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In[61]:= ClearAll["Global`*"]
N6i = {{1 - 3  $\epsilon$  - 3  $\eta$  + 2  $\epsilon^2$  + 2  $\eta^2$  + 4  $\epsilon \eta$ }, {2  $\epsilon^2$  -  $\epsilon$ },
      {2  $\eta^2$  -  $\eta$ }, {4  $\epsilon$  - 4  $\epsilon^2$  - 4  $\epsilon \eta$ }, {4  $\epsilon \eta$ }, {4  $\eta$  - 4  $\eta^2$  - 4  $\epsilon \eta$ }};
MatrixForm[N6i]
N6j = Transpose[N6i];
N3i = {{1 -  $\epsilon$  -  $\eta$ }, { $\epsilon$ }, { $\eta$ }};
MatrixForm[N3i]
N3j = Transpose[N3i];

xj = {{x1, x2, x3, x4, x5, x6}};
yj = {{y1, y2, y3, y4, y5, y6}};
xi = Transpose[xj];
yi = Transpose[yj];

xa = N6j.xi;
ya = N6j.yi;

dxade = D[xa,  $\epsilon$ ];
dyade = D[ya,  $\epsilon$ ];
dxadn = D[xa,  $\eta$ ];
dyadn = D[ya,  $\eta$ ];

J = {{dxade, dyade}, {dxadn, dyadn}};
mJ = (dxade * dyadn) - (dyade * dxadn);
mJ = mJ[[1, 1]];
B = {{dyadn, -dyade}, {-dxadn, dxade}}/mJ;
MatrixForm[Collect[J, { $\epsilon$ ,  $\eta$ }]]
MatrixForm[Collect[B, { $\epsilon$ ,  $\eta$ }]]

dxade = j11 + j12 *  $\epsilon$  + j13 *  $\eta$ ;
dyade = j21 + j22 *  $\epsilon$  + j23 *  $\eta$ ;
dxadn = j31 + j32 *  $\epsilon$  + j33 *  $\eta$ ;
dyadn = j41 + j42 *  $\epsilon$  + j43 *  $\eta$ ;
mJ = (dxade * dyadn) - (dyade * dxadn);
B = {{dyadn, -dyade}, {-dxadn, dxade}}/mJ;
MatrixForm[B]

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Out[63]//MatrixForm=

$$\begin{pmatrix} 1 - 3\epsilon + 2\epsilon^2 - 3\eta + 4\epsilon\eta + 2\eta^2 \\ -\epsilon + 2\epsilon^2 \\ -\eta + 2\eta^2 \\ 4\epsilon - 4\epsilon^2 - 4\epsilon\eta \\ 4\epsilon\eta \\ 4\eta - 4\epsilon\eta - 4\eta^2 \end{pmatrix}$$

Out[66]//MatrixForm=

$$\begin{pmatrix} \mathbf{1} - \epsilon - \eta \\ \epsilon \\ \eta \end{pmatrix}$$

Out[82]//MatrixForm=

$$\begin{pmatrix} (-3x_1 - x_2 + 4x_4 + (4x_1 + 4x_2 - 8x_4)\epsilon + (4x_1 - 4x_4 + 4x_5 - 4x_6)\eta) & (-3y_1 - y_2 + 4y_4 + (4y_1 + 4y_2 - 8y_4)\epsilon + (4y_1 - 4y_4 + 4y_5 - 4y_6)\eta) \\ (-3x_1 - x_3 + 4x_6 + (4x_1 - 4x_4 + 4x_5 - 4x_6)\epsilon + (4x_1 + 4x_3 - 8x_6)\eta) & (-3y_1 - y_3 + 4y_6 + (4y_1 - 4y_4 + 4y_5 - 4y_6)\epsilon + (4y_1 + 4y_3 - 8y_6)\eta) \end{pmatrix}$$

Out[83]//MatrixForm=

$$\left(\begin{array}{l} \frac{-4 y_4 \epsilon + 4 y_5 \epsilon + y_6 (4 - 4 \epsilon - 8 \eta) + y_3 (-1 + \epsilon)}{(-4 x_4 \epsilon + 4 x_5 \epsilon + x_6 (4 - 4 \epsilon - 8 \eta) + x_3 (-1 + 4 \eta) + x_1 (-3 + 4 \epsilon + 4 \eta)) (y_2 (-1 + 4 \epsilon) + y_4 (4 - 8 \epsilon - 4 \eta) + 4 y_5 \eta - 4 y_6 \eta + y_1 (-3 + 4 \epsilon + 4 \eta))} + (x_2 (-1 + 4 \epsilon) + 4 x_4 \epsilon - 4 x_5 \epsilon - x_6 (4 - 4 \epsilon - 8 \eta) - x_3 (-1 + 4 \eta) + x_1 (-3 + 4 \epsilon + 4 \eta)) \\ \frac{4 x_4 \epsilon - 4 x_5 \epsilon - x_6 (4 - 4 \epsilon - 8 \eta) - x_3 (-1 + 4 \eta) + x_1 (-3 + 4 \epsilon + 4 \eta)}{(-4 x_4 \epsilon + 4 x_5 \epsilon + x_6 (4 - 4 \epsilon - 8 \eta) + x_3 (-1 + 4 \eta) + x_1 (-3 + 4 \epsilon + 4 \eta)) (y_2 (-1 + 4 \epsilon) + y_4 (4 - 8 \epsilon - 4 \eta) + 4 y_5 \eta - 4 y_6 \eta + y_1 (-3 + 4 \epsilon + 4 \eta))} + (x_2 (-1 + 4 \epsilon) + 4 x_4 \epsilon - 4 x_5 \epsilon - x_6 (4 - 4 \epsilon - 8 \eta) - x_3 (-1 + 4 \eta) + x_1 (-3 + 4 \epsilon + 4 \eta)) \end{array} \right)$$

Out[90]//MatrixForm=

$$\left(\begin{array}{c|c} \frac{j_{41}+j_{42} \in +j_{43} \eta}{-(j_{21}+j_{22} \in +j_{23} \eta) (j_{31}+j_{32} \in +j_{33} \eta) + (j_{11}+j_{12} \in +j_{13} \eta) (j_{41}+j_{42} \in +j_{43} \eta)} & \frac{-j_{21}-j_{22} \in -j_{23} \eta}{-(j_{21}+j_{22} \in +j_{23} \eta) (j_{31}+j_{32} \in +j_{33} \eta) + (j_{11}+j_{12} \in +j_{13} \eta) (j_{41}+j_{42} \in +j_{43} \eta)} \\ \hline \frac{-j_{31}-j_{32} \in -j_{33} \eta}{-(j_{21}+j_{22} \in +j_{23} \eta) (j_{31}+j_{32} \in +j_{33} \eta) + (j_{11}+j_{12} \in +j_{13} \eta) (j_{41}+j_{42} \in +j_{43} \eta)} & \frac{j_{11}+j_{12} \in +j_{13} \eta}{-(j_{21}+j_{22} \in +j_{23} \eta) (j_{31}+j_{32} \in +j_{33} \eta) + (j_{11}+j_{12} \in +j_{13} \eta) (j_{41}+j_{42} \in +j_{43} \eta)} \end{array} \right)$$