

1.

a. Define half adder.

The half adder is a type of combinational logic circuit that adds two of the 1-bit binary digits. It generates carry and sum of both the inputs. The full adder is also a type of combinational logic that adds three of the 1-bit binary digits for performing an addition operation.

b. Draw a truth table for the sum and carry of half adder.

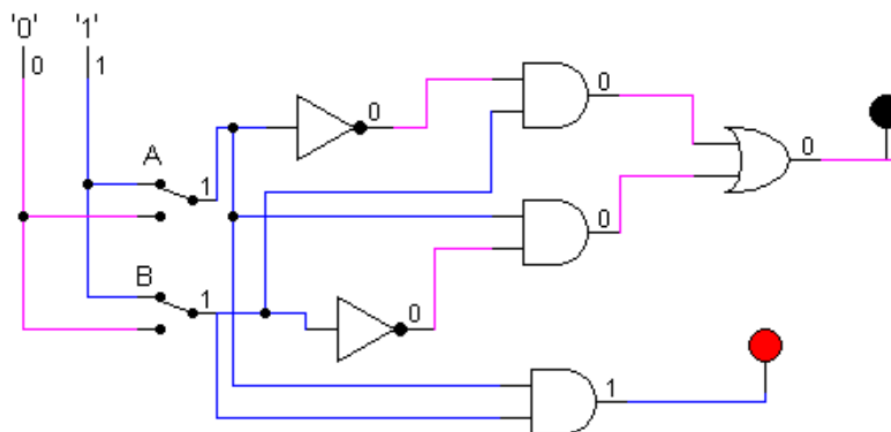
Truth table

-Input A	-input B	-S(Sum)	Carry
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

c. Write the sop expression from the truth table.

-SOP expression sum= $A'B + AB'$ -SOP expression carry= $A.B$

d. Draw the circuit using logsim.



Half adder
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2.

a. Draw the truth table for the outputs of the full adder

A	B	C	Sum	Carry Out
0	0	0	0	0
0	0	1	1	0
0	1	0	0	0
0	1	1	1	1
1	0	0	0	0
1	0	1	1	1
1	1	0	0	1
1	1	1	1	1

Write the corresponding sop expression for sum and carry of full adder and simplify the expression

$$\begin{aligned} \text{SOP expression sum} &= A'B'C + A'BC' + AB'C' + ABC \\ &= A'B'C + A'BC' + AB'C' + ABC \end{aligned}$$

$$= A'(B'C + BC') + A(B'C' + BC)$$

$$= A'(B + C) + A(B + C)$$

$$= A'X + AX$$

$$= A + X$$

$$\text{Sum} = A + B + C$$

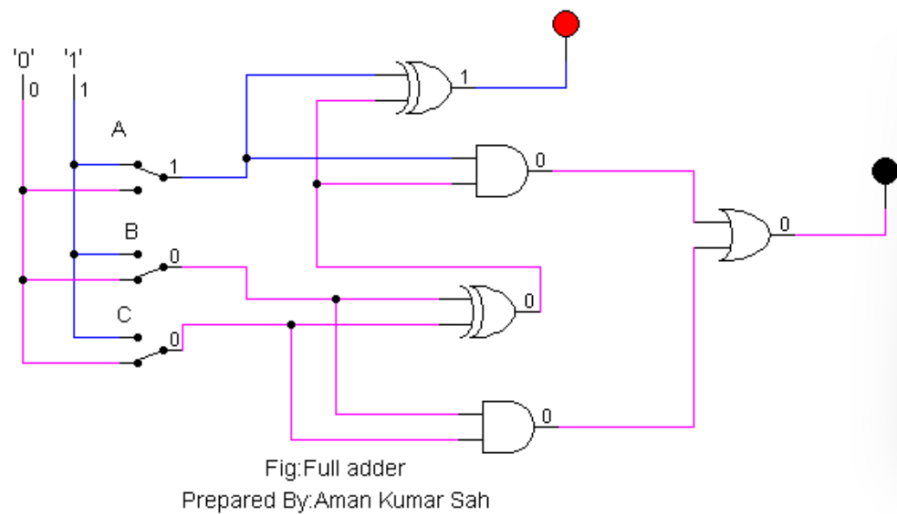
$$\text{SOP expression carry} = A'B'C + AB'C + A'BC' + ABC$$

$$= A'BC + AB'C + ABC' + ABC + ABC$$

$$= BC(A' + B) + AC(B' + B) + AB(C' + C)$$

$$\text{Carry} = BC + AC + AB$$

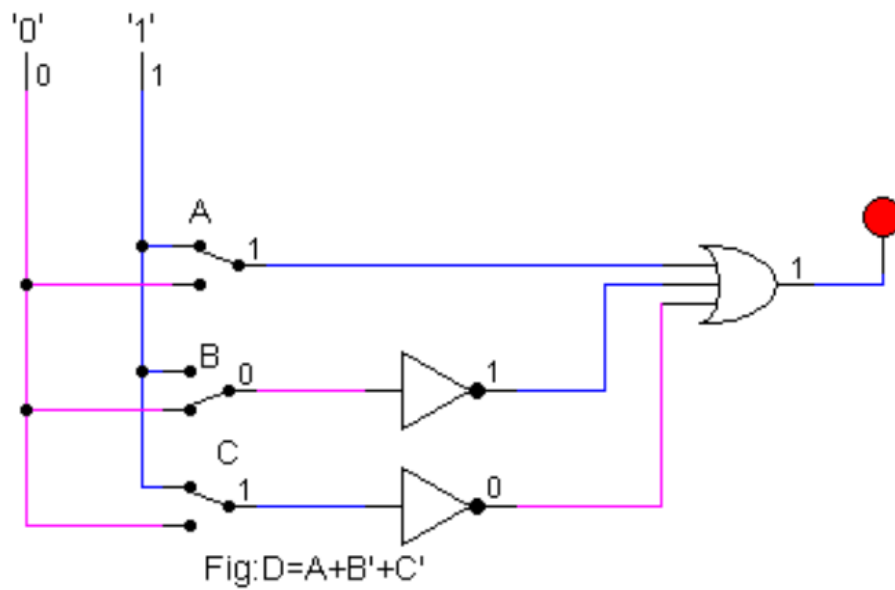
Draw full adder using two half adder and an OR gate



3. Using the three stages of design, construct the circuits for the following input /output values. Here A, B and C are the inputs whereas D, E, F, G, H and I are outputs. *Note: Draw circuit diagram using logsim corresponding to the simplified expression of outputs D, E, F, G, H and I.*

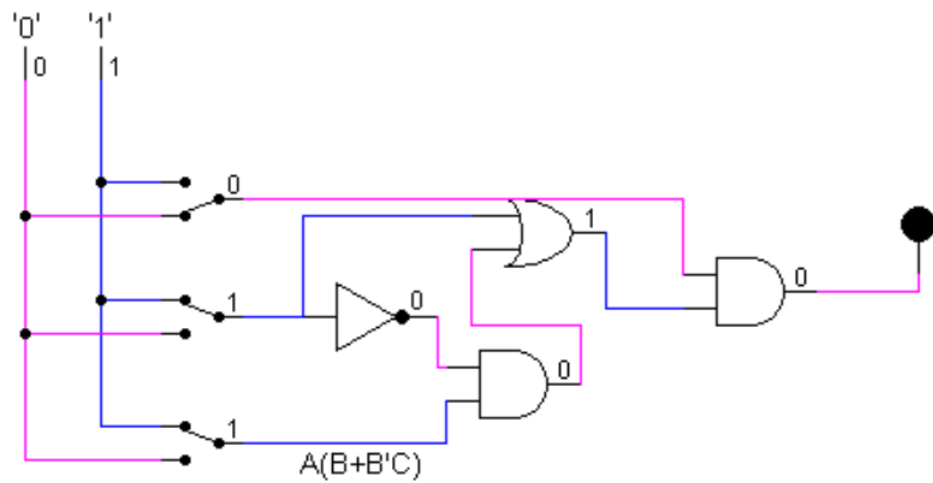
A	B	C	D	E	F	G	H	I
0	0	0	1	0	1	0	1	1
0	0	1	1	0	1	1	0	1
0	1	0	1	0	1	1	1	1
1	0	0	1	0	0	1	0	1
1	1	1	1	1	1	1	1	1
1	1	0	1	1	0	1	0	1
1	0	1	1	1	1	1	1	0
0	1	1	0	0	0	1	1	1

1) POS Of $D = A + B' + C'$



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$$\begin{aligned}
 2) \quad E &= ABC + ABC' + AB'C \\
 &= AB(C + C') + AB'C \\
 &= AB + AB'C \\
 &= A(B + B'C)
 \end{aligned}$$



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For F result:

$$3) F = A'BC' + AB'C = A'BC' + AB'C$$

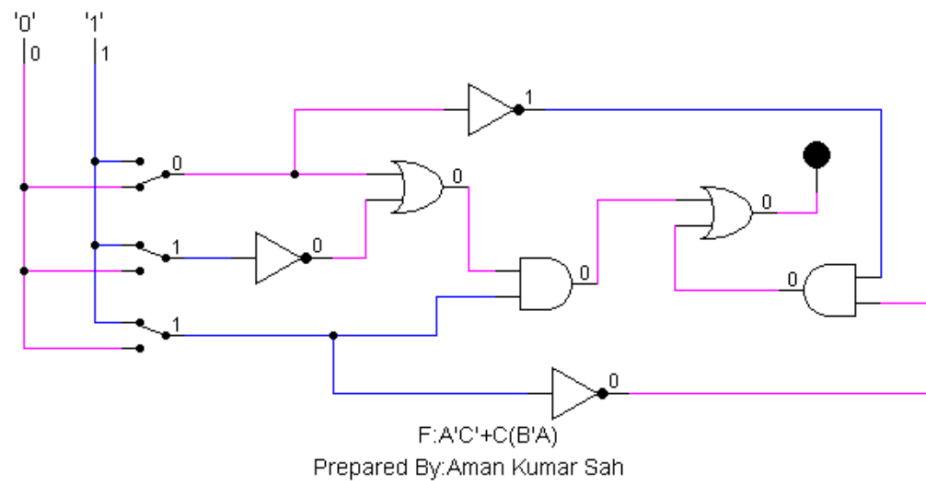
$$=A'C'(B'+B)+B'C(A'+A)+ABC$$

$$=A'C'+B'C+ABC$$

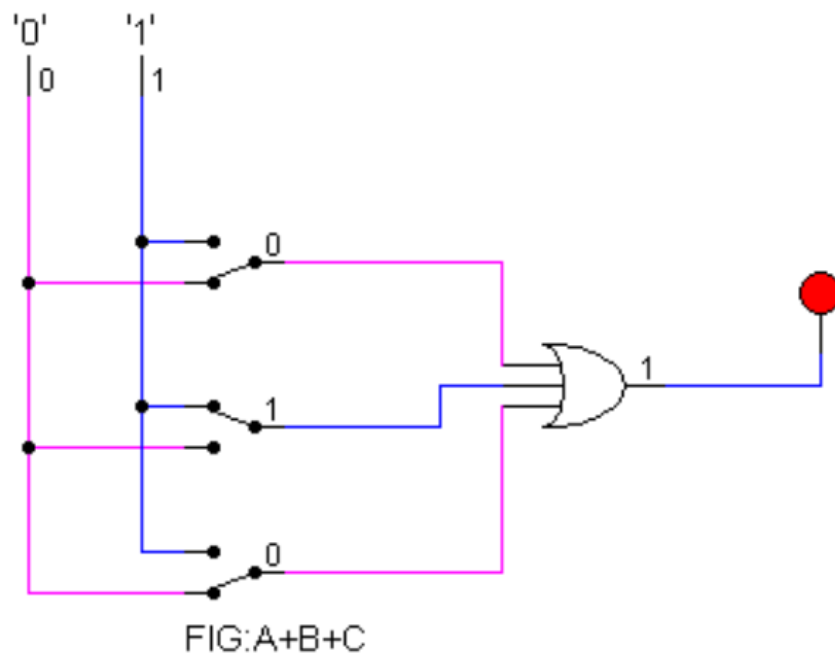
$$=A'C'+C'(B+AB)$$

$$=A'C'+C(B'+A)(B'+B)$$

$$=A'C'+(B'+A)$$

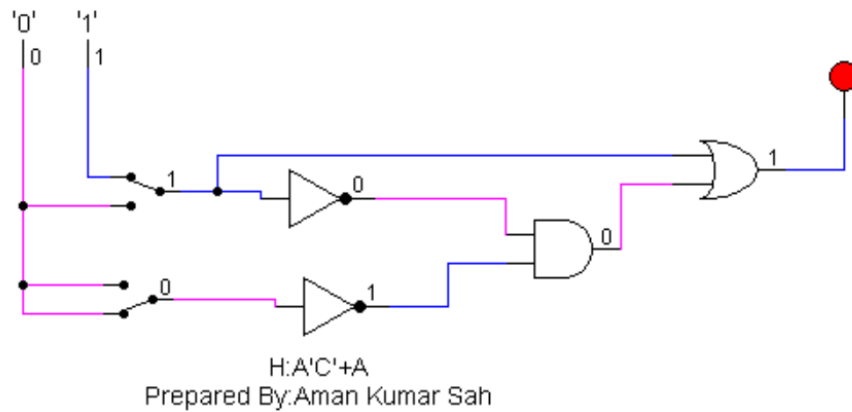


4) POS of $G = A + B + C$



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$$\begin{aligned}
 5) H &= A'B'C' + A'BC' + ABC + AB'C + AB'C' \\
 &= A'C'(B+B') + AC(B+B') + A(B'C+BC) \\
 &= A'C' + A
 \end{aligned}$$



$$6) \text{POS of } I = A' + B + C'$$

