Mathematics

1 Unit Conversion

Why is unit conversion?
Try *Googling* the **Mars Climate Orbiter Crash & the Gimli Glider**.
Questions:

1. Identify the dimensions the following values and calculate their values in another possible unit:
   (a) Example: 2 metres
   Answer: The unit "meter" has the dimensions of length. Alternative units for length may be inches and chain. Therefore,
   $$2\ m \approx 78.74\ inches \approx 0.0994194\ chain$$
   (b) 20 ^oC
   (c) 15 kg
   (d) 54 $\times 10^3$ seconds
2. Argue what unit would be suitable for each situation:
   (a) Example: Between light years or metres, which one is more suitable for the length of an average person's arms span?
   Answer: To measure the length of an average person's arms span, the unit metres would be more appropriate, considering the average arm span is unlikely to reach the astronomical scale of that described using light years.
   (b) Between Angstrom or centimetres, which one is more suitable for measuring the size of atoms?
   (c) Between years or nanoseconds, which one is more suitable for estimating the average age of a human population?
   (d) Between grams or ounces, which one is more suitable for explaining the weight of a cup of sugar to a Malaysian?

Fun exercise + extra knowledge: Name the few countries that still refuses to use S.I. unit nationwide.

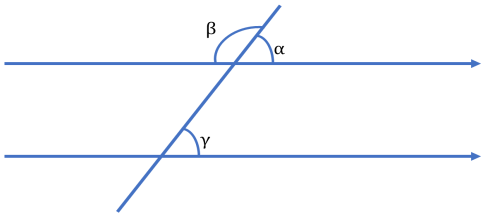
2 Dimensional Analysis

1. What are the dimensions of the derived quantities below:
   (a) Quantity c given that $c^2 = b^2 + a^2$, where a and b both has dimension of length.
   (b) Quantity S given that $S = k_B\ ln(W)$ where W is dimensionless and k_B has dimensions of $[\frac{Mass}{Temperature}]$.
   (c) Quantity y given that $y = A\ sin\ (\omega t)$, where A has dimension of length, t has the dimension of time and ω has the unit of $rad\ s^{-1}$.

3 Algebra, Geometry & Trigonometry

1. Algebra:
   Writing down the quadratic formula used to solve for the zeroes of a second-degree polynomial function. Please include the general equation for a second-degree polynomial function in your answer.
2. Exponents:
   Write down the exponent rules for multiplication, division, fractional exponent and negative exponent.
3. Geometry:

(a) Angles:

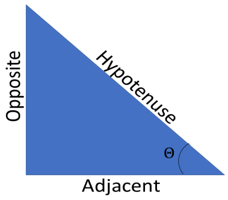


Based on the diagram above, write down equations that relates α to β, α to γ and γ to β.

(b) Write down the equations for the surface area and volume of a cylinder, cone. sphere.

(c) Write down the trigonometric identities, Law of cosines and Law of sines.

4. Trigonometry:



$$sin(\theta) = \frac{Opposite}{Hypotenuse}$$
$$cos(\theta) = \frac{Adjacent}{Hypotenuse}$$
$$tan(\theta) = \frac{sin(\theta)}{cos(\theta)} = \frac{Opposite}{Adjacent}$$

(a) Based on the diagram above, calculate θ is opposite is 18.4112cm and the hypotenuse is 32.0989cm.

(b) Calculate the value of $tan(\theta)$ if the opposite is 21.98cm and the hypotenuse is 25.41cm.

(c) sketch a graph describing $y = sin(\theta)$, $y = cos(\theta)$ and $y = tan(\theta)$.

4 Scalar & Vectors

1. What is the difference between scalars and vectors? Give examples.

2. Given

$$\vec{a} =< a_1, a_2, a_3 > \text{and} \vec{b} =< b_1, b_2, b_3 >$$

Calculate $\vec{c}$ where:

(a) $\vec{c} = \vec{a} + \vec{b}$

(b) $\vec{c} = \vec{a} - \vec{b}$

(c) $\vec{c} = \vec{a} \cdot \vec{b}$

(d) $\vec{c} = \vec{a} \times \vec{b}$

Also, evaluate the magnitude $|\vec{c}|$ and the angle it makes, please specify from which axes you are referring to when working out the angle. Relate components of each vector in its unit vectors to the magnitude and angle.

3. Write down the properties of scalar product and vector product.

5 Calculus

1. Differentiation

(a) What are the differentiation rules for

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i. A constant
ii. Power functions
iii. Product rule
iv. Chain Rules

(b) Evaluate the derivative with respect to x for functions:

- $f(x) = ln(x)$
- $f(x) = sin(x)$
- $f(x) = cos(x)$
- $f(x) = e^{kx}$ where k is a constant

2. Integration:
Evaluate the following integral:

- $\int x^n\ dx$ where $n \neq -1$ $\int x^{-1}\ dx$
- $\int e^x\ dx$
- $\int kx^n\ dx$ where k is a constant
- $\int sin(x)\ dx$
- $\int cos(x)\ dx$

Also, describe the method of integrating by parts.

6 Graphs

1. Given that (2,8) and (4,13) are coordinates of 2 points of a straight line on the x-y graph, determine the gradient and y-intercept of the graph.

2. Given the equation $k = \frac{df(x)}{dx}$ and $l = \int f(x)dx$, which one represents the area under the graph $f(x)$ and which one determines the gradient at a given point of the graph $f(x)$. Support your answer diagrammatically.