# **Parallel Processing**

# **Xeon Phi**

Guy Tel-Zur 4/1/2016

# **Agenda**

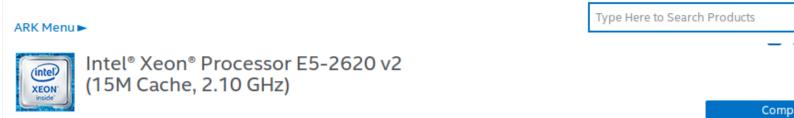
Introduction to Xeon Phi

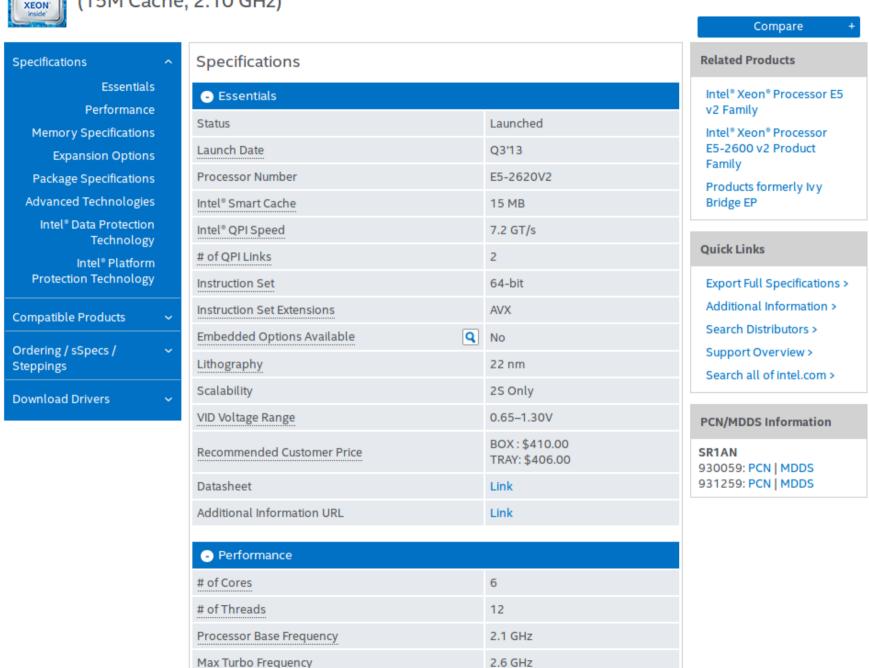
http://www.colfaxintl.com/nd/resources/Files/Stanford-Conference-2015-Scientific-Computing-with-Intel-Xeon-Phi-Coprocessors.pdf

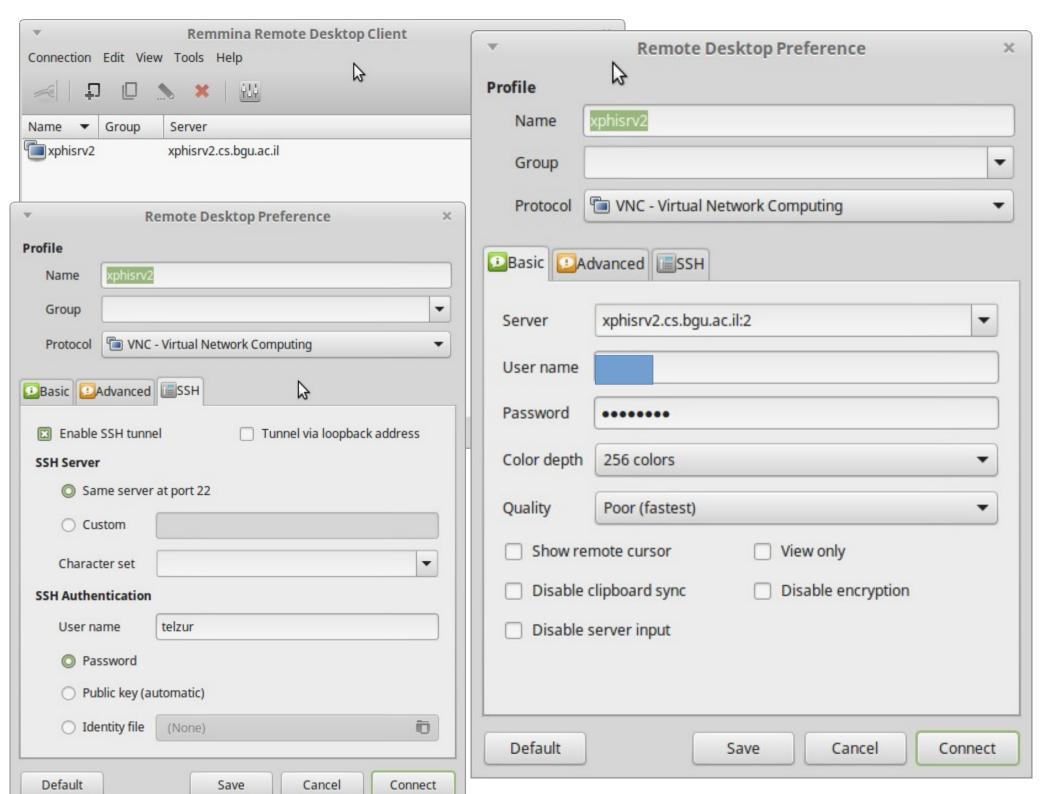
- Code modernization
  - Part 1: nbody
  - Part 2: Optimizations techniques

# Tests were performed on xphisrv2.cs.bgu.ac.il

- Cpu 2x Intel(R) Xeon(R) CPU E5-2620 v2 @ 2.10GHz
- 6 cores each x 2 (hyperthreading), total 24 cores
- MIC: 5110P (x 2)







### Part 1: nbody

#### Colfax material:

http://colfaxresearch.com/test-drivingintel-xeon-phi-coprocessors-with-a-basi c-n-body-simulation/

**GitHub** 

Search GitHut

#### Paper:

http://colfaxresearch.com/download/53

Example code is based on: mini-nbody: A simple N-body Code https://github.com/harrism/mini-nbody
By Mark Harris



Mark Harris harrism

- ₩ NVIDI
- Larnook, NSW Australia
- http://www.markmark.net

# nbody

- Unzip mini-nbody-master
- Baseline: put into comment // rate
- icc compile: icc -std=c99 -qopenmp -o
   nbody ./nbody.c -lm
- gcc compile: gcc -std=c99 -fopenmp -o nbody gcc ./nbody.c -lm
- Working dir on xphisrv2: /home/telzur/Teaching/PP/XeonPhi

#### **Baseline version**

export OMP\_NUM\_THREADS=24

# Tests on the CPUs gcc versus icc (no optimizations)

[telzur@xphisrv2 mini-nbody-master]\$ time ./nbody gcc

[telzur@xphisrv2 mini-nbody-master]\$ time ./nbody\_icc

Iteration 1: 2.005 seconds

Iteration 1: 0.230 seconds
Iteration 2: 0.202 seconds

Iteration 2: 1.991 seconds

11.01.011 2. 0.202 300011d3

Iteration 3: 1.990 seconds

Iteration 3: 0.201 seconds

Iteration 4: 1.990 seconds

Iteration 4: 0.202 seconds

Iteration 5: 1.990 seconds

Iteration 5: 0.206 seconds

Iteration 6: 1.990 seconds

Iteration 6: 0.202 seconds

Iteration 7: 1.990 seconds

Iteration 7: 0.201 seconds

Iteration 8: 1.989 seconds

Iteration 8: 0.201 seconds

Iteration 9: 1.990 seconds

Iteration 9: 0.201 seconds

Iteration 10: 1.991 seconds

Iteration 10: 0.204 seconds

30000 Bodies: average 0.452 Billion Interactions / second

30000 Bodies: average 4.450 Billion Interactions / second

real 0m19.927s

real 0m2.058s

user 6m18.485s

user 0m40.860s

sys 0m0.010s

svs 0m0.026s

# Test on the mic: nbody-orig

24 threads

telzur@xphisrv2-mic0:~/nbody\$ time ./nbody-orig

Iteration 1: 0.733 seconds

Iteration 2: 0.691 seconds

Iteration 3: 0.691 seconds

Iteration 4: 0.688 seconds

Iteration 5: 0.686 seconds

Iteration 6: 0.689 seconds

Iteration 7: 0.689 seconds

Iteration 8: 0.693 seconds

Iteration 9: 0.689 seconds

Iteration 10: 0.693 seconds

30000 Bodies: average 1.304 Billion Interactions / second

real 0m6.980s

user 2m45.660s

sys 0m0.060s

240 threads

telzur@xphisrv2-mic0:~/nbody\$ time ./nbody-orig

Iteration 1: 0.357 seconds

Iteration 2: 0.098 seconds

Iteration 3: 0.099 seconds

Iteration 4: 0.100 seconds

Iteration 5: 0.100 seconds

Iteration 6: 0.100 seconds

Iteration 7: 0.100 seconds

Iteration 8: 0.100 seconds

Iteration 9: 0.100 seconds

Iteration 10: 0.100 seconds

30000 Bodies: average 9.050 Billion Interactions / second

real 0m1.343s

user 3m59.170s

sys 0m2.300s

mic0, /home/telzur/nbody

### Test on the mic: nbody-soa

24 threads

telzur@xphisrv2-mic0:~/nbody\$ time ./nbody-soa

Iteration 1: 0.191 seconds

Iteration 2: 0.145 seconds

Iteration 3: 0.145 seconds

Iteration 4: 0.145 seconds

Iteration 5: 0.145 seconds

Iteration 6: 0.145 seconds

Iteration 7: 0.145 seconds

Iteration 8: 0.145 seconds

Iteration 9: 0.145 seconds

Iteration 10: 0.145 seconds

30000 Bodies: average 6.217 Billion Interactions / second

real 0m1.532s

user 0m34.830s

sys 0m0.050s

240 threads

telzur@xphisrv2-mic0:~/nbody\$ time ./nbody-soa

Iteration 1: 0.274 seconds

Iteration 2: 0.026 seconds

Iteration 3: 0.027 seconds

Iteration 4: 0.027 seconds

Iteration 5: 0.027 seconds

Iteration 6: 0.027 seconds

Iteration 7: 0.027 seconds

Iteration 8: 0.026 seconds

Iteration 9: 0.027 seconds

Iteration 10: 0.027 seconds

30000 Bodies: average 33.747 Billion Interactions / second

real 0m0.607s

user 1m4.960s

sys 0m2.380s

#### diffe Seath / repure philosofy. C. / mic/nbody-soa. c

```
XPHI> diff ./nbody.c ./mic/nbody-soa.c
5a6
8c9
< typedef struct { float x, y, z, vx, vy, vz; } Body;
> typedef struct {    float *x, *y, *z, *vx, *vy, *vz;    }    BodySystem;
16c17,18
< void bodyForce(Body *p, float dt, int n) {</pre>
> void bodyForce(BodySystem p, float dt, int n) {
22,24c24,26
        float dx = p[j].x - p[i].x;
        float dy = p[j].y - p[i].y;
        float dz = p[j].z - p[i].z;
<
        float dy = p.y[j] - p.y[i];
        float dz = p.z[j] - p.z[i];
        float dx = p.x[j] - p.x[i];
32c34
      p[i].vx += dt*Fx; p[i].vy += dt*Fy; p[i].vz += dt*Fz;
      p.vx[i] += dt*Fx; p.vy[i] += dt*Fy; p.vz[i] += dt*Fz;
44c46
< int bytes = nBodies*sizeof(Body);</pre>
   int bytes = 6*nBodies*sizeof(float);
46c48,50
   Body *p = (Body*)buf;
   BodySystem p;
   p.x = buf+0*nBodies; p.y = buf+1*nBodies; p.z = buf+2*nBodies;
   p.vx = buf+3*nBodies; p.vy = buf+4*nBodies; p.vz = buf+5*nBodies;
58,60c62,64
        p[i].x += p[i].vx*dt;
        p[i].y += p[i].vy*dt;
        p[i].z += p[i].vz*dt;
        p.x[i] += p.vx[i]*dt;
        p.y[i] += p.vy[i]*dt;
        p.z[i] += p.vz[i]*dt;
XPHT>
```

# Test on the mic: nbody-block

24 threads

telzur@xphisrv2-mic0:~/nbody\$ time ./nbody-block

Iteration 1: 0.196 seconds

Iteration 2: 0.152 seconds

Iteration 3: 0.152 seconds

Iteration 4: 0.152 seconds

Iteration 5: 0.152 seconds

Iteration 6: 0.152 seconds

Iteration 7: 0.152 seconds

Iteration 8: 0.152 seconds

Iteration 9: 0.152 seconds

Iteration 10: 0.152 seconds

30000 Bodies: average 5.923 Billion Interactions / second

real 0m1.601s

user 0m36.540s

sys 0m0.070s

240 threads

telzur@xphisrv2-mic0:~/nbody\$ time ./nbody-block

Iteration 1: 0.280 seconds

Iteration 2: 0.027 seconds

Iteration 3: 0.027 seconds

Iteration 4: 0.027 seconds

Iteration 5: 0.027 seconds

Iteration 6: 0.027 seconds

Iteration 7: 0.027 seconds

Iteration 8: 0.027 seconds

Iteration 9: 0.027 seconds

Iteration 10: 0.027 seconds

30000 Bodies: average 33.335 Billion Interactions / second

real 0m0.614s

user 1m5.250s

sys 0m2.220s

```
File Edit View Search Terminal Help
```

```
XPHI>
XPHI> diff ./mic/nbody-soa.c ./mic/nbody-block.c
6c6
> #define CACHELINE 64 // size of cache line [bytes]
18,31c18,38
< void bodyForce(BodySystem p, float dt, int n) {
    #pragma omp parallel for schedule(dynamic)
    for (int i = 0; i < n; i++) {
      float Fx = 0.0f; float Fy = 0.0f; float Fz = 0.0f;
      for (int j = 0; j < n; j++) {
        float dy = p.y[j] - p.y[i];
        float dz = p.z[j] - p.z[i];
        float dx = p.x[j] - p.x[i];
        float distSqr = dx*dx + dy*dy + dz*dz + SOFTENING;
        float invDist = 1.0f / sqrtf(distSqr);
        float invDist3 = invDist * invDist * invDist;
        Fx += dx * invDist3; Fy += dy * invDist3; Fz += dz * invDist3;
 void bodyForce(BodySystem p, float dt, int n, int tileSize) {
    for (int tile = 0; tile < n; tile += tileSize) {
      int to = tile + tileSize;
      if (to > n) to = n;
      #pragma omp parallel for schedule(dynamic)
      for (int i = 0; i < n; i++) {
        float Fx = 0.0f; float Fy = 0.0f; float Fz = 0.0f;
        for (int j = tile; j < to; j++) {
          float dy = p.y[j] - p.y[i];
          float dz = p.z[j] - p.z[i];
          float dx = p.x[j] - p.x[i];
          float distSqr = dx*dx + dy*dy + dz*dz + SOFTENING;
          float invDist = 1.0f / sqrtf(distSqr);
          float invDist3 = invDist * invDist;
          Fx += dx * invDist3; Fy += dy * invDist3; Fz += dz * invDist3;
        p.vx[i] += dt*Fx; p.vy[i] += dt*Fy; p.vz[i] += dt*Fz;
33,34d39
```

### Test on the mic: nbody-align

24 threads

telzur@xphisrv2-mic0:~/nbody\$ time ./nbody-align

Iteration 1: 0.170 seconds

Iteration 2: 0.125 seconds

Iteration 3: 0.126 seconds

Iteration 4: 0.125 seconds

Iteration 5: 0.125 seconds

Iteration 6: 0.125 seconds

Iteration 7: 0.126 seconds

Iteration 8: 0.125 seconds

Iteration 9: 0.125 seconds

Iteration 10: 0.126 seconds

30000 Bodies: average 7.175 Billion Interactions / second

real 0m1.338s

user 0m30.210s

sys 0m0.040s

240 threads

telzur@xphisrv2-mic0:~/nbody\$ time ./nbody-align

Iteration 1: 0.275 seconds

Iteration 2: 0.023 seconds

Iteration 3: 0.023 seconds

Iteration 4: 0.024 seconds

Iteration 5: 0.023 seconds

Iteration 6: 0.023 seconds

Iteration 7: 0.024 seconds

Iteration 8: 0.023 seconds

Iteration 9: 0.023 seconds

Iteration 10: 0.024 seconds

30000 Bodies: average 38.823 Billion Interactions / second

real 0m0.568s

user 0m57.530s

sys 0m0.640s

XPHI>

#### Part 2:

#### Materials thanks to: Colfax Research

Optimization Techniques for the Intel MIC Architecture

- http://colfaxresearch.com/optimization-techniques-for-theintel-mic-architecture-part-1-of-3-multi-threading-and-parallelreduction/
- http://colfaxresearch.com/optimization-techniques-for-theintel-mic-architecture-part-2-of-3-strip-mining-for-vectorization/
- http://colfaxresearch.com/optimization-techniques-for-theintel-mic-architecture-part-3-of-3-false-sharing-and-padding/
- http://colfaxresearch.com/download/1233/
- http://colfaxresearch.com/download/1241/



LEVEL OF ACCOMPLISHMENT

FUNDAMENTAL

**GUY TEL-ZUR** 

September 08, 2015

has successfully completed

#### PARALLEL PROGRAMMING AND OPTIMIZATION FOR INTEL® ARCHITECTURE

The HOW (Hands-on Workshop) series, a 20-hour Web-based training program with hands-on component on best practices for programming Intel® Xeon® processors and Intel® Xeon Phi™ coprocessors.



Gautam Shah

President and CEO, Colfax International

Fundamental

- issued to students who attended training for courses that do not have post-training exams

Craftsman

- issued to students who attended training and successfully passed post-training exams

Trainer

- issued to students who attended special courses and passed tests that qualify the attendee to conduct the named Colfax Developer Training program

Jailan Shals

```
[telzur@xphisrv2 Colfax_Tutorial_Binning]$ ./app-CPU
```

Particle Binning Optimization Demo (single precision) Additional information is available in accompanying papers at http://colfaxresea rch.com/

(c) Colfax International, 2015.

```
Initialization... done in 0.661 seconds.
Computing reference result... done in 2.457 seconds.
Benchmarking...
```

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#### IMPLEMENTATION θ: serial

Trial	Time, s	Speedup	GP/s	*
1	2.432e+00	n/a	5.52e-02	**
2	2.415e+00	n/a	5.56e-02	**
3	2.414e+00	n/a	5.56e-02	
4	2.412e+00	n/a	5.57e-02	
5	2.406e+00	n/a	5.58e-02	
6	2.407e+00	n/a	5.58e-02	
7	2.400e+00	n/a	5.59e-02	
8	2.412e+00	n/a	5.57e-02	
9	2.406e+00	n/a	5.58e-02	
10	2.414e+00	n/a	5.56e-02	

Average performance: 1.00 5.57e-02 +- 1.05e-04 GP/s

- Performance unit 1 GP/s is 10^9 particles binned per second.
- \*\* warm-up, not included in average

......

```
telzur@xphisrv2:~/Teaching/PP/XeonPhi/Colfax_Tutorial_Binning
 File Edit View Search Terminal Help
IMPLEMENTATION 1: parallel, atomics for reduction
Trial Time, s
                          Speedup
                                          GP/s *
     1 3.213e+00
                              0.75 4.18e-02 **
    2 3.016e+00
3 2.984e+00
4 2.983e+00
5 2.984e+00
6 2.984e+00
7 2.986e+00
                              0.80 4.45e-02 **
                              0.81 4.50e-02
                              0.81 4.50e-02
                              0.81 4.50e-02
                              0.81 4.50e-02
                              0.81 4.50e-02
   8 2.985e+00
9 2.984e+00
10 2.985e+00
                              0.81 4.50e-02
                              0.81 4.50e-02
                              0.81 4.50e-02
Average performance: 0.81 4.50e-02 +- 1.40e-05 GP/s
   - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
IMPLEMENTATION 2: parallel, thread-private containers for reduction
Trial Time, s
                          Speedup
                                            GP/s *
     1 1.852e-01 13.01 7.25e-01 **
2 1.852e-01 13.01 7.25e-01 **
    2 1.852e-01 13.01 7.25e-01

3 1.853e-01 13.00 7.24e-01

4 1.851e-01 13.01 7.25e-01

5 1.852e-01 13.01 7.25e-01

6 1.852e-01 13.01 7.25e-01

7 1.852e-01 13.01 7.25e-01

8 1.851e-01 13.01 7.25e-01

9 1.852e-01 13.00 7.25e-01
    10 1.855e-01 12.98 7.23e-01
```

Average performance: 13.01 7.25e-01 +- 4.73e-04 GP/s

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Performance unit 1 GP/s is 10^9 particles binned per second.

<sup>\*\* -</sup> warm-up, not included in average

GP/s \*

Trial Time, s

Speedup

1 8.954e-02 26.90 1.50e+00 \*\*

```
1 8.954e-02 26.90 1.50e+00 **
2 8.946e-02 26.93 1.50e+00 **
3 8.947e-02 26.92 1.50e+00
4 8.950e-02 26.91 1.50e+00
5 8.953e-02 26.90 1.50e+00
6 8.955e-02 26.90 1.50e+00
7 8.949e-02 26.92 1.50e+00
8 8.948e-02 26.92 1.50e+00
    9 8.948e-02 26.92 1.50e+00
10 8.949e-02 26.92 1.50e+00
Average performance: 26.91 1.50e+00 +- 4.15e-04 GP/s
  - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
IMPLEMENTATION 4: vectorized, aligned
Trial Time, s
                              Speedup
                                               GP/s *
     1 5.861e-02 41.10 2.29e+00 **
     2 5.848e-02 41.19 2.30e+00 **
3 5.851e-02 41.17 2.29e+00
     4 5.851e-02 41.17 2.29e+00

5 5.852e-02 41.16 2.29e+00

6 5.854e-02 41.15 2.29e+00

7 5.867e-02 41.06 2.29e+00

8 5.850e-02 41.18 2.29e+00
    9 5.850e-02 41.18 2.29e+00
10 5.854e-02 41.15 2.29e+00
Average performance: 41.15 2.29e+00 +- 2.07e-03 GP/s
   - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
```

```
telzur@xphisrv2:~/Teaching/PP/XeonPhi/Colfax Tutorial Binning
File Edit View Search Terminal Help
IMPLEMENTATION 5: global container for reduction in threads-first layout
Trial
       Time, s
                  Speedup
                               GP/s *
                    2.02 1.12e-01 **
   1 1.194e+00
   2 1.193e+00
                    2.02 1.12e-01 **
   3 1.194e+00
                    2.02 1.12e-01
                    2.02 1.12e-01
   1.194e+00
5 1.194e+00
   4 1.194e+00
                    2.02 1.12e-01
                    2.02 1.12e-01
   6 1.193e+00
                    2.02 1.12e-01
   7 1.193e+00
   8 1.194e+00
9 1.196e+00
                    2.02 1.12e-01
                    2.01 1.12e-01
  10 1.193e+00
                    2.02 1.12e-01
Average performance: 2.02 1.12e-01 +- 6.35e-05 GP/s
  - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
       Time, s
                  Speedup
                               GP/s *
                 16.45 9.17e-01 **
   1 1.464e-01
   2 1.468e-01
                  16.41
                           9.14e-01 **
   3 1.465e-01 16.44
                           9.16e-01
   4 1.468e-01
                  16.41 9.15e-01
   5 1.467e-01 16.42 9.15e-01
   6 1.459e-01
                  16.51 9.20e-01
   7 1.464e-01 16.45 9.17e-01
```

IMPLEMENTATION 6: global container for reduction in threads-last layout

```
Trial
    8 1.464e-01 16.46 9.17e-01
9 1.471e-01 16.38 9.12e-01
   10 1.462e-01 16.47 9.18e-01
Average performance: 16.44 9.16e-01 +- 2.11e-03 GP/s
```

<sup>-</sup> Performance unit 1 GP/s is 10^9 particles binned per second.

<sup>\*\* -</sup> warm-up, not included in average

```
telzur@xphisrv2:~/Teaching/PP/XeonPhi/Colfax_Tutorial_Binning
 File Edit View Search Terminal Help
IMPLEMENTATION 6: global container for reduction in threads-last layout
Trial Time, s
                               Speedup
                                                      GP/s *
      1 1.464e-01 16.45 9.17e-01 **
2 1.468e-01 16.41 9.14e-01 **
    2 1.468e-01 16.41 9.14e-01

3 1.465e-01 16.44 9.16e-01

4 1.468e-01 16.41 9.15e-01

5 1.467e-01 16.42 9.15e-01

6 1.459e-01 16.51 9.20e-01

7 1.464e-01 16.45 9.17e-01

8 1.464e-01 16.46 9.17e-01

9 1.471e-01 16.38 9.12e-01

10 1.462e-01 16.47 9.18e-01
Average performance: 16.44 9.16e-01 +- 2.11e-03 GP/s
   - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
IMPLEMENTATION 7: global container for reduction in threads-last layout with pad
ding
Trial Time, s
                               Speedup
                                                  GP/s *
   1 6.128e-02 39.31 2.19e+00 **
2 6.123e-02 39.34 2.19e+00 **
3 6.122e-02 39.35 2.19e+00
4 6.122e-02 39.35 2.19e+00
5 6.122e-02 39.35 2.19e+00
6 6.127e-02 39.32 2.19e+00
7 6.123e-02 39.34 2.19e+00
8 6.126e-02 39.32 2.19e+00
9 6.125e-02 39.33 2.19e+00
10 6.126e-02 39.32 2.19e+00
      1 6.128e-02 39.31 2.19e+00 **
Average performance: 39.33 2.19e+00 +- 7.39e-04 GP/s
   - Performance unit 1 GP/s is 10^9 particles binned per second.
 ** - warm-up, not included in average
```

[telzur@xphisrv2 Colfax Tutorial Binning]\$

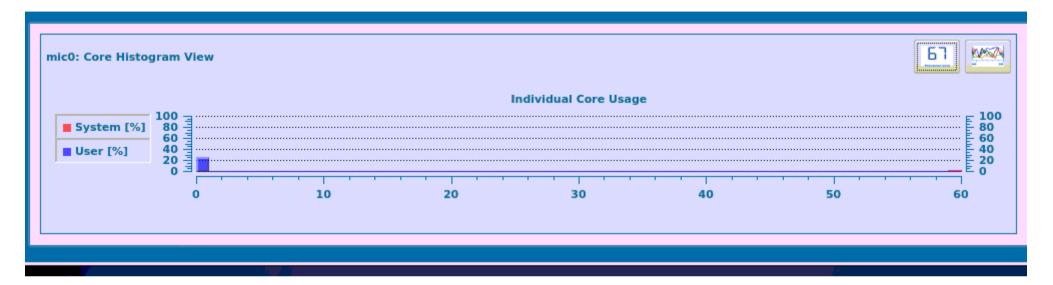
#### Same tests on the mic

cp the application to mic0:/home/telzur/colfax

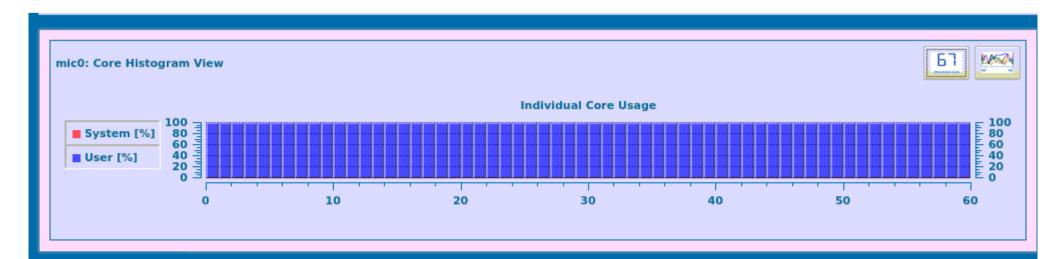
Cp the libraries:

[telzur@xphisrv2 Colfax\_Tutorial\_Binning]\$ scp /opt/intel/composer\_xe\_2015.3.187/mkl/lib/mic/\* mic0:/home/telzur/lib/.

# **Implementation 0: serial**



# Implementations 1..7: parallel



```
telzur@xphisrv2:~/Teaching/PP/XeonPhi/mini-nbody-master
 File Edit View Search Terminal Help
telzur@xphisrv2-mic0:~/colfax$ ./app-MIC
Particle Binning Optimization Demo (single precision)
Additional information is available in accompanying papers at http://colfaxresearch.com/
 (c) Colfax International, 2015.
Initialization... done in 1.748 seconds.
Computing reference result... done in 28.269 seconds.
Benchmarking...
IMPLEMENTATION 0: serial
Trial Time, s Speedup
                                                                       GP/s *

        ial
        Time, s
        Speedup
        GP/s *

        1 2.892e+01
        n/a 4.64e-03 **

        2 2.892e+01
        n/a 4.64e-03 **

        3 2.892e+01
        n/a 4.64e-03

        4 2.892e+01
        n/a 4.64e-03

        5 2.892e+01
        n/a 4.64e-03

        6 2.892e+01
        n/a 4.64e-03

        7 2.892e+01
        n/a 4.64e-03

        8 2.892e+01
        n/a 4.64e-03

        9 2.892e+01
        n/a 4.64e-03

        10 2.892e+01
        n/a 4.64e-03

Average performance: 1.00 4.64e-03 +- 6.12e-08 GP/s
   - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
IMPLEMENTATION 1: parallel, atomics for reduction
Trial Time, s Speedup GP/s *

        ial
        Time, s
        Speedup
        GP/s *

        1
        3.561e+00
        8.12
        3.77e-02 **

        2
        3.558e+00
        8.13
        3.77e-02 **

        3
        3.561e+00
        8.12
        3.77e-02

        4
        3.558e+00
        8.13
        3.77e-02

        5
        3.558e+00
        8.13
        3.77e-02

        7
        3.558e+00
        8.13
        3.77e-02

        8
        3.561e+00
        8.12
        3.77e-02

        9
        3.560e+00
        8.12
        3.77e-02

        10
        3.560e+00
        8.13
        3.77e-02

Average performance: 8.13 3.77e-02 +- 1.25e-05 GP/s
    - Performance unit 1 GP/s is 10^9 particles binned per second.
```

```
IMPLEMENTATION 2: parallel, thread-private containers for reduction
```

```
Trial Time, s Speedup GP/s *

1 4.457e-01 64.90 3.01e-01 **

2 4.438e-01 65.18 3.02e-01 **

3 4.444e-01 65.09 3.02e-01

4 4.463e-01 64.80 3.01e-01

5 4.454e-01 64.94 3.01e-01

6 4.499e-01 64.28 2.98e-01

7 4.449e-01 65.01 3.02e-01

8 4.450e-01 65.00 3.02e-01

9 4.442e-01 65.11 3.02e-01

10 4.453e-01 64.95 3.01e-01
```

Average performance: 64.90 3.01e-01 +- 1.15e-03 GP/s

- Performance unit 1 GP/s is 10^9 particles binned per second.
- \*\* warm-up, not included in average

#### IMPLEMENTATION 3: vectorized

```
Trial Time, s
                Speedup
                          GP/s *
   1 4.975e-02 581.43 2.70e+00 **
   2 5.737e-02 504.20 2.34e+00 **
   3 3.303e-02 875.68 4.06e+00
   4 3.262e-02
                 886.55 4.11e+00
   5 3.243e-02
                 891.94 4.14e+00
   6 3.306e-02
                 874.81 4.06e+00
   7 3.243e-02
                891.91 4.14e+00
   8 3.267e-02 885.43 4.11e+00
   9 3.249e-02 890.34 4.13e+00
  10 3.302e-02
                 875.94 4.06e+00
Average performance: 884.08 4.10e+00 +- 3.25e-02 GP/s
```

- Performance unit 1 GP/s is 10^9 particles binned per second.
- \*\* warm-up, not included in average

```
File Edit View Search Terminal Help
IMPLEMENTATION 4: vectorized, aligned
Trial Time, s
                    Speedup GP/s *
    1 3.467e-02 834.19 3.87e+00 **
   2 2.911e-02 993.54 4.61e+00 **
3 2.899e-02 997.71 4.63e+00
    4 2.911e-02 993.70
                             4.61e+00
   5 2.902e-02 996.79 4.63e+00
    6 2.911e-02 993.53 4.61e+00
    7 2.920e-02 990.37 4.60e+00
    8 2.917e-02 991.46 4.60e+00
    9 2.888e-02 1001.48 4.65e+00
   10 2.856e-02 1012.77 4.70e+00
Average performance: 997.23 4.63e+00 +- 3.14e-02 GP/s
 - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
IMPLEMENTATION 5: global container for reduction in threads-first layout
Trial Time, s Speedup
                                   GP/s *
   1 5.467e-01 52.91 2.46e-01 **
2 5.282e-01 54.76 2.54e-01 **
   3 5.283e-01 54.74 2.54e-01
4 5.281e-01 54.77 2.54e-01
    5 5.292e-01 54.66 2.54e-01
6 5.276e-01 54.82 2.54e-01
   7 5.280e-01 54.78 2.54e-01 8 5.279e-01 54.79 2.54e-01
   9 5.280e-01 54.78 2.54e-01
10 5.294e-01 54.63 2.54e-01
Average performance: 54.75 2.54e-01 +- 2.86e-04 GP/s
  - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
```

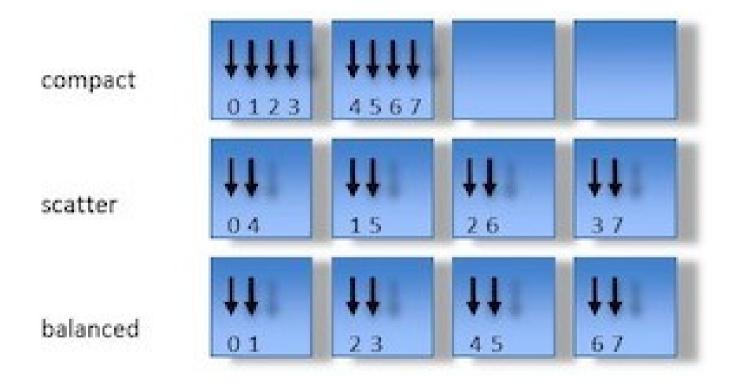
```
File Edit View Search Terminal Help
IMPLEMENTATION 6: global container for reduction in threads-last layout
Trial Time, s
                  Speedup
                               GP/s *
   1 5.146e-02 562.07 2.61e+00 **
   2 3.995e-02 724.01 3.36e+00 **
3 4.076e-02 709.54 3.29e+00
   4 4.049e-02 714.34 3.31e+00
   5 4.017e-02 720.00 3.34e+00
   6 4.080e-02 708.95 3.29e+00
   7 4.028e-02 718.03 3.33e+00
   8 4.070e-02 710.66 3.30e+00
9 4.059e-02 712.51 3.31e+00
  10 4.053e-02 713.60 3.31e+00
Average performance: 713.45 3.31e+00 +- 1.71e-02 GP/s
 - Performance unit 1 GP/s is 10^9 particles binned per second.
** - warm-up, not included in average
IMPLEMENTATION 7: global container for reduction in threads-last layout with padding
Trial Time, s
                  Speedup
                               GP/s *
   1 2.884e-02 1002.80 4.65e+00 **
   2 2.913e-02 992.89 4.61e+00 **
   3 2.912e-02 993.19 4.61e+00
   4 2.915e-02 992.17 4.60e+00
   5 2.915e-02
                   992.20
                          4.60e+00
   6 2.915e-02 992.20
                          4.60e+00
   7 2.910e-02 993.94 4.61e+00
   8 4.611e-02
                   627.22 2.91e+00
   9 3.049e-02 948.62 4.40e+00
  10 2.916e-02 992.03 4.60e+00
Average performance: 941.45 4.37e+00 +- 5.55e-01 GP/s
```

- Performance unit 1 GP/s is 10^9 particles binned per second.

\*\* - warm-up, not included in average

telzur@xphisrv2-mic0:~/colfax\$

#### KMP\_AFFINITY



#### That's it