## Paper / Subject Code: 51401 / Applied Mathematics-III

14-Nov-2019 1T01223 - S.E.(Information Technology Engineering)(Choice Base) / 51401 - Applied Mathematics-III 76566

[Time: 3 Hours]

[ Marks:80]

## Please check whether you have got the right question paper.

**N.B:** 1. Q 1 is compulsory.

- 2. Attempt any three from remaining
- 3. Rights indicate full marks.
- 1. a. If A, B, C are subset of universal set V then prove that  $A \times (B \cap C) = (A \times B) \cap (A \times C)$  05
  - b. If f: R $\rightarrow$ R is given by y = 2x + 1, prove that f is one to one and onto and find  $f^{-1}$
  - c. Find L  $\{(1+t\bar{e}^t)^3\}$
  - d. Check whether the following function Harmonic or not  $3x^2 + sinx + y^2 + 5y + 4$  05
- 2. a. Find k if  $f(z) = \frac{1}{2} \log (x^2 + y^2) + i \tan^{-1} \frac{kx}{y}$  is analytic **06** 
  - b. Find L {|sin2t|} 06
  - c. Let f:  $R \to R$   $f(x) = x^2 + 2x 1$ g:  $R \to R$   $g(x) = 4x^2 + 2$

Find (I) f 0 (gof) (II) go (fog)

- 3. a. Find Bilinear transformation under which Z=1, -i, -1 from point w=i, 0, -i
  - b. If A be the set of non-integers and let R be a relation on A×A defined by (a, b) R(c, d) if ad=bc, then prove that R is an equivalence relation.
  - c. Find (1) L  $\left\{ \int_{0}^{t} \bar{e}^{u} \frac{\sin u}{u} du \right\}$  (2) L  $\left\{ (1 + 2t + 3t^{2} + t^{3})H(t 2) \right\}$
- 4. a. Use convolution them and evaluate  $L^{-1}\left\{\frac{(s+5)^2}{(s^2+10s+16)^2}\right\}$ 
  - b. Find transitive clouser of following relation defined on  $A = \{a, b, c, d, e\}$  by Warshal **06** algorithm  $R = \{(a, a) (a, b) (b, c) (c, d) (c, c) (d, e)\}$
  - c. A man speaks truth 3 times out of 5 when a die is thrown he states that it gave an ace what is probability that this event has actually happened.

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- 5. a. How many four digit numbers can be formed out of the digits 1, 2, 3, 5, 7, 8, 9 if no digit is **06** repeated twice? How many of them will be greater than 3000.
  - 66

b. Solve using Laplace transform  $\frac{d^2y}{dt^2} + 9y = 18 \text{ given that } y(0) = 0 \text{ and } y(\frac{\pi}{2}) = 0$ 

06

08

- c. Evaluate (1) L<sup>-1</sup>  $\left\{ \frac{1}{\sqrt{2s+1}} \right\}$ 
  - (2) L<sup>-1</sup>  $\left\{ \frac{2s^2 6s + 5}{s^3 6s^2 + 115 6} \right\}$
- 6. a. Solve  $a_n = 5a_{n-1} 6a_{n-2}$  for  $n \ge 2$ ,  $a_0 = 0$ ,  $a_1 = 1$ 
  - b. Find orthogonal curves of family of curves  $e^{-x} \cos y + xy = \alpha$ , where  $\alpha$  is the real constant 06
  - c. i. Find the image of rectangular region bounded by x=0, x=3, y=0, y=2 under the transformation w=z+(1+i)
    - ii. A fair dice is thrown thrice. Find probability that sum of numbers obtained is 10.



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