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In[169]:= ClearAll["Global`*"]
N6i = {{1 - 3  $\epsilon$  - 3  $\eta$  + 2  $\epsilon^2$  + 2  $\eta^2$  + 4  $\epsilon \eta$ }, {2  $\epsilon^2$  -  $\epsilon$ },
      {2  $\eta^2$  -  $\eta$ }, {4  $\epsilon$  - 4  $\epsilon^2$  - 4  $\epsilon \eta$ }, {4  $\epsilon \eta$ }, {4  $\eta$  - 4  $\eta^2$  - 4  $\epsilon \eta$ }};
MatrixForm[N6i]
N6j = Transpose[N6i];
(*N3i={{1- $\epsilon$ - $\eta$ },{ $\epsilon$ },{ $\eta$ }};
MatrixForm[N3i]
N3j=Transpose[N3i];*)

(*xj={{15,18,16,16.5,17,15.5}};
yj={{22,23.5,26,22.75,24.75,24}};*)
xj = {{x1, x2, x3, (x1 + x2) / 2, (x2 + x3) / 2, (x3 + x1) / 2}};
yj = {{y1, y2, y3, (y1 + y2) / 2, (y2 + y3) / 2, (y3 + y1) / 2}};
xi = Transpose[xj];
yi = Transpose[yj];

xa = N6j.xi;
ya = N6j.yi;

dxade = D[xa,  $\epsilon$ ];
dyade = D[ya,  $\epsilon$ ];
dxadn = D[xa,  $\eta$ ];
dyadn = D[ya,  $\eta$ ];

dxade = dxade[[1, 1]];
dyade = dyade[[1, 1]];
dxadn = dxadn[[1, 1]];
dyadn = dyadn[[1, 1]];

J = {{dxade, dyade}, {dxadn, dyadn}};
mJ = Det[J];
mJ = Collect[mJ, { $\epsilon$ ,  $\eta$ }]
B = Inverse[J];
MatrixForm[Simplify[Collect[J, { $\epsilon$ ,  $\eta$ }]]]
MatrixForm[Simplify[Collect[B, { $\epsilon$ ,  $\eta$ }]]]

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Out[171]//MatrixForm=

$$\begin{pmatrix} 1 - 3 \epsilon + 2 \epsilon^2 - 3 \eta + 4 \epsilon \eta + 2 \eta^2 \\ -\epsilon + 2 \epsilon^2 \\ -\eta + 2 \eta^2 \\ 4 \epsilon - 4 \epsilon^2 - 4 \epsilon \eta \\ 4 \epsilon \eta \\ 4 \eta - 4 \epsilon \eta - 4 \eta^2 \end{pmatrix}$$

Out[189]=  $-x_2 y_1 + x_3 y_1 + x_1 y_2 - x_3 y_2 - x_1 y_3 + x_2 y_3$ 

Out[191]//MatrixForm=

$$\begin{pmatrix} -x_1 + x_2 & -y_1 + y_2 \\ -x_1 + x_3 & -y_1 + y_3 \end{pmatrix}$$

Out[192]//MatrixForm=

$$\begin{pmatrix} \frac{y_1 - y_3}{x_2 y_1 - x_3 y_1 - x_1 y_2 + x_3 y_2 + x_1 y_3 - x_2 y_3} & \frac{y_1 - y_2}{x_3 (y_1 - y_2) + x_1 (y_2 - y_3) + x_2 (-y_1 + y_3)} \\ \frac{x_1 - x_3}{x_3 (y_1 - y_2) + x_1 (y_2 - y_3) + x_2 (-y_1 + y_3)} & \frac{x_1 - x_2}{x_2 y_1 - x_3 y_1 - x_1 y_2 + x_3 y_2 + x_1 y_3 - x_2 y_3} \end{pmatrix}$$