



Linear Dynamics

2: KINEMATICS

1. (PSPM 00/01)

The motion of a particle is described by the following equation

$$x = 3t^2$$

where x is displacement and t is time. Sketch the displacement time graph of the equation.

2. (PSPM 07/08) A bullet is fired from a rifle with a muzzle velocity of 100ms^{-1} at 15° above the horizontal. Calculate the horizontal range of the bullet. (**Ans:** $R = 510\text{m}$).

3. (PSPM 08/09) A stone is thrown vertically upwards with initial velocity 24ms^{-1} . Calculate the

- (a) Displacement of the stone after 4.0s.
- (b) Velocity of the stone at 10m above the point of launch.
- (c) Time to reach maximum height.

(**Ans:** $s = 17.5\text{m}$; $v = \pm 19.5\text{ms}^{-1}$; $t = 2.45\text{s}$)

4. (PSPM 09/10) A particle moving with uniform acceleration a has initial velocity u . With the aid of a velocity-time graph, show that the displacement s after time t is given by $s = ut + \frac{1}{2}at^2$.

5. (PSPM 09/10) A long jump athlete take-off at 25° with the horizontal and achieves a jumping distance of 9.12m

- (a) Calculate the initial take-off speed
- (b) Calculate the maximum height of the jump
- (c) Suggest two ways to increase the jumping distance.

(**Ans:** 10.8ms^{-1} ; 1.06m)

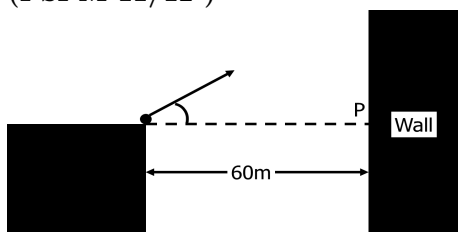
6. (PSPM 10/11) A drunken motorist who is moving at a constant velocity of 90kmh^{-1} passes a stationary police patrol car. The patrol car immediately gives a chase at a constant acceleration and catches up with the motorist after a distance of 10km .

- (a) Calculate the time taken by the patrol car to catch up with the motorist.
- (b) Calculate the acceleration of the patrol car.
- (c) Calculate the velocity of the patrol car when it catches up with the motorist.
- (d) On the same axes, sketch and label graphs of displacement versus time for both the vehicles.

(**Ans:** $t = 400\text{s}$; $a = 0.125\text{ms}^{-2}$; $v = 50\text{ms}^{-1}$)

7. (PSPM 11/12) A plane travels at three times the speed of sound. If the speed of sound is 343ms^{-1} , how far it travels in 10minutes? (**Ans:** $s = 6.17 \times 10^5\text{m}$)

8. (PSPM 11/12)



The figure above shows a balls being thrown from the top of a building towards a wall 60m away. The initial velocity is 20ms^{-1} at 40° to the horizontal.

- (a) How much time does it take to hit the wall?
- (b) What is the distance between P and the position the ball strike the wall?



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Rasulan, S.
+60105520080
KMSw

(c) What is the speed of the ball when it strikes the wall?

(Ans: $t = 3.92s$; $s_y = -24.8m$; $v = 29.8ms^{-1}$)

9. (PSPM 12/13)

(a) A train initially at rest, accelerates uniformly until its speed reaches $8ms^{-1}$ in $25s$. For the next $200s$, the train continues its journey with constant speed, before it slows down uniformly and comes to a complete stops in $20s$.

i. Sketch a labels graph of speed versus time for the whole journey.

ii. Calculate the acceleration of the train for the three parts of the journey.

(Ans: $0.32ms^{-2}$; $0ms^{-2}$; $0.4ms^{-2}$)

iii. Determine the total distance travelled by the train. (Ans: $1780m$)

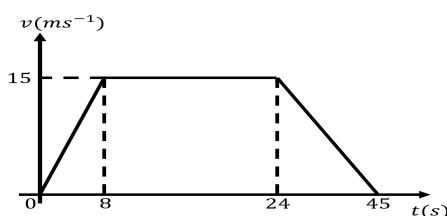
(b) An object is thrown vertically downward at $5ms^{-1}$ from a height of $30m$. Calculate

i. The speed of the object just before it hits the ground. (Ans: $24.77ms^{-1}$)

ii. the time taken by the object to reach the ground. (Ans: $2.02s$)

(c) A ball is thrown horizontally at $10ms^{-1}$ from a height of $15m$ above the ground. Calculate the horizontal range covered by the ball. (Ans: $17.5m$)

10. (PSPM 13/14)



(a)

The figure above shows velocity-time graph of a motion along a straight line.

i. Calculate the average velocity and average acceleration of the entire motion.

ii. Sketch a labelled displacement-time graph of the motion.

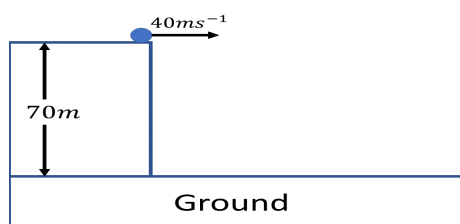
(b) A bullet is fired vertically upwards with an initial speed of $600ms^{-1}$. Calculate the time interval, Δt for the bullet to be $800m$ above ground.

(c) i. Why is the displacement and velocity in a projectile motion can be analysed separately in the x and y-directions?

ii. A projectile is launched with a velocity of $45ms^{-1}$ at an angle of 60° from the horizontal. Determine the time when the velocity makes an angle 30° with the horizontal for first time.

11. (PSPM 14/15)

(a) Distinguish between distance and displacement.



(b)

The figure above shows a stone is thrown horizontally with initial velocity $40ms^{-1}$ from the top of $70m$ high building.

i. Sketch the path traversed by the stone to the ground and indicate the velocity components and resultant velocity of the stone $15m$ from the ground.

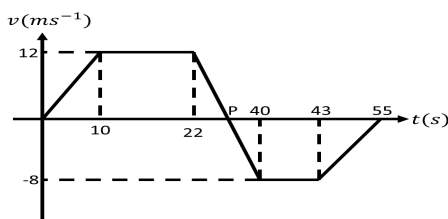
ii. Calculate the resultant velocity of the stone $15m$ from the ground. (Ans: $v_{res} = 51.73ms^{-1}$)



- iii. Sketch a graph of vertical acceleration versus time (a vs t) for the falling stone and label the value of acceleration.
- iv. Calculate the time of flight. (**Ans:** $t = 3.78s$)
- v. Calculate the range. (**Ans:** $R = 151.2m$)

12. (PSPM 15/16)

- (a) Describe a free falling body.



- (b)

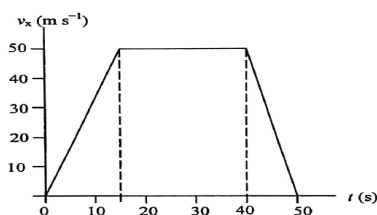
The figure above shows the velocity-time graph of a toy train moving on a straight track in 55s.

- i. Determine the time and acceleration at point P when the velocity is zero. (**Ans:** $t = 32.8s$; $a = -1.11ms^{-2}$)
 - ii. Is the total distance travelled by the train less than, equal or greater than its total displacement? Justify your answer using calculation. (**Ans:** $d > s$)
- (c) A javelin is thrown with a speed of $55 ms^{-1}$ at an angle of 42° with the horizontal. Calculate the velocity of the javelin after 5s. (**Ans:** $v = 42.7ms^{-1}$)

13. (PSPM 17/18)

- (a) Define

- i. average velocity
- ii. instantaneous velocity

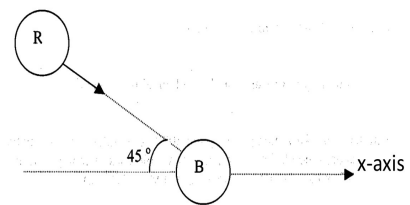


- (b) ■

- i. The figure above shows a part of car performance data.
 - A. Calculate the total distance travelled by the car. (**Ans:** $d = 1875m$)
 - B. Draw a graph of its acceleration against time between $t = 0s$ and $t = 50s$. Show your calculation.
- (c) A ball on the field was kicked with an initial velocity of $16.5ms^{-1}$ at an angle of 35° above the horizontal line. After passing a maximum height, the ball hit the goal post bar at a height of 3m from the ground.
 - i. Determine the time taken by the ball to hit the bar. (**Ans:** $t = 1.53s$)
 - ii. Calculate the distance of the goal post from the footballer. (**Ans:** $d = 20.7m$)

3: MOMENTUM & IMPULSE

1. (00/01)

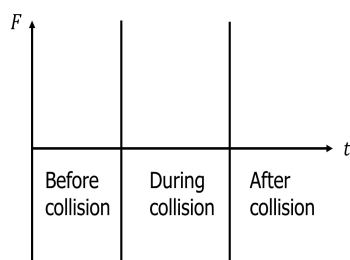


A red ball, R , of mass 0.1 kg moving at velocity 0.8 ms^{-1} at an angle of 45° from the x-axis, collides with a blue ball, B , of mass 0.2 kg at rest as shown in the figure above. After the collision, ball R moves with velocity 0.5 ms^{-1} at angle 20° from the x-axis, whilst ball B moves at an angle of θ from the axis x-axis. Calculate the momentum of R and B before and after the collision, and determine the magnitude and direction of the velocity of B after the collision. (**Ans:** $v_B = 0.2\text{ ms}^{-1}$ at an angle of 78° from the x-axis)

2. (PSPM 05/06) A body P of mass m moves with velocity u collides and sticks to a stationary body Q of mass $3m$.

(a) State two physical characteristics of the collision.

(b) Determine the total kinetic energy after collision in terms of m and u . (**Ans:** $E_k = [0.125mu^2]$)

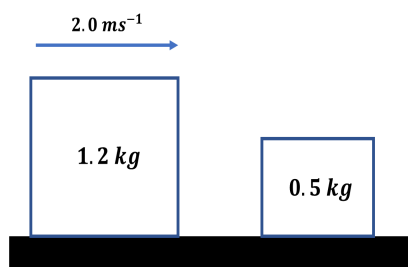


(c)

Copy the figure above and sketch on the same axes, the changes in the force F on body Q with time t before, during and after collision.

3. (PSPM 07/08)

(a) Explain the principle used to determine whether a collision between two bodies is elastic or inelastic.



(b)

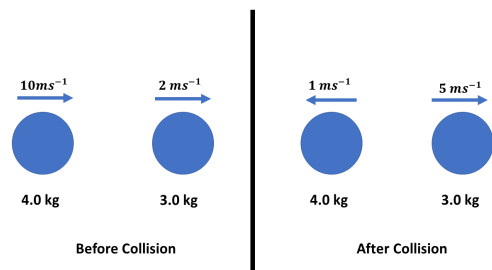
A 1.2 kg object moving at initial velocity 2.0 ms^{-1} collides elastically with a stationary 0.5 kg object as shown in the figure above. Calculate

i. the velocity of each object after the collision. (**Ans:** $v_i = (0.824, 2.82)\text{ ms}^{-1}$)

ii. the impulsive force if their contact time is 0.3 s . (**Ans:** $F = -4.70\text{ N}$)

(c) State ONE physical property of a material that is used as car bumper. Explain your answer.

4. (PSPM 08/09)



The figure above shows the velocities of two metal balls of mass 4.0 kg and 3.0 kg before and after a collision. Determine the type of the collision.

5. (PSPM 10/11) A 50 g marble is released from a height of 1 m above the floor. Calculate its momentum just before hitting the floor. [**Ans:** $p = 0.222 \text{ kgms}^{-1}$ downward]

6. (PSPM 11/12) An 8 g bullet moving at 50 ms^{-1} strikes a wooden block. The bullet undergoes uniform deceleration and stopped 12 cm inside the block. Calculate the

- time taken for the bullet to stop [**Ans:** $t = 4.81 \times 10^{-3} \text{ s}$]
- impulse on the block [**Ans:** $J = -0.4 \text{ kgms}^{-1}$]
- average force on the block [**Ans:** $F_{av} = -83.2 \text{ N}$]

7. (PSPM 12/13) Two identical balls with speed 4 ms^{-1} and 2 ms^{-1} collide head-on and stick together. Calculate their speed after the collision. [**Ans:** 1 ms^{-1}]

8. (PSPM 13/14) What is meant by impulse?

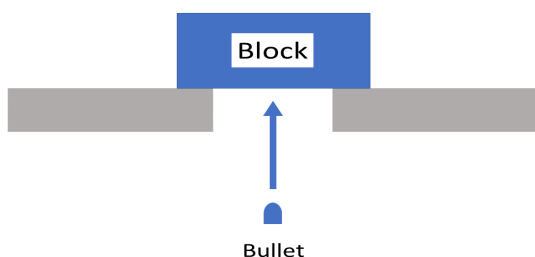
9. (PSPM 14/15)

- State the principle of conservation of momentum.
- A 6.25 kg trolley moving with the velocity 5.5 ms^{-1} hits a stationary 1.2 kg trolley. After the collision the trolleys stick together and move with a constant velocity. Calculate
 - the velocity after the collision [**Ans:** 4.6 ms^{-1}]
 - the loss of kinetic energy [**Ans:** 15.7 J]

10. (PSPM 15/16)

- How is force related to momentum?
- State a physical quantity used to indicate the difference between elastic and inelastic collision.

11. (PSPM 16/17)



The figure above shows a 12 g bullet shot vertically into a 5 kg block and lifting it upwards to a maximum height of 4 mm . The bullet travelled for 1 ms in the block before stopping completely. Calculate the

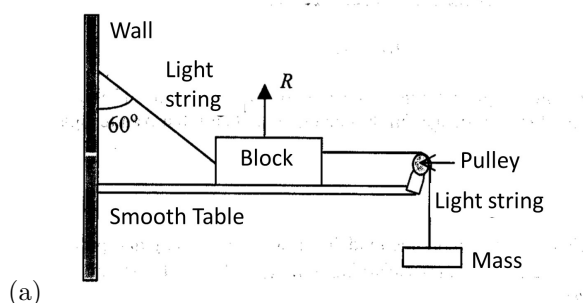
- the speed of the block and the bullet just after the collision.
- impulse on the block
- depth of the bullet embedded in the block

12. (PSPM 17/18)

- State **one (1)** similarity and **one (1)** difference between elastic collision and inelastic collision.
- A tennis player hits a 0.06kg ball horizontally approaching at 50ms^{-1} perpendicularly to his racquet's surface. He returns the shot at 40ms^{-1} in the opposite direction.
 - Calculate the impulse to the ball by the racquet? [**Ans:** 5.4Ns]
 - How much work does the racquet do on the ball? [**Ans:** 27J]
 - If the ball hits the plane of the racquet at an angle, will the impulse delivered to the ball increase, decrease or remain the same? Explain. [**Ans:** Decrease]

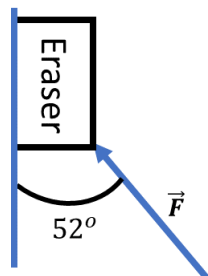
4: FORCES

1. (PSPM 00/01)



- The diagram above shows a pulley system with weighted blocks attached by light strings. If the weight of the block is 30N , calculate the magnitude of the reaction force, R . [**Ans:** 30N]
- (PSPM 05/06) A block of mass 2kg is pushed along a horizontal surface with a force $F = 3.2\text{N}$. The block experiences an acceleration $a = 0.3\text{ms}^{-2}$. What is the coefficient of friction between the block and the horizontal surface? (**Ans:** $\mu = 0.133$).
 - (PSPM 05/06) A man pulls a 45kg block at constant velocity on a rough surface. The angle between the rope and the horizontal is 30° and the coefficient of kinetic friction between the block and the surface is 0.6 .
 - Sketch and label all the forces acting on the block.
 - Calculate the tension in the rope. (**Ans:** $T = 227\text{N}$).

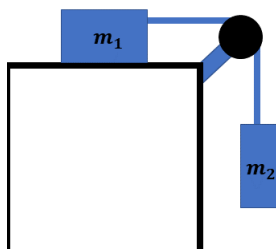
4. (PSPM 06/07)



The figure above shows a 0.2kg eraser being pressed against a whiteboard by a force F inclined at 52° to the whiteboard. The coefficient of static friction, μ , between the eraser and whiteboard is 0.3 .

- Draw all the forces acting on the eraser.
- Calculate the force F needed just to keep the eraser from sliding down. [**Ans:** $F = 2.30\text{N}$]
- What will happen to the eraser if a stronger force \vec{F}_1 is exerted at the same angle? Give a reason for your answer.

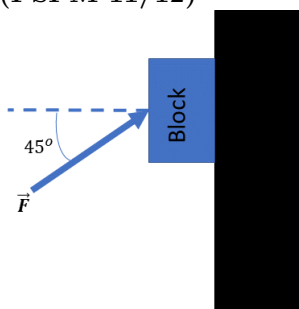
5. (PSPM 09/10)



The figure above shows a block of mass $m_1 = 6.0\text{kg}$ on a horizontal surface with coefficient of kinetic friction, $\mu_k = 0.22$ is connected by a string through a pulley to another block of mass $m_2 = 3.0\text{kg}$. The system is released from rest.

- Draw the forces acting on the blocks when they are in motion.
- Calculate the acceleration of the blocks. [Ans: $|\vec{a}| = 1.82\text{ms}^{-2}$]
- Calculate the tension in the string. [Ans: $T = 23.9\text{N}$]

6. (PSPM 11/12)

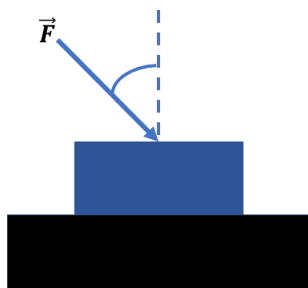


The figure above shows a 0.4kg block being pushed against a rough vertical wall by a force F at an angle 45° with respect to the horizontal. The block remains stationary.

- Sketch a free body diagram of all the forces acting on the block.
- If the coefficient of static friction, $\mu_s = 0.20$, what is the magnitude of \vec{F} ? [Ans: $|\vec{F}| = 4.62\text{N}$]

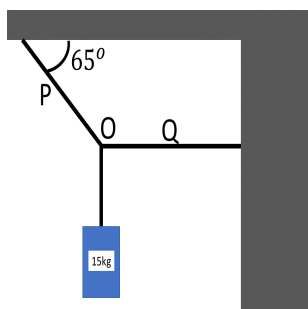
7. (PSPM 12/13)

- A 0.5 kg box is initially at rest on a smooth horizontal surface. It is acted upon by a horizontal force for a distance of 3 m . If the final speed of the box is 5ms^{-1} , calculate the magnitude of the force. [Ans: $F = 2.08\text{N}$]



- The figure above shows a 2.0kg block is being pushed along a rough surface by a force $F = 30\text{N}$ at an angle 60° from the normal.
 - Sketch a free body diagram for the block. Use common symbol for each force.
 - If the block moves at constant acceleration 0.5ms^{-2} , calculate the coefficient of friction. [$\mu = 0.72$]

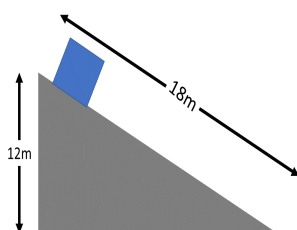
8. (PSPM 13/14)



(a)

The figure shows a 15kg load held in equilibrium by ropes, P & Q fastened to the ceiling and the wall respectively.

- Sketch a free body diagram at point O.
- Calculate the tension of ropes P and Q.

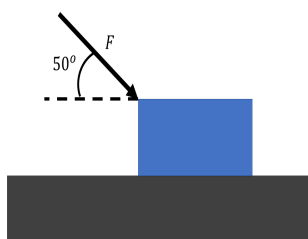


(b)

The figure shows a block held at rest at the top of a 18m long rough slope with a coefficient of kinetic friction of 0.19 . The height of the box on the slope is 12m . When released, the block slides down.

- Calculate the final speed of the block at the bottom of the slope.
- If the mass of the block is increased, will the final speed of the block decrease, same or increase? Justify your answer.

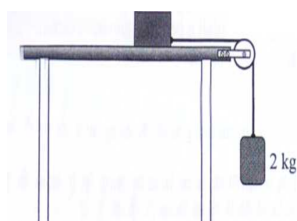
9. (PSPM 14/15)



The figure shows a 500N , F acts on a stationary 25kg box lying on a rough surface. After 4s , the speed of the box is 2ms^{-1} . Calculate

- the frictional force on the box, [**Ans:** $F_f = 308.9\text{N}$]
- the coefficient of the kinetic friction between the box and the rough surface. [**Ans:** $\mu = 0.49$]

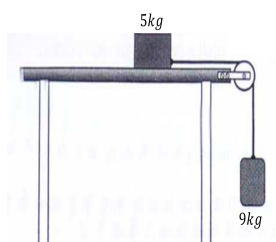
10. (PSPM 15/16)



The figure shows a 2.5kg block connected to a 2kg load by a light string through a pulley of negligible mass. The coefficient of kinetic friction between the block and table is 0.18 . When the system is released, calculate the

- acceleration of the block [**Ans:** $a = 3.38\text{ms}^{-2}$]
- tension in the string [**Ans:** $T = 12.86\text{N}$]
- total kinetic energy of the system after the block has moved 0.6m using the work-energy theorem. [**Ans:** $E_k = 9.12\text{J}$]
- final velocity, v_f of the block. [**Ans:** $v = 2.01\text{ms}^{-1}$]

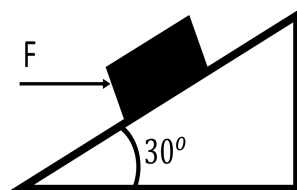
11. (PSPM 17/18)



The figure shows a 5kg block placed on frictionless horizontal table, is connected to a 9kg hanging box by a string that passes over a pulley.

- Draw free-body diagram of both boxes
- Determine the magnitude of acceleration of both boxes [**Ans:** $a = 6.3\text{ms}^{-1}$]
- Determine the magnitude of tension in the string [**Ans:** $T = 31.5\text{N}$]

12. (PSPM 17/18)

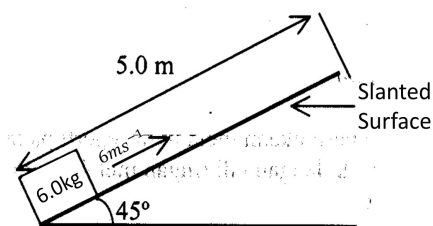


The figure shows an object of mass 2.0kg placed on a rough plane inclined at 30° with the horizontal. The coefficient of kinetic friction between the object and the plane surface is 0.25 . A constant horizontal force of $F = 50\text{N}$ acts on the object and pushes it along the inclined plane with acceleration a .

- Draw free-body diagram of both boxes
- Determine the magnitude of acceleration of both boxes.

5: WORK, ENERGY & POWER

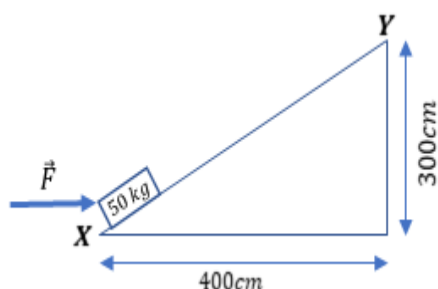
1. (PSPM 00/01)



(a)

The diagram above shows a block of mass 6.0 kg moving up the slope at 6 ms^{-1} through a distance of 5.0 m before it comes to a stop. Calculate the energy loss by friction. [$E_{\text{loss}} = 100\text{ J}$]

2. (PSPS 01/02)



The figure above shows a horizontal force, \vec{F} , pushing a safe of mass 50 kg on a smooth inclined plane from position X to position Y. If $|\vec{F}|$ is 400 N , calculate

(a) the work done to move the safe (in Joule) [**Ans:** $W = 128\text{ J}$]

(b) the potential energy at position Y. [**Ans:** $E_{\text{grav}} = 1471.5\text{ J}$]

3. (PSPS 04/05)

A Proton car has maximum power of 82 kW and may attain maximum speed of 190 km h^{-1} . Calculate the force of the car at maximum speed. [**Ans:** $F|_{\text{max speed}} = 1553.6\text{ N}$]

4. (PSPM 05/06)

A 10.0 J of work is needed to stretch an elastic spring by 2.0 cm . Calculate the work required to further extend the spring to 5.0 cm . [**Ans:** $W|_{5\text{ cm}} = 52.5\text{ J}$]

5. (PSPM 06/07)

A motorcycle overtakes a slow moving lorry by speeding up from 16 ms^{-1} to 10 ms^{-1} in 2 s . If the total mass of the rider and the motorcycle is 150 kg , calculate the required power. [**Ans:** $P|_{150\text{ kg}} = 2550\text{ W}$]

6. (PSPM 09/10)

A particle undergoes displacement $\vec{s} = -4\hat{i} - 5\hat{j}\text{ m}$ when acted by a force, $\vec{F} = 3\hat{i} - 5\hat{j}\text{ N}$. Calculate the

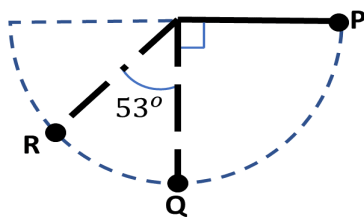
(a) work done by the force. [**Ans:** $W = 13\text{ J}$]

(b) average power if the force acts for 5 seconds . [**Ans:** $P = 2.6\text{ W}$]

7. (PSPM 10/11)

A spring stretches by 4 mm when a 1.5 kg mass is suspended at its end. Calculate the spring constant. [**Ans:** $k = 3.68 \times 10^3\text{ Nm}^{-1}$]

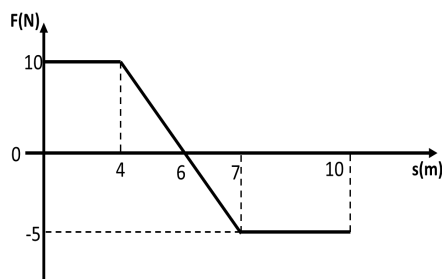
8. (PSPM 11/12)



The figure above shows a 0.8 kg pendulum bob being released from rest at P. The length of the string is 0.75 m . Calculate the

- work done by gravity on the bob at R. [**Ans:** $W = 2.35\text{ J}$]
- speed of the bob at Q. [**Ans:** $v = 3.84\text{ ms}^{-1}$]

9. (PSPM 18/19)



An object of mass 2.0 kg travels along horizontal floor under the action of force F . The figure above shows the graph of F against the displacement s . The speed of the object at $s = 0$ is 10 ms^{-1} . Determine the speed of the object at $s = 10\text{ m}$. [**Ans:** 11.5 ms^{-1}]

10. (PSPM 18.19)

A 2.0 kg object is released vertically onto the top end of a vertical spring 30 cm away. The spring constant is 2000 Nm^{-1} .

- Calculate the speed of the object just before striking the spring [**Ans:** $v = 2.43\text{ ms}^{-1}$]
- Determine the maximum compression x . [**Ans:** $8.7 \times 10^{-2}\text{ m}$]