

2.

$$\lambda = 5.80 \times 10^{-7} \text{ m}$$

$$d = 5.30 \times 10^{-4} \text{ m}$$

$$a = 3.20 \times 10^{-4} \text{ m}$$

a.

$$d \sin \theta_1 = \lambda$$

$$\theta_1 = \sin^{-1} \left( \frac{\lambda}{d} \right)$$

$$\theta_1 = 0.0627^\circ$$

$$d \sin \theta_2 = 2\lambda$$

$$\theta_2 = \sin^{-1} \left( \frac{2\lambda}{d} \right)$$

$$\theta_2 = 0.125^\circ$$

b.

$$\alpha_1 = \frac{\pi a}{\lambda} \sin \theta_1$$

$$= 1.90$$

$$\alpha_2 = \frac{\pi a}{\lambda} \sin \theta_2$$

$$= 3.78$$

$$I(\theta_1) = \cos^2 \left( \frac{\pi d \theta_1}{\lambda} \right) \cdot \frac{\sin^2 \alpha_1}{\alpha_1^2} \cdot I_0$$

$$I(\theta_1) = 0.248 I_0$$

$$I(\theta_2) = \cos^2 \left( \frac{\pi d \theta_2}{\lambda} \right) \cdot \frac{\sin^2 \alpha_2}{\alpha_2^2} \cdot I_0$$

$$I(\theta_2) = 0.0144 I_0$$

2.

$$l = 5.43 \times 10^{-11} \text{ m}$$

$$x = 2.50 \times 10^{-5} \text{ m}$$

$$\lambda = 5.100 \times 10^{-7} \text{ m}$$

$$\sin \theta_{\text{ref}} = \frac{x}{l}$$

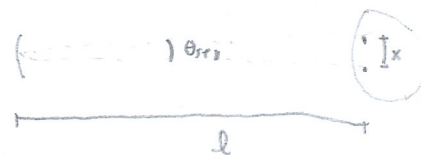
$$\theta_{\text{ref}} = \sin^{-1} \left( \frac{x}{l} \right)$$

$$\theta_{\text{ref}} \approx 1.22 \frac{\lambda}{a}$$

$$\sin^{-1} \left( \frac{x}{l} \right) \approx 1.22 \frac{\lambda}{a}$$

$$a = \frac{1.22 \lambda}{\sin^{-1} \left( \frac{x}{l} \right)}$$

$$a = 1.45 \text{ m}$$



3.

$$V = 0.900 \text{ L}$$

$$P = 1.00 \text{ atm}$$

$$T = 295 \text{ K}$$

$$M_{\text{air}} = 28.97 \text{ g/mol}$$

$$R = 0.0821 \frac{\text{L atm}}{\text{mol K}}$$

$$M_{\text{He}} = 4.003 \text{ g/mol}$$

$$a. \quad PV = nRT$$

$$= \frac{m}{M} RT$$

$$m = \frac{PV M_{\text{air}}}{RT}$$

$$m = 1.07 \text{ g}$$

$$m = \frac{PV M_{\text{He}}}{RT}$$

$$m = 0.149 \text{ g}$$

4.

$$p = 9.00 \times 10^{-14} \text{ atm}$$

$$T = 300.0 \text{ K}$$

$$V = 1.00 \times 10^{-3} \text{ L}$$

$$N_A = 6.02 \times 10^{23}$$

$$R = 0.0821 \frac{\text{L atm}}{\text{mol K}}$$

$$p_2 = 1.00 \text{ atm}$$

a.

$$p_1 V = n RT$$

$$p_1 V = \frac{N}{N_A} RT$$

$$N = \frac{p_1 V N_A}{RT}$$

$$N = 2,200,000 \text{ molecules}$$

b.

$$N = \frac{p_2 V N_A}{RT}$$

$$N = 2.44 \times 10^{19} \text{ molecules}$$

6.

$$\Delta Q_V = 300 \text{ J}$$

$$\Delta T_{H_2} = 2.50 \text{ K}$$

$$R = 8.314 \text{ J/mol} \cdot \text{K}$$

$$C_{V_{H_2}} = \frac{5}{2} R = \frac{1}{n} \frac{\Delta Q_V}{\Delta T_{H_2}}$$

$$n = \frac{2 \Delta Q_V}{5 R \Delta T_{H_2}}$$

$$n = 5.77$$

$$C_{V_{He}} = \frac{5}{2} R = \frac{1}{n} \frac{\Delta Q_V}{\Delta T_{He}}$$

$$\Delta T_{He} = \frac{2 \Delta Q_V}{3 R n}$$

$$\Delta T_{He} = 4.17^\circ \text{C}$$

6.

$$n = 5$$

$$T_0 = 400 \text{ K}$$

$$\Delta Q = 1500 \text{ J}$$

$$\Delta W = 2100 \text{ J}$$

$$R = 8.314 \text{ J/mol K}$$

$$E_{\text{int}_0} = \frac{3}{2} n R T_0$$

$$\Delta E_{\text{int}} = \Delta Q - \Delta W$$

$$E_{\text{int}_2} = E_{\text{int}_0} + \Delta E_{\text{int}}$$

$$\frac{3}{2} n R T_1 = \frac{3}{2} n R T_0 + \Delta Q - \Delta W$$

$$T_1 = T_0 + \frac{2}{3nR} (\Delta Q - \Delta W)$$

$$T_1 = 390 \text{ K}$$

7.

$$n = 0.0040 \text{ mol}$$

$$V_0 = 0.20 \text{ L}$$

$$P_0 = 2.0 \text{ atm}$$

$$P_1 = 0.50 \text{ atm}$$

$$R = 0.0821 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}}$$

$$R' = 8.314 \text{ J/mol} \cdot \text{K}$$

$$a. \quad P_0 V_0 = P_1 V_1$$

$$V_1 = \frac{P_0 V_0}{P_1}$$

$$V_1 = 0.80 \text{ L}$$

b.

$$P_1 V_0 = n R T_a$$

$$T_a = \frac{P_1 V_0}{n R}$$

$$T_a = 305 \text{ K}$$

$$T_b = T_c = \frac{P_0 V_0}{n R}$$

$$T_b = T_c = 1220 \text{ K}$$

c.

$$\Delta E_{\text{int}ab} = \Delta Q_{ab} \quad (\text{Isochoric})$$

$$\Delta Q_{ab} = \frac{5}{2} n R' \Delta T$$

$$\Delta Q_{ab} = 76.1 \text{ J}$$

$$\Delta E_{\text{int}bc} = 0 = Q - W \quad (\text{isothermal})$$

$$\Delta Q_{bc} = W$$

$$= n R' T_b \ln \left( \frac{V_1}{V_0} \right)$$

$$\Delta Q_{bc} = 56.2 \text{ J}$$

$$\Delta Q_{ca} = C_p n \Delta T \quad (\text{Isobaric})$$

$$= \frac{7}{2} n R' (T_a - T_c)$$

$$\Delta Q_{ca} = -107 \text{ J}$$

d.

$$\Delta E_{\text{int}ab} = \Delta Q_{ab}$$

$$\Delta E_{\text{int}ab} = +76.1 \text{ J} \quad \text{inc.}$$

$$\Delta E_{\text{int}bc} = 0 \text{ J}$$

(adiabatic)

same

$$\Delta E_{\text{int}ab} + \Delta E_{\text{int}bc} + \Delta E_{\text{int}ca} = 0$$

$$\Delta E_{\text{int}ca} = -\Delta E_{\text{int}ab}$$

$$\Delta E_{\text{int}ca} = -76.1 \text{ J} \quad \text{dec.}$$

8.

$$T_F = \frac{9}{5} T_C + 32$$

$$T_F = T_C$$

$$T_C = \frac{9}{5} T_C + 32$$

$$-32 = \frac{4}{5} T_C$$

$$T_C = -40^\circ \text{C or } ^\circ \text{F}$$

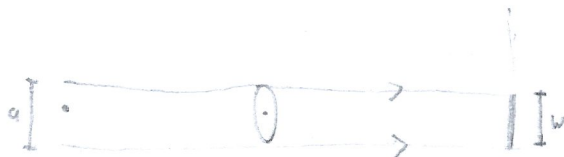


9.

$$\lambda = 0.305 \text{ m}$$

$$\lambda = 5,500 \times 10^{-7} \text{ m}$$

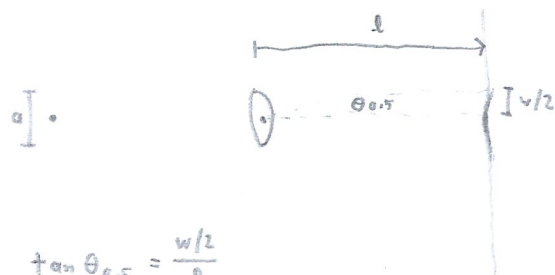
Bundle of rays: For a small hole, approximate parallel rays, making image diameter equal to aperture diameter, i.e.,  $a$ .



$$w = a$$

Diffraction:

Let  $\theta_{0.5}$  denote  $\theta_{\frac{1}{2}}$  width of central max.



$$\tan \theta_{0.5} = \frac{w/2}{l}$$

$$\tan \left( \frac{1.22 \lambda}{a} \right) = \frac{w}{2l}$$

$$w = 2l \tan \left( \frac{1.22 \lambda}{a} \right)$$

$$a = 2l \tan \left( \frac{1.22 \lambda}{a} \right)$$

$$a = 6.40 \times 10^{-4} \text{ m} \quad - \text{ from calculator}$$