

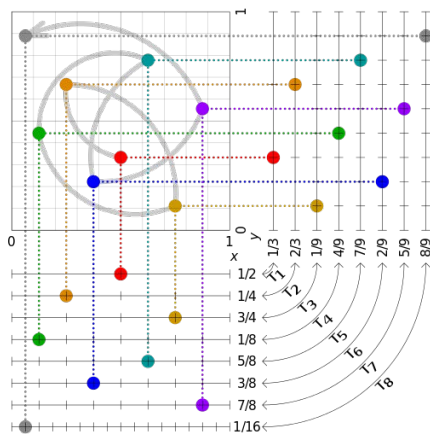
Quasi-Random Sequences

1. What are the first two points generated by the 2-dimensional Hammersley Sequence $p_i = (\frac{i}{n}, \Phi_2(i))$ when we generate a set containing 10 points?

i=1: (1/10, 1/2)

i=2: (1/5, 1/4)

2. What are the first two points generated by the 2,3 Halton Sequence $p_i = (\Phi_2(i), \Phi_3(i))$?



(1/2, 1/3), (1/4, 2/3),

Filters

In ray-tracing, a filter will generate value for a given pixel by taking a weighted average of samples around that pixel center. The weights used are usually generated by a function $w(d_i)$ of the distance d_i from a sample location to the pixel-center: $p = \frac{\sum w(d_i)s(x_i, y_i)}{\sum w(d_i)}$

3. Suppose we use the following weight function:

$$w(x, y) = \frac{1}{n}$$

when filtering using n samples.
How would you categorize the filter?

- a. Box Filter
- b. Tent Filter
- c. Cubic Filter
- d. Gaussian Filter

Intersections

4. Derive a formula for intersecting a ray and a parabolic cylinder given by $x^2 = 4y$.

The ray is $r(t) = o + dt$...substitute into the function for the cylinder:

$$(o_x + d_x t)^2 = 4(o_y + d_y t)$$

$$o_x^2 - 4o_y + (2o_x d_x - 4d_y) t + (d_x)^2 t^2 = 0$$

Which can be solved by the quadratic formula...