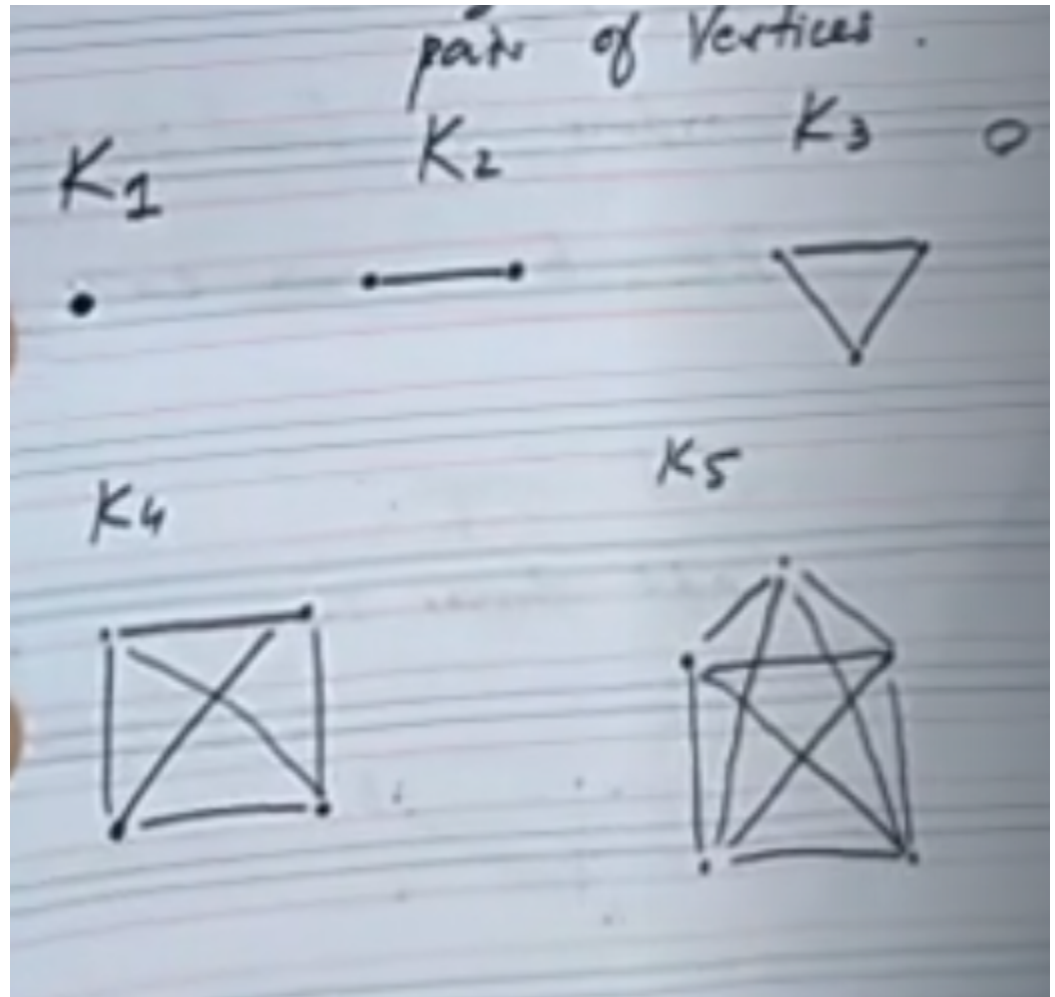


## Discrete Lecture # 20 Part 2

- Complete Graph  $K_n$ 
  - Simple Graph
  - $N$  vertices
  - Edge between each pair of vertices
  - $K$ -graph



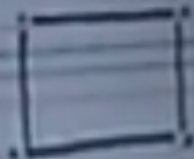
- 
- Cycle graph
  - $N \geq 3$
  - Simple Graph

Cycles:-  $n \geq 3$  Simple

$C_3$



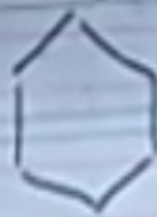
$C_4$



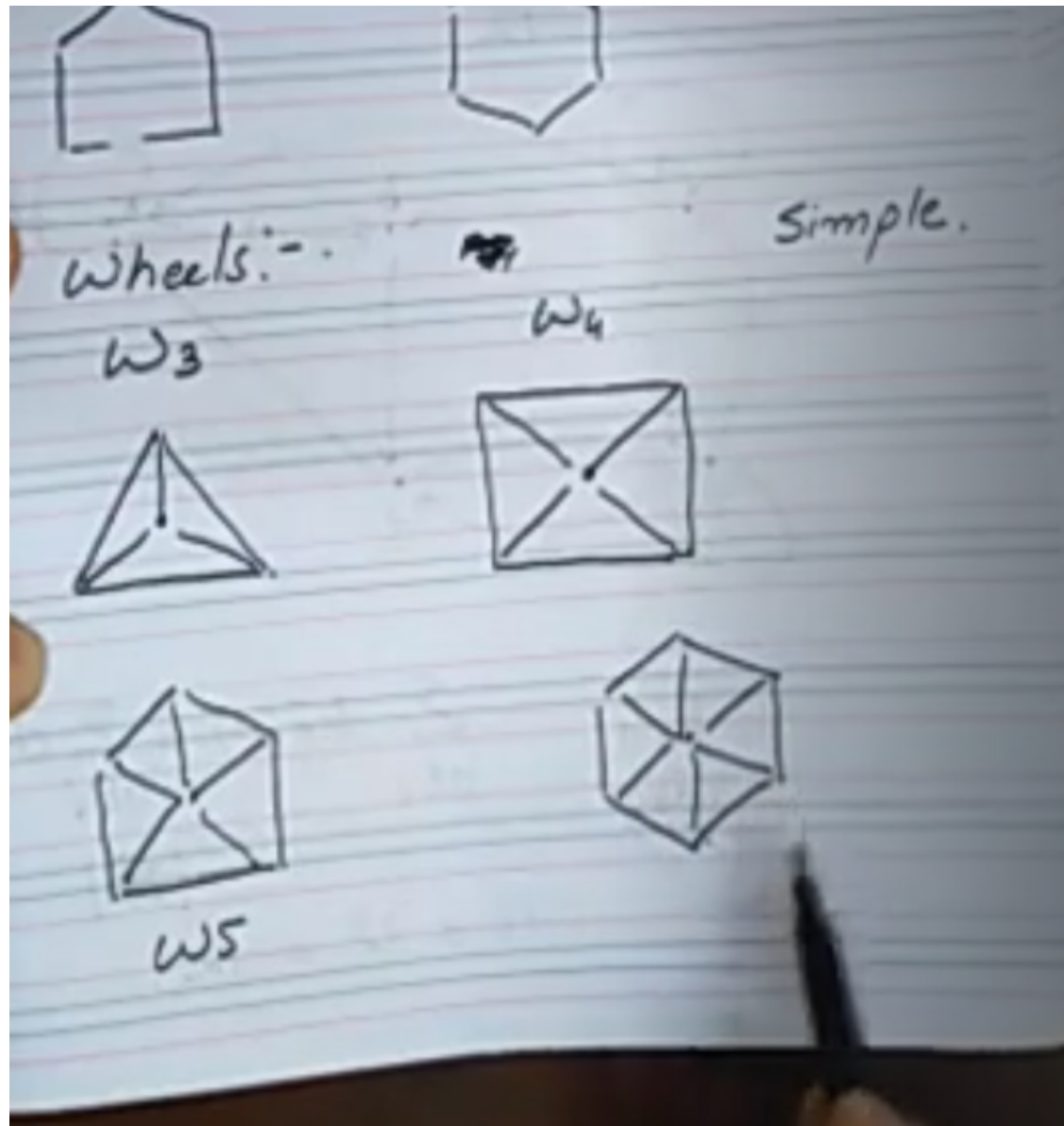
$C_5$



$C_6$



- Wheel graph



- **Cuboid  $Q_n$**

- We represent these with binary digits
- $Q_n$ ,  $n=1$ ,  $2^n$
- $Q_1$ ,  $= 2^1 = 2$  vertices
- $Q_2$ ,  $= 2^2 = 4$  vertices
  - Every Vertex will have one bit difference with their other paired vertex

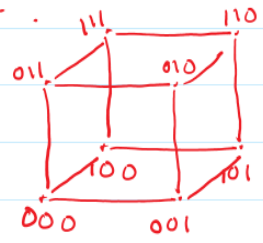
Cuboid:-  $Q_n$   $2^n$  Vertices.  $n=1, \dots$

0 — 1

$Q_1$ .



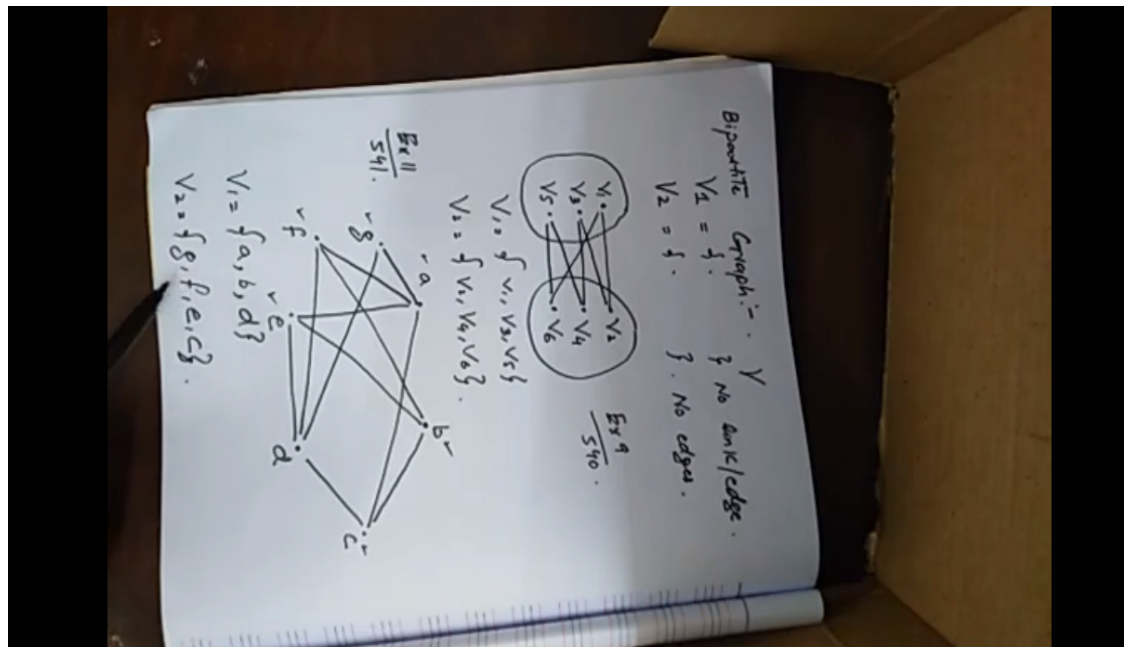
$Q_2$



$Q_3$ .

## • Bi-Partile graph

- A graph that can be divided into two parts
- Set of vertices can be divided into two parts :  $V_1$  and  $V_2$  such that  $v_1$  and  $v_2$  elements do not have any edge and no link between  $v_2$  to  $v_2$  elements
- $V_1 \{ \}$  No link
- $V_2 \{ \}$  No edge
- Vertices that are not directly connected to each other we put them separately into another group and the other into other group



## ○ Complete Bi-Partile Graph

Complete bi-partite Graph.

$K_{m,n}$ .

$K_{1,1}$



New Section 1 Page 1

$K_{1,2}$ .

$K_{1,2}$



$K_{2,2}$



$K_{2,3}$



$K_{3,3}$



○

### Sub-GRAPH

Sub Graph:-

$G = (V, E)$

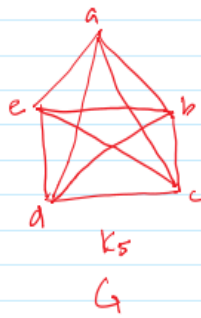
$H = (W, F)$ .

$H$  is a Subgraph of  $G$  if  $W \subseteq V$   $\wedge$   $F \subseteq E$ .

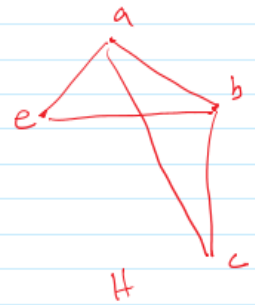
○

$\wedge$

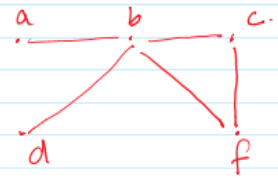
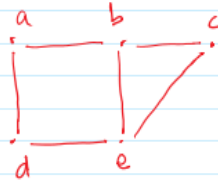
$\wedge$



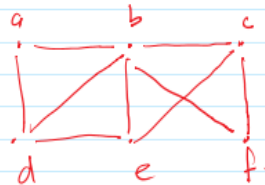
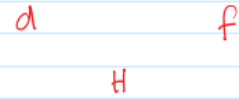
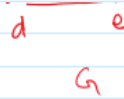
$V = \{a, b, c, d, e\}$



$\frac{5!}{2} = 546$



New Section 1 Page 2



$G \cup H$

- Formula for Edges

	Vertices	Edges
$K_2$	2	1
$K_3$	3	3
$K_4$	4	6
$\vdots$	$\vdots$	$\vdots$
$K_n$	$n$	$\frac{n(n-1)}{2}$

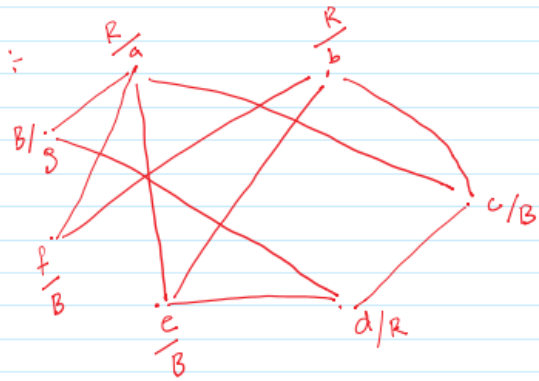
- **Formula for Vertices**

	Vertices	Edges
$K_2$	2	1
$K_3$	3	3
$K_4$	4	6
$\vdots$	$\vdots$	$\vdots$
$K_n$	$n$	$\frac{n(n-1)}{2}$

- **Graph Coloring**

- In graph coloring we assign a color group to one vertex and assign another color group to its corresponding vertex with which it is linked

Ex 22:  
541



Red = {a, b, d}.

Blue = {c, e, f, g}.

