Problem 1. (10 points):

Consider the source code below, where M and N are constants declared with #define.

```
int mat1[M][N];
int mat2[N][M];

int sum_element(int i, int j)
{
  return mat2[i][j] += mat1[j][i];
}
```

A. Suppose the above code generates the following assembly code:

```
sum_element:
       movslq %edi, %rdi
       movslq %esi, %rsi
       leaq 0(,%rdi,8), %rax
       subq %rdi, %rax
       leaq (%rdi,%rax,4), %rdx
       leaq (%rsi,%rsi,8), %rax
       leaq (%rsi, %rax, 2), %rax
       addq %rsi, %rdx
       leaq (%rax, %rdi), %rdi
            mat2(,%rdx,4), %eax
       movl
       addl mat1(,%rdi,4), %eax
       movl
            %eax, mat2(,%rdx,4)
       ret
```

What are the values of M and N?

M =

N =

Problem 2. (10 points):

Consider the following assembly code for a C for loop:

```
decode_me:
       cmpl
             %esi, %edi
              .L5
       jle
       leal
              (%rdi,%rdi), %edx
             $1, %eax
       movl
       subl %esi, %edx
.L4:
       subl $1, %edi
       addl
             $4, %esi
       addl %edx, %eax
             $6, %edx
       subl
           %esi, %edi
       cmpl
              .L4
       jg
              $46, %eax
       addl
       ret
.L5:
       movl $47, %eax
       ret
```

Based on the assembly code above, fill in the blanks below in its corresponding C source code. (Note: you may only use the symbolic variables x, y, and result in your expressions below — do not use register names.)

```
int decode_me(int x, int y)
{
  int result;
  for (result = 1; ______; x--, y = y + 4 ) {
    _____;
  }
  return _____;
}
```

Problem 3. Stack Discipline (20 points)

Examine the following recursive function:

```
long sunny(long a, long *b) {
  long temp;
  if (a < 1) {
    return *b - 8;
  } else {
    temp = a - 1;
    return temp + sunny(temp - 2, &temp);
  }
}</pre>
```

Here is the x86 64 assembly for the same function:

0000000000400536 <sunny>:

```
400536:
                      %rdi,%rdi
               test
400539:
                      400543 <sunny+0xd>
               jg
40053b:
                      (%rsi),%rax
              mov
                      $0x8,%rax
40053e:
               sub
                                                       Breakpoint
400542:
              retq
400543:
                      %rbx
              push
400544:
                      $0x10,%rsp
               sub
400548:
                      -0x1(%rdi),%rbx
               lea
40054c:
                      %rbx,0x8(%rsp)
              mov
400551:
              sub
                      $0x3,%rdi
400555:
              lea
                      0x8(%rsp),%rsi
40055a:
                     400536 <sunny>
              callq
40055f:
                      %rbx,%rax
               add
400562:
               add
                      $0x10,%rsp
400566:
              pop
                      %rbx
400567:
              retq
```

We call sunny from main(), with registers %rsi = 0x7ff...ffad8 and %rdi = 6. The value stored at address 0x7ff...ffad8 is the long value 32 (0x20). We set a <u>breakpoint</u> at "return *b - 8" (i.e. we are just about to return from sunny() without making another recursive call). We have executed the sub instruction at 40053e but have not yet executed the retq.

Fill in the register values on the next page and draw what the stack will look like when the program hits that breakpoint. Give both a description of the item stored at that location and the value stored at that location. If a location on the stack is not used, write "unused" in the Description for that address and put "-----" for its Value. You may list the Values in hex or decimal. Unless preceded by 0x we will assume decimal. It is fine to use f...f for sequences of f's as shown above for f. Add more rows to the table as needed. Also, fill in the box on the next page to include the value this call to sunny will finally return to main.

Register	Original Value	Value at Breakpoint
rsp	0x7ffffad0	
rdi	6	
rsi	0x7ffffad8	
rbx	4	
rax	5	

DON'T	
FORGET	-

What value is **finally** returned to **main** by this call?

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Memory address on stack	Name/description of item	Value
0x7fffffffffffad8	Local var in main	0x20
0x7fffffffffffad0	Return address back to main	0x400827
0x7fffffffffffac8		
0x7fffffffffffac0		
0x7fffffffffffab8		
0x7fffffffffffab0		
0x7fffffffffffaa8		
0x7fffffffffffaa0		
0x7fffffffffffa98		
0x7fffffffffffa90		
0x7fffffffffffa88		
0x7fffffffffffa80		
0x7fffffffffffa78		
0x7fffffffffffa70		
0x7fffffffffffa68		
0x7fffffffffffa60		

Problem 4. (4+6 points):

A. Consider an implementation of a processor where the combinational circuit latency is α ns (nanosecond). You are going to pipeline this implementation, and in your system the latency of each pipeline register is β ns. If you are to divide this entire combinational circuit in k stages, what is the throughput of your pipelined implementation? What about the total latency of a single instruction?

B. Now, assume that the parameters α , β and k described above have the following relation:

$$\beta = \begin{cases} \alpha/10 & \text{if } k \le 5, \\ \alpha/10 + k/50 \bullet 9\alpha/10 & \text{if } k > 5. \end{cases}$$
 (1)

Based on the equation above, clearly present an analysis when would you pipeline this processor. Please consider three different values of k in your analysis: (i) k = 5; (ii) k = 50; and (iii) k = 500.