```
In\{*\}:= X[\mathcal{E}] := \frac{c}{H0 \operatorname{Sqrt} \left[\Omega m \left(1+\mathcal{E}\right)^{3} + \Omega \Lambda + \left(1-\Omega m - \Omega \Lambda\right) \left(1+\mathcal{E}\right)^{2}\right]}
                    (*use \xi until we integrate the function, then switch to z*)
  ln[*]:= seriesExpansion = x[0] + \xi x'[0] + \frac{\xi^2}{2} x''[0] (*expansion of the stuff inside the integral*)
Out[0]=
                In[@]:= xSeries[z] := Integrate[seriesExpansion, g] /. {g \rightarrow z};
                 Print["Series Expansion for \chi: ", xSeries[z]](*integrated series,
                 so this is the series we will be using for X. switch variables to z_\star)
                   Series Expansion for \chi:
                      \frac{c\;z}{\text{H0}}\;-\;\frac{3\;c\;z^2\;\Omega\text{m}}{4\;\text{H0}}\;+\;\frac{c\;z^3\;\left(3\;\Omega\text{m}\;+\;2\;\left(1\;-\;\Omega\text{m}\;-\;\Omega\Lambda\right)\;\right)^2}{8\;\text{H0}}\;-\;\frac{c\;z^3\;\left(6\;\Omega\text{m}\;+\;2\;\left(1\;-\;\Omega\text{m}\;-\;\Omega\Lambda\right)\;\right)}{12\;\text{H0}}\;-\;\frac{c\;z^2\;\left(1\;-\;\Omega\text{m}\;-\;\Omega\Lambda\right)}{2\;\text{H0}}
   In[@]:= dH0[z_] := D[xSeries[z], H0];
                Print \left[ \frac{\partial \chi}{\partial u} = \frac{\partial \chi}{\partial u} \right] (*write out our three partial derivatives*)
                d\Omega m[z_{-}] := D[xSeries[z], \Omega m]; Print[" <math>\frac{\partial \chi}{\partial \Omega m} = ", d\Omega m[z]]
                d\Omega\Lambda[z_{-}] := D[xSeries[z], \Omega\Lambda];
                Print \Big[ \frac{\partial \chi}{\partial \Omega} = 0, \, d\Omega \Lambda[z] \Big]
                \begin{split} \frac{\partial \chi}{\partial \Omega m} & = & -\frac{c \ z^2}{4 \ H0} - \frac{c \ z^3}{3 \ H0} + \frac{c \ z^3 \ (3 \ \Omega m + 2 \ (1 - \Omega m - \Omega \Lambda) \ )}{4 \ H0} \\ \frac{\partial \chi}{\partial \Omega \Lambda} & = & \frac{c \ z^2}{2 \ H0} + \frac{c \ z^3}{6 \ H0} - \frac{c \ z^3 \ (3 \ \Omega m + 2 \ (1 - \Omega m - \Omega \Lambda) \ )}{2 \ H0} \end{split}
   In[a]:= FisherM[z] := { dH0[z] × dH0[z], dH0[z] × d\Omegam[z], dH0[z] × d\Omega\Left[z]},
                                                           \{d\Omega m[z] \times dHO[z], d\Omega m[z] \times d\Omega m[z], d\Omega m[z] \times d\Omega \Lambda[z]\},
                                                           \{d\Omega\Lambda[z]\times dH0[z], d\Omega\Lambda[z]\times d\Omega m[z], d\Omega\Lambda[z]\times d\Omega\Lambda[z]\}\}
   In[*]:= Simplify[FisherM[z]] // MatrixForm
Out[]//MatrixForm=
                  = \frac{\frac{c^2 \ z^2 \ \left(24 - 6 \ z \ \left(2 + \Omega m - 2 \ \Omega \Lambda\right) + z^2 \ \left(8 + 4 \ \Omega m + 3 \ \Omega m^2 - 20 \ \Omega \Lambda - 12 \ \Omega m \ \Omega \Lambda + 12 \ \Omega \Lambda^2\right)\right)^2}{576 \ H0^4} }{ 576 \ H0^4} \\ = \frac{c^2 \ z^3 \ \left(-3 + z \ \left(2 + 3 \ \Omega m - 6 \ \Omega \Lambda\right)\right) \ \left(24 - 6 \ z \ \left(2 + \Omega m - 2 \ \Omega \Lambda\right) + z^2 \ \left(8 + 4 \ \Omega m + 3 \ \Omega m^2 - 20 \ \Omega \Lambda - 12 \ \Omega m \ \Omega \Lambda + 12 \ \Omega \Lambda^2\right)\right)}{288 \ H0^3} \\ = \frac{c^2 \ z^3 \ \left(-3 + z \ \left(5 + 3 \ \Omega m - 6 \ \Omega \Lambda\right)\right) \ \left(24 - 6 \ z \ \left(2 + \Omega m - 2 \ \Omega \Lambda\right) + z^2 \ \left(8 + 4 \ \Omega m + 3 \ \Omega m^2 - 20 \ \Omega \Lambda - 12 \ \Omega m \ \Omega \Lambda + 12 \ \Omega \Lambda^2\right)\right)}{144 \ H0^3}
```

 $ln[a]:= \text{vars} = \{HO \rightarrow 70, \Omega m \rightarrow 0.3, \Omega \Lambda \rightarrow 0.7, c \rightarrow 1\}; (*assign values to all the variables*)$

```
ln[*]:= fisherSum = \frac{\text{FisherM}[0.01]}{(0.01 \text{ xSeries}[0.01])^2} + \frac{\text{FisherM}[0.1]}{(0.01 \text{ xSeries}[0.1])^2} + \frac{ln[*]:=}{(0.01 \text{ xSeries}[0.1])^2} + \frac{ln
                                                      \frac{\text{FisherM}[0.2]}{(0.01 \, \text{xSeries}[0.2])^2} + \frac{\text{FisherM}[0.3]}{(0.01 \, \text{xSeries}[0.3])^2} /. \, \text{vars; fisherSum // MatrixForm}
Out[]//MatrixForm=
                                            8.16327 25.3626 -40.0625
                                           25.3626 123.075 - 188.545
                                          -40.0625 -188.545 290.053
      In[@]:= CovarianceM = Inverse[fisherSum]; CovarianceM // MatrixForm
Out[]//MatrixForm=
                                          0.577383 0.762929 0.57568
                                         0.762929 2.95275 2.02477
                                      0.57568 2.02477 1.39913
      In[@]:= Print["H0 = ", Around[H0 /. vars, Sqrt[CovarianceM[1, 1]]]]]
                                  Print["\Omegam = ", Around[\Omegam /. vars, Sqrt[CovarianceM[2, 2]]]]
                                  Print["\Omega\Lambda = ", Around[\Omega\Lambda /. vars, Sqrt[CovarianceM[3, 3]]]]
                                        H0 = 70.0 \pm 0.8
                                        \Omega m = 0.3 \pm 1.7
                                        \Omega\Lambda = 0.7 \pm 1.2
```