

Chapter 40

Quantum Mechanics I: Wave Functions

40.1 The Wave Equation

8/24:

- **Quantum wave:** The wave-like nature of an electron.
- But waves must satisfy a wave equation.
 - The classical one didn't work.
 - In 1925, Schrödinger determined that in one dimension, an electron moving in a potential V (the nucleus-electron Coulombic attraction) satisfies

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \Psi(x, t)}{\partial x^2} + V\Psi = i\hbar \frac{\partial \Psi}{\partial t}$$

- This wave equation wasn't derived in an analogous method to Figure 15.2, but rather was constructed from conservation of energy.
- This wave function has both real and imaginary parts with the inclusion of $i = \sqrt{-1}$.

40.2 Electrons in the Double Slit Experiment

- Electrons exhibit both diffraction and interference in the double slit experiment.
 - $d \sin \theta = m\lambda$ applies when λ is the deBroglie wavelength.
 - Even with only one electron being emitted at a time, you get interference (further confirms wave-like nature of electrons): $\Psi_{\text{electron}} = \Psi_{\text{slit 1}} + \Psi_{\text{slit 2}}$.
 - Observing which slit an electron goes through removes the interference pattern.
- $P \propto \Psi^2$ is independent of time, so you have static charge distributions.