

Manual

Meshless Multi–Physics Software MeMPhyS

Version 1.4

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Chapter 1. Installation

Install the following software (links to websites provided in blue colors):

1. Latest version of Ubuntu LTS:
 - Tested on [Ubuntu 20.04.1 LTS](#)
 - May work on other Linux distributions and versions
2. Install and test MPI: [example](#)
3. [HYPRE Solver](#):
 - Tested on [Version 2.11.1](#)
 - Steps provided in ‘INSTALL’ file in HYPRE directory to ‘make install’ its code files
 - Edit the variable ‘HYPRE_DIR’ in ‘Makefile’ to specify location of the HYPRE directory
4. [Eigen Library](#):
 - Tested on [Version 3.3.7](#)
 - No need to install; extract the source files to a directory
 - Edit the variable ‘Eigen_directory’ in ‘Makefile’ and point to above directory
5. [Spectra Library](#):
 - Tested on [Version 0.8.1](#)
 - No need to install; extract the source files to a directory
 - Edit the variable ‘spectra_directory’ in ‘Makefile’ and point to above directory
6. Mesh files generated using [GMSH](#).
 - Install latest version of GMSH with these [instructions](#):
 - MSH file should be exported with version 2 (not default setting of 4)
7. Visualization of contours using [Tecplot](#). Download from [UIUC webstore](#).
8. Install [Visual Studio Code](#) for code development/editing

All the above software other than Tecplot are free or open source.

Chapter 2. Setup

Steps for setting new problems:

1. Make a copy of any '.cpp' files in the examples folder with a new name say, 'filename.cpp'
2. Generate msh file from GMSH and link it in 'filename.cpp'
3. MSH file should be exported with version 2 (not default setting of 4)
4. Set appropriate boundary conditions inside the code 'filename.cpp'
5. Add two lines for compiling 'filename.cpp' in the 'Makefile'
6. Update 'parameters_file.csv' if needed
7. Compile with command: **time make filename**
8. Execute with command: **time ./out**
9. Use command **make clean** occasionally to clear all object files

Chapter 3. Software Capabilities

3.1 Multi-Physics Components

MeMPhyS solves partial differential equations arising from various engineering and physics problems. It uses the Polyharmonic spline radial basis function with appended polynomials to estimate the differential operators over point clouds. Current capabilities include:

- Interpolation over scattered points
- Gradient and Laplacian stencils for 2D and 3D geometries
- Heat conduction (Poisson’s equation) with Dirichlet and Neumann boundary conditions
- Scalar transport equation
- Incompressible fluid flow problems in 2D (Navier–Stokes equations)
- Forced convection problems
- Solidification of metal alloys for 2D and 3D geometries

3.2 Parameters Setting

The accuracy and efficiency of MeMPhyS can be tuned by setting appropriate values in the ‘parameters_file.csv’:

- **poly_deg**: degree of appended polynomial: integer in range [2, 15]
A degree of k is expected to give $\mathcal{O}(k+1)$, $\mathcal{O}(k)$ and $\mathcal{O}(k-1)$ convergence in the numerical interpolation, gradient and Laplacian operators respectively. However, condition number of the radial basis function matrix increases with higher degree. This also increases the bandwidth of the assembled solution matrix thus, making a higher order solution more expensive.
- **phs_deg**: exponent of polyharmonic spline: integer with options: 3, 5, 7, 9, 11
A value of ‘3’ is recommended. This has minimal impact on the condition number and stability of the system.
- **cloud_size_multiplier**: fraction in the range [1.5, 2.5]
It is recommended to set this around ‘2.0’. Higher value increases the bandwidth and slows down convergence.
Usage: `cloud_size = cloud_size_multiplier*(No. of appended polynomials)`
- **nt**: No. of timesteps: positive integer

- **Courant:** courant number (CFL criterion)
Set in range $[0,1]$ for explicit time marching schemes. Implicit Euler is unconditionally stable
Usage: $[dt=2*\text{Courant}/\lambda]$ where, λ : sum of largest magnitude convection and diffusion eigenvalues
- **solver_type:** options: `hypr_ilu_gmres`, `eigen_direct`, `eigen_ilu_bicgstab`
`hypr_ilu_gmres`: ILU preconditioned GMRES from the library HYPRE
`eigen_direct` direct solver from the library Eigen
`eigen_ilu_bicgstab`: ILU preconditioned BiCGSTAB from the library Eigen
`eigen_direct` is not recommended for large size problems
- **steady_tolerance:** solved to steady state till absolute difference between consecutive timesteps for all variables is less than this tolerance. Useful only for problems having steady state solution.
- **solver_tolerance:** used in iterative solvers for absolute and relative residuals (recommended: less than `steady_tolerance`)
- **gmres_kdim:** dimension of Krylov subspace in GMRES solver (refer the [HYPRE manual](#) for details)
- **precond_droptol:** Drop tolerance for ILU preconditioner (refer the [HYPRE manual](#) or [Eigen manual](#) for details)
- **n_iter:** no. of iterations of the GMRES or BiCGSTAB solvers

3.3 List of Current Examples

The ‘examples’ folder has following problems setup under various sub-folders:

1. Problems involving single scalar transport under sub-folder ‘advection_diffusion’:
 - (a) ‘heat_conduction_manuf_soln.cpp’: heat conduction using implicit (Euler) time-marching with manufactured solution in 2D and 3D
 - (b) ‘heat_conduction.cpp’: heat conduction using implicit (Euler) time-marching on general geometries in 2D and 3D
 - (c) ‘euler_steady_heat_cond_manuf_sol.cpp.cpp’: heat conduction using explicit (Euler) time-marching with steady manufactured solution in 2D and 3D
 - (d) ‘euler_unsteady_heat_cond_manuf_sol.cpp.cpp’: heat conduction using explicit (Euler) time-marching with unsteady manufactured solution in 2D and 3D
 - (e) ‘ab2_unsteady_heat_cond_manuf_sol.cpp.cpp’: heat conduction using explicit (second order Adam-Bashforth) time-marching with unsteady manufactured solution in 2D and 3D

- (f) 'scalar_transport_implicit.cpp': scalar transport using implicit (Euler) time-marching on general geometries in 2D and 3D
- 2. Two-dimensional fluid flow problems under sub-folder 'navier_stokes_2D':
 - (a) 'channel_flow.cpp': developing flow in a channel
 - (b) 'couette_flow.cpp': Couette flow to analyze spatial errors in solution
 - (c) 'eccentric_couette_flow.cpp': Couette flow with eccentric inner cylinder
 - (d) 'elliptic_couette_flow.cpp': Couette flow with outer cylinder as ellipse
 - (e) 'kovasznay_flow.cpp': Kovasznay flow to analyze spatial errors in solution
 - (f) 'flow_over_cylinder.cpp': steady and unsteady flow over a circular cylinder
 - (g) 'taylor_green_steady.cpp': steady version of Taylor-Green flow to analyze spatial errors in solution
 - (h) 'taylor_green_modified.cpp': modified Taylor-Green flow to analyze temporal errors in solution (second order Adam-Bashforth)
- 3. Miscellaneous problems under sub-folder 'miscellaneous':
 - (a) 'check_coeff.cpp': analyze error in gradient and Laplacian coefficients for 2D and 3D problems
 - (b) 'interpolate_check.cpp': analyze error of interpolation stencil for 2D and 3D problems
- 4. Solidification problem under sub-folder 'solidification':
 - (a) 'solidification_problem_1.cpp': 2D and 3D solidification of Aluminum alloy

Chapter 4. Details of Current Version

4.1 Modifications

- All main files of various problems categorized inside the ‘examples’ directory
- Setup of solidification problem
- For Navier–stokes problems: option for 2 types of outlet BCs:
 - Fixed uniform pressure
 - $\frac{\partial u}{\partial \hat{n}} = 0$ and $\frac{\partial v}{\partial \hat{n}} = 0$

4.2 Bugs fixed

- Corrected the nearest neighbor function to get sufficient neighbors for boundary points

Chapter 5. Details of Previous Versions

5.1 Version 1.3: 4 December 2020

5.1.1 Modifications

- Fractional step algorithm with Adam–Bashforth giving second order temporal accuracy
- Outlet boundary implemented with Dirichlet condition for pressure
- Efficient cloud computation by coupling with open source library [Nanoflann](#)

5.1.2 Bugs fixed

- No bugs reported/fixed

5.2 Version 1.2: 29 November 2020

5.2.1 Modifications

- Function for sparse matrix to compute spectrally accurate interpolation
- Modularized fractional step function into class
- Added optional body force terms in the fractional step algorithm
- Main files for steady and unsteady Taylor–Green vortices
- Explicit Euler and 2nd Order Adam-Bashforth giving 1st and 2nd order temporal accuracies respectively for 2D unsteady heat conduction problems

5.2.2 Bugs fixed

- No bugs reported/fixed

5.3 Version 1.1: 15 November 2020

5.3.1 Modifications

- Added an option to choose ILU preconditioned BiCGSTAB solver implemented in the Eigen library
- For 2D problems till 10000 points, performance similar to ILU+GMRES from HYPRE
- For refined grids in 3D Eigen’s solver is computationally efficient

5.3.2 Bugs fixed

- No bugs reported/fixed

5.4 Version 1.0: 8 November 2020

- Works on 2D (triangular elements) and 3D (tetrahedral elements) from GMSH grids
- Exponential convergence based on the degree of appended polynomial
- Direct solver from Eigen used to calculate gradient and Laplacian coefficients
- Preconditioned GMRES from HYPRE or direct solver from Eigen are available for solution of the assembled linearized system
- Tested with manufactured solutions of heat conduction and scalar transport
- Fractional step algorithm with explicit convection and diffusion terms used to solve the Navier–Stokes equations
- As of now, following 2D fluid flow problems are setup:
 1. Kovasznay flow
 2. Couette flow (concentric rotating circle inside circle)
 3. Eccentric Couette flow (eccentric rotating circle inside circle)
 4. Elliptical Couette flow (concentric rotating circle inside ellipse)
 5. Steady and unsteady flow over circular cylinder
- Steps for setting new problems:
 1. Make a copy of the file ‘flow_over_cylinder.cpp’ with a new name say, ‘filename.cpp’
 2. Generate msh file from GMSH and link it in ‘filename.cpp’
 3. MSH file should be exported with version 2 (not default setting of 4)
 4. Set appropriate boundary conditions inside the code ‘filename.cpp’
 5. Add two lines for compiling ‘filename.cpp’ in the ‘Makefile’ (similar to the lines for ‘flow_over_cylinder.cpp’)
 6. Update ‘parameters_file.csv’ if needed
 7. Compile with command: **time make filename**
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 9. Use command **make clean** occasionally to clear all object files