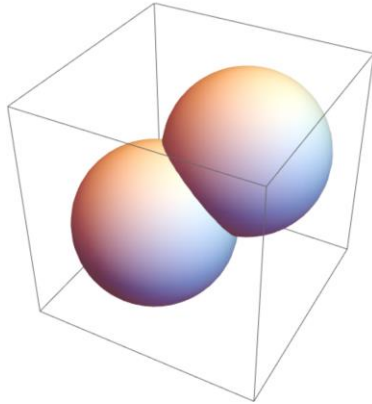


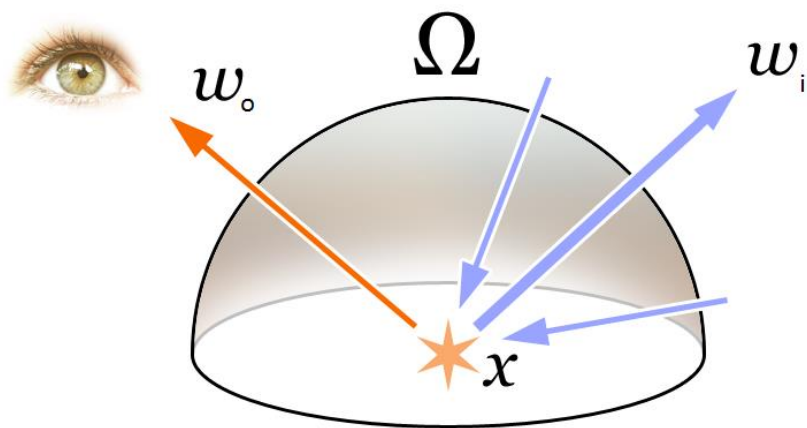
## Monte Carlo Methods

1. We want to calculate the volume of intersection between two spheres of radius 1. Sphere  $S_1$  is centered at  $(1,1,0)$  and  $S_2$  is at  $(1,2,0)$ . Describe how you could use a Monte Carlo method to compute this volume.



2. Suppose we generate an insufficiently converged approximation to an integral using a Monte Carlo method and  $N$  samples. If we wish to reduce the error by  $1/3$  with high probability, how many samples are needed?

## Rendering Equation



The hemisphere form of the rendering equation was developed by James Kajiya in 1986. Describe, as best you can, what each of the components below represents:

$$L_o(p, w_o) = L_e(p, w_o) + \int_{\Omega} f_r(p, w_i, w_o) L_i(p, w_i) \cos \theta_i d\omega_i$$