

# LR Parser Table

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# Example

Grammar

$$S \rightarrow AA$$
$$A \rightarrow aA \mid b$$

# Step 1:

## Grammar Augmentation

- $S' \rightarrow .S \dots$  Rule 0
- $S \rightarrow .AA \dots$  Rule 1
- $A \rightarrow .aA \dots$  Rule 2
- $A \rightarrow .b \dots$  Rule 3

# Step 2

Closure operation = I0

- $S' \rightarrow .S$
- $S \rightarrow .AA$
- $A \rightarrow .aA$
- $A \rightarrow .b$

Goto (I0, S) = I1

- $S' \rightarrow S. // **$

Goto(I0, A) = I2

- $S \rightarrow A.A$
- $A \rightarrow .aA$
- $A \rightarrow .b$

Goto(I0, a) = I3

- $A \rightarrow a.A$
- $A \rightarrow .aA$
- $A \rightarrow .b$

Goto(I0,b) = I4

$A \rightarrow b. // **$

Goto(I2, A) = I5

$S \rightarrow AA.$

Goto (I2, a) = I3

Goto (I2, b) = I4

Goto (I3, A) = I6

$A \rightarrow aA.$

Goto (I3, a) = I3

Goto (I3, b) = I4

# Example

## Grammar

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow (E) \mid \text{id}$

G:

$E \rightarrow E + T$  (1)

$E \rightarrow T$  (2)

$T \rightarrow T * F$  (3)

$T \rightarrow F$  (4)

$F \rightarrow (E)$  (5)

$F \rightarrow \text{id}$  (6)

# Step1

Grammar Augumentation G':

$E' \rightarrow E$  (0)

$E \rightarrow E + T$  (1)

$E \rightarrow T$  (2)

$T \rightarrow T * F$  (3)

$T \rightarrow F$  (4)

$F \rightarrow (E)$  (5)

$F \rightarrow id$  (6)

# LR(0) items

Closure of  $E' \rightarrow \cdot E = i_0$

$i(0): E' \rightarrow \cdot E$

$E \rightarrow \cdot E + T$

$E \rightarrow \cdot T$

$T \rightarrow \cdot T * F$

$T \rightarrow \cdot F$

$F \rightarrow \cdot (E)$

$F \rightarrow \cdot id$



# Step 3

GOTO(i0,E) = i1

GOTO(i0,T) = i2

GOTO(i0, F) =i3

GOTO(i0, ( ) = i4

GOTO(i0, id) = i5

GOTO(i1, +) = i6

GOTO(i2, \*) = i7

GOTO(i4, E) = i8

GOTO(i4, T)=i2

GOTO(i4, F)=i3

GOTO(i4, ( )=i4

GOTO(i4,id) =i5

GOTO(i6,T) = i9

GOTO(i6,F)=i3

GOTO(i6,( )=i4

GOTO(i6, id) = i5

GOTO(i7,F)=i10

GOTO(i7,( )=i4

GOTO(i7,id) =i5

GOTO(i8, ) )=i11

GOTO(i8,+)=i6

GOTO(i9,\*)=i7

# Rules for construction of parsing table LR(0) from Canonical collections of LR(0) items

## Action part: For Terminal Symbols

- If  $A \rightarrow \alpha.a\beta$  is state  $l_x$  in Items and  $\text{goto}(l_x, a) = l_y$  then set action  $[l_x, a] = S_y$  (represented as shift to state  $l_y$ )
- If  $A \rightarrow \alpha.$  is in  $l_x$ , then set action  $[l_x, f]$  to reduce  $A \rightarrow \alpha$  for all symbols 'f'.
- If  $S' \rightarrow S.$  is in  $l_x$  then set action  $[l_x, \$] = \text{accept}$ .

## Go To Part: For Non Terminal Symbols

- If  $\text{goto}(l_x, A) = l_y$ , then  $\text{goto}(l_x, A)$  in table =  $Y$
- It is numeric value of state  $Y$ .
- All other entries are considered as error.
- Initial state is  $S' \rightarrow .S$



# SLR(1)

- SLR(1) Parser is used for accepting the certain grammar which is not accepted by LR(0) parser. SLR(1) Parser stands for Simple LR(1).
- SLR(1) parsers use the same LR(0) Sets and have the Same Table Structure and Parser Operation,
- The difference in SLR(1) Parser with LR(0) Parser comes in Assigning Table Actions.
- SLR(1) Parsers use one token of look-ahead to eliminate the conflicts.
- The Simple Improvement that SLR(1) makes on the basic LR(0) parser is to reduce only if the next input token is a member of the Follow Set of the non-terminal being reduced.

# Rules for construction of parsing table SLR(1) from Canonical collections of LR(0) items

## Action part: For Terminal Symbols

- If  $A \rightarrow \alpha.a\beta$  is state  $l_x$  in Items and  $\text{goto}(l_x, a) = l_y$  then set action  $[l_x, a] = S_y$  (represented as shift to state  $l_y$ )
- If  $A \rightarrow \alpha.$  is in  $l_x$ , then set action  $[l_x, f]$  to reduce  $A \rightarrow \alpha$  for all symbols 'f' where 'f' is in  $\text{Follow}(A)$
- If  $S' \rightarrow S.$  is in  $l_x$  then set action  $[l_x, \$] = \text{accept}$ .

## Go To Part: For Non Terminal Symbols

- If  $\text{goto}(l_x, A) = l_y$ , then  $\text{goto}(l_x, A)$  in table =  $Y$
- It is numeric value of state  $Y$ .
- All other entries are considered as error.
- Initial state is  $S' \rightarrow .S$

**Note:** SLR(1) parser avoids the above shift / reduce conflicts by reducing only if the next input token is a member of the Follow Set of the nonterminal being reduced. So the above grammar is not LR(0), but it's SLR(1).

# Follow Set

- $\text{Follow}(E) = \{\$, ), +\}$
- $\text{Follow}(T) = \{\$, +, ), *\}$
- $\text{Follow}(F) = \{*, +, ), \$\}$

# Parsing Table SLR(1)

states	id	+	*	(	)	\$	E	T	F
	Action Part						GOTO Part		
I0	s5			s4			1	2	3
I1		s6				acc			
I2		r2	s7		r2	r2			
I3		r4	r4		r4	r4			
I4	s5			s4			8	2	3
I5		r6	r6		r6	r6			
I6	s5			s4				9	3
I7	s5			s4					10
I8		s6			s11				
i9		r1	s7		r1	r1			
I10		r3	r3		r3	r3			
I11		r5	r5		r5	r5			

Parsing Table: No multiple entries: LR(0) Grammar



# Example

Grammar

$$S \rightarrow AA$$
$$A \rightarrow aA \mid b$$

# Follow Set

- $\text{Follow}(S) = \$$
- $\text{Follow}(A) = \{a, b, \$\}$

# Parsing Table SLR(1)

	a	b	\$	S	A
	ACTION			GOTO	
I0	S3	S4		1	2
I1			Accept		
I2	S3	S4			5
I3	S3	S4			6
I4	r3	r3	r3		
I5			r1		
I6	r2	r2	r2		

Parsing Table: No multiple entries: LR(0) Grammar