# Week 11

# Kinetics

## 11.1 Experimental Determination of Kinetic Isotope Effects

- Lecture 18 recap.

  - The physical basis and mechanistic interpretation of kinetic isotope effects.
  - We also began discussing independent absolute rate measurement.
    - Alex reviews the discussion associated with Figure 10.18.

- Today: Experimental determination of KIEs.

  - All of these examples are pulled from Simmons and Hartwig (2012).

- Topic 2: Competition experiments.

  - Can be run a couple of different ways.
  - Most simple/natural progression from independent absolute rate measurement: Intermolecular competition.
  - Then there is intramolecular competition.

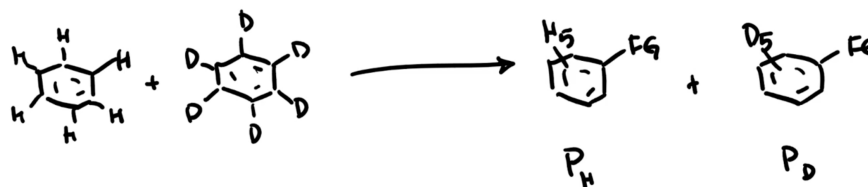- Subtopic 2.1: Intermolecular competition.



Figure 11.1: Competition experiment (intermolecular).

  - Instead of running the protonated and deuterated substrates independently, throw them into the same pot at the same time.
  - Take half an equivalent of the normal substrate and half an equivalent of the perdeuterated substrate.
    - It doesn't have to be half an equivalent, but this makes the analysis easier.
    - We also don't have to use the perdeuterated substrate, but it's often the easiest to make.
  - We then measure the ratio of undeuterated functionalized product vs. the deuterated functionalized product.

  – We can then extract our KIE from the $[P_H]/[P_D]$ ratio.
  – Caveat (this reaction is frequently run incorrectly in the literature!): We have to account for the fact that the concentrations of the starting materials are changing throughout.
    ■ Indeed, the product and starting material are highly dependent on the conversion.
    ■ The ratio of the products is equal to the ratio of the starting materials at high conversion.
    ■ However, if we only run the reaction to low conversion, we can assume that the concentration of the starting material hasn't changed too much! Thus, the product ratio will reflect the actual KIE.
  – We can quantify products by NMR, LC-MS, GC-MS, etc.!
    ■ So this reaction is experimentally simple to do because products are easy to quantify.
  – We can measure extremely small KIEs because our product-detection methods are so good!
  – There is a contrasting paradigm in which we run to large conversions and characterize the remaining starting material ratio at the end.
    ■ We'll get there later in the lecture.

• We have to apply a correction for conversion to extract the KIE at any conversion.

  – Define

$$C := \frac{[P_H]}{[SM_H]_0} \qquad\qquad R := \left(\frac{[SM_D]}{[SM_H]}\right)_t \qquad\qquad R_0 := \left(\frac{[SM_D]}{[SM_H]}\right)_0$$

    ■ $C$ is the conversion.
      ➢ From the definition, we can tell that it is a number between 0 and 1.
    ■ $R$ gives the isotopic enrichment at any moment $t$.
    ■ $R_0$ is the initial isotopic enrichment.
  – Thus, we can do some algebra to get a correction term that allows us to calculate the KIE from any time point.

$$\frac{R}{R_0} = (1-C)^{k_D/k_H - 1}$$

$$\text{KIE} = \frac{k_H}{k_D} = \frac{\ln(1-C)}{\ln\left[(1-C)\cdot\frac{R}{R_0}\right]}$$

  – Takeaways.
    ■ If we can extract both the conversion $C$ and isotopic composition $R/R_0$, we can extract the KIE accurately.
    ■ If we run these reactions in replicates, we can get *very* accurate KIEs!

• Note that at high conversions, the ratio of the deuterated to protonated starting materials goes to infinity. Symbolically,

$$\frac{[SM_D]}{[SM_H]} \to \infty$$

  – Implication: As we get higher and higher conversions, we'll eventually reach a point where we only have a few molecules of starting material left, and almost all of them are the deuterated ones.
  – This high-conversion exaggeration makes measurement easier.
  – Indeed, at ultra-high conversions, we can get extremely accurate measurements for even very small KIEs!

- Example: Kinetic isotope effects can narrow down which steps are or are not rate-determining.



Figure 11.2: Assigning peaks on a potential energy surface by using kinetic isotope effects.

  – Consider the reaction of $H_5$- and $D_5$-isotopologoues run both under a palladium-catalyzed arylation.
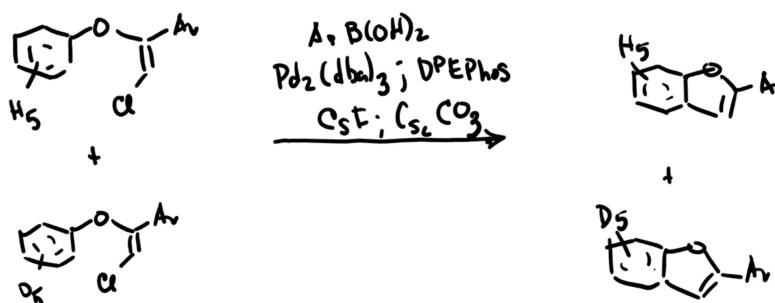


  ■ Meant to be a Suzuki coupling (there's a boronic acid in there), but that ended up being irrelevant to the chemistry.
  ■ In reality, the observed products are ring-closed.

  – We have *no* intermolecular KIE (that is, $k_H/k_D = 1.0$).

  ■ This means that the rate of reaction is *not* determined by the presence or absence of heavy isotopes.
  ■ It follows that $C-H/D$ cleavage is *not* the rate-determining step!

  – What does this mean in terms of the potential energy surface?

  ■ It means that the largest peak (the RDS) does *not* involve $C-H/D$ cleavage, but one of the other peaks could.

  – Reference: Simmons and Hartwig (2012).

- Subtopic 2.2: Intramolecular competition.

- Example: Kinetic isotope effects can probe post-rate determining steps!

  – Consider the same palladium-catalyzed arylation, but our substrate has one H and one D that can be cleaved.
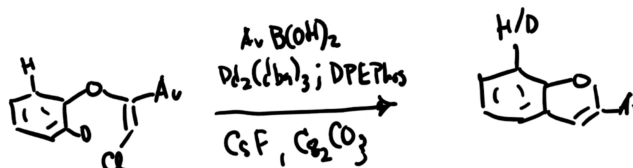


  – Then you can quantify the amount of H vs. D at the *ortho*-position in the product and extract an intramolecular KIE of 4.

- Thus, we have probed a post-rate determining step!
- In this case, oxidative addition to the $sp^2$-Cl is believed to be rate-determining; but we can still use this intramolecular KIE to learn something useful for mechanistic analysis or further reaction development.
- Reference: Simmons and Hartwig (2012).

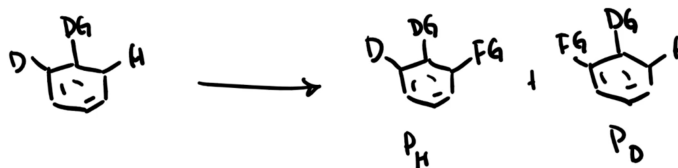- General structure of intramolecular KIEs.



Figure 11.3: Competition experiment (intramolecular).

- We design a symmetric reactant with a donating group, an H on one side, and a D on the other side.
- Then the KIE can be rigorously extracted from

$$\text{KIE} = \frac{[\text{P}_\text{H}]}{[\text{P}_\text{D}]}$$

at *any* conversion.
- We get to use any conversion because the reaction does *not* enrich the isotopic composition.
  - ■ The (local) concentrations of H and D are fixed by the synthesis of the molecule!
- This method gets us an "intrinsic" KIE, even for post-rate limiting steps.

- To recap.

  - Independent, intermolecular, and intramolecular.
  - The results depend heavily on the conditions we use!

- Topic 3: Heavy atom KIEs.

  - We'll talk a bit more about the measurement of extremely small KIEs here.
  - The most common heavy atoms to investigate are $^{12}\text{C}/^{13}\text{C}$.
    - ■ However, it can also be N, O, P, Cl, etc.
  - The magnitude tends to be small because of the smaller change in reduced mass (see Table 10.2).
  - Example: $^{12}\text{C}/^{13}\text{C}$ KIEs tend to be 1.0-1.05.
    - ■ 1.05 is large, even — by $^{12}\text{C}/^{13}\text{C}$ standards, that is!
  - Because we have a small enrichment that is difficult to measure, it is very important to use sensitive methods.
  - This also means that we can pretty much only measure *primary* heavy atom KIEs; secondary heavy atom KIEs are usually too small to measure.
  - Reference: Dale et al. (2021).
    - ■ Alex highly recommends to learn more about all aspects of heavy atom KIEs.

- We experimentally measure heavy atom KIEs using a series of experiments developed in the '90s.

- The most common is the Singleton Method for KIE determination.

  - This is a determination done at the natural abundance of the various isotopologues.

- Singleton's key insight #1: $^{13}C$ is a naturally occurring (typically 1.1% abundance) heavier isotope of $^{12}C$.

  - It follows that every molecule is already labeled with this heavy isotopologoue, and already labeled at every position.

- Singleton's key insight #2: $^{13}C$ can be measured via $^{13}C$ NMR for quantitation.

- Both of these insights are important because $^{13}C$ precursors are few and far between, and they're expensive! Labeling a certain position can be very difficult (and expensive).

- Singleton's key insight #3: Recall that $R/R_0 = (1 - C)^{1/\,\mathrm{KIE}\,-1}$. As $C \to 1$, $R/R_0$ becomes very sensitive to the KIE.
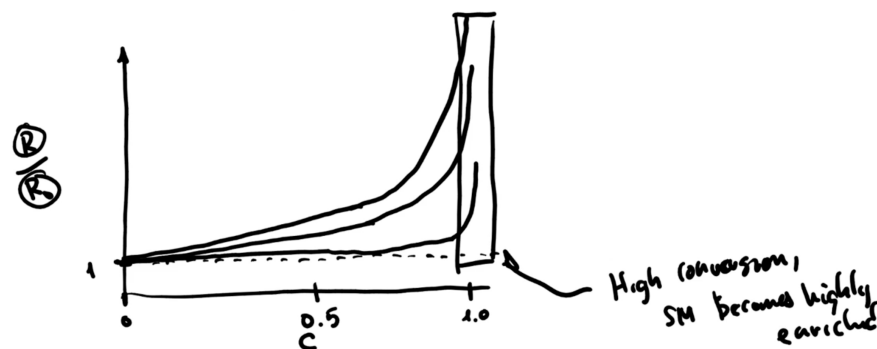


Figure 11.4: Isotopic enrichment at high conversions.

  - We can visualize this relationship through a series of plots of $R/R_0$ vs. $C$.
    - If we run a reaction with a KIE of 1.0, we'll have $R/R_0 = 1$ at any $C \in [0, 1)$.
    - If we run a reaction with even a KIE of 1.1, we'll get enrichment in the slower-reacting isotope later on that leads to larger KIEs!
  - Takeaway: At sufficiently high conversions, the starting material becomes highly enriched in the slow-reacting isotopologue.

- Numerical data in support of Figure 11.4.

| $C$ | $R/R_0$ |
|------|---------|
| 0.5  | 1.03    |
| 0.75 | 1.07    |
| 0.9  | 1.12    |
| 0.99 | 1.25    |

Table 11.1: Isotopic enrichment at high conversions.

  - Suppose the light over heavy rate constant ratio $(k_\mathrm{L}/k_\mathrm{H})$ is fixed equal to 1.05.
  - We can get extremely accurate KIE measurements for even very such a small intrinsic KIEs, provided again that we run to sufficient converions.

- Example: Measuring heavy atom kinetic isotope effects for an intermolecular reaction.
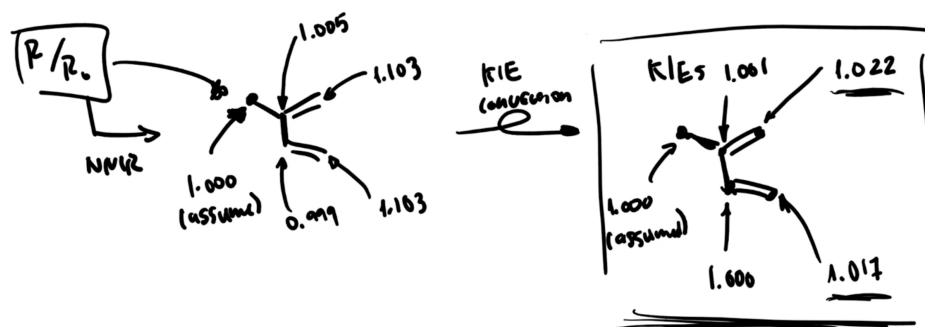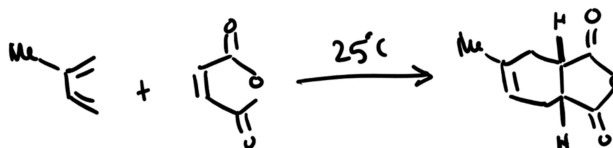


Figure 11.5: Singleton method for intermolecular heavy atom kinetic isotope effects.

- Consider the following Diels-Alder reaction.



- It was run to a conversion of 98.9%.
- We then looked at the $R/R_0$ ratio in the diene starting material.
  - ■ We do this with NMR measurements.
  - ■ Assume that there is a position in the molecule (e.g., the remote methyl) that is not isotopically sensitive, and hence has KIE = 1.000.
    - ➤ If we pick our site well, this is a reasonable assumption.
  - ■ We then measure the raw integrals at the other sites.
  - ■ Take these integrals, put them back into the equation we derived previously to obtain the KIE ratio.
    - ➤ Example:
$$\text{KIE} = \frac{k_\text{L}}{k_\text{H}} = \frac{\ln(1 - 0.989)}{\ln\left[(1 - 0.989) \cdot \frac{1.103}{1.000}\right]} = 1.022$$

- Conclusion: The biggest KIEs are at the terminal methyl groups (as expected from the Woodward-Hoffmann rules; this is another confirmation!), and we get a slight improvement in rate on the side near the methyl group.

  - ■ It would probably be prohibitive to label each position in the diene, but just a good mathematical knowledge of conversions gets us everything we need.
- Reference: Singleton and Thomas (1995).

- Limitations of the Singleton method.

  - We need a large amount of sample.
    - ■ This is because we're running the reaction to high conversion, but need to isolate the starting material.
    - ■ So in order to get accurate NMRs, we need sufficiently high concentrations of the sample.
    - ■ We can run Diels-Alders on nearly mole scales, and potentially isolate grams; that's why the previous example worked.
  - The reaction must be irreversible.
    - ■ It it isn't, we're going to get equilibrium isotope effects mixed in.

  – The results can be difficult to interpret.
    ■ Any individual number might not be too helpful, but with modern quantum mechanical calculations, we can match our results to a DFT-computed potential energy surface!
    ■ This will show that one pathway has a better experimental match with KIEs.
    ■ This is good evidence for a mechanistic course!!
  – Natural abundance experiments can be run in both inter- and intramolecular modes.

- Example: Measuring heavy atom kinetic isotope effects (aka "natural abundance experiments") in an intramolecular mode.



(a) Relevant labeling for intermolecular data.    (b) Relevant labeling for intramolecular data.



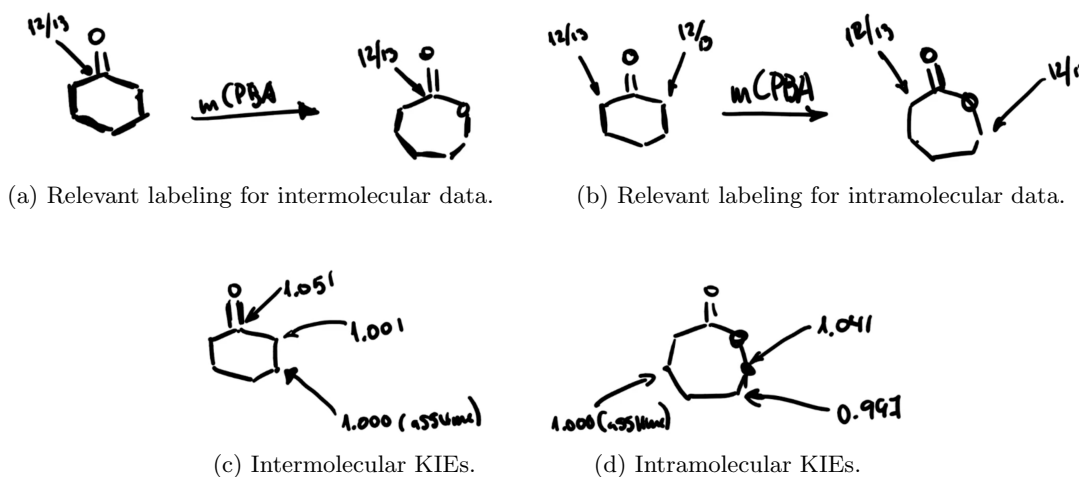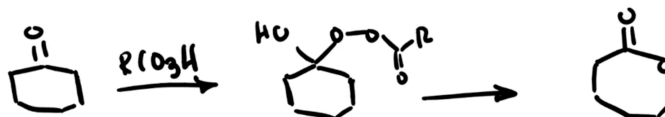(c) Intermolecular KIEs.          (d) Intramolecular KIEs.

Figure 11.6: Singleton method for intramolecular heavy atom kinetic isotope effects.

  – Consider the Baeyer-Villiger reaction.



    ■ A ketone reacts with a peracid.
    ■ The mechanism is believed to proceed through a hemiacetal, followed by ring expansion to the lactone.
  – So we have a two-step mechanism.
    ■ We can probe the first step with natural abundance KIE to determine whether or not hemiacetal formation is rate-determining.
    ■ Simultaneously (in the same pot/set of experiments), we can probe the second step with an intramolecular heavy atom KIE.
  – Intermolecular variant: Consider the labeling at the *ipso*-position.
    ■ Run this reaction to a known conversion, quantitate that conversion well, isolate the starting material, and quantitate its $^{12}C/^{13}C$ well (using, e.g, mass spec).
    ■ Isotopic enrichment of the starting material, here, is conversion-dependent (because it's affiliated with the RDS).
    ■ We assume that the $\beta$-position has an isotopic enrichment of 1.000.
    ■ The resultant significant isotopic fractionation of the starting material (KIE = 1.051) implies that the initial conversion of the ketone to the acetal is rate-determining.

– Intramolecular variant: Consider the labeling at the $\alpha$-positions.

■ Isotopic enrichment of the product, here, is conversion-independent (because it's post-RDS).

■ We assume that the $\beta$-position has an isotopic enrichment of 1.000.

■ The resultant significant isotopic fractionation of the product (KIE = 1.041) implies that the migration step occurs after the RDS, and involves the $\alpha$-position.

– It is somewhat counterintiutive that hemiacetal formation (typically fast) would be rate-limiting!

– Reference: Singleton and Szymanski (1999).

• Takeaways from today.

– We get deep and important information about reaction courses, rate-determining steps, etc. from isotope effects.

• Next time: Kinetics and kinetic rate laws.

## 11.2 Kinetic Rate Laws

11/14:
• Today: Experimental kinetics, rate laws, etc.

– This topic will proceed through the next several lectures.

– Today, we'll focus on general background.

– This will probably be review for many people, but it's *important* review and good for general understanding.

• How can we experimentally determine the rate at which a reaction occurs? By measuring the kinetics.

• The goal of a kinetics experiment is to characterize the mechanism of a given transformation.

– Kinetics help us rule out possibilities.

– We can experimentally determine the **rate law** and see if it fits a proposed arrow-pushing mechanism.

• We begin with some definitions.

• **Rate law**: A mathematical expression for the reaction rate, involving a **rate constant** as well as the concentrations of the involved species scaled by exponents. *General form*

$$\text{rate} = k[\text{A}]^x[\text{B}]^y[\text{C}]^z$$

– Note that the above general form pertains to a reaction $\text{A} + \text{B} + \text{C} \longrightarrow \text{P}$.

– These exponents give us information on the composition of the transition state structure relative to the ground state. Remember that we can't directly observe the activated complex, so we need techniques like this!

– Specifically, the values of the exponents tell us the number of A's, B's, and C's in the transition state structure during the RDS.

• **Rate constant**: A proportionality constant that relates the rate of reaction to the concentrations of the starting materials. *Denoted by $k$*.

– Falls out of our discussion of transition state theory.

• Example: rate $= k[\text{A}]^1$.

– The number of molecules of A in the transition state is the same as in the ground state.

- Example: rate $= k[\text{A}]^2$.

  - There are twice as many A's in the transition state vs. the ground state.
  - It is important to note that this is *relative* to the ground state; $x = 2$ does *not* necessarily imply that there are specifically two molecules of A in the transition state, only that there are twice as many in the ground state.
  - This is similar to how we were always referencing ground states in Transition State Theory.

- We can have **zeroeth-**, **first-**, **second-**, etc. order reactions.

- Example: rate $= k[\text{A}][\text{B}]$.

  - There are an equal number of molecules of A and B in the transition state.
  - This reaction may be said to be "first order in A" and "first order in B" but "second order overall."

- **Rate**: The growth in the concentration of the product(s) as a function of time; equivalently, the decay of the starting material as a function of time.

- **Half-life**: The time at which $[\text{A}]_t = [\text{A}]_0/2$.

- Topic I: Simple kinetic rate laws.

- The simplest case is zero-order kinetics.
$$\text{A} \xrightarrow{k} \text{P}$$
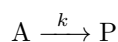
  - Note that this reaction need not have a single-step mechanism.
  - The rate law looks like the following.

  $$\text{rate} = \frac{d[\text{P}]}{dt} = -\frac{d[\text{A}]}{dt} = k$$

    - Specifically, this is a **differential rate law**.
    - The important thing is that the rate is independent of $[\text{A}]$.
  - This case is surprisingly common!

- We don't typically measure rate directly (though we can with calorimetry; we'll talk about this more later).

  - More typically, we measure concentrations.
  - To relate measured concentrations to rates, we need **integrated rate laws**.

- Alex derives the integrated rate law for zeroeth-order kinetics.

$$-\frac{d[\text{A}]}{dt} = k$$
$$\int_{[\text{A}]_0}^{[\text{A}]_t} d[\text{A}] = \int_0^t -k\, dt$$
$$[\text{A}]_t - [\text{A}]_0 = -kt$$
$$[\text{A}]_t = -kt + [\text{A}]_0$$

  - This integrated rate law tells us that a plot of $[\text{A}]_t$ vs. time should be linear with slope $-k$.
  - Correlated with this would be the increase in $[\text{P}]$ with slope $k$.

- Equally common is first-order kinetics.

  - The differential rate law here is
  $$\text{rate} = k[\text{A}]$$

– The integrated rate law may be derived from here.

$$-\frac{d[A]}{dt} = k[A]$$

$$\int_{[A]_0}^{[A]_t} \frac{d[A]}{[A]} = \int_0^t -k\,dt$$

$$\ln([A]_t) - \ln([A]_0) = -kt$$

$$[A]_t = [A]_0 e^{-kt}$$

– This tells us that a plot of $[A]_t$ vs. time will follow a nonlinear decay, i.e., the rate of reaction will slow down over time as the concentration of A is depleted.

■ We can also linearize this plot by taking $\ln([A]_t)$ vs. time, and know that the slope will be $-k$ and the $y$-intercept $\ln([A]_0)$.

- Aside: Many of these linearization methods come from a time when we didn't have computers, so linearization was computationally necessary to extract things like rate constants.

  – In the computer age — where manipulating vast datasets is easy — linearization is antiquated.
  – But it still gives us a good intuitive appreciation for trends.

- The half-life of a first-order reaction is given by

$$t_{1/2} = \frac{\ln(2)}{k}$$

  – We can derive this by substituting $[A]_{t_{1/2}} = [A]_0/2$ into the integrated rate law.
  – Importantly, the half-life does not depend on $[A]$!

  ■ On a plot, this means that each time a half-life elapses, the concentration of $[A]$ has halved.

  – First-order reactions move faster at the beginning than at any other time, so if you go into lab and your reaction is not working early on, it's not then just going to start working later! You should probably cut your losses and change something.
  – Also tells you how many half-lives you'd need in order to achieve a certain desired conversion.

- Next up is second-order kinetics.

  – There are two situations here.

- Situation 1: Consider a reaction of the following form.

$$A + A \xrightarrow{k} P$$

  – The differential rate law here is

$$\text{rate} = k[A]^2$$

  – The integrated rate law may be derived from here.

$$\frac{1}{[A]_t} = kt + \frac{1}{[A]_0}$$

  – A raw plot of this data is pitched down steeper in the beginning than a first-order plot.
  – We can also linearize once again.
  – Note that if we take natural logs (instead of plotting regular or linearized), the data will *look* first-order early on and then diverge from linearity at higher conversions.

  ■ This reveals a challenge: For rigorous determination of reaction orders, we need to follow the kinetic course over many, many half-lives.

- Situation 2: Consider a reaction of the following form.

$$A + B \xrightarrow{\ k\ } P$$
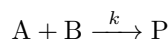
  – The differential rate law here is

$$\text{rate} = k[A][B]$$

  – Deriving the integrated rate law.
    ∎ If $[B]_0 \neq [A]_0$, then we can scale $[B]$ by $[A]$:

$$[B]_t = [B]_0 - ([A]_0 - [A]_t)$$

    ∎ We can then drop this substitution into the differential rate law, go through the integration, and arrive at

$$\frac{1}{[B]_0 - [A]_0} \left( \ln \frac{[B]_t}{[A]_t} - \ln \frac{[B]_0}{[A]_0} \right) = kt$$

  – We can linearize by plotting $\ln([B]_t/[A]_t)$ vs. time.
    ∎ The $y$-intercept defines our initial concentrations.
    ∎ The slope is of the form $([B]_0 - [A]_0)k$.

- In situation 2, deriving $k$ through linearization would require the simultaneous tracking of $[A]$ and $[B]$. But this comes with experimental challenges.
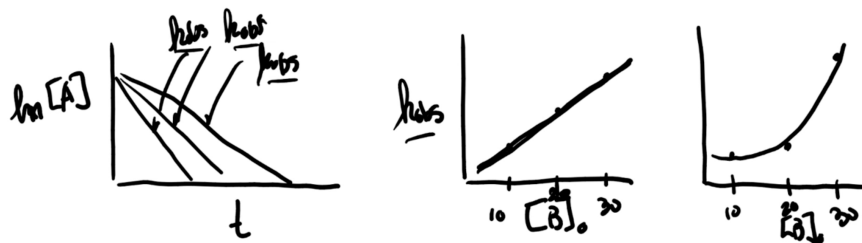


Figure 11.7: Experimentally measuring the rate constant for a two-component second-order reaction.

  – Thus, we use a simplification: Pseudo-first order kinetics.
  – Here, we simplify our analysis by changing the reaction conditions. Specifically, we want to do this in such a way that the concentration of one component in this overall second-order reaction is constant with respect to time.
  – Most typically, this is done by using one reagent in a large excess so that changes in its concentration are negligible. Mathematically, the assumption is that if $[B]_0 \gg [A]_0$, then $[B]_t \approx [B]_0$.
  – When we do this, we say that we're running the reaction "pseudofirst in A."
  – Essentially, we've changed the rate law into

$$\text{rate} = \frac{d[P]}{dt} = k[A][B] \approx \underbrace{k[B]_0}_{k_{\text{obs}}}[A]$$

  – Practically, in order for the condition to be fulfilled, we need at least a 5 times excess of B; 10 times is better.
  – When doing this in the lab, run the experiment with $[B]_0$ equal to several different multiples of $[A]_0$ — e.g., $10[A]_0$, $20[A]_0$, and $30[A]_0$ — and extract $k_{\text{obs}}$ for each of them.
    ∎ Then plot $k_{\text{obs}}$ vs. $[B]_0$ and extract $k$ (if the reaction is first-order in B).
    ∎ If the reaction is second order in B, fit your data to $k_{\text{obs}} = k[B]^2$.

- Let's now discuss the kinetics of multistep chemical processes.

- Example: Consider a mechanism of the following form.

$$\text{A} \underset{k_2}{\overset{k_1}{\rightleftharpoons}} \text{I} \overset{k_2}{\longrightarrow} \text{P}$$
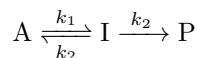
  – The overall differential rate law here is

  $$\text{rate} = \frac{\text{d[P]}}{\text{d}t} = k_2[\text{I}]$$

  – The issue here is that we can't easily measure [I] directly! Thus, we need to measure it indirectly from what we know about the action of A on the system.

  – Two main assumptions are used to solve for [I]: The **steady-state approximation** and the **quasi-equilibrium assumption**.

- **Steady-state approximation**: If $[\text{I}] \ll [\text{A}]$, then $\text{d[I]}/\text{d}t \approx 0$. *Also known as* **SSA**.
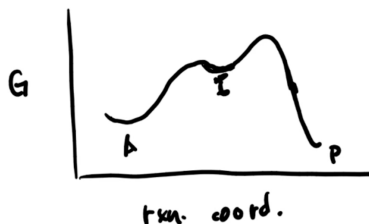


Figure 11.8: Steady-state approximation potential energy surface.

  – On a reaction coordinate diagram, this condition looks like A having to proceed *uphill* through I to the product.

  – In rate law nomenclature, we want $k_{-1} \gg k_1$.[1] This defines an endothermic equilibrium.

- **Quasi-equilibrium assumption**: A $\rightleftharpoons$ I is reversible and remains in equilibrium throughout the process.
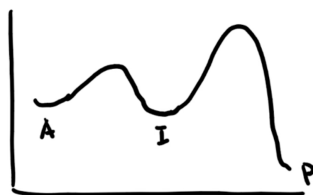


Figure 11.9: Quasi-equilibrium assumption potential energy surface.

  – On a reaction coordinate diagram, this condition looks like A and I reaching a finite equilibrium before product conversion.

  – Here, we expect [I] to build up during the reaction!

    ■ Thus, the steady-state approximation is not applicable in this case.

- Reference: Raines and Hansen (1988).

  – A very lucid description of these two approximations by a colleague, Ron Raines!

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[1]HWE as final mechanistic proposal??

- Let's try applying the steady-state approximation to our model reaction.

  – We begin by writing an expression for all the ways that the concentration of I can change.

  $$\frac{d[I]}{dt} = k_1[A] - k_{-1}[I] - k_2[I]$$

  – Then applying the SSA, we obtain

  $$0 = k_1[A] - k_{-1}[I] - k_2[I]$$

  – Rearranging then allows us to solve for [I].
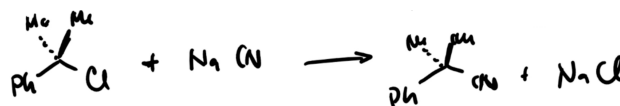
  $$[I] = \frac{k_1[A]}{k_{-1} + k_2}$$

  – We can then substitute this expression of observables back into our rate law, arriving at

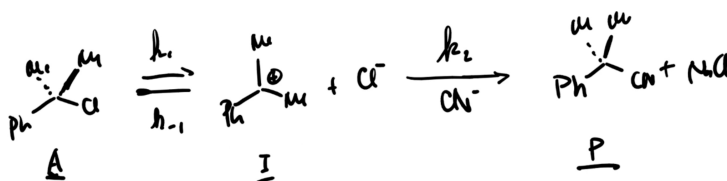  $$\text{rate} = \frac{d[P]}{dt} = k_2[I] = \frac{k_1 k_2[A]}{k_{-1} + k_2} = k_{\text{obs}}[A]$$

  where $k_{\text{obs}} = k_1 k_2/(k_{-1} + k_2)$.

- Example: Seeing the chemistry in all this math.

  – Consider the following reaction.

  

  – Using our knowledge of organic chemistry, we can propose the following $S_N1$ mechanism.

  

  – Mathematically, the growth in product comes from the reaction of the intermediate with the cyano nucleophile.

  $$\frac{d[P]}{dt} = k_2[I][CN^-]$$

  – Now as before, write an expression for $d[I]/dt$.

  $$\frac{d[I]}{dt} = k_1[A] - k_{-1}[I][Cl^-] - k_2[I][CN^-]$$

  – Apply the SSA and solve for I.

  $$[I] = \frac{k_1[A]}{k_{-1}[Cl^-] + k_2[CN^-]}$$

  – Dropping this back into our rate law yields

  $$\frac{d[P]}{dt} = \frac{k_1 k_2[A][CN^-]}{k_{-1}[Cl^-] + k_2[CN^-]}$$

  – This is a wild rate law for a sophomore organic transformation!

- We can simplify the above rate law in some limiting cases.

  – We do this by finding extrema that simplify the denominator.

- Limiting case #1: $k_{-1}[\text{Cl}^-] \gg k_2[\text{CN}^-]$.



Figure 11.10: Potential energy surface for an $S_N1$ with an late rate-determing step.

  – What does this case mean, physically, though?
    - In terms of the potential energy surface, it means that the return of I to A is faster than the conversion of I to P.
    - This implies that the second step is rate-determining.
  – Mathematically, we can drop the $k_2[\text{CN}^-]$ term out of the denominator to simplify the rate law to
  $$\frac{d[\text{P}]}{dt} = \frac{k_1 k_2[\text{A}][\text{CN}^-]}{k_{-1}[\text{Cl}^-]} = k_{\text{obs}}[\text{A}][\text{CN}^-][\text{Cl}^-]^{-1}$$
    - This means that the reaction is inverse order in $\text{Cl}^-$, hence inhibited by the addition of exogeneous chloride.
    - However, it is also first-order in $[\text{A}]$ and $[\text{CN}^-]$.

- Limiting case #1: $k_2[\text{CN}^-] \gg k_{-1}[\text{Cl}^-]$.



Figure 11.11: Potential energy surface for an $S_N1$ with an early rate-determing step.

  – Physical interpretation.
    - In terms of the potential energy surface, it means that the conversion of I to P is faster than the return of I to A.
  – Mathematically, we can drop the $k_{-1}[\text{Cl}^-]$ term out of the denominator to simplify the rate law to
  $$\frac{d[\text{P}]}{dt} = \frac{k_1 k_2[\text{A}][\text{CN}^-]}{k_2[\text{CN}^-]} = k_1[\text{A}]$$
    - This reflects the sophomore-organic understanding of $S_N1$ as a reaction in which the RDS depends only on $[\text{A}]$.

- But how could the rate not depend on $CN^-$ at all? If there's no $CN^-$, the reaction won't proceed at all!

  – The trick is that we have zeroeth-order dependence on the rate in the limit of large $CN^-$ concentrations, and first-order dependence at very small $CN^-$ concentrations.

  – Entering this so-called **saturation regime** is very common.

  – As $CN^-$ is consumed, we transit along this curve and eventually enter a different kinetic regime!

    ■ Not a different mechanism, but yes a change in the RDS.
    ■ Takeaway: The kinetic rate law depends on the conditions!

- Always having to derive the rate law is a bit laborious, so here's a rule of thumb/cheat code (in the context of the SSA).

  – The rate can be expressed as the product of all of the forward rate constants and concentrations, over the sum of the rate constants and concentrations of the ways that the intermediate can react.

  – Alex uses this shortcut to rederive the rate laws for the two previous applications of the SSA.

- Caveat: In order for the SSA to work, it can only be applied to *one* intermediate.

  – Otherwise, the math breaks down.

  – So for a multistep process in which I changes appreciably, we need to use the quasi-equilibrium assumption.

- Using the quasi-equilibrium assumption.

  – We know that

  $$K_{\text{eq}} = \frac{[\text{I}]}{[\text{A}]}$$

  – Additionally, we know that

  $$K_{\text{eq}} = \frac{k_1}{k_{-1}}$$

  – Thus, substituting back into the original rate law gives

  $$\text{rate} = k_2[\text{I}] = \underbrace{k_2 K_{\text{eq}}}_{k_{\text{obs}}}[\text{A}]$$