a DFA with $\Sigma = \{0, 1, 2\}$ to accept any string with 001 as a substring
(c) Give the language accepted by the following Nondeterministic Finite Automaton (NFA)



Construct a DFA equivalent to the NFA shown above.

8+3+6.5

Part B Full Marks: 30

1. Define Universal Turing Machine (UTM) and discuss its implementation.

6

- 2(a) Prove that Context Free Languages (CFLs) are not closed under intersection.

- (b) How would you check if a CFL is infinite?

3+1.5

- 3(a) Give a Context Free Grammar (CFG) to define the language $\{a^i b^j c^k | i, j, k \geq 0 \text{ & } i+j=k\}$

- (b) Give the transition diagram of the Push Down Automata (PDA) that accepts the language defined by the following grammar:

$$\begin{aligned} S &\rightarrow aAA \\ A &\rightarrow aS|bS|a \end{aligned}$$

2.5+2

4. Assuming that L is a Regular language and h is a homomorphism on its alphabet, define h(L).

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5. Using Pumping Lemma, prove that $L=\{0^{n!} | n \geq 0\}$ is not a Regular language.

4.5

6(a) Given an arbitrary Non -deterministic Finite Automaton (NFA) with n states, the maximum number of states in an equivalent minimized DFA is

- (i) n^2
- (ii) 2^n
- (iii) $2n$
- (iv) $n!$

Explain your answer.

(b) Give a Regular expression representing all binary strings with an odd number of 1's.

4.5+3