

Learning by extrapolation from marginal to full-multivariate probability distributions: Decreasingly naive Bayesian classification

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Abstract

Averaged n -Dependence Estimators ($AnDE$) is an approach to probabilistic classification learning that learns by extrapolation from marginal to full-multivariate probability distributions. It utilizes a single parameter that transforms the approach between a low-variance high-bias learner (Naive Bayes) and a high-variance low-bias learner with Bayes optimal asymptotic error. It extends the underlying strategy of Averaged One-Dependence Estimators (AODE), which relaxes the Naive Bayes independence assumption while retaining many of Naive Bayes' desirable computational and theoretical properties. $AnDE$ further relaxes the independence assumption by generalizing AODE to higher-levels of dependence. Extensive experimental evaluation shows that the bias-variance trade-off for Averaged 2-Dependence Estimators results in strong predictive accuracy over a wide range of data sets. It has training time linear with respect to the number of examples, supports incremental learning, handles directly missing values, and is robust in the face of noise. Beyond the practical utility of its lower-dimensional variants, $AnDE$ is of interest in that it demonstrates that it is possible to create low-bias high-variance generative learners and suggests strategies for developing even more powerful classifiers.

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1 Introduction

This paper presents a family of learning algorithms that utilize a predefined function to extrapolate from observed marginal distributions to the full multivariate distribution of interest. This stands in contrast to the majority of learning algorithms that instead seek to fit a model directly to the observed multivariate probability distribution. Whereas learning is sometimes cast as a problem of searching through a space of hypotheses to find one that best fits the training data [1], this new approach does not employ search and does not perform model selection.

The members of this new family of algorithms have a unique combination of features that is well suited to many applications. We discuss these features in more detail below. Notable amongst them are training complexity linear with respect to the number of training examples; direct capacity for incremental learning; and accuracy that is competitive with the state-of-the-art. They are of further theoretical interest because they demonstrate that it is possible to create low bias generative learners.

The family contains a range of algorithms that range from low variance coupled with high bias through to high variance coupled with low bias. Successive members of the family will be best suited to differing quantities of data, starting with low variance for small data, with successively lower bias but higher variance suiting ever increasing data quantities [2]. The asymptotic error of the lowest bias variant is Bayes optimal.

One member of this family of algorithms, naive Bayes (NB), is already well known. A second member, Averaged One-Dependence Estimators (AODE) [3], has enjoyed considerable popularity since its introduction in 2005 [4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26]. The work presented in this paper arises from the realization that NB and AODE are but two instances of a family of algorithms, which we call *AnDE*.

In Section 2 we explain the underlying learning strategy, and define the *AnDE* family of algorithms. The *AnDE* family of algorithms build upon the method pioneered by AODE [3]. In Section 3 we discuss how the *AnDE* algorithms relate to Feating [27], a generic approach to ensembling that also builds upon techniques pioneered by AODE. In Section 4 we present an extensive evaluation of the *AnDE* family of algorithms, comparing their performance to relevant Bayesian techniques, to Feating and to the state-of-the-art Random Forests classifier. Section 5 presents conclusions and directions for future research.

2 The *AnDE* family of algorithms

We wish to estimate from a training sample \mathcal{T} of t classified objects the probability $P(y|\mathbf{x})$ that an example $\mathbf{x} = \langle x_1, \dots, x_a \rangle$ belongs to class y , where x_i is the value of the i^{th} attribute and $y \in \{c_1, \dots, c_k\}$. We use \bar{v} to denote the average number of values per attribute. These and other elements of notation are listed in Table 1.

Table 1: Notation

$P(e)$	the unconditioned probability of event e
$P(e w)$	the conditional probability of event e given event w
$\hat{P}(e)$	an estimate of $P(e)$
$\hat{P}_{NB}(e)$	a naive Bayes estimate of $P(e)$
$\hat{P}_{AODE}(e)$	an AODE estimate of $P(e)$
$\hat{P}_{AnDE}(e)$	an AnDE estimate of $P(e)$
a	the number of attributes
c_i	the i^{th} class
k	the number of classes
t	the number of training examples in \mathcal{T}
\bar{v}	the average number of values per attribute
y	a value from the set of all classes $\{c_1, \dots, c_k\}$
\mathcal{T}	a training sample of t classified objects
$\mathbf{x} = \langle x_1, \dots, x_a \rangle$	an object
x_i	the value of the i^{th} attribute of $\mathbf{x} = \langle x_1, \dots, x_a \rangle$
$x_{\{i,j,\dots,q\}}$	the subset of attributes values from \mathbf{x} with the specified indices. For example, $x_{\{2,3,5\}} = \langle x_2, x_3, x_5 \rangle$
$\binom{\mathcal{A}}{n}$	the set of all size- n subsets of $\{1, \dots, a\}$
$\delta(x_\alpha)$	a function that is 1 if \mathcal{T} contains an object with the value x_α , otherwise 0

From the definition of conditional probability we have

$$P(y | \mathbf{x}) = P(y, \mathbf{x}) / P(\mathbf{x}) \quad (1)$$

As $P(\mathbf{x}) = \sum_{i=1}^k P(c_i, \mathbf{x})$, we can always estimate Eq 1 from estimates of $P(y, \mathbf{x})$ for each class using

$$P(y, \mathbf{x}) / P(\mathbf{x}) = P(y, \mathbf{x}) / \sum_{i=1}^k P(c_i, \mathbf{x}). \quad (2)$$

In consequence, in the remainder of this paper we consider only the problem of estimating $P(y, \mathbf{x})$, thereby setting the work in a generative framework.

We define the *dimensionality* of a probability or probability estimate as the number of attributes in the distribution to which the probability or estimate relates. Hence, the dimensionality of $P(y, \mathbf{x})$ is $a + 1$.

If the training data do not include sufficient examples of \mathbf{x} to directly derive accurate estimates of each $P(c_i, \mathbf{x})$, we must extrapolate these estimates from observations of lower-dimensional probabilities in the data. All other things being equal, an estimate of a lower-dimensional probability from a given finite training set will be more accurate than an estimate of a higher-dimensional probability, and estimates of higher-dimensional probabilities will vary more

from training sample to training sample. Hence, models derived from lower-dimensional probability estimates are likely to have lower variance than models derived from higher-dimensional probability estimates. On the other hand, models derived from higher-dimensional probabilities are likely to have lower bias, as less restrictive assumptions are made about the form of the probability distribution.

This is illustrated in Figure 1, that shows a simple attribute-space with three ternary attributes and a binary class. To classify a new object with attribute-values *Age=Old*, *Pulse=Slow* and *Temperature=High*, one wishes to infer the class distribution in the cell highlighted in Figure 1(a), which is a four-dimensional probability distribution. If there are insufficient examples to directly estimate that distribution, it might be extrapolated from any of a number of lower dimensional probability distributions. The prior class distribution $P(y)$ is a one-dimensional probability distribution that can be estimated from the entire attribute-space (Figure 1(b)). The two-dimensional probabilities $P(y \wedge \textit{Age}=\textit{Old})$, $P(y \wedge \textit{Pulse}=\textit{Slow})$, $P(y \wedge \textit{Temperature}=\textit{High})$ can be estimated from the regions depicted in (Figure 1(c-e)). The regions associated with the three-dimensional probabilities $P(y \wedge \textit{Age}=\textit{Old} \wedge \textit{Pulse}=\textit{Slow})$, $P(y \wedge \textit{Age}=\textit{Old} \wedge \textit{Temperature}=\textit{High})$ and $P(y \wedge \textit{Pulse}=\textit{Slow} \wedge \textit{Temperature}=\textit{High})$ are illustrated in (Figure 1(f-h)).

From the definition of conditional probability we have

$$P(y, \mathbf{x}) = P(y)P(\mathbf{x} | y). \quad (3)$$

If the number of classes, k , is small, it should be possible to obtain a sufficiently accurate estimate of $P(y)$ from the sample frequencies. However, we still have the problem that \mathbf{x} may not occur sufficiently frequently in the training data and hence accurate estimates of $P(\mathbf{x} | y)$ cannot be obtained directly from the sample frequencies.

The solution used by NB is to extrapolate to $\hat{P}(\mathbf{x} | y)$ from each two-dimensional probability estimate $\hat{P}(x_i | y)$ by assuming the attributes are independent given the class:

$$P(\mathbf{x} | y) = \prod_{i=1}^a P(x_i | y). \quad (4)$$

Hence we classify using

$$\hat{P}_{\text{NB}}(y, \mathbf{x}) = \hat{P}(y) \prod_{i=1}^a \hat{P}(x_i | y). \quad (5)$$

With reference to Figure 1, NB estimates the distribution in (a) by extrapolation from the distributions in (b) (that gives $\hat{P}(y)$), (c) (that gives $\hat{P}(\textit{Age} = \textit{old} | y)$), (d) (that gives $\hat{P}(\textit{Pulse} = \textit{slow} | y)$) and (e) (that gives $\hat{P}(\textit{Temperature} = \textit{high} | y)$).

The independence assumption is a very strong assumption about the underlying probability distribution. As a result, NB has very high bias. However, due to the low dimensionality of the base probabilities from which the model is estimated, it has low variance.

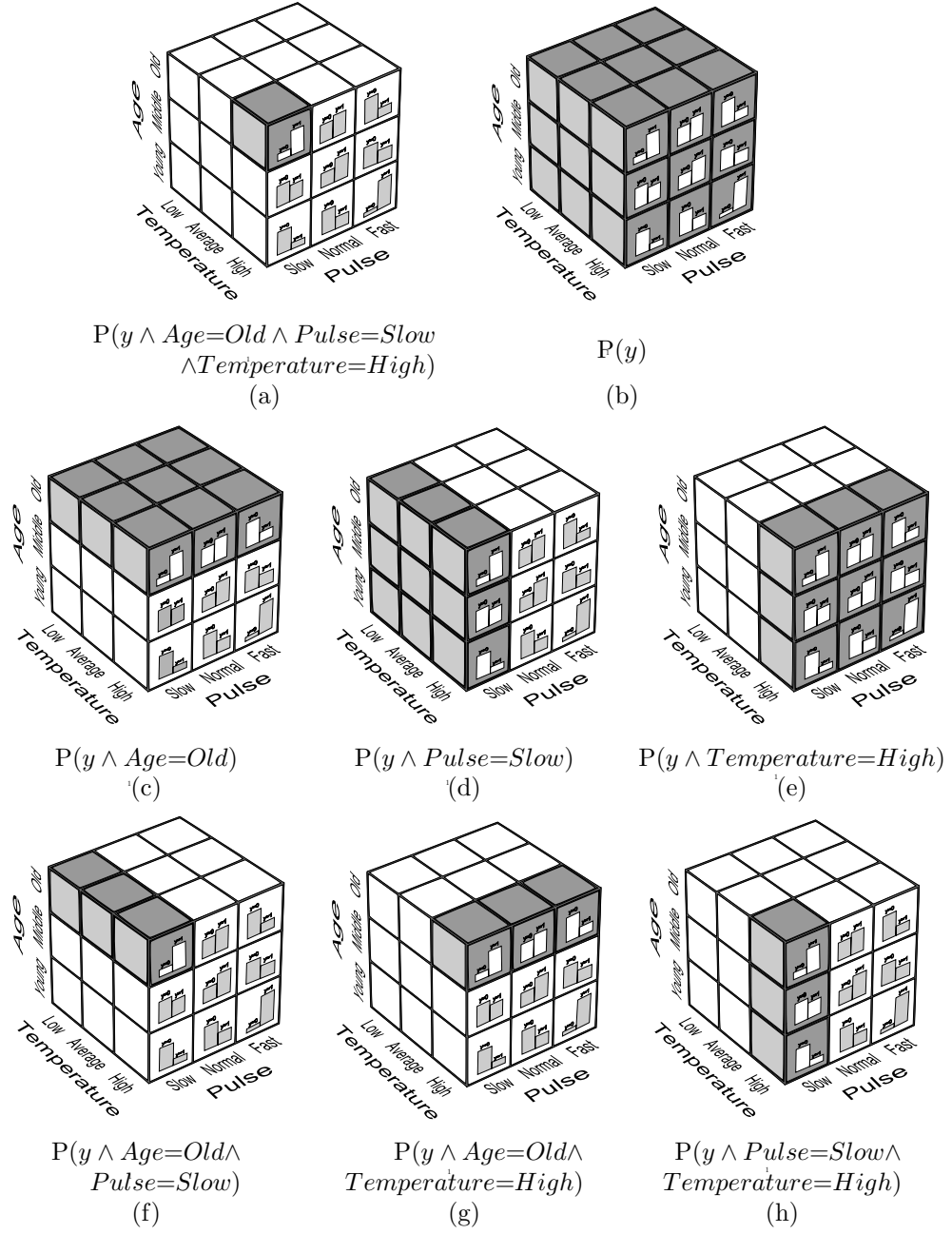


Figure 1: Probabilities of varying dimensionality for an attribute-space with three ternary attributes and a binary class

2.1 AODE

Averaged One-Dependence Estimators (AODE) [3] extends to three-dimensional probabilities NB's search-free strategy of extrapolation from lower-dimensional probabilities. It does so by averaging the estimates of all of a class of three-dimensional estimators.

A Super-Parent One-Dependence Estimator (SPODE) is a three-dimensional probability estimator that relaxes the assumption of conditional independence by making all other attributes independent given the class and one privileged attribute, the super-parent, x_α . This is a weaker conditional independence assumption than NB's, as it is necessarily true if NB's is true and may also be true when NB's is not.

It uses

$$P(y, \mathbf{x}) = P(y, x_\alpha)P(\mathbf{x} | y, x_\alpha) \quad (6)$$

together with a conditional independence assumption

$$P(\mathbf{x} | y, x_\alpha) = \prod_{i=1}^a P(x_i | y, x_\alpha). \quad (7)$$

As this is a weaker assumption than (4), the bias of the model should be lower than that of NB. However, it is derived from higher-dimensional probability estimates and hence its variance should be higher.

AODE exploits the lower bias of SPODEs while addressing their higher variance by averaging over all estimates of $P(y, \mathbf{x})$ produced by using different super-parents. AODE seeks to use

$$\hat{P}(y, \mathbf{x}) = \sum_{\alpha=1}^a \hat{P}(y, x_\alpha) \hat{P}(\mathbf{x} | y, x_\alpha) / a. \quad (8)$$

However, in practice it is desirable to only use estimates of probabilities for which relevant examples occur in the data. Hence, AODE actually uses

$$\hat{P}_{\text{AODE}}(y, \mathbf{x}) = \begin{cases} \frac{\sum_{\alpha=1}^a \delta(x_\alpha) \hat{P}(y, x_\alpha) \hat{P}(\mathbf{x} | y, x_\alpha)}{\sum_{\alpha=1}^a \delta(x_\alpha)} & : \sum_{\alpha=1}^a \delta(x_\alpha) > 0 \\ \hat{P}_{\text{NB}}(y, \mathbf{x}) & : \text{otherwise} \end{cases} \quad (9)$$

where $\delta(x_\alpha)$ is 1 if attribute-value x_α is present in the data, otherwise 0. That is, it averages over all superparents whose value occurs in the data, and defaults to NB if there are no such superparents.

As AODE uses all of a predefined family of estimators, each of which extrapolates the desired high-dimensional probability from lower-dimensional probabilities, it does not perform search.

In terms of the example attribute space, AODE extrapolates to Figure 1(a) from the lower-dimensional probabilities illustrated in Figure 1(c-h) with (f)

conditioned on (c) and (d), (g) conditioned on (c) and (e), and (g) conditioned on (d) and (e).

AODE has demonstrated strong prediction accuracy (both zero-one loss and mean-squared error) with relatively modest computational requirements for low dimensional data [3]. In consequence, it has enjoyed substantial uptake [4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26].

2.2 AnDE

In this paper we generalize to higher-dimensional probabilities the strategy of search-free extrapolation from lower-dimensional probabilities.

For notational convenience we define

$$x_{\{i,j,\dots,q\}} = \langle x_i, x_j, \dots, x_q \rangle. \quad (10)$$

For example, $x_{\{2,3,5\}} = \langle x_2, x_3, x_5 \rangle$.

AnDE aims to use

$$\hat{P}(y, \mathbf{x}) = \sum_{s \in \binom{A}{n}} \hat{P}(y, x_s) \hat{P}(\mathbf{x} | y, x_s) / \binom{a}{n}, \quad (11)$$

where $\binom{A}{n}$ indicates the set of all size- n subsets of $\{1, \dots, a\}$.

However, in practice we also need to avoid using pairs of superparents whose values do not occur in the data, and hence use

$$\hat{P}_{\text{AnDE}}(y, \mathbf{x}) = \begin{cases} \sum_{s \in \binom{A}{n}} \delta(x_s) \hat{P}(y, x_s) \hat{P}(\mathbf{x} | y, x_s) / \sum_{s \in \binom{A}{n}} \delta(x_s) & : \sum_{s \in \binom{A}{n}} \delta(x_s) > 0 \\ \hat{P}_{\text{A}(n-1)\text{DE}}(y, \mathbf{x}) & : \text{otherwise} \end{cases} \quad (12)$$

Attributes are assumed independent given the superparents and the class. Hence, $P(\mathbf{x} | y, x_s)$ is estimated by

$$\hat{P}(\mathbf{x} | y, x_s) = \prod_{i=1}^a \hat{P}(x_i | y, x_s). \quad (13)$$

Note that $P(x_i | y, x_s) = 1$ when $i \in s$. Whereas other probability estimates should be smoothed or regularized, smoothed estimates should not be used in this case, and in practice these values are not included in the calculation.

It should be recalled that A0DE is NB and A1DE is AODE.

In terms of the simple attribute-space depicted in Figure 1, A2DE extrapolates to (a) from (a) conditioned on each of (f), (g) and (h), and A3DE makes inferences directly from the class distribution in (a).

When $n = a$, $\binom{A}{n} = \{\{1, \dots, a\}\}$, so $x_s = \mathbf{x}$. Therefore, the ultimate expression of AnDE, AaDE seeks to classify using

$$\hat{P}_{\text{AaDE}}(y, \mathbf{x}) = \hat{P}(y, \mathbf{x}) \hat{P}(\mathbf{x} | y, \mathbf{x}) / \binom{a}{a} \quad (14)$$

where $\hat{P}(y, \mathbf{x})$ is estimated directly from \mathcal{T} , cascading to ever lower dependence estimators should the combination of attribute-values not be present in \mathcal{T} . As $P(\mathbf{x}|y, \mathbf{x})$ and $\binom{a}{a}$ both equal 1, it classifies using only its direct estimate of $P(y, \mathbf{x})$.

Observation 1 *The asymptotic classification performance of AaDE equals that of the Bayes optimal classifier.*

Proof 1 AaDE classifies using

$$\operatorname{argmax}_y \left(\hat{P}(y, \mathbf{x}) / \sum_{z \in \{c_1, \dots, c_k\}} \hat{P}(z, \mathbf{x}) \right)$$

where each $\hat{P}(\cdot)$ is directly estimated from the observed data and hence approaches $P(\cdot)$ as the quantity of data approaches infinity. Hence, in the limit, AaDE approaches

$$\operatorname{argmax}_y \left(P(y, \mathbf{x}) / \sum_{z \in \{c_1, \dots, c_k\}} P(z, \mathbf{x}) \right)$$

which is the Bayes optimal classifier. ■

However, assuming there is sufficient data to compute the necessary probabilities, and we wish to store the necessary probabilities rather than computing them as required for classification, the space complexity of AaDE is $O(k\bar{v}^a)$. This is because joint frequencies must be stored for every combination of attribute value and class value. Except in cases of low dimensional data, even the computational requirements of A3DE defeat our Weka implementation, and hence in this paper we present primarily results for A2DE with some illustrative examples of A3DE.

AnDE forms an $(n+2)$ -dimensional probability table containing the observed frequency for each combination of $n+1$ attribute values and the class labels. The space complexity of the table is $O(k\binom{a}{n+1}\bar{v}^{n+1})$ and the time complexity of compiling it is $O(t\binom{a}{n+1})$, as we need to update each entry for every combination of the $n+1$ attribute-values for every instance. The time complexity of classifying a single example is $O(ka\binom{a}{n})$ as we need to consider each attribute for every qualified combination of n parent attributes within each class.

We demonstrate that as n increases, averaged n -dependence estimators achieve lower bias at the cost of higher variance. In consequence, the ideal dimensionality of dependence will depend on the degree to which the underlying probability distribution fits the assumptions of the n -dependence estimator, the quantity of data available to estimate the base probabilities, and the computational demands of averaging over higher-dimensional estimators.

2.3 Weighted averaging

AODE and its generalization An DE perform an unweighted average of the component n -dependence estimators. It has been demonstrated that weighted averaging can improve upon the accuracy of AODE's estimates [28, 29, 30]. The empirical evidence suggests that the Bayesian model averaging of Maximum a Posteriori Linear Mixture of Generative Distributions (MAPLMG) is the most effective of current approaches [28, 30]. It seems likely that similar approaches will be equally effective with n -dependence estimators.

It is notable that the introduction of Bayesian model averaging to the An DE framework introduces both search and discriminative learning, as a search is performed for the set of weights that optimize the posterior probabilities relative to the training data. Doing so can be expected to reduce bias at the cost of introduction of variance.

One of the interesting questions that this paper investigates is the relative payoff for the investment of additional computation in either performing Bayesian model averaging on An DE or increasing n and using $A(n+1)$ DE. Both approaches can be expected to reduce bias at the cost of an increase in both variance and computation. Which provides the more effective trade-off?

2.4 Tree Augmented Naive Bayes

An n -dependence Bayesian classifier (n -DBC) [31] is a Bayesian network in which each attribute depends upon the class and at most n other non-class attributes. An n -DBC uses $(n+2)$ -dimensional probabilities. Within this framework, NB is a 0-DBC, AODE is a 1-DBC and the full Bayesian classifier is an $(a-1)$ -DBC.

An alternative to the An DE approach to relaxing NB's independence assumption is to use search to select a single model that adds selected interdependencies between attributes. Tree Augmented Naive Bayes (TAN) [32] is a popular approach of this type. It uses conditional mutual information to select a best single parent for each attributes, in addition to the class. Thus, it is a 1-DBC.

It is interesting to consider how search for a single Bayesian classifier model compares with averaging over a class of Bayesian classifier models of the same level of dependence or of a higher level of dependence. This paper also investigates this issue.

3 Relationship to Feating

Feating [27] is a generic ensemble learning technique that also builds upon the ensembling strategy of AODE. Like An DE, Feating operates by building a local model for each combination of n attribute values. To classify a new instance, Feating applies all applicable local models and aggregates the results by performing a majority vote of the resulting classifications. An DE is similar to Feating NB. However, Feating aggregates the predictions of its base learners

by taking the mode of the class predictions. For probabilistic classifiers, these class predictions correspond to the maximum posterior probability. In contrast, *AnDE* uses the ensemble to estimate the joint probability, $P(\mathbf{x}, y)$ for each class, and then calculates its estimate of the posterior probability from this ensembled estimate of the joint probability. A generic ensembling technique, such as Feating, cannot work by calculating an ensemble estimate of the joint probabilities because many classifiers do not produce appropriate probability estimates.

Despite the close relationship to Feating, *AnDE* is worthy of study in its own right for three reasons.

First, irrespective of which aggregation method is used, coupling the search-less ensembling strategy embodied by Feating with search-less base learner NB creates a learner that can deliver low bias using a predefined mapping from low dimensional probabilities to the desired high dimensional probabilities without search or model selection. Hence, *AnDE* provides an example of an alternative to the traditional search-based learning paradigm which is able to deliver low bias classifiers.

Second, as already noted, *AnDE* utilizes a different aggregation method to Feating. It is interesting to examine the consequences of these differences. Cerquides and de Mántaras [28] found that weighted ensembles of joint probability estimates achieved lower error than weighted ensembles of posterior probability estimates, so there is some evidence that the outcomes may be substantially different.

Third, as there is overlap in the information required by each of its local models, *AnDE* can use a single compiled matrix of joint frequencies, saving considerable space relative to storing all of the local models independently. The space complexity of an *AnDE* model is $O(k \binom{a}{n+1} \bar{v}^{n+1})$ whereas the space complexity of Feating NB to level n is $O(k(a-n) \binom{a}{n} \bar{v}^{n+1})$, which is $(n+1)$ times the space complexity of *AnDE*. Most base models formed by Feating will not have this property, and hence *AnDE* is a notable special case.

4 Evaluation

In this section, we evaluate the efficacy of *AnDE*. Due to relatively high time complexity of higher-dimensional estimators, the highest level of *AnDE* with which we perform detailed assessment is A2DE. The primary metrics we use are bias, variance, zero-one loss and RMSE. To assess computational overheads we use total training and classification times divided by the number of examples.

We first study the performance of NB, AODE and A2DE to reveal how performance varies as n increases within the *AnDE* framework. TAN and MAPLMG are studied to show how the search-free generative *AnDE* strategy compares with, respectively, discriminative search for a single Bayesian network classifier of the same dimensionality of dependence, and discriminative search for a weighted classifier of the next lower dimensionality of dependence. We also compare A2DE, that estimates the mean joint probability of the submodels, with variants that calculate the mean posterior probability (PA2DE) and

perform Feating of NB by taking the mode of the class predictions of the sub-models (FA2DE). Finally, to explore how the classification performance of A2DE compares to state-of-the-art classifiers, we also study Random Forests [33] with ten trees (RF10) and Random Forests with 100 trees (RF100).

We compare these algorithms implemented in the Weka workbench [34] on the 62 data sets described in Table 2 that have been used previously in related research [3, 35, 36, 37, 38, 39]. Each algorithm is tested on each data set using the repeated cross-validation bias-variance estimation method [40]. In order to maximize the variation in the training data from trial to trial, we use two-fold cross validation. To minimize the variance in our measurments we report average values over 50 cross-validation trials.

We also form learning curves for NB, AODE, A2DE and A3DE on the Adult data set to further investigate how increasing n within the An DE framework affects performance as the quantity of data increases.

The current implementations of AODE and A2DE are limited to categorical data. A number of approaches have been developed for extending AODE to numeric data [41]. These could be generalized to the An DE framework, but how best to do so is a matter for future research. Hence, we assess only the relative capacities of these algorithms with respect to categorical data. To this end, all numeric attributes are discretized. When MDL discretization [42], a common discretization method for NB, is used to discretize quantitative attributes within each cross-validation fold, many attributes have only one value. In these experiments, we discretize quantitative attributes using three-bin equal-frequency discretization prior to classification.

The base probabilities are estimated using m -estimation [43] ($m = 1$), as it often appears to lead to more accurate probabilities than Laplace estimation for NB and AODE. An exception is that we always use 1.0 for $\hat{P}(x_i | y, x_s)$ when $i \in s$.

The above experiments were conducted on a single CPU single core virtual Linux machine running on a Dell PowerEdge 1950 with dual quad core Intel Xeon E5410 processors running at 2333Mhz with 32 GB of RAM.¹

Average values for each combination of metric, algorithm and dataset are provided in the Appendix. Summary results are provided in the text.

4.1 Varying n within An DE

We first consider the relative performance of the three variants of An DE. For each performance measure, the number of data sets for which A2DE has lower, equal or higher outcomes relative to AODE and NB are summarized

¹Due to technical issues including memory leaks in the Weka implementation of Random Forests, it was not possible to complete all 50 runs of 2-fold cross validation for RF10 on Coverttype and RF100 on Coverttype and Census-Income (KDD). These experiments were instead completed on a Linux Cluster of Xeon 2.8 GHz CPUs, an environment that does not allow reliable time measurements to be taken. For RF10 and RF100 on Coverttype, compute times were estimated by averaging over those runs that could be completed on the virtual machine. No runs could be completed on the virtual machine for RF100 on Census-Income (KDD) and so no time results are reported.

Table 2: Data sets used for experiments

No. Domain				Case Att Class				No. Domain				Case Att Class			
1	Abalone			4177	9	3		32	Letter Recognition			20000	17	26	
2	Adult			48842	15	2		33	Liver Disorders (Bupa)			345	7	2	
3	Annealing			898	39	6		34	Lung Cancer			32	57	3	
4	Audiology			226	70	24		35	Lymphography			148	19	4	
5	Auto Imports			205	26	7		36	MAGIC Gamma Telescope			19020	11	2	
6	Balance Scale			625	5	3		37	Mushrooms			8124	23	2	
7	Breast Cancer (Wisconsin)			699	10	2		38	Nettalk(Phoneme)			5438	8	52	
8	Car Evaluation			1728	8	4		39	New-Thyroid			215	6	3	
9	Census-Income (KDD)			299285	40	2		40	Nursery			12960	9	5	
10	Connect-4 Opening			67557	43	3		41	Optical Digits			5620	49	10	
11	Contact-lenses			24	5	3		42	Page Blocks			5473	11	5	
12	Contraceptive Method Choice			1473	10	3		43	Pen Digits			10992	17	10	
13	Covertypes			581012	55	7		44	Pima Indians Diabetes			768	9	2	
14	Credit Screening			690	16	2		45	Postoperative Patient			90	9	3	
15	Cylinder Bands			540	40	2		46	Primary Tumor			339	18	22	
16	Dermatology			366	35	6		47	Promoter Gene Sequences			106	58	2	
17	Echocardiogram			131	7	2		48	Segment			2310	20	7	
18	German			1000	21	2		49	Sick-euthyroid			3772	30	2	
19	Glass Identification			214	10	3		50	Sign			12546	9	3	
20	Haberman's Survival			306	4	2		51	Sonar Classification			208	61	2	
21	Heart Disease (Cleveland)			303	14	2		52	SPAM E-mail			4601	58	2	
22	Hepatitis			155	20	2		53	Splice-junction Gene Sequences			3190	62	3	
23	Horse Colic			368	22	2		54	Syncon			600	61	6	
24	House Votes 84			435	17	2		55	Teaching Assistant Evaluation			151	6	3	
25	Hungarian			294	14	2		56	Tic-Tac-Toe Endgame			958	10	2	
26	Hypothyroid(Garavan)			3772	30	4		57	Vehicle			846	19	4	
27	Ionosphere			351	35	2		58	Volcanoes			1520	4	4	
28	Iris Classification			150	5	3		59	Vowel			990	14	11	
29	King-rook-vs-king-pawn			3196	37	2		60	Waveform-5000			5000	41	3	
30	Labor negotiations			57	17	2		61	Wine Recognition			178	14	3	
31	LED			1000	7	10		62	Zoo			101	17	7	

Table 3: Win/Draw/Loss: A_n DE, $n = 0, 1$ and 2 , on all 62 data sets

	A2DE vs AODE		A2DE vs NB		AODE vs NB	
	W/D/L	p	W/D/L	p	W/D/L	p
Bias	47/0/15	< 0.001	49/2/11	< 0.001	48/0/14	< 0.001
Variance	19/1/42	< 0.001	15/0/47	< 0.001	20/1/41	0.005
Zero-one loss	33/2/27	0.259	42/1/19	0.002	44/1/17	< 0.001
RMSE	35/1/26	0.153	15/0/47	< 0.001	49/1/12	< 0.001

into win/draw/loss records, and likewise for AODE relative to NB. For each win/draw/loss record a binomial sign test is performed to assess the probability of observing the given number of wins and losses if each were equally likely. These results are presented in Table 3. As expected, we see that increasing n from 0 (NB) to 1 (AODE) to 2 (A2DE) consistently decreases bias at the cost of an increase in variance. As we believe that different bias and variance profiles suit different data quantities [2], we believe that the zero-one loss and RMSE results tell us as much about the composition of the data collection as they do about the algorithms. Specifically, we contend that whether one algorithm or another will win on a given dataset is determined by how well the two algorithms’ learning biases match the underlying distribution, by their variance, and by the quantity of data. A low variance algorithm will usually have an advantage for small data while a low bias algorithm will usually be advantaged by large data. For our datasets, both AODE and A2DE reduce both zero-one loss and RMSE significantly often relative to NB. While A2DE obtains lower zero-one loss and RMSE than AODE more often than the reverse, this difference is not found to be significant.

To investigate in greater detail our expectation that algorithms with lower variance will be advantaged for small data and those with lower bias for larger data, we form learning curves for Adult, replicating the method of Webb et al. [3]. 1000 objects are selected at random as a test set and training sets were sampled from the remaining objects. The training set size starts from 23 and then doubles up to 47104, this being a progression that ends with as close to all the available data as possible once the 1000 test cases are removed. This process is repeated 50 times and each algorithm is evaluated on the resulting training-test set pairs. The learning curves of zero-one loss and RMSE for NB, AODE, A2DE and A3DE are presented in Figure 2.

The plots for zero-one loss clearly show the predicted trade-off for increasing n . At the smallest data size, where low variance is more important than low bias, zero-one loss is minimized by $n = 0$ (NB) and increases as n increases. At the largest data size, where low bias is most important, this dimensionality is reversed. A similar trend is shown with respect to RMSE although the algorithms have not yet achieved their asymptotic rates at the largest data sizes

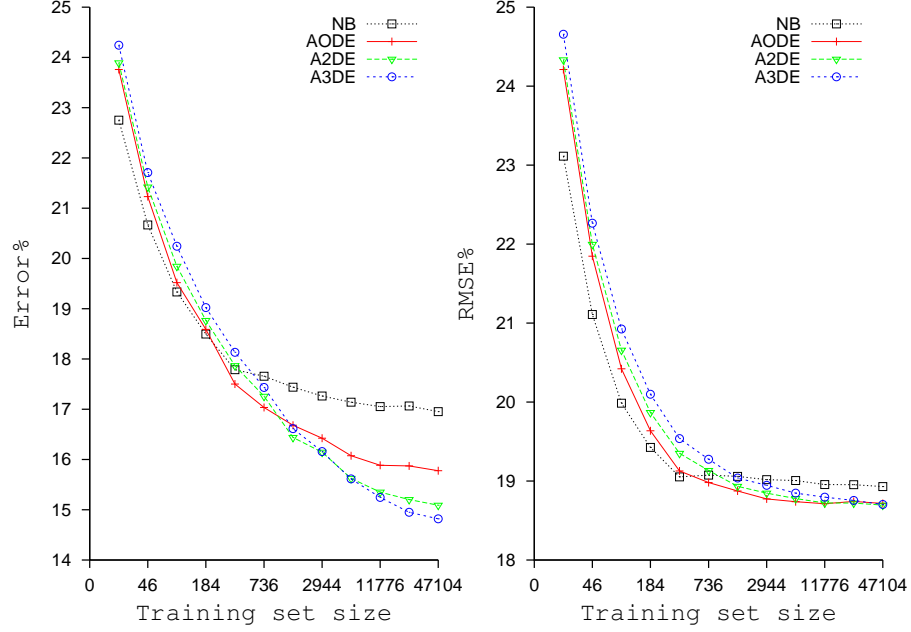


Figure 2: Zero-one loss and RMSE of NB and $AnDE$ on Adult dataset, as function of training set size

available.

It is interesting to see how the relative bias/variance trade-offs of increasing n play off when NB’s attribute independence assumption holds. The LED dataset has a specific configuration of attribute-values for each class, making the attributes conditionally independent given the class. Each attribute has 10% noise added. AODE and A2DE overfit this noise, leading to increased error. NB’s zero-one loss is 0.2627, AODE’s is 0.2639 and A2DE’s is 0.2667. These outcomes are with training set sizes of 500. Using the UCI data generator, we generated 10 LED datasets comprising 2,000 and 10 comprising 4,000 instances and repeated the cross-validation experiments thereon. For the datasets of 2,000, the training set size is 1,000 and the mean and standard deviation of the respective zero-one loss is NB: 0.2603 ± 0.0099 , AODE: 0.2601 ± 0.0101 and A2DE 0.2603 ± 0.0102 . For the datasets of 4,000, the training set size is 2,000 and the mean and standard deviation of the respective zero-one loss is NB: 0.2597 ± 0.0049 , AODE: 0.2598 ± 0.0051 and A2DE: 0.2603 ± 0.0053 . It seems clear that increasing training set sizes rapidly reduces the error advantage that NB enjoys in this context where its conditional attribute assumption is satisfied.

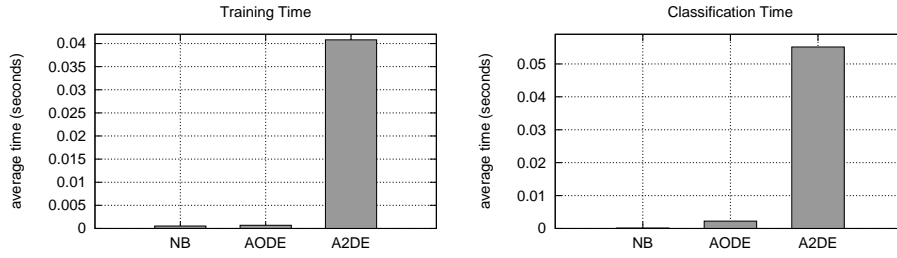
As final confirmation that higher n is best suited to larger data, on the ten largest datasets, those with more than 8,000 examples, A2DE always achieves lower zero-one loss and RMSE than AODE ($p = 0.001$), see Table 4.

As expected, both training and classification compute times increase as n

Table 4: Win/Draw/Loss: $AnDE$, $n = 0, 1$ and 2 , on the ten largest data sets

	A2DE vs AODE		A2DE vs NB		AODE vs NB	
	W/D/L	p	W/D/L	p	W/D/L	p
Zero-one loss	10/0/0	0.001	10/0/0	0.001	10/0/0	0.001
RMSE	10/0/0	0.001	10/0/0	0.001	10/0/0	0.001

Figure 3: Average per-example training and classification times for NB, AODE and A2DE



increases. Figure 3 shows the grand averages for the per-example training and classification times for each algorithm.

4.2 Comparison with TAN

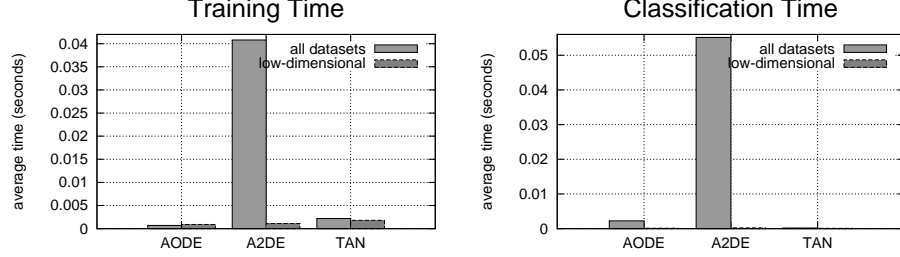
We here explore the relative benefits of discriminative search for a single best Bayesian classifier model against $AnDE$'s search-free approach of averaging over a class of Bayesian classifier models. To this end we compare AODE and A2DE with TAN. Table 5 presents win/draw/loss results comparing AODE and A2DE to TAN.

Table 5: Win/Draw/Loss: $AnDE$, $n = 1$ and 2 vs TAN on all 62 data sets

	A2DE vs TAN		AODE vs TAN	
	W/D/L	p	W/D/L	p
Bias	34/0/28	0.263	20/1/41	0.005
Variance	48/0/14	<0.001	52/1/9	<0.001
Zero-one loss	48/0/14	<0.001	43/1/18	0.001
RMSE	43/1/18	0.001	40/1/21	0.010

Figure 4: Average per-example training and classification times for AODE, A2DE and TAN

Two values are shown for each algorithm, the average across all datasets and the average across the ten lowest-dimensional (4–7 attributes) datasets.



Overall, TAN has an advantage in bias but a disadvantage is variance relative to AODE. When using search to select a single 1-DBC model is compared to averaging over a class of 2-DBCs, the bias advantage is lost but the variance disadvantage remains. The relative bias-variance tradeoffs of AODE and TAN result in a general error advantage to AODE. Comparing TAN to A2DE, TAN no longer has a bias advantage, and at this higher value of n , the error advantage of the A n DE classifier becomes even more consistent.

Figure 4 shows the relative training and classification times for AODE, A2DE and TAN. It is clear that A2DE has a considerably greater computational requirements both for training and classification. However, this disadvantage disappears when we consider only the ten lowest dimensional datasets, also illustrated in this figure.

4.3 Comparison with MAPLMG

As discussed above, we wish to investigate the relative payoffs obtained by investing additional computation to that required by AODE by respectively using discriminative learning of weights or, alternatively, increasing the dimensionality of the probabilities from which the posterior probability is extrapolated. To this end, Table 6 presents win/draw/loss results comparing A2DE and AODE to MAPLMG.

As established by previous research [28], MAPLMG’s approach of using discriminative learning of weights for the AODE linear combination significantly reduces bias relative to AODE at the cost of an increase in variance. However, relative to this discriminative approach to extrapolating from three-dimensional probabilities, A2DE’s search-free approach to extrapolating from four-dimensional probabilities further reduces bias at the cost of an increase in variance. While the resulting difference in error is not found to be significant across the full suite of 62 datasets, when the ten largest datasets are considered, the lower bias algorithm, A2DE, consistently achieves lower zero-one loss and RMSE than MAPLMG ($p = 0.001$) (see Table 7).

Table 6: Win/Draw/Loss: $AnDE$, $n = 1$ and 2 vs MAPLMG on all 62 data sets

	A2DE vs MAPLMG		AODE vs MAPLMG	
	W/D/L	p	W/D/L	p
Bias	40/0/22	0.015	17/4/41	0.001
Variance	19/1/42	0.002	36/5/21	0.031
Zero-one loss	30/1/31	0.500	22/4/36	0.043
RMSE	34/1/28	0.263	19/0/39	0.006

Table 7: Win/Draw/Loss: $AnDE$, $n = 1$ and 2 vs MAPLMG on the ten largest data sets

	A2DE vs MAPLMG		AODE vs MAPLMG	
	W/D/L	p	W/D/L	p
Zero-one loss	10/0/0	0.001	1/0/8	0.039
RMSE	10/0/0	0.001	0/0/10	0.001

MAPLMG’s Bayesian model averaging comes at considerable cost in training time. Figure 5 shows the average per-example training and test times for AODE, A2DE and MAPLMG. Note that MAPLMG is implemented as an external function to Weka, and hence is likely to be inherently more efficient. The training and test times include a substantial fixed overhead, and hence the per-instance training times should decrease if the complexity is linear with respect to the training set size. However, MAPLMG’s super-linear training complexity minimizes this effect, demonstrating that it will not be feasible to apply it to very large data.

4.4 Comparison with Feating

To understand how the $AnDE$ approach performs relative to Feating NB, we compare A2DE, that calculates the mean of the joint probabilities, with a variant PA2DE, that calculates the mean of the posterior probabilities, and another variant FA2DE, that calculates the mode of the classes predicted by the sub-models. As described in Section 3 and the start of Section 4, these embody the two main differences between $AnDE$ and Feating NB.

Table 8 shows the win/draw/loss results comparing A2DE to these variants. It is clear that both variants have higher bias but lower variance than A2DE. It is straightforward to understand why Feating would have lower variance. The mode is a much more stable estimator of central tendency than the mean, which can be greatly influenced by a single outlier. It is less obvious why lower variance should result from averaging over the estimates of the posterior rather than of

Figure 5: Average per-example training and classification times for AODE, A2DE and MAPLMG

In addition to the times for all datasets, training times are shown for the ten largest datasets.

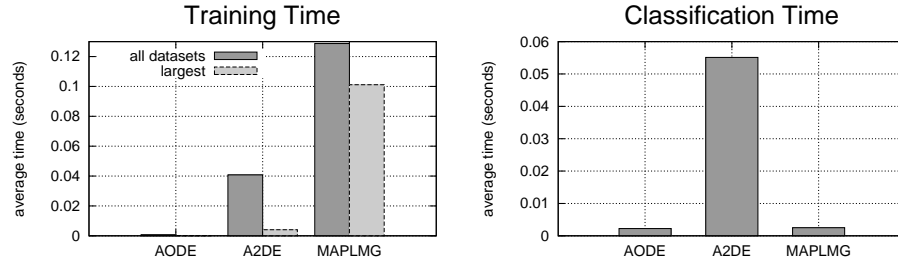


Table 8: Win/Draw/Loss: A2DE vs PA2DE and FA2DE

	A2DE vs PA2DE		A2DE vs FA2DE	
	W/D/L	p	W/D/L	p
Bias	41/2/19	<0.001	46/1/15	<0.001
Variance	21/3/38	0.018	22/1/39	0.020
Zero-one loss	33/1/28	0.304	36/2/24	0.078
RMSE	30/0/32	0.449	49/0/13	<0.001

Table 9: Win/Draw/Loss: A2DE vs PA2DE and FA2DE on the ten largest datasets

	A2DE vs PA2DE		A2DE vs FA2DE	
	W/D/L	p	W/D/L	p
Zero-one loss	8/0/2	0.109	9/0/1	0.021
RMSE	8/0/2	0.109	8/0/1	0.039

the joint probability. Nonetheless, the result is consistent with Cerquides and de Mántaras’ [28] finding that a linear combination of joint probability estimates resulted in higher accuracy than a linear combination of posterior probability estimates. This remains an interesting unexplained phenomena worthy of further investigation.

Over the full range of datasets these differences in bias and variance profiles do not result in statistically significant differences on either measure of error, except with respect to RMSE for Feating. This reflects the manner in which Feating selects a single class rather than producing a distribution of class probabilities.

Due to its lower bias, A2DE achieves lower zero-one loss than PA2DE on eight and FA2DE on nine of the ten largest datasets. This outcome is statistically significant at the 0.05 level with respect to FA2DE, but misses out on being statistically significant with respect to PA2DE. A2DE achieves lower RMSE than both the alternatives on eight of the ten largest datasets, and draws on one of the remaining datasets with respect to FA2DE, again attaining statistical significance at the 0.05 level relative to FA2DE but failing to do so relative to PA2DE. Hence, the evidence is suggestive that for large data the $AnDE$ approach is preferable to the selection of the mode, and calculating the mean of the joint probabilities is preferable to calculation the mean of the posteriors.

4.5 Comparison with the state-of-the-art

In addition to the relative performance of these related algorithms, it is useful to understand how the performance compares to well known examples of the state-of-the-art. We choose Random Forests [33] as the comparator algorithm because it is relatively unparameterized and hence readily produces clearly understood performance outcomes. We use Random Forests with both the default setting of 10 trees (RF10) and with 100 trees (RF100), allowing us to explore the relative computational/accuracy trade-offs. Table 10 shows the win/draw/loss results for each of A2DE, AODE and NB against RF10 and RF100 for each of zero-one loss, Bias, Variance and RMSE.

All three levels of $AnDE$ have higher bias but lower variance than both levels of Random Forests. This trade-off delivers lower error significantly more often than not for both A2DE and AODE relative to RF10. Both deliver lower error

Table 10: Win/Draw/Loss: $AnDE$, $n = 0, 1$ and 2 , vs RF10 and RF100 on all 62 data sets

		$AnDE$ vs RF10		$AnDE$ vs RF100	
		W/D/L	p	W/D/L	p
A2DE	Bias	18/1/43	0.001	22/2/38	0.026
	Variance	57/0/5	<0.001	45/1/16	<0.001
	Zero-one loss	42/0/20	0.004	36/3/23	0.059
	RMSE	40/0/22	0.015	35/0/27	0.187
AODE	Bias	16/0/46	<0.001	20/0/42	0.004
	Variance	57/1/4	<0.001	47/0/15	<0.001
	Zero-one loss	41/0/21	0.008	33/1/28	0.304
	RMSE	39/0/23	0.028	34/0/28	0.263
NB	Bias	14/1/47	<0.001	16/1/45	<0.001
	Variance	56/0/6	<0.001	51/0/11	<0.001
	Zero-one loss	33/0/29	0.352	30/1/31	0.500
	RMSE	30/0/32	0.450	28/0/34	0.263

more often than RF100, but not significantly so. Notably, relative to both RF10 and RF100, NB achieves higher error almost as often as lower. This illustrates the weaknesses of such ‘bake-offs’ with respect to error. As we have argued above, low variance algorithms such as NB will be advantaged by the relatively small data sets used in this study. To assess this effect, we repeated the error comparisons using only the ten largest datasets, those containing more than 8000 examples. The results are shown in Table 11. For these larger datasets, both R10 and RF100 achieve lower error more often than all three of A2DE, AODE and NB, significantly so with respect to AODE and NB and when comparing RF100 to A2DE on zero-one loss. This suggests that for very large training data, in the absence of any prior knowledge of the nature of the multivariate probability distribution that the data embodies, Random Forests are likely to achieve lower error than an $AnDE$ classifier, although the data quantity at which this is achieved will be ever greater as the dimensionality of $AnDE$ is increased.

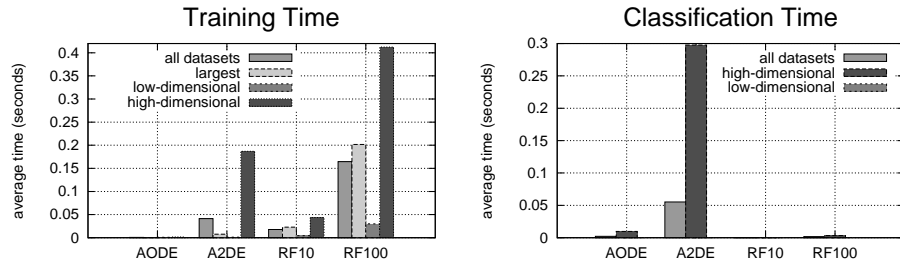
However, Random Forests’ error advantage for large data comes at a cost in training time. Figure 6 shows the training and classification times for AODE, A2DE, RF10 and RF100. It is apparent that, overall, RF100 has very high training times. While A2DE’s training time does approach RF100’s for high dimensional data, for small data and low dimensional data its training times are competitive with RF10. On the other hand, A2DE requires substantially more classification time on average than Random Forests. This requirement grows greatly with high-dimensional data. A2DE will not be feasible for classification of large numbers of high-dimensional objects. In contrast, its classification time is very competitive on low-dimensional data.

Table 11: Win/Draw/Loss: $AnDE$, $n = 0, 1$ and 2 , vs RF10 and RF100 on the ten largest data sets

		$AnDE$ vs RF10		$AnDE$ vs RF100	
		W/D/L	p	W/D/L	p
AODE	Zero-one loss	2/0/8	0.055	1/1/8	0.020
	RMSE	3/0/7	0.172	2/0/8	0.055
A2DE	Zero-one loss	0/0/10	0.001	0/0/10	0.001
	RMSE	1/0/9	0.011	0/0/10	0.001
NB	Zero-one loss	0/0/10	0.001	0/0/10	0.001
	RMSE	0/0/10	0.001	0/0/10	0.001

Figure 6: Average per-example training and classification times for AODE, A2DE, RF10 and RF100

Training times are presented for all, the ten largest (excluding Census Income, for which RF100 could not be executed on a machine for which reliable times could be obtained, thus 5,620–581,012 examples), the ten lowest dimensional (5–7 attributes) and the ten highest dimensional (43–70 attributes) datasets. Classification times are presented for all, the ten lowest dimensional and the ten highest dimensional datasets.



5 Conclusions and Directions for Future Research

$AnDE$ provides an attractive framework for developing machine learning techniques. A single parameter n controls a bias-variance trade-off such that $n = a$ provides a classifier whose asymptotic error is the Bayes optimal error rate. However, for high-dimensional data only very low-dimensional forms of $AnDE$ are feasible. Nonetheless, we have established that higher-dimensional variants are likely to deliver greater accuracy than lower-dimensional alternatives when the number of training examples is high. In consequence, a promising direction for future research is to develop computationally efficient techniques for approximating $AnDE$ for high values of n .

A further unresolved issue is how to select an appropriate value of n for any specific dataset \mathcal{T} . Are there more computationally efficient approaches than a simple wrapper-based comparison of each possible value?

A number of techniques have been developed for extending AODE to handle numeric data [41]. There is a need to extend this work to the more general $AnDE$ framework.

We have presented a strategy for learning without fitting the full multivariate probability distribution. We do not argue, however, that fitting the full multivariate probability distribution should necessarily be avoided. Indeed, it has been demonstrated that it is possible to reduce the error of AODE both by appropriate feature selection [44, 45, 46] and weighting of the submodels [28, 29, 30] in order to better fit the full multivariate probability distribution. Therefore, it is likely to be worthwhile to explore efficient methods for each of these strategies for higher values of n . If fast classification is required, and time for training is less constrained, approaches that use search to select a small number of submodels from an $AnDE$ model are likely to be desirable. Where there is sufficient training time available, search for appropriate submodel weights is also likely to be useful.

We have developed a generative learning algorithm that generalizes the principles that underlie AODE to ever higher levels of dimensionality. It has the following desirable features:

- both time and space complexity are linear with respect to the number of training examples;
- it performs direct prediction of class probabilities;
- it has integrated handling of missing values;
- it is robust in the face of noise;
- other than the choice of which instantiation (choice of n) and choice of smoothing technique, the approach uses no tuneable parameters;
- it does not perform model selection;

- a simple mechanism controls the bias/variance trade-off;
- it supports incremental learning;
- learning and classification can readily utilize parallel computation; and
- there is a direct theoretical basis that provides optimal prediction except insofar as clearly specified assumptions are violated.

A single parameter n provides control over a bias-variance trade-off, such that higher values of n are appropriate for greater numbers of training cases. *AnDE* demonstrates that it is possible to develop competitive learners without using search. Of further interest, this family of algorithms show that it is possible to develop low bias algorithms in a generative framework. Finally, *A2DE* proves to be a computationally tractable version of *AnDE* that delivers strong classification accuracy for large data without any parameter tuning.

Acknowledgements

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A Detailed Results

Detailed results for Bias, Variance, zero-one Loss, RMSE, Training Time and Classification Times are presented in Tables 8 to 13. The datasets are listed in ascending order on number of instances.

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Table 12: Bias

Dataset	NB	AODE	A2DE	PA2DE	FA2DE	TAN	MAPLMG	RF10	RF100
Contact-lenses	0.1897	0.1970	0.1967	0.2018	0.2002	0.3245	0.1913	0.1710	0.1728
Lung Cancer	0.3413	0.3423	0.3443	0.3702	0.3726	0.3174	0.3428	0.3454	0.3739
Labor negotiations	0.0555	0.0608	0.0650	0.0662	0.0654	0.0807	0.0627	0.1009	0.1011
Postoperative Patient	0.2730	0.2893	0.2949	0.2941	0.2923	0.2717	0.2878	0.2809	0.2907
Zoo	0.0382	0.0308	0.0311	0.0317	0.0315	0.0518	0.0308	0.0302	0.0329
Promoter Gene Sequences	0.0692	0.0902	0.2299	0.1624	0.1737	0.0808	0.0934	0.0901	0.0576
Echocardiogram	0.2653	0.2678	0.2628	0.2613	0.2637	0.2416	0.2616	0.2500	0.2543
Lymphography	0.1286	0.1202	0.1164	0.1153	0.1181	0.1256	0.1185	0.1307	0.1373
Iris Classification	0.0308	0.0286	0.0296	0.0307	0.0293	0.0270	0.0288	0.0306	0.0308
Teaching Assistant Evaluation	0.3567	0.3075	0.2997	0.2999	0.3066	0.3280	0.3109	0.2969	0.3001
Hepatitis	0.1368	0.1262	0.1230	0.1276	0.1267	0.1008	0.1244	0.1307	0.1327
Wine Recognition	0.0430	0.0387	0.0405	0.0391	0.0413	0.0406	0.0388	0.0434	0.0435
Auto Imports	0.2615	0.1775	0.1680	0.1724	0.1740	0.1996	0.1768	0.1380	0.1362
Sonar Classification	0.2227	0.1610	0.1422	0.1501	0.1508	0.1439	0.1593	0.1221	0.1344
Glass Identification	0.2133	0.2124	0.2110	0.2075	0.2105	0.2142	0.2126	0.2041	0.2074
New-Thyroid	0.0997	0.0944	0.0960	0.0933	0.0927	0.1026	0.0947	0.0981	0.0998
Audiology	0.2193	0.2196	0.2193	0.2179	0.2179	0.1817	0.2196	0.1568	0.1712
Hungarian	0.1232	0.1225	0.1232	0.1240	0.1237	0.1262	0.1219	0.1458	0.1496
Heart Disease (Cleveland)	0.1490	0.1470	0.1454	0.1483	0.1483	0.1397	0.1468	0.1514	0.1530
Haberman's Survival	0.2416	0.2408	0.2413	0.2425	0.2420	0.2406	0.2418	0.2342	0.2369
Primary Tumor	0.3811	0.3819	0.3810	0.3827	0.3815	0.3764	0.3833	0.3719	0.3824
Liver Disorders (Bupa)	0.3269	0.3209	0.3204	0.3213	0.3201	0.3137	0.3202	0.3203	0.3242
Ionosphere	0.1758	0.0688	0.0615	0.0633	0.0636	0.0476	0.0672	0.0547	0.0585
Dermatology	0.0107	0.0120	0.0123	0.0113	0.0116	0.0130	0.0119	0.0219	0.0195
Horse Colic	0.1735	0.1527	0.1457	0.1446	0.1448	0.1412	0.1516	0.1283	0.1343
House Votes 84	0.0917	0.0471	0.0367	0.0436	0.0408	0.0450	0.0415	0.0299	0.0339
Cylinder Bands	0.1548	0.1317	0.1315	0.1378	0.1374	0.3326	0.1293	0.1862	0.2007
Syncon	0.1018	0.0536	0.0436	0.0728	0.0740	0.0300	0.0486	0.0384	0.0382
Balance Scale	0.1381	0.1453	0.1505	0.1503	0.1508	0.1432	0.1454	0.1429	0.1436
Credit Screening	0.1266	0.1197	0.1191	0.1204	0.1209	0.1181	0.1188	0.1137	0.1165
Breast Cancer (Wisconsin)	0.0255	0.0276	0.0263	0.0261	0.0255	0.0269	0.0272	0.0307	0.0314
Pima Indians Diabetes	0.2499	0.2406	0.2276	0.2259	0.2295	0.2189	0.2393	0.2107	0.2122
Vehicle	0.3849	0.2948	0.2821	0.2876	0.2854	0.2678	0.2901	0.2404	0.2458
Annealing	0.0908	0.0676	0.0671	0.0647	0.0654	0.0625	0.0673	0.0969	0.0986
Tic-Tac-Toe Endgame	0.2509	0.2010	0.0719	0.1003	0.1114	0.1693	0.1961	0.0400	0.0275
Vowel	0.3308	0.1370	0.1194	0.1200	0.1244	0.1674	0.1189	0.1054	0.1056
LED	0.2261	0.2268	0.2270	0.2272	0.2266	0.2241	0.2269	0.2261	0.2277
German	0.2100	0.2010	0.1970	0.2023	0.2035	0.1840	0.2012	0.1826	0.1977
Contraceptive Method Choice	0.4683	0.4339	0.4074	0.4168	0.4105	0.3830	0.4247	0.3682	0.3754
Volcanoes	0.5034	0.4630	0.4577	0.4577	0.4583	0.4557	0.4656	0.4539	0.4577
Car Evaluation	0.1061	0.0591	0.0411	0.0379	0.0417	0.0482	0.0520	0.0395	0.0388
Segment	0.1605	0.1211	0.1162	0.1177	0.1178	0.1104	0.1156	0.0925	0.0933
Splice-junction Gene Sequences	0.0383	0.0304	0.0266	0.0581	0.0569	0.0376	0.0302	0.0355	0.0259
King-rook-vs-king-pawn	0.1074	0.0716	0.0541	0.0722	0.0858	0.0626	0.0458	0.0079	0.0062
Hypothyroid(Garavan)	0.0743	0.0738	0.0737	0.0740	0.0742	0.0746	0.0739	0.0739	0.0741
Sick-euthyroid	0.0663	0.0624	0.0613	0.0618	0.0623	0.0589	0.0603	0.0590	0.0590
Abalone	0.4737	0.3925	0.3902	0.3860	0.3903	0.3907	0.3921	0.3745	0.3769
SPAM E-mail	0.3322	0.3324	0.3323	0.3322	0.3322	0.3310	0.3324	0.3308	0.3312
Waveform-5000	0.2070	0.1692	0.1625	0.1854	0.1879	0.1569	0.1629	0.1312	0.1531
Nettalk(Phoneme)	0.1957	0.1476	0.1512	0.1322	0.1373	0.1878	0.1361	0.1063	0.1098
Page Blocks	0.0721	0.0771	0.0774	0.0767	0.0781	0.0795	0.0776	0.0775	0.0776
Optical Digits	0.0804	0.0286	0.0229	0.0410	0.0421	0.0382	0.0279	0.0243	0.0221
Mushrooms	0.0205	0.0002	0.0000	0.0000	0.0000	0.0002	0.0002	0.0000	0.0000
Pen Digits	0.1562	0.0601	0.0474	0.0516	0.0508	0.0770	0.0531	0.0330	0.0341
Sign	0.4530	0.4001	0.3661	0.3685	0.3678	0.3859	0.3833	0.3378	0.3391
Nursery	0.0901	0.0655	0.0433	0.0454	0.0427	0.0546	0.0668	0.0105	0.0084
MAGIC Gamma Telescope	0.2387	0.2171	0.1992	0.2073	0.2057	0.2135	0.2166	0.2045	0.2049
Letter Recognition	0.4450	0.3740	0.3473	0.3568	0.3635	0.3668	0.3697	0.2564	0.2591
Adult	0.1777	0.1668	0.1579	0.1652	0.1661	0.1552	0.1600	0.1397	0.1416
Connect-4 Opening	0.2646	0.2250	0.2107	0.2421	0.2584	0.2224	0.2203	0.1304	0.1427
Census-Income (KDD)	0.2358	0.0853	0.0604	0.1318	0.1224	0.0628	0.0806	0.0429	0.0447
Coverttype	0.3444	0.3180	0.3075	0.3335	0.3444	0.3233	0.3114	0.2363	0.2369
Mean	0.1971	0.1690	0.1632	0.1679	0.1693	0.1693	0.1663	0.1493	0.1521

Table 13: Variance

Dataset	NB	AODE	A2DE	PA2DE	FA2DE	TAN	MAPLMG	RF10	RF100
Contact-lenses	0.1419	0.1472	0.1675	0.1415	0.2098	0.0972	0.1379	0.1873	0.1647
Lung Cancer	0.1794	0.1921	0.1963	0.1967	0.1967	0.2157	0.1916	0.2596	0.2218
Labor negotiations	0.0393	0.0483	0.0470	0.0415	0.0433	0.0902	0.0468	0.1001	0.0827
Postoperative Patient	0.0859	0.0782	0.0876	0.0832	0.0822	0.1027	0.0810	0.1091	0.0961
Zoo	0.0343	0.0308	0.0302	0.0302	0.0324	0.0472	0.0308	0.0478	0.0386
Promoter Gene Sequences	0.0693	0.1119	0.1180	0.0905	0.0897	0.1562	0.1140	0.1661	0.0909
Echocardiogram	0.0636	0.0697	0.0823	0.0858	0.0857	0.0868	0.0742	0.1109	0.1043
Lymphography	0.0410	0.0444	0.0479	0.0421	0.0443	0.1041	0.0457	0.0898	0.0622
Iris Classification	0.0112	0.0110	0.0119	0.0131	0.0152	0.0171	0.0116	0.0126	0.0127
Teaching Assistant Evaluation	0.1649	0.1958	0.1945	0.1980	0.1911	0.1998	0.1965	0.2151	0.2108
Hepatitis	0.0237	0.0327	0.0374	0.0333	0.0338	0.0622	0.0334	0.0605	0.0464
Wine Recognition	0.0174	0.0183	0.0207	0.0199	0.0194	0.0364	0.0184	0.0389	0.0203
Auto Imports	0.1371	0.1375	0.1378	0.1325	0.1311	0.1273	0.1375	0.1550	0.1289
Sonar Classification	0.0756	0.0883	0.0781	0.0843	0.0847	0.1197	0.0865	0.1380	0.0904
Glass Identification	0.0484	0.0400	0.0449	0.0466	0.0455	0.0565	0.0428	0.0618	0.0616
New-Thyroid	0.0192	0.0258	0.0269	0.0247	0.0242	0.0338	0.0256	0.0298	0.0287
Audiology	0.1014	0.0995	0.0986	0.0990	0.1008	0.1588	0.0997	0.1619	0.1104
Hungarian	0.0249	0.0291	0.0381	0.0370	0.0363	0.0596	0.0313	0.0710	0.0568
Heart Disease (Cleveland)	0.0209	0.0299	0.0395	0.0348	0.0343	0.0635	0.0316	0.0867	0.0708
Haberman's Survival	0.0411	0.0569	0.0639	0.0646	0.0595	0.0645	0.0505	0.0853	0.0808
Primary Tumor	0.1594	0.1582	0.1607	0.1576	0.1589	0.2001	0.1580	0.2361	0.2029
Liver Disorders (Bupa)	0.0968	0.1075	0.1100	0.1111	0.1133	0.1186	0.1086	0.1183	0.1155
Ionosphere	0.0326	0.0117	0.0168	0.0096	0.0097	0.0198	0.0131	0.0378	0.0177
Dermatology	0.0095	0.0111	0.0112	0.0106	0.0102	0.0288	0.0111	0.0364	0.0179
Horse Colic	0.0245	0.0369	0.0436	0.0335	0.0332	0.0587	0.0382	0.0499	0.0313
House Votes 84	0.0061	0.0096	0.0137	0.0098	0.0113	0.0204	0.0112	0.0173	0.0084
Cylinder Bands	0.1065	0.1112	0.1073	0.0954	0.0960	0.0703	0.1100	0.1272	0.0910
Syncon	0.0092	0.0199	0.0196	0.0166	0.0163	0.0259	0.0197	0.0582	0.0254
Balance Scale	0.0555	0.0606	0.0712	0.0724	0.0718	0.0672	0.0622	0.0828	0.0808
Credit Screening	0.0256	0.0270	0.0281	0.0278	0.0272	0.0451	0.0275	0.0578	0.0441
Breast Cancer (Wisconsin)	0.0016	0.0095	0.0127	0.0076	0.0073	0.0241	0.0105	0.0138	0.0076
Pima Indians Diabetes	0.0254	0.0349	0.0508	0.0513	0.0478	0.0576	0.0369	0.0772	0.0729
Vehicle	0.0857	0.0986	0.1049	0.0997	0.1023	0.1233	0.1024	0.1461	0.1305
Annealing	0.0117	0.0174	0.0169	0.0182	0.0179	0.0206	0.0162	0.0452	0.0383
Tic-Tac-Toe Endgame	0.0407	0.0508	0.0536	0.0562	0.0599	0.0787	0.0541	0.0809	0.0490
Vowel	0.2268	0.1637	0.1451	0.1398	0.1444	0.2153	0.1528	0.1424	0.1183
LED	0.0367	0.0371	0.0397	0.0398	0.0392	0.0465	0.0376	0.0551	0.0509
German	0.0481	0.0540	0.0602	0.0519	0.0507	0.0969	0.0546	0.0993	0.0689
Contraceptive Method Choice	0.0719	0.1036	0.1315	0.1190	0.1258	0.1592	0.1132	0.1982	0.1875
Volcanoes	0.0829	0.1333	0.1415	0.1415	0.1413	0.1413	0.1305	0.1469	0.1427
Car Evaluation	0.0506	0.0472	0.0436	0.0405	0.0452	0.0335	0.0456	0.0517	0.0389
Segment	0.0198	0.0184	0.0166	0.0184	0.0189	0.0217	0.0178	0.0269	0.0245
Splice-junction Gene Sequences	0.0083	0.0097	0.0126	0.0175	0.0172	0.0232	0.0098	0.0824	0.0222
King-rook-vs-king-pawn	0.0199	0.0204	0.0200	0.0179	0.0188	0.0155	0.0128	0.0112	0.0067
Hypothyroid(Garavan)	0.0008	0.0006	0.0007	0.0006	0.0007	0.0016	0.0005	0.0076	0.0063
Sick-euthyroid	0.0145	0.0034	0.0028	0.0029	0.0033	0.0053	0.0033	0.0085	0.0073
Abalone	0.0234	0.0837	0.0866	0.0917	0.0859	0.0864	0.0839	0.1052	0.1032
SPAM E-mail	0.0051	0.0050	0.0050	0.0050	0.0051	0.0074	0.0050	0.0067	0.0061
Waveform-5000	0.0132	0.0292	0.0330	0.0166	0.0161	0.0587	0.0328	0.1071	0.0475
Nettalk(Phoneme)	0.1076	0.1167	0.1295	0.1132	0.1246	0.1602	0.0985	0.0865	0.0686
Page Blocks	0.0177	0.0076	0.0063	0.0070	0.0057	0.0043	0.0061	0.0051	0.0049
Optical Digits	0.0099	0.0086	0.0076	0.0090	0.0091	0.0142	0.0089	0.0419	0.0118
Mushrooms	0.0029	0.0001	0.0000	0.0001	0.0001	0.0001	0.0001	0.0001	0.0000
Pen Digits	0.0079	0.0064	0.0059	0.0054	0.0064	0.0170	0.0068	0.0186	0.0131
Sign	0.0113	0.0100	0.0160	0.0123	0.0189	0.0136	0.0174	0.0193	0.0176
Nursery	0.0077	0.0088	0.0113	0.0104	0.0117	0.0146	0.0123	0.0231	0.0160
MAGIC Gamma Telescope	0.0095	0.0095	0.0182	0.0080	0.0117	0.0079	0.0071	0.0098	0.0089
Letter Recognition	0.0520	0.0478	0.0473	0.0439	0.0469	0.0768	0.0477	0.1000	0.0917
Adult	0.0051	0.0085	0.0105	0.0079	0.0071	0.0140	0.0097	0.0370	0.0331
Connect-4 Opening	0.0146	0.0189	0.0212	0.0146	0.0145	0.0144	0.0196	0.0831	0.0449
Census-Income (KDD)	0.0033	0.0121	0.0110	0.0055	0.0064	0.0077	0.0130	0.0139	0.0102
Coverttype	0.0029	0.0028	0.0038	0.0031	0.0024	0.0035	0.0045	0.0149	0.0141
Mean	0.0469	0.0519	0.0551	0.0519	0.0536	0.0664	0.0519	0.0786	0.0626

Table 14: Zero-One Loss

Dataset	NB	AODE	A2DE	PA2DE	FA2DE	TAN	MAPLMG	RF10	RF100
Contact-lenses	0.3317	0.3442	0.3642	0.3433	0.4100	0.4217	0.3292	0.3583	0.3375
Lung Cancer	0.5206	0.5344	0.5406	0.5669	0.5694	0.5331	0.5344	0.6050	0.5956
Labor negotiations	0.0947	0.1091	0.1119	0.1077	0.1088	0.1709	0.1095	0.2011	0.1839
Postoperative Patient	0.3589	0.3676	0.3824	0.3773	0.3744	0.3744	0.3689	0.3900	0.3869
Zoo	0.0725	0.0616	0.0614	0.0620	0.0640	0.0990	0.0616	0.0780	0.0715
Promoter Gene Sequences	0.1385	0.2021	0.3479	0.2528	0.2634	0.2370	0.2074	0.2562	0.1485
Echocardiogram	0.3289	0.3376	0.3450	0.3472	0.3495	0.3284	0.3359	0.3609	0.3586
Lymphography	0.1696	0.1646	0.1643	0.1574	0.1624	0.2297	0.1642	0.2204	0.1995
Iris Classification	0.0420	0.0396	0.0415	0.0437	0.0445	0.0441	0.0404	0.0432	0.0435
Teaching Assistant Evaluation	0.5216	0.5033	0.4942	0.4979	0.4977	0.5278	0.5074	0.5119	0.5109
Hepatitis	0.1605	0.1588	0.1604	0.1609	0.1605	0.1630	0.1578	0.1912	0.1791
Wine Recognition	0.0604	0.0570	0.0612	0.0590	0.0608	0.0770	0.0572	0.0824	0.0638
Auto Imports	0.3986	0.3149	0.3059	0.3049	0.3051	0.3268	0.3143	0.2931	0.2651
Sonar Classification	0.2983	0.2493	0.2204	0.2344	0.2355	0.2637	0.2458	0.2601	0.2248
Glass Identification	0.2617	0.2524	0.2559	0.2541	0.2560	0.2707	0.2554	0.2659	0.2690
New-Thyroid	0.1190	0.1202	0.1229	0.1180	0.1169	0.1365	0.1204	0.1279	0.1285
Audiology	0.3206	0.3191	0.3179	0.3169	0.3188	0.3404	0.3193	0.3188	0.2816
Hungarian	0.1482	0.1516	0.1614	0.1610	0.1599	0.1858	0.1532	0.2167	0.2064
Heart Disease (Cleveland)	0.1699	0.1769	0.1849	0.1832	0.1826	0.2032	0.1784	0.2381	0.2238
Haberman's Survival	0.2827	0.2977	0.3052	0.3071	0.3014	0.3051	0.2923	0.3195	0.3178
Primary Tumor	0.5405	0.5401	0.5417	0.5403	0.5405	0.5765	0.5412	0.6079	0.5853
Liver Disorders (Bupa)	0.4237	0.4283	0.4305	0.4323	0.4334	0.4323	0.4288	0.4386	0.4397
Ionosphere	0.2084	0.0806	0.0782	0.0729	0.0733	0.0674	0.0803	0.0925	0.0762
Dermatology	0.0203	0.0231	0.0235	0.0219	0.0218	0.0418	0.0230	0.0584	0.0374
Horse Colic	0.1979	0.1897	0.1893	0.1781	0.1780	0.1998	0.1898	0.1782	0.1656
House Votes 84	0.0978	0.0567	0.0503	0.0534	0.0521	0.0654	0.0527	0.0471	0.0423
Cylinder Bands	0.2613	0.2430	0.2388	0.2331	0.2334	0.4029	0.2392	0.3134	0.2917
Syncon	0.1110	0.0735	0.0633	0.0894	0.0904	0.0559	0.0684	0.0966	0.0636
Balance Scale	0.1936	0.2059	0.2217	0.2228	0.2226	0.2104	0.2076	0.2258	0.2244
Credit Screening	0.1523	0.1467	0.1473	0.1482	0.1482	0.1632	0.1463	0.1714	0.1606
Breast Cancer (Wisconsin)	0.0271	0.0371	0.0390	0.0337	0.0329	0.0509	0.0377	0.0445	0.0390
Pima Indians Diabetes	0.2752	0.2754	0.2784	0.2772	0.2772	0.2765	0.2763	0.2879	0.2851
Vehicle	0.4707	0.3933	0.3870	0.3873	0.3878	0.3911	0.3924	0.3865	0.3764
Annealing	0.1025	0.0850	0.0840	0.0829	0.0833	0.0831	0.0834	0.1420	0.1369
Tic-Tac-Toe Endgame	0.2916	0.2519	0.1255	0.1566	0.1713	0.2480	0.2502	0.1209	0.0766
Vowel	0.5577	0.3007	0.2645	0.2598	0.2687	0.3827	0.2717	0.2477	0.2239
LED	0.2627	0.2639	0.2667	0.2670	0.2659	0.2706	0.2644	0.2811	0.2786
German	0.2581	0.2550	0.2573	0.2542	0.2542	0.2809	0.2559	0.2819	0.2666
Contraceptive Method Choice	0.5402	0.5375	0.5389	0.5358	0.5363	0.5422	0.5379	0.5664	0.5630
Volcanoes	0.5863	0.5963	0.5992	0.5992	0.5995	0.5970	0.5962	0.6007	0.6004
Car Evaluation	0.1567	0.1063	0.0846	0.0785	0.0869	0.0818	0.0976	0.0912	0.0776
Segment	0.1803	0.1394	0.1328	0.1361	0.1367	0.1321	0.1334	0.1194	0.1178
Splice-junction Gene Sequences	0.0466	0.0401	0.0392	0.0755	0.0741	0.0608	0.0400	0.1179	0.0480
King-rook-vs-king-pawn	0.1273	0.0920	0.0741	0.0901	0.1046	0.0780	0.0586	0.0191	0.0129
Hypothyroid(Garavan)	0.0751	0.0744	0.0744	0.0746	0.0749	0.0761	0.0745	0.0815	0.0804
Sick-euthyroid	0.0808	0.0657	0.0641	0.0647	0.0656	0.0643	0.0636	0.0675	0.0664
Abalone	0.4971	0.4762	0.4769	0.4777	0.4762	0.4770	0.4760	0.4796	0.4801
SPAM E-mail	0.3373	0.3373	0.3373	0.3372	0.3373	0.3384	0.3373	0.3375	0.3373
Waveform-5000	0.2203	0.1984	0.1955	0.2020	0.2040	0.2155	0.1957	0.2383	0.2006
Nettalk(Phoneme)	0.3032	0.2643	0.2807	0.2454	0.2618	0.3480	0.2346	0.1927	0.1784
Page Blocks	0.0898	0.0847	0.0836	0.0837	0.0837	0.0839	0.0838	0.0826	0.0825
Optical Digits	0.0903	0.0372	0.0305	0.0500	0.0512	0.0524	0.0367	0.0662	0.0339
Mushrooms	0.0234	0.0003	0.0000	0.0001	0.0001	0.0003	0.0003	0.0001	0.0000
Pen Digits	0.1641	0.0665	0.0534	0.0570	0.0572	0.0940	0.0599	0.0517	0.0472
Sign	0.4643	0.4101	0.3821	0.3808	0.3867	0.3995	0.4006	0.3571	0.3567
Nursery	0.0979	0.0743	0.0546	0.0558	0.0544	0.0692	0.0791	0.0336	0.0244
MAGIC Gamma Telescope	0.2482	0.2265	0.2174	0.2153	0.2174	0.2215	0.2237	0.2143	0.2139
Letter Recognition	0.4969	0.4217	0.3946	0.4007	0.4104	0.4436	0.4173	0.3564	0.3508
Adult	0.1828	0.1753	0.1684	0.1731	0.1732	0.1692	0.1698	0.1767	0.1747
Connect-4 Opening	0.2792	0.2440	0.2319	0.2567	0.2729	0.2368	0.2400	0.2135	0.1876
Census-Income (KDD)	0.2391	0.0974	0.0714	0.1373	0.1289	0.0706	0.0936	0.0569	0.0550
Coverttype	0.3473	0.3208	0.3113	0.3366	0.3468	0.3268	0.3159	0.2512	0.2510
Mean	0.2440	0.2209	0.2183	0.2199	0.2229	0.2358	0.2182	0.2280	0.2146

Table 15: RMSE

Dataset	NB	AODE	A2DE	PA2DE	FA2DE	TAN	MAPLMG	RF10	RF100
Contact-lenses	0.3782	0.3907	0.3972	0.3924	0.4109	0.4462	0.3837	0.4098	0.3941
Lung Cancer	0.5623	0.5705	0.5736	0.4966	0.4991	0.5169	0.5706	0.4875	0.4736
Labor negotiations	0.2684	0.2820	0.2840	0.2924	0.2857	0.3516	0.2822	0.3708	0.3592
Postoperative Patient	0.4205	0.4266	0.4355	0.4274	0.4510	0.4213	0.4274	0.4448	0.4377
Zoo	0.1245	0.1163	0.1140	0.1125	0.1149	0.1408	0.1160	0.1312	0.1248
Promoter Gene Sequences	0.3342	0.3987	0.4265	0.4159	0.4168	0.4455	0.4019	0.4237	0.3946
Echocardiogram	0.4645	0.4743	0.4841	0.4795	0.5276	0.4769	0.4745	0.5041	0.4993
Lymphography	0.2601	0.2542	0.2557	0.2421	0.2462	0.2895	0.2546	0.2814	0.2710
Iris Classification	0.1450	0.1415	0.1441	0.1472	0.1526	0.1472	0.1424	0.1564	0.1559
Teaching Assistant Evaluation	0.5157	0.5060	0.5078	0.4876	0.5164	0.4875	0.5038	0.4868	0.4825
Hepatitis	0.3654	0.3548	0.3561	0.3427	0.3492	0.3543	0.3538	0.3642	0.3516
Wine Recognition	0.1775	0.1721	0.1784	0.1773	0.1767	0.1952	0.1723	0.2100	0.1965
Auto Imports	0.3053	0.2710	0.2686	0.2490	0.2515	0.2711	0.2706	0.2441	0.2330
Sonar Classification	0.4954	0.4425	0.4176	0.3911	0.3932	0.4490	0.4384	0.4164	0.3935
Glass Identification	0.3618	0.3568	0.3573	0.3541	0.3811	0.3603	0.3575	0.3678	0.3645
New-Thyroid	0.2427	0.2440	0.2463	0.2444	0.2662	0.2592	0.2438	0.2535	0.2518
Audiology	0.1463	0.1462	0.1461	0.1412	0.1498	0.1409	0.1462	0.1398	0.1333
Hungarian	0.3403	0.3374	0.3431	0.3420	0.3545	0.3710	0.3380	0.3911	0.3799
Heart Disease (Cleveland)	0.3714	0.3679	0.3718	0.3685	0.3827	0.3871	0.3687	0.4118	0.3973
Haberman's Survival	0.4552	0.4644	0.4801	0.4814	0.5422	0.4703	0.4626	0.4887	0.4853
Primary Tumor	0.1810	0.1801	0.1801	0.1792	0.1935	0.1813	0.1802	0.1934	0.1890
Liver Disorders (Bupa)	0.4962	0.4962	0.4986	0.4994	0.6126	0.5024	0.4965	0.5193	0.5168
Ionosphere	0.4260	0.2673	0.2591	0.2606	0.2611	0.2369	0.2662	0.2822	0.2672
Dermatology	0.0725	0.0755	0.0767	0.0797	0.0786	0.1009	0.0754	0.1417	0.1306
Horse Colic	0.4067	0.3881	0.3877	0.3740	0.3774	0.4057	0.3885	0.3753	0.3667
House Votes 84	0.2988	0.2092	0.1947	0.2008	0.2016	0.2277	0.2019	0.1936	0.1842
Cylinder Bands	0.4655	0.4437	0.4400	0.3974	0.4023	0.4900	0.4416	0.4440	0.4353
Syncon	0.1831	0.1373	0.1275	0.1384	0.1399	0.1203	0.1318	0.1708	0.1565
Balance Scale	0.3155	0.3108	0.3099	0.3103	0.3416	0.3148	0.3117	0.3177	0.3150
Credit Screening	0.3414	0.3358	0.3365	0.3326	0.3463	0.3572	0.3346	0.3628	0.3518
Breast Cancer (Wisconsin)	0.1597	0.1777	0.1780	0.1778	0.1715	0.2002	0.1783	0.1915	0.1834
Pima Indians Diabetes	0.4329	0.4309	0.4315	0.4297	0.4794	0.4309	0.4309	0.4542	0.4513
Vehicle	0.4314	0.3560	0.3506	0.3483	0.3684	0.3555	0.3542	0.3654	0.3583
Annealing	0.1535	0.1429	0.1411	0.1417	0.1514	0.1373	0.1416	0.1863	0.1843
Tic-Tac-Toe Endgame	0.4336	0.4044	0.3176	0.3455	0.3385	0.4108	0.4029	0.3132	0.2921
Vowel	0.2556	0.1945	0.1838	0.1855	0.1871	0.2178	0.1869	0.1832	0.1747
LED	0.1986	0.1993	0.2003	0.2007	0.2193	0.2033	0.1994	0.2099	0.2088
German	0.4204	0.4185	0.4223	0.4128	0.4283	0.4470	0.4193	0.4377	0.4218
Contraceptive Method Choice	0.4647	0.4536	0.4540	0.4537	0.5108	0.4586	0.4533	0.5029	0.4970
Volcanoes	0.4116	0.4125	0.4147	0.4149	0.5430	0.4135	0.4125	0.4162	0.4158
Car Evaluation	0.2292	0.2083	0.1922	0.1905	0.1786	0.1848	0.1963	0.1884	0.1782
Segment	0.1922	0.1682	0.1629	0.1664	0.1821	0.1628	0.1630	0.1538	0.1525
Splice-junction Gene Sequences	0.1539	0.1430	0.1428	0.1980	0.1951	0.1751	0.1427	0.2827	0.2601
King-rook-vs-king-pawn	0.3049	0.2719	0.2541	0.2712	0.2604	0.2392	0.2354	0.1449	0.1265
Hypothyroid(Garavan)	0.1865	0.1846	0.1843	0.1848	0.1921	0.1866	0.1848	0.1917	0.1909
Sick-euthyroid	0.2385	0.2302	0.2266	0.2281	0.2441	0.2264	0.2247	0.2317	0.2305
Abalone	0.4801	0.4347	0.4318	0.4325	0.5161	0.4328	0.4314	0.4366	0.4362
SPAM E-mail	0.4524	0.4523	0.4522	0.4521	0.5800	0.4534	0.4523	0.4529	0.4526
Waveform-5000	0.3415	0.3058	0.3022	0.3072	0.3160	0.3230	0.3023	0.3321	0.3146
Nettalk(Phoneme)	0.0953	0.0884	0.0909	0.0883	0.0886	0.0986	0.0844	0.0760	0.0731
Page Blocks	0.1614	0.1598	0.1593	0.1591	0.1753	0.1593	0.1595	0.1590	0.1588
Optical Digits	0.1227	0.0767	0.0699	0.0853	0.0852	0.0921	0.0762	0.1301	0.1172
Mushrooms	0.1322	0.0153	0.0064	0.0295	0.0288	0.0165	0.0142	0.0123	0.0086
Pen Digits	0.1652	0.1001	0.0895	0.0964	0.0966	0.1186	0.0958	0.0922	0.0886
Sign	0.4369	0.4169	0.4062	0.4050	0.4741	0.4150	0.4114	0.3911	0.3908
Nursery	0.1770	0.1583	0.1424	0.1428	0.1301	0.1425	0.1482	0.1092	0.1009
MAGIC Gamma Telescope	0.4083	0.3956	0.3917	0.3914	0.4184	0.3949	0.3942	0.3896	0.3893
Letter Recognition	0.1573	0.1453	0.1404	0.1421	0.1517	0.1489	0.1444	0.1359	0.1344
Adult	0.3664	0.3519	0.3442	0.3467	0.3649	0.3422	0.3460	0.3542	0.3516
Connect-4 Opening	0.3591	0.3381	0.3303	0.3458	0.3783	0.3322	0.3351	0.3215	0.3057
Census-Income (KDD)	0.4628	0.2731	0.2308	0.3058	0.3085	0.2275	0.2660	0.2098	0.2048
Coverttype	0.2604	0.2482	0.2445	0.2545	0.2940	0.2546	0.2460	0.2205	0.2204
Mean	0.3092	0.2890	0.2853	0.2854	0.3045	0.2955	0.2866	0.2945	0.2866

Table 16: Per Instance Training Time

Dataset	NB	AODE	A2DE	PA2DE	FA2DE	TAN	MAPLMG	RF10	RF100
Contact-lenses	0.00571	0.00471	0.00554	0.00521	0.01246	0.00683	0.24567	0.01429	0.04650
Lung Cancer	0.00409	0.00553	0.71631	0.64828	0.69800	0.02534	0.43744	0.03013	0.25059
Labor negotiations	0.00212	0.00219	0.00349	0.00333	0.00295	0.00447	0.10225	0.01247	0.09011
Postoperative Patient	0.00151	0.00146	0.00166	0.00160	0.00124	0.00220	0.05910	0.00791	0.05682
Zoo	0.00131	0.00129	0.00216	0.00223	0.00196	0.00287	0.09247	0.00739	0.04889
Promoter Gene Sequences	0.00192	0.00180	0.18512	0.15537	0.17721	0.01249	0.22453	0.01630	0.14082
Echocardiogram	0.00088	0.00096	0.00104	0.00111	0.00088	0.00157	0.04179	0.00626	0.05076
Lymphography	0.00091	0.00093	0.00205	0.00186	0.00355	0.00228	0.06530	0.00889	0.07238
Iris Classification	0.00102	0.00070	0.00099	0.00083	0.00071	0.00121	0.03442	0.00291	0.01227
Teaching Assistant Evaluation	0.00100	0.00083	0.00125	0.00104	0.00077	0.00427	0.03600	0.00742	0.07446
Hepatitis	0.00100	0.00079	0.00283	0.00174	0.00160	0.00192	0.05664	0.00864	0.07545
Wine Recognition	0.00074	0.00070	0.00266	0.00106	0.00097	0.00146	0.04089	0.00509	0.04271
Auto Imports	0.00074	0.00082	0.01486	0.00898	0.01964	0.00272	0.12048	0.01619	0.14782
Sonar Classification	0.00075	0.00113	0.05417	0.05225	0.06712	0.00514	0.20219	0.01983	0.26942
Glass Identification	0.00064	0.00053	0.00072	0.00072	0.00062	0.00100	0.02960	0.00514	0.04545
New-Thyroid	0.00057	0.00051	0.00066	0.00062	0.00052	0.00251	0.02459	0.00275	0.01636
Audiology	0.00068	0.00552	0.63403	0.58634	0.55959	0.01365	2.24021	0.04293	0.45907
Hungarian	0.00043	0.00041	0.00074	0.00079	0.00065	0.00121	0.02706	0.00712	0.06659
Heart Disease (Cleveland)	0.00045	0.00041	0.00074	0.00092	0.00071	0.00087	0.02678	0.00631	0.06091
Haberman's Survival	0.00041	0.00038	0.00048	0.00041	0.00039	0.00058	0.01670	0.00245	0.01966
Primary Tumor	0.00039	0.00047	0.00130	0.00183	0.00239	0.00119	0.13380	0.01654	0.16519
Liver Disorders (Bupa)	0.00035	0.00030	0.00041	0.00080	0.00037	0.00059	0.01695	0.00328	0.02885
Ionosphere	0.00040	0.00056	0.00463	0.00556	0.00674	0.00175	0.07723	0.01104	0.10150
Dermatology	0.00040	0.00073	0.02099	0.01990	0.02824	0.00230	0.15539	0.01026	0.09502
Horse Colic	0.00037	0.00040	0.00162	0.00161	0.00214	0.00100	0.04104	0.02723	0.25749
House Votes 84	0.00029	0.00032	0.00086	0.00080	0.00075	0.00070	0.02766	0.00395	0.03675
Cylinder Bands	0.00030	0.00266	0.52135	0.47019	0.15990	0.01125	0.16161	0.16264	1.39439
Syncon	0.00029	0.00087	0.12126	0.11658	0.11387	0.00397	0.47564	0.01881	0.18113
Balance Scale	0.00023	0.00018	0.00023	0.00021	0.00020	0.00029	0.00980	0.00203	0.01860
Credit Screening	0.00023	0.00022	0.00065	0.00065	0.00063	0.00048	0.02263	0.00878	0.08624
Breast Cancer (Wisconsin)	0.00019	0.00019	0.00036	0.00036	0.00084	0.00042	0.01505	0.00252	0.02392
Pima Indians Diabetes	0.00019	0.00016	0.00024	0.00024	0.00023	0.00030	0.01179	0.00446	0.04201
Vehicle	0.00017	0.00020	0.00093	0.00092	0.00127	0.00052	0.03882	0.01148	0.11048
Annealing	0.00019	0.00036	0.01070	0.01043	0.01415	0.00082	0.18188	0.05706	0.62783
Tic-Tac-Toe Endgame	0.00014	0.00013	0.00024	0.00024	0.00022	0.00025	0.01190	0.00430	0.03970
Vowel	0.00014	0.00016	0.00062	0.00058	0.00071	0.00044	0.04711	0.00907	0.09508
LED	0.00012	0.00011	0.00017	0.00017	0.00018	0.00022	0.01648	0.00380	0.03551
German	0.00017	0.00019	0.00114	0.00113	0.00139	0.00051	0.03143	0.00958	0.09459
Contraceptive Method Choice	0.00010	0.00010	0.00020	0.00020	0.00018	0.00029	0.01211	0.00636	0.06713
Volcanoes	0.00009	0.00008	0.00009	0.00008	0.00008	0.00011	0.00551	0.00093	0.00834
Car Evaluation	0.00008	0.00008	0.00011	0.00012	0.00011	0.00014	0.01192	0.00244	0.02308
Segment	0.00008	0.00013	0.00125	0.00094	0.00111	0.00030	0.06186	0.00608	0.06088
Splice-junction Gene Sequences	0.00015	0.00058	0.06743	0.06842	0.06433	0.00200	0.23156	0.02216	0.21648
King-rook-vs-king-pawn	0.00010	0.00024	0.00440	0.00446	0.00463	0.00062	0.10376	0.01554	0.15649
Hypothyroid (Garavan)	0.00009	0.00017	0.00290	0.00265	0.00277	0.00041	0.09119	0.02219	0.22663
Sick-euthyroid	0.00009	0.00016	0.00244	0.00248	0.00254	0.00043	0.05123	0.01783	0.17659
Abalone	0.00005	0.00005	0.00012	0.00012	0.00011	0.00008	0.01016	0.00293	0.02821
SPAM E-mail	0.00013	0.00049	0.01767	0.01750	0.01689	0.00141	0.14233	0.11317	1.15056
Waveform-5000	0.00010	0.00028	0.00724	0.00687	0.00710	0.00076	0.11678	0.02298	0.21661
Nettalk (Phoneme)	0.00004	0.00031	0.01817	0.01616	0.01508	0.00169	0.05430	0.01762	0.17862
Page Blocks	0.00004	0.00005	0.00017	0.00017	0.00017	0.00009	0.01504	0.00271	0.02672
Optical Digits	0.00012	0.00040	0.04919	0.04899	0.04632	0.00126	0.45907	0.02529	0.21022
Mushrooms	0.00006	0.00012	0.00138	0.00148	0.00149	0.00028	0.02641	0.00457	0.04698
Pen Digits	0.00004	0.00008	0.00059	0.00059	0.00070	0.00016	0.05931	0.00776	0.07362
Sign	0.00003	0.00003	0.00010	0.00010	0.00010	0.00006	0.01297	0.00360	0.03670
Nursery	0.00003	0.00003	0.00011	0.00010	0.00010	0.00006	0.01743	0.00307	0.02825
MAGIC Gamma Telescope	0.00003	0.00004	0.00015	0.00015	0.00015	0.00007	0.01042	0.00494	0.04798
Letter Recognition	0.00005	0.00008	0.00067	0.00063	0.00070	0.00017	0.13907	0.01397	0.13481
Adult	0.00004	0.00007	0.00043	0.00040	0.00042	0.00012	0.02277	0.01949	0.19112
Connect-4 Opening	0.00010	0.00029	0.00722	0.00742	0.00725	0.00076	0.17049	0.03772	0.37281
Census-Income (KDD)	0.00010	0.00033	0.01304	0.01326	0.01279	0.00078	0.11065	0.06108	—
Covertypes	0.00013	0.00044	0.01723	0.01756	0.01707	0.00118	0.44194	0.10864	0.87340
Mean (excluding Census-Income)	0.00054	0.00072	0.04129	0.03778	0.03402	0.00220	0.12898	0.01769	0.16448

Table 17: Per Instance Classification Time

Dataset	NB	AODE	A2DE	PA2DE	FA2DE	TAN	MAPLMG	RF10	RF100
Contact-lenses	0.00025	0.00029	0.00071	0.00025	0.00033	0.00033	0.00063	0.00008	0.00021
Lung Cancer	0.00022	0.00416	0.14209	0.14331	0.14019	0.00041	0.00459	0.00009	0.00025
Labor negotiations	0.00009	0.00026	0.00072	0.00100	0.00072	0.00012	0.00065	0.00004	0.00074
Postoperative Patient	0.00014	0.00017	0.00058	0.00050	0.00050	0.00023	0.00044	0.00012	0.00058
Zoo	0.00018	0.00093	0.00446	0.00466	0.00437	0.00018	0.00166	0.00010	0.00039
Promoter Gene Sequences	0.00013	0.00281	0.15011	0.13926	0.14086	0.00025	0.00318	0.00010	0.00034
Echocardiogram	0.00010	0.00015	0.00016	0.00015	0.00016	0.00008	0.00023	0.00009	0.00062
Lymphography	0.00023	0.00076	0.00473	0.00459	0.00416	0.00018	0.00112	0.00016	0.00049
Iris Classification	0.00015	0.00015	0.00023	0.00013	0.00011	0.00009	0.00023	0.00007	0.00029
Teaching Assistant Evaluation	0.00026	0.00013	0.00019	0.00025	0.00014	0.00017	0.00028	0.00015	0.00047
Hepatitis	0.00015	0.00046	0.00554	0.00317	0.00307	0.00012	0.00068	0.00012	0.00057
Wine Recognition	0.00010	0.00042	0.00324	0.00184	0.00164	0.00012	0.00058	0.00013	0.00042
Auto Imports	0.00019	0.00227	0.04120	0.02235	0.02201	0.00026	0.00296	0.00009	0.00068
Sonar Classification	0.00016	0.00378	0.16124	0.16418	0.15268	0.00019	0.00338	0.00008	0.00067
Glass Identification	0.00008	0.00027	0.00068	0.00068	0.00062	0.00008	0.00037	0.00012	0.00054
New-Thyroid	0.00009	0.00011	0.00017	0.00017	0.00018	0.00010	0.00021	0.00008	0.00036
Audiology	0.00073	0.04319	1.25924	1.32199	1.26469	0.00192	0.04573	0.00020	0.00169
Hungarian	0.00008	0.00022	0.00070	0.00079	0.00067	0.00009	0.00038	0.00006	0.00066
Heart Disease (Cleveland)	0.00006	0.00026	0.00127	0.00142	0.00126	0.00007	0.00040	0.00008	0.00054
Haberman's Survival	0.00005	0.00004	0.00006	0.00007	0.00005	0.00005	0.00014	0.00006	0.00030
Primary Tumor	0.00024	0.00300	0.01350	0.02424	0.01361	0.00045	0.00479	0.00022	0.00217
Liver Disorders (Bupa)	0.00008	0.00012	0.00018	0.00028	0.00017	0.00005	0.00017	0.00009	0.00054
Ionosphere	0.00013	0.00132	0.02340	0.02868	0.02342	0.00012	0.00140	0.00011	0.00058
Dermatology	0.00017	0.00313	0.04434	0.04540	0.04470	0.00026	0.00373	0.00008	0.00052
Horse Colic	0.00008	0.00041	0.00276	0.00279	0.00271	0.00011	0.00062	0.00030	0.00399
House Votes 84	0.00009	0.00039	0.00245	0.00255	0.00243	0.00010	0.00053	0.00007	0.00040
Cylinder Bands	0.00010	0.00154	0.04088	0.04253	0.04065	0.00015	0.00203	0.00008	0.00076
Syncon	0.00025	0.01067	0.33385	0.34002	0.34039	0.00044	0.01024	0.00010	0.00069
Balance Scale	0.00003	0.00008	0.00008	0.00008	0.00007	0.00004	0.00016	0.00006	0.00042
Credit Screening	0.00006	0.00031	0.00192	0.00198	0.00192	0.00008	0.00046	0.00008	0.00078
Breast Cancer (Wisconsin)	0.00005	0.00017	0.00042	0.00045	0.00041	0.00007	0.00028	0.00004	0.00028
Pima Indians Diabetes	0.00004	0.00015	0.00035	0.00036	0.00032	0.00007	0.00021	0.00007	0.00067
Vehicle	0.00009	0.00085	0.00577	0.00607	0.00581	0.00011	0.00105	0.00009	0.00122
Annealing	0.00014	0.00109	0.00335	0.00349	0.00337	0.00016	0.00237	0.00050	0.01097
Tic-Tac-Toe Endgame	0.00005	0.00016	0.00045	0.00048	0.00045	0.00005	0.00026	0.00006	0.00059
Vowel	0.00013	0.00120	0.00484	0.00505	0.00482	0.00019	0.00175	0.00011	0.00144
LED	0.00009	0.00037	0.00058	0.00064	0.00057	0.00012	0.00077	0.00010	0.00076
German	0.00005	0.00049	0.00463	0.00476	0.00468	0.00007	0.00063	0.00007	0.00078
Contraceptive Method Choice	0.00004	0.00018	0.00053	0.00057	0.00053	0.00005	0.00036	0.00008	0.00134
Volcanoes	0.00004	0.00007	0.00005	0.00006	0.00005	0.00004	0.00018	0.00004	0.00035
Car Evaluation	0.00004	0.00014	0.00020	0.00021	0.00019	0.00005	0.00030	0.00005	0.00051
Segment	0.00010	0.00149	0.01394	0.01096	0.01072	0.00017	0.00178	0.00009	0.00069
Splice-junction Gene Sequences	0.00011	0.00464	0.20874	0.21927	0.21233	0.00024	0.00489	0.00008	0.00128
King-rook-vs-king-pawn	0.00006	0.00120	0.02491	0.02568	0.02505	0.00011	0.00145	0.00009	0.00106
Hypothyroid(Garavan)	0.00008	0.00153	0.01972	0.01805	0.01806	0.00014	0.00185	0.00016	0.00280
Sick-euthyroid	0.00005	0.00080	0.01135	0.01198	0.01144	0.00009	0.00098	0.00012	0.00128
Abalone	0.00003	0.00017	0.00042	0.00044	0.00042	0.00005	0.00029	0.00007	0.00064
SPAM E-mail	0.00010	0.00343	0.11847	0.12060	0.11844	0.00016	0.00300	0.00031	0.00310
Waveform-5000	0.00009	0.00263	0.05807	0.05722	0.05632	0.00015	0.00248	0.00011	0.00293
Nettalk(Phoneme)	0.00030	0.00220	0.00313	0.00337	0.00297	0.00061	0.00626	0.00024	0.00239
Page Blocks	0.00005	0.00038	0.00118	0.00125	0.00118	0.00008	0.00057	0.00006	0.00053
Optical Digits	0.00030	0.01246	0.28798	0.29286	0.28091	0.00055	0.01034	0.00015	0.00249
Mushrooms	0.00004	0.00054	0.00597	0.00601	0.00581	0.00007	0.00071	0.00004	0.00034
Pen Digits	0.00012	0.00164	0.00876	0.00923	0.00881	0.00020	0.00204	0.00012	0.00240
Sign	0.00003	0.00016	0.00042	0.00044	0.00042	0.00004	0.00028	0.00007	0.00084
Nursery	0.00004	0.00024	0.00054	0.00058	0.00055	0.00006	0.00045	0.00007	0.00121
MAGIC Gamma Telescope	0.00003	0.00016	0.00061	0.00063	0.00060	0.00004	0.00025	0.00008	0.00094
Letter Recognition	0.00029	0.00417	0.02229	0.02370	0.02235	0.00048	0.00496	0.00032	0.00595
Adult	0.00004	0.00027	0.00169	0.00167	0.00160	0.00005	0.00037	0.00042	0.00803
Connect-4 Opening	0.00011	0.00289	0.06617	0.06875	0.06519	0.00017	0.00256	0.00039	0.00682
Census-Income (KDD)	0.00009	0.00177	0.05312	0.05313	0.05193	0.00013	0.00180	0.00060	—
Coverttype	0.00022	0.00926	0.24854	0.24937	0.24217	0.00045	0.00889	0.00040	0.01561
Mean (excluding Census-Income)	0.00012	0.00224	0.05516	0.05645	0.05434	0.00019	0.00253	0.00013	0.00167

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